

The Hong Kong Polytechnic University  
Department of Aeronautical and Aviation Engineering  
2024/25 Semester 2  
AAE6102 Satellite Communication and Navigation  
Assignment 1

# Technical Report

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## Introduction

Developing a comprehensive understanding of GNSS Software-Defined Receiver (SDR) signal processing is crucial for researchers in the GNSS navigation field. You are provided with two real Intermediate Frequency (IF) datasets, which were collected in open-sky area and urban environment, respectively (see Figure 1). The urban dataset likely exhibits typical urban effects such as multipath and non-line-of-sight (NLOS) receptions, which can degrade signal quality and lead to positioning errors. The collected GPS L1 data are described in Table 1. You are required to process and analyze the IF data using any open-source GNSS SDR code.

## Installation

Make sure you have a working MATLAB environment. To install GPSSDR, simply unzip the file into a folder, e.g., ./GPSSDR/. The package contains six folders and one technical report. The sample data set is located in the folder called DataSample. The data file is compressed due to its large size, so before using the sample data set, please unzip the data file. The MATLAB source code is located in three folders, acqtckpos and geo and plot. The results for the sample data are found in the folders OpenSky\_Result and Urban\_Result, respectively. Set the current folder to ./GPSSDR/ in MATLAB, and then run the main program, SDR\_main.m.

## Usage

GPSSDR is very easy to use. This section presents the usage through two examples. The raw IF data were collected in open-sky and urban environments (see Figure 1). The sampling frequency is 58 MHz and 26 MHz, respectively. The urban dataset likely exhibits typical urban effects such as multipath and non-line-of-sight (NLOS) receptions, which can degrade signal quality and lead to positioning errors. The collected GPS L1 data are described in Table 1.



Figure 1. Data collection locations

Table 1 Sample data description

|                        | Opensky                                    | Urban                             |
|------------------------|--|-----------------------------------|
| Carrier frequency      | 1575.42 MHz                                | 1575.42 MHz                       |
| Intermediate frequency | 4.58MHz                                    | 0                                 |
| Sampling frequency     | 58MHz                                      | 26MHz                             |
| Data Format            | 8 bit I/Q samples                          | 8 bit I/Q samples                 |
| Ground truth           | (22.328444770087565,<br>114.1713630049711) | (22.3198722,<br>114.209101777778) |
| Data length            | 90 seconds                                 | 90 seconds                        |

To begin with, it is necessary to understand the folder structure of the software, as shown in Figure 2. This software consists of three separate files: the main program, the initialization functions (`initParameters_OpenSky.m` and `initParameters_Urban.m`), and three folders containing baseband signal processing functions, geo-related functions, and plot functions. The baseband signal processing functions handle signal acquisition, tracking, navigation data extraction, etc., while the geo-related functions perform coordinate transformation, atmospheric corrections, and so on. The plot-related functions are responsible for plotting. Each file contains comments that clearly specify the purpose of the respective function.

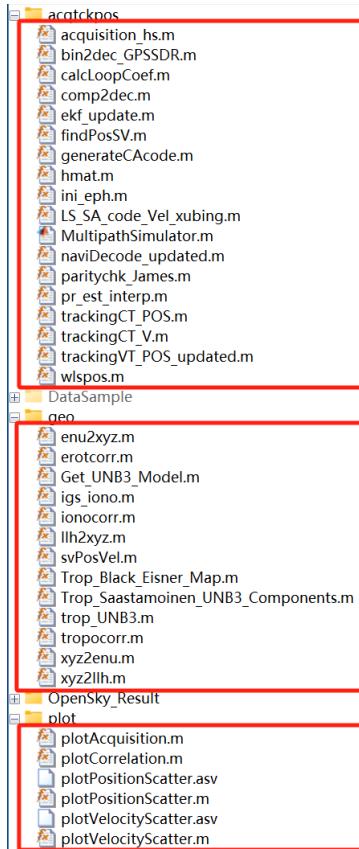


Figure 2 Folder structure.

#### Initialization parameters

To process the raw IF data, the first step is to initialize necessary parameters for acquisition, tracking, positioning, etc. in the file named `initParameters_OpenSky.m` and `initParameters_Urban.m`. Some important initialization parameters are listed in Table 2:

Table2. Initialization parameters.

|                            | <b>Parameter</b>        | <b>Description</b>  |
|----------------------------|-------------------------|---|
| <b>Raw data parameters</b> | <i>file.filename</i>    | Raw data file name  |
|                            | <i>file.skip</i>        | Skip time in milliseconds, from when raw data is processed              |
| Acquisition Parameters     | acq.prnList             | PRNs to be searched   |
|                            | acq.freqStep            | Frequency search step   |
|                            | acq.freqMin             | Minimum frequency to be searched  |
|                            | acq.freqNum             | Frequency bin numbers   |
|                            | acq.threshold           | Acquisition threshold   |
|                            | acq.L                   | Numbers of code periods to find fine frequency                          |
| Tracking Parameters        | track.CorrelatorSpacing | Correlator spacing between the Early and Late code                      |
|                            | track.msToProcessCT     | Time to do positioning via LSE/EKF in milliseconds                      |
|                            | track.msToProcessVT     | Time to do positioning in vector tracking mode in milliseconds          |
|                            | track.pdi               | Prediction integration time   |
| Navigation Parameters      | solu.iniPos             | Initial position, latitude (degree), longitude (degree), height (meter) |
|                            | solu.mode               | Position method: 0-WLS algorism;1-EKF algorism                          |
| Common Parameters          | cmn.vtEnable            | Tracking mode: 0 - Conventional tracking, 1 - Vector tracking           |
| Signal Parameters          | file.skiptimeVT         | Skip time in milliseconds, from when vector tracking begins             |
|                            | file.dataType           | Raw data type: 1 - I, 2 - I/Q   |
|                            | file.dataPrecision      | Data size: 1 - 'int8', 2 - 'int16'                                      |
|                            | signal.IF               | Intermediate frequency  |
|                            | signal.Fs               | Sampling rate   |
|                            | signal.Fc               | Carrier frequency   |
|                            | signal.codeFreqBasis    | Code frequency  |
|                            | signal.Sample           | Numbers of samples in one code period                                   |
|                            | signal.codelength       | Code length   |

### Task 1 – Acquisition

**Process the IF data using a GNSS SDR and generate initial acquisition outputs.**

After initialization, type 'SDR\_main' in the MATLAB command window and press [Return]. This software will first acquire the visible satellites, outputting the satellite number (SV), signal-to-noise ratio (SNR), code phase, and Doppler frequency in the command window, as shown in Figure 3. The acquisition result is saved in the current folder with the name 'Acquired + raw data file name + .mat'.

```

30

svindex =
31

svindex =
32

SV[ 1] SNR = 42.21, Code phase = 22672, Raw Doppler = 1000, Fine Doppler = 1205.000000
SV[ 3] SNR = 29.71, Code phase = 829, Raw Doppler = 4500, Fine Doppler = 4280.000000
SV[ 7] SNR = 20.43, Code phase = 10810, Raw Doppler = 500, Fine Doppler = 370.000000
SV[11] SNR = 26.13, Code phase = 24845, Raw Doppler = 500, Fine Doppler = 410.000000
SV[18] SNR = 21.80, Code phase = 15421, Raw Doppler = -500, Fine Doppler = -325.000000
SV[22] SNR = 16.52, Code phase = 1805, Raw Doppler = 3500, Fine Doppler = 3365.000000
Acquisition Completed.

```

Figure3. Acquisition results shown in MATLAB command window

To further visualize the acquisition results, use a bar chart to plot the satellite signal acquisition results. The x-axis represents each PRN number in Acquired.sv, and the y-axis corresponds to the SNR value for each satellite. A peak higher than the acquisition threshold indicates a successful acquisition of that satellite. If satellites are not detected, use an 'x' marker. When the acquisition threshold is set to 16, the model acquisition results for OpenSky and Urban data are as follows (Figure4 and 5):

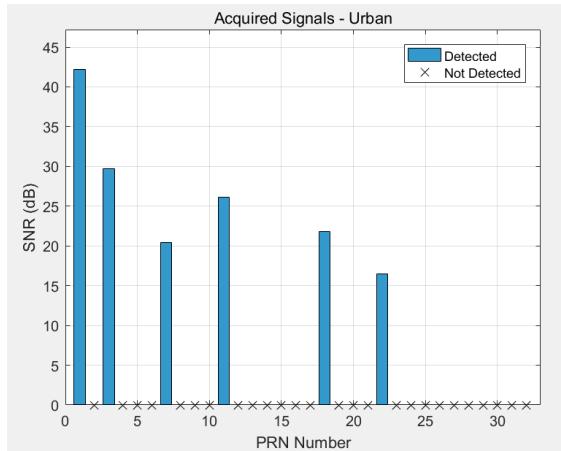


Figure4. Acquisition results of Urban data.

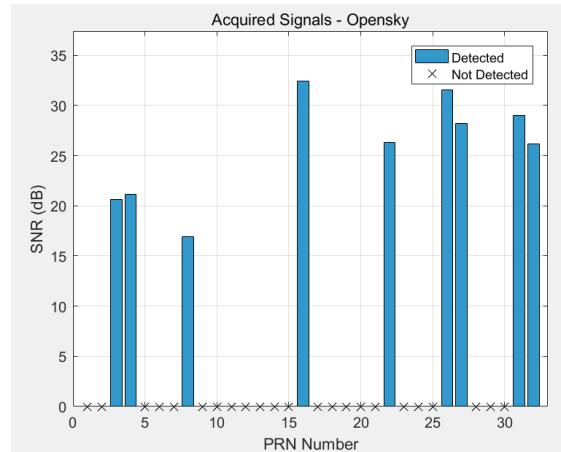


Figure 5. Acquisition results of OpenSky data.

From Figures 4 and 5, when the threshold value was set to 16, the Urban data acquired signals from 6 satellites, and the OpenSky data acquired signals from 8 satellites.

### Task 2 – Tracking

**Adapt the tracking loop (DLL) to produce correlation plots and analyze the tracking performance. Discuss the impact of urban interference on the correlation peaks. (Multiple correlators must be implemented for plotting the correlation function)**

After acquisition, perform signal tracking and obtain satellite ephemeris. In conventional tracking, a DLL with fixed bandwidths is used to track the code. The DLL employs a normalized noncoherent early-minus-late envelope discriminator. A progress bar will appear during the conventional tracking period. The conventional tracking result is saved in the current folder with the name 'TckRstct\_Eph + raw data file name + .mat'.

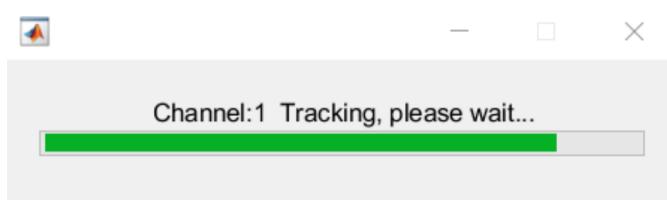


Figure 6. Progress bar during conventional tracking period

To analyze the tracking performance, correlation values against the time delay for each PNR were plotted. The x-axis represents the time delay, with the unit in chips, and the y-axis represents the correlation values. When  $x = 0$ , it refers to the prompt time; -0.5 represents 0.5 chips earlier relative to the present, and 0.5 represents 0.5 chips later relative to the present. Different colors are used to represent the correlation values for different satellites.

For the Urban and OpenSky data, 6 and 8 satellites were acquired, respectively. Both datasets have a length of 90 seconds. This means that if 1 ms is recorded for each time step, the Urban and OpenSky data will acquire 540,000 and 640,000 results, respectively. To avoid clutter in the correlation lines, the correlation value line is plotted once for every 1,000 time steps. The OpenSky (Figure 7) and Urban (Figure 8) results are shown as follows:

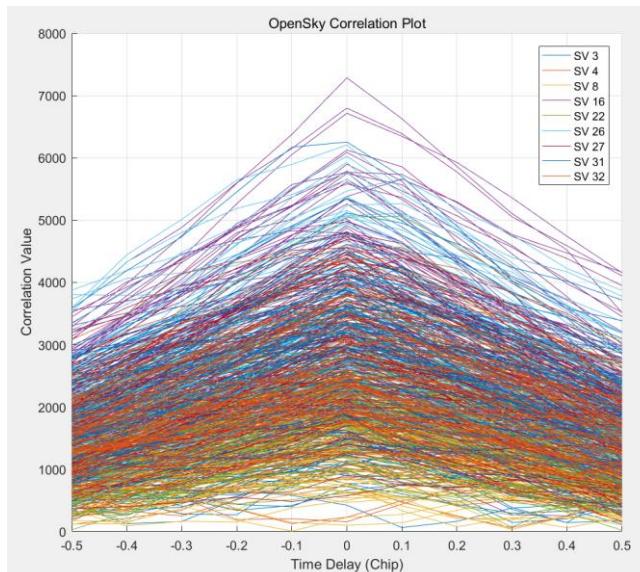


Figure 7. Correlation plots for OpenSky data

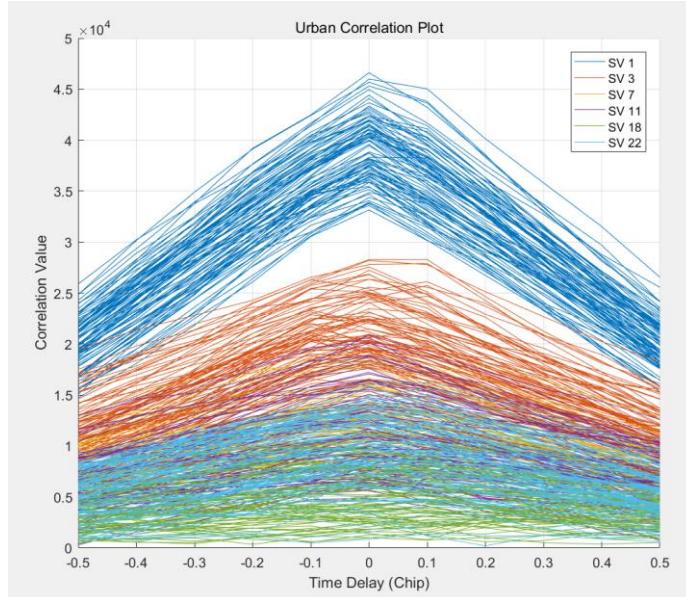


Figure 8. Correlation plots for Urban data

**Analysis:** Compared to OpenSky data, urban environments introduce multipath effects, where signals reflect off buildings and other structures, causing multiple delayed versions of the signal to arrive at the receiver. This can lead to broader and less distinct correlation peaks, as seen in the urban correlation plot. Additionally, buildings and other obstacles can attenuate the signal, reducing the overall correlation values. This is evident in the urban plot, where the correlation values are generally lower compared to the OpenSky plot.

### Task 3 – Navigation data decoding

**Decode the navigation message and extract key parameters, such as ephemeris data, for at least one satellite.**

After tracking, the decoded satellite ephemeris, named 'eph + raw data file name + .mat', is saved, along with the subframe information, named 'sbf + raw data file name + .mat'. Taking PRN 1 as an example, the decoded key parameters of the OpenSky and Urban data are shown as follows (Table 3):

Table3: Decoded Key Parameters of OpenSky and Urban Data for PRN 1

| Parameter | explanation  | Value (OpenSky)     | Value(Urban)        |
|-----------|--|---------------------|---------------------|
| $t_{oe}$  | Ephemerides reference epoch in seconds within the week | 396000              | 453600              |
| $a^{0.5}$ | Square root of semi-major axis                         | 5153.75657081604    | 5153.65564346314    |
| $e$       | Eccentricity   | 0.00388247426599264 | 0.00892308494076133 |
| $M_0$     | Mean anomaly at reference epoch                        | 2.74664157628070    | 0.517930887728971   |
| $w$       | Argument of perigee                                    | 0.999580010005351   | 0.711497598513720   |
| $i_0$     | Inclination at reference                               | 0.970650171544315   | 0.976127704025529   |

|                  | epoch  |   |  |
|------------------|--|---|--|
| $\Omega_0$       | Longitude of ascending node at the beginning of the week | 1.37716785453468                                | -3.10603580061843                              |
| $\Delta n$       | Mean motion difference                                   | 4.40196907396673e-09                            | 4.19088885305685e-09                           |
| i                | Rate of inclination angle                                | -1.30005415247375e-10                           | -1.81078971237415e-10                          |
| $\Omega$         | Rate of node's right ascension                           | -8.04104922769063e-09                           | -8.16962601200122e-09                          |
| $C_{uc}, C_{us}$ | Latitude argument correction                             | -5.73135912418366e-06,<br>6.02193176746368e-06  | -6.33485615253449e-06,<br>5.30108809471130e-06 |
| $C_{rc}, C_{rs}$ | Orbital radius correction                                | 266.0312500000000,<br>-111.1562500000000        | 287.4687500000000,<br>-120.7187500000000       |
| $C_{ic}, C_{is}$ | Inclination correction                                   | -2.60770320892334e-08,<br>-6.33299350738525e-08 | -7.45058059692383e-08,<br>1.60187482833862e-07 |
| $a_0$            | SV clock offset  | -0.000324650201946497                           | -3.48975881934166e-05                          |
| $a_1$            | SV clock drift   | -1.37561073643155e-11                           | -9.43600753089413e-12                          |
| $a_2$            | SV clock drift rate                                      | 0   | 0  |

#### Task 4 – Position and velocity estimation

Using the pseudorange measurements obtained from tracking, implement the Weighted Least Squares (WLS) algorithm to compute user's position and velocity. Plot the user position and velocity, compare it to the provided ground truth values, and comment on the impact of multipath effects on the WLS solution.

Obtain pseudorange measurements from multiple satellites. Start with an initial guess of the user's position and clock bias. Use the solu.mode parameter to set the method for computing the user's position and velocity. If solu.mode is set to 0, it indicates the use of the Weighted Least Squares (WLS) algorithm to compute the user's position and velocity. The position and velocity estimation results are saved in the current folder with the name 'navSolCT\_WLS\_ + num2str(track.pdi) + ms\_ + file.filename'.

| 字段             | 值             |
|----------------|---------------|
| rawPseudorange | 3595x6 double |
| usrPos         | 3595x3 double |
| usrVel         | 3595x3 double |
| usrPosENU      | 3595x3 double |
| usrPosLLH      | 3595x3 double |
| clkBias        | 1x3595 double |
| usrVelENU      | 3595x3 double |
| clkDrift       | 1x3595 double |
| DOP            | []            |
| satEA          | 3595x6 double |
| sataZ          | 3595x6 double |
| localTime      | 3595x1 double |
| codePhaseMeas  | 3595x6 double |

Figure 9: Storage of position and velocity estimation result variables.

For OpenSky and Urban data, the ground truth latitude and longitude coordinates are (22.328444770087565, 114.1713630049711) and (22.3198722, 114.209101777778), respectively. The estimated user position's latitude and longitude results are stored in usrPosLLH, and the specific results are as follows:

| navSolutionsCT.usrPosLLH |         |          |        |   |   |
|--------------------------|---------|----------|--------|---|---|
|                          | 1       | 2        | 3      | 4 | 5 |
| 1                        | 22.3284 | 114.1714 | 2.9998 |   |   |
| 2                        | 22.3284 | 114.1714 | 2.9924 |   |   |
| 3                        | 22.3284 | 114.1714 | 2.9796 |   |   |
| 4                        | 22.3284 | 114.1714 | 2.9613 |   |   |
| 5                        | 22.3284 | 114.1714 | 2.9376 |   |   |
| 6                        | 22.3284 | 114.1714 | 2.9085 |   |   |
| 7                        | 22.3284 | 114.1714 | 2.8739 |   |   |
| 8                        | 22.3284 | 114.1714 | 2.8338 |   |   |
| 9                        | 22.3284 | 114.1714 | 2.7884 |   |   |
| 0                        | 22.3284 | 114.1714 | 2.7374 |   |   |
| 1                        | 22.3284 | 114.1714 | 2.6811 |   |   |
| 2                        | 22.3284 | 114.1714 | 2.6193 |   |   |

Figure 10: Longitude, Latitude, and Height Prediction Results for OpenSky data using the WLS

|    | 1       | 2        | 3       | 4 | 5 |
|----|---------|----------|---------|---|---|
| 1  | 22.3198 | 114.2098 | 46.2169 |   |   |
| 2  | 22.3198 | 114.2097 | 44.6558 |   |   |
| 3  | 22.3197 | 114.2098 | 61.7558 |   |   |
| 4  | 22.3197 | 114.2100 | 95.0503 |   |   |
| 5  | 22.3199 | 114.2096 | 17.4333 |   |   |
| 6  | 22.3199 | 114.2095 | 14.6864 |   |   |
| 7  | 22.3199 | 114.2096 | 29.4117 |   |   |
| 8  | 22.3196 | 114.2099 | 94.0810 |   |   |
| 9  | 22.3198 | 114.2098 | 47.4349 |   |   |
| 10 | 22.3197 | 114.2097 | 50.9768 |   |   |
| 11 | 22.3196 | 114.2099 | 70.9961 |   |   |
| 12 | 22.3196 | 114.2101 | 99.9986 |   |   |
| 13 | 22.3197 | 114.2098 | 58.2782 |   |   |
| 14 | 22.3197 | 114.2096 | 44.5552 |   |   |
| 15 | 22.3198 | 114.2096 | 18.6451 |   |   |
| 16 | 22.3198 | 114.2095 | 19.5301 |   |   |
| 17 | 22.3199 | 114.2095 | 7.7432  |   |   |

Figure 11: Longitude, Latitude, and Height Prediction Results for Urban data using the WLS

In addition, the error between the estimated position and ground truth values was saved in the 'usrPosENU' field with the ENU coordinate system. Furthermore, the estimation errors of the coordinates were visualized using a scatter plot, where the x-axis represents the user's position offset eastward from the reference point (m), and the y-axis represents the offset northward from the reference point. Different points represent different local estimated reception times (s), with the color of the points becoming bluer as time progresses.

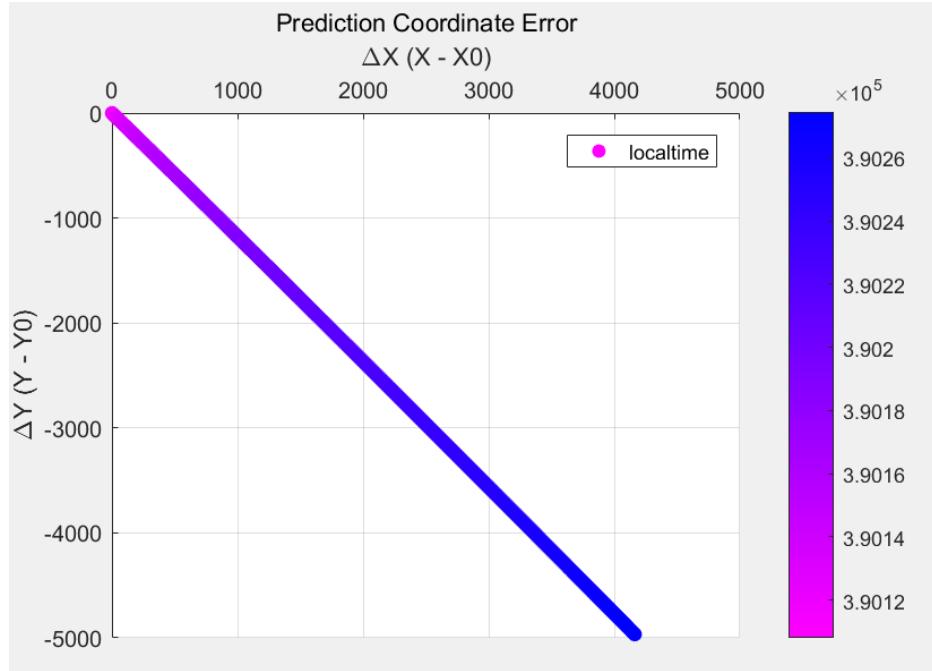


Figure 12. OpenSky position estimation error by WLS algorithm over time

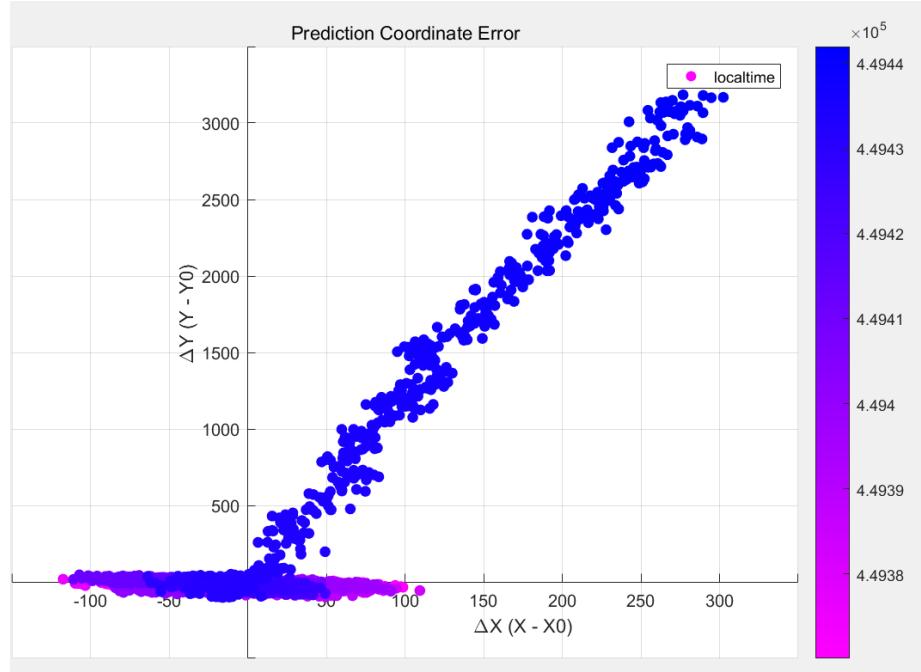


Figure 13. Urban position estimation error by WLS algorithm over time

**Analysis:** Using the WLS algorithm to estimate the user's position, for the OpenSky environment, the error points are distributed along a clearly linear path, and as time progresses (with the color shifting from purple to blue), the error gradually increases. This could be due to some systematic errors (such as receiver clock drift or satellite orbit errors) that have not been fully corrected.

In the Urban environment, the error points are more dispersed, and as time progresses, the error gradually increases and become more dispersed, showing larger offset. This may not only be influenced by systematic errors, but multipath effects and signal occlusion also significantly affect the positioning accuracy, thus affecting the overall positioning accuracy.

At the same time, the velocity components of the user device in the local East-North-Up (ENU) coordinate system were visualized. In this visualization (Figure 14 and 15), the x-axis represents the user's velocity moving eastward, the y-axis represents the user's velocity moving northward, and points in different colors represent the estimated local reception times.

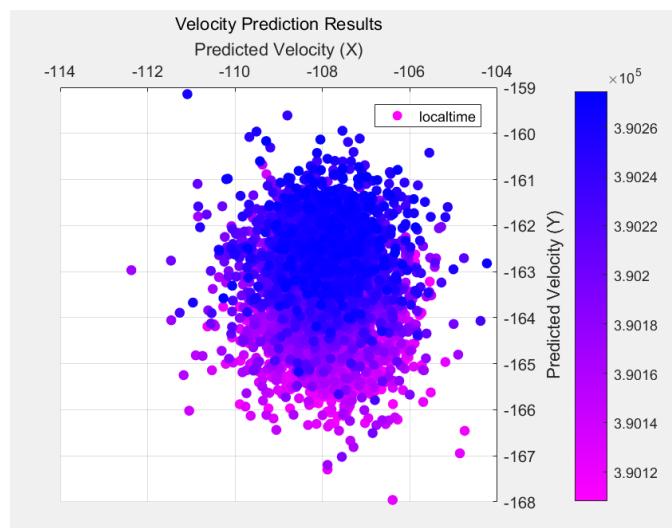


Figure 14. OpenSky data velocity estimation error by WLS algorithm over time

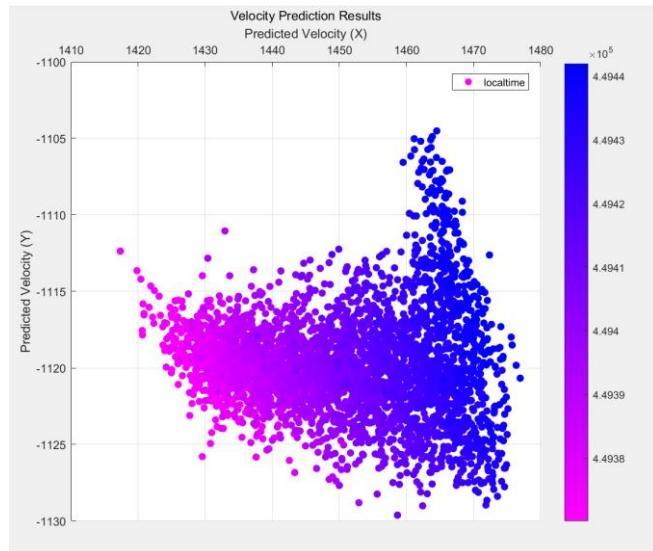


Figure 15. Urban data velocity estimation error by WLS algorithm over time

**Analysis:** In the OpenSky environment, the velocity estimation points estimated using the WLS algorithm show a relatively uniform distribution along the eastward (X-axis) and northward (Y-axis) directions, and the distribution is concentrated. This may be because the signal propagation path in the OpenSky environment is relatively direct, with high signal quality, leading to smaller velocity estimation errors and a more compact distribution of points. It also suggests that over time, the velocity estimation remains relatively stable with little variation. However, in the Urban environment, the velocity estimation points show a more dispersed distribution along the eastward and northward directions, with a noticeable bias trend. Due to the presence of multipath effects and signal occlusion in the Urban environment, the signal quality is poorer, which leads to larger velocity estimation errors and a more dispersed distribution of points. Moreover, as time progresses, the velocity estimation fluctuates more significantly, likely due to environmental changes causing variations in signal quality.

### Task 5 – Kalman filter-based positioning

Develop an Extended Kalman Filter (EKF) using pseudorange and Doppler measurements to estimate user position and velocity.

If solu.mode is set to 1, it represents using the Extended Kalman Filter (EKF) algorithm to compute the user's position and velocity. The position and velocity estimation results are saved in the current folder with the filename 'navSolCT\_EKF\_ + num2str(track.pdi) + ms\_ + file.filename.

| 字段             | 值             |
|----------------|---------------|
| rawPseudorange | 4167x9 double |
| usrPos         | 4167x3 double |
| usrVel         | 4167x3 double |
| usrPosENU      | 4167x3 double |
| usrPosLLH      | 4167x3 double |
| clkBias        | 1x4167 double |
| usrVelENU      | 4167x3 double |
| clkDrift       | 1x4167 double |
| DOP            | []            |
| satEA          | 4167x9 double |
| satAZ          | 4167x9 double |
| localTime      | 4167x1 double |
| codePhaseMeas  | 4167x9 double |

Figure 16: Storage of position and velocity estimation result variables.

For the OpenSky and Urban data, the ground truth latitude and longitude coordinates are (22.328444770087565, 114.1713630049711) and (22.3198722, 114.209101777778), respectively. Using the EKF algorithm, the estimated user position in latitude and longitude is stored in usrPosLLH. The specific results are as follows:

| 1       | 2        | 3      | 4 |
|---------|----------|--------|---|
| 22.3284 | 114.1714 | 2.9998 |   |
| 22.3284 | 114.1714 | 2.9924 |   |
| 22.3284 | 114.1714 | 2.9796 |   |
| 22.3284 | 114.1714 | 2.9613 |   |
| 22.3284 | 114.1714 | 2.9376 |   |
| 22.3284 | 114.1714 | 2.9085 |   |
| 22.3284 | 114.1714 | 2.8739 |   |
| 22.3284 | 114.1714 | 2.8338 |   |
| 22.3284 | 114.1714 | 2.7884 |   |
| 22.3284 | 114.1714 | 2.7374 |   |

Figure 17: Longitude, Latitude, and Height Prediction Results for OpenSky data using the EKF

| 1       | 2        | 3      | 4 |
|---------|----------|--------|---|
| 22.3199 | 114.2091 | 2.2930 |   |
| 22.3199 | 114.2091 | 2.2887 |   |
| 22.3199 | 114.2091 | 2.2847 |   |
| 22.3199 | 114.2091 | 2.2791 |   |
| 22.3199 | 114.2091 | 2.2811 |   |
| 22.3199 | 114.2091 | 2.2792 |   |
| 22.3199 | 114.2091 | 2.2801 |   |
| 22.3199 | 114.2091 | 2.2847 |   |
| 22.3199 | 114.2091 | 2.2747 |   |
| 22.3199 | 114.2091 | 2.2775 |   |

Figure 18: Longitude, Latitude, and Height Prediction Results for Urban data using the EKF

In addition, the error between the estimated position and ground truth values is saved in the 'usrPosENU' field using the ENU coordinate system. Furthermore, the estimation error of the coordinates is visualized using a scatter plot, where the x-axis represents the user's displacement eastward from the reference point (in meters), the y-axis represents the displacement northward from the reference point, and different points represent different local estimated reception times (in seconds). The further in time, the bluer the color of the points.

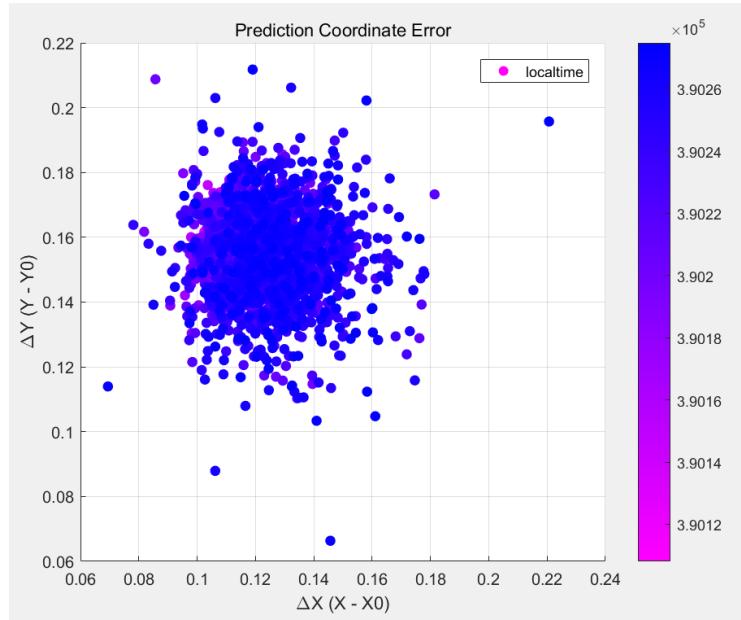


Figure 19. OpenSky data position estimation error by EKF algorithm over time

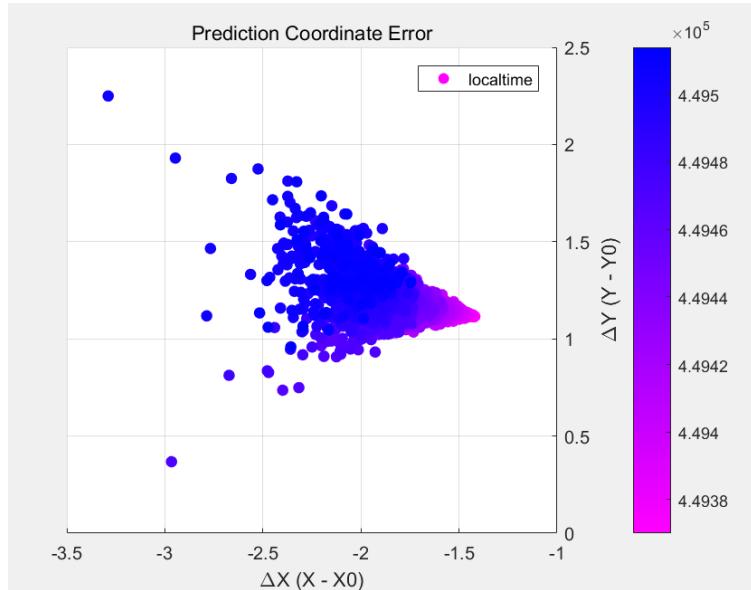


Figure 20. Urban data position estimation error by EKF algorithm over time

**Analysis:** In the OpenSky environment, the error points are more concentrated, and the error magnitude is relatively small, indicating good positioning accuracy. Furthermore, as time progresses, the error remains relatively stable, demonstrating good system stability and excellent positioning performance. In contrast, in the Urban environment, the error points show greater dispersion, and as time passes, the error not only increases but also exhibits a certain bias trend. This may be due to signal quality fluctuations caused by environmental changes. Additionally, compared to the WLS algorithm, the use of the EKF algorithm significantly reduces the user position estimation error in both the Urban and OpenSky environments. This could be because the EKF can update the state estimate in real-time, adapting to dynamic environmental changes. Moreover, the EKF is better at handling complex dynamic models and nonlinear relationships, improving positioning accuracy.

At the same time, the velocity components of the estimated user device in the local East-North-Up (ENU) coordinate system were visualized. The x-axis represents the user's velocity moving eastward, the y-axis represents the user's velocity moving northward, and the points of different colors represent the estimated local reception times.

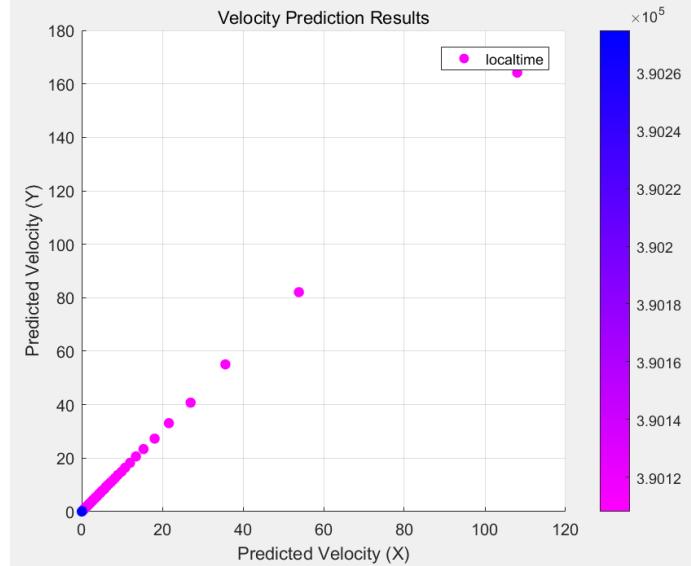


Figure 21. OpenSky data velocity estimation error by EKF algorithm over time

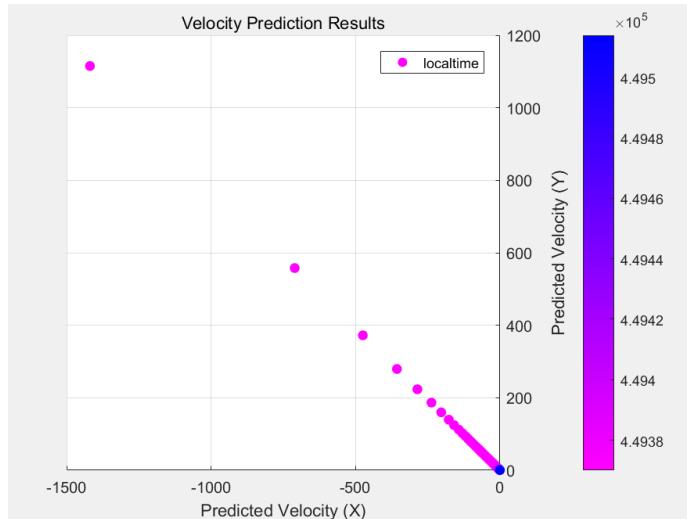


Figure 22. Urban data velocity estimation error by EKF algorithm over time

Using the EKF algorithm to estimate the user's velocity, in the OpenSky environment, where the signal quality is higher, the velocity estimation is quite accurate. As time progresses, the velocity decreases linearly, gradually approaching zero. In the Urban environment, the initial velocity estimation error is relatively large, but over time, the velocity decreases linearly and approaches zero. This indicates that the EKF algorithm can accurately estimate the velocity in both OpenSky and Urban environments. Especially in open spaces with minimal signal obstruction and multipath effects, such as in the OpenSky environment, the velocity estimation results are superior to those of the WLS algorithm.

**References**

Xu, Bing, and Li-Ta Hsu. "Open-source MATLAB code for GPS vector tracking on a software-defined receiver." GPS solutions 23.2 (2019): 46.

**Declaration**

The code for this assignment is modified based on the original code (from References, written by Prof. Xu, Bing, and Li-Ta Hsu.).