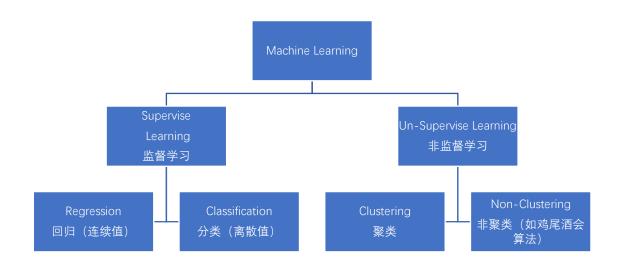
Week 1 笔记

by 骆剑 2017/5/21

Introduction



Supervise Learning 监督学习

数据有标签,模型用来预测输入对应的输出

Regression 回归:预测连续的输出值

Classification 分类: 预测离散的输出值

UnSupervise Learning 非监督学习 数据没有标签、模型用来学习数据之间的关系

Linear Regression (线性回归)

Basic Concept (基本概念):

1. Hypothesis:
$$h_{\theta}(x) = \theta_0 + \theta_1 x$$

(假设函数)

2. Parameters:
$$\theta_0$$
; θ_1

3.Cost Function:
$$J(\theta_0,\theta_1) = \frac{1}{2m} \sum_{i=1}^m \left(h_\theta(x^{(i)}) - y^{(i)} \right)^2$$
 (损失函数)

4.Goal: minimize
$$J(\theta_0, \theta_1)$$
 θ_0, θ_1

【注】: 式 3 中的 $x^{(i)}$ $y^{(i)}$ 表示第 i 个 example 样本的 x 和 y 样本总数为 m

Gradient descent algorithm (梯度下降算法)

Repeat until convergence (循环直至收敛)

{//同步更新, 赋值(3)(4)必须在计算(1)(2)之后, 设 tmp

$$tmp0 := \theta_0 - \alpha \cdot \frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1)$$
 (1)

$$tmp1 := \theta_1 - \alpha \cdot \frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1)$$
 (2)

$$\theta_0 := tmp0 \tag{3}$$

$$\theta_1 := tmp1 \tag{4}$$

}

推导(一)

$$tmp0 := \theta_0 - \alpha \cdot \frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1)$$
$$:= \theta_0 - \alpha \cdot \frac{1}{m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})$$

推导(二)

$$tmp1 := \theta_1 - \alpha \cdot \frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1)$$
$$:= \theta_1 - \alpha \cdot \frac{1}{m} \sum_{i=1}^{m} [(h_{\theta}(x^{(i)}) - y^{(i)}) \cdot x^{(i)}]$$

偏导推导过程 (一)

$$\begin{split} \frac{\partial}{\partial \theta_0} J(\theta_0, \theta_1) &= \ \frac{\partial}{\partial \theta_0} \{ \frac{1}{2m} \sum\nolimits_{i=1}^m \left(h_\theta \big(x^{(i)} \big) - y^{(i)} \big)^2 \} \\ &= \frac{\partial}{\partial \theta_0} \{ \frac{1}{2m} \sum\nolimits_{i=1}^m \left(\theta_0 + \theta_1 x^{(i)} - y^{(i)} \right)^2 \} \\ &= \frac{1}{m} \sum\nolimits_{i=1}^m \left(\theta_0 + \theta_1 x^{(i)} - y^{(i)} \right) \\ &= \frac{1}{m} \sum\nolimits_{i=1}^m \left(h_\theta \big(x^{(i)} \big) - y^{(i)} \right) \end{split}$$

偏导推导过程(二)

$$\begin{split} \frac{\partial}{\partial \theta_1} J(\theta_0, \theta_1) &= \frac{\partial}{\partial \theta_1} \{ \frac{1}{2m} \sum\nolimits_{i=1}^m \left(h_\theta \big(x^{(i)} \big) - y^{(i)} \big)^2 \} \\ &= \frac{\partial}{\partial \theta_1} \{ \frac{1}{2m} \sum\nolimits_{i=1}^m \left(\theta_0 + \theta_1 x^{(i)} - y^{(i)} \right)^2 \} \\ &= \frac{1}{m} \sum\nolimits_{i=1}^m \left(\theta_0 + \theta_1 x^{(i)} - y^{(i)} \right) \\ &= \frac{1}{m} \sum\nolimits_{i=1}^m \left[\ \left(h_\theta \big(x^{(i)} \big) - y^{(i)} \right) \cdot x^{(i)} \ \right] \end{split}$$