

Homework #3
Due by Friday 5/4, 11:55pm

Submission instructions:

1. You should submit your homework in the NYU Classes system.
2. For this assignment, you should turn in 7 files:
 - Six '.cpp' files, one for each question 1 to 6.
Name your files 'YourNetID_hw3_q1.cpp', 'YourNetID_hw3_q2.cpp', etc.
 - A '.pdf' file with your answers for questions 7-12.
Name your file 'YourNetID_hw3_q7to12.pdf'
3. For the coding questions, pay special attention to the style of your code. Indent your code correctly, choose meaningful names for your variables, define constants where needed, choose the most appropriate control flow statements, etc.
4. For the math questions, explain your answers.

Question 1:

Write a program that computes how much a customer has to pay after purchasing two items. The price is calculated according to the following rules:

- Buy one get one half off promotion: the lower price item is half price.
- If the customer is club card member, additional 10% off.
- Tax is added.

Inputs to the program include:

- Two items' prices
- Have club card or not (User enters 'Y' or 'y' for "yes"; 'N' or 'n' for "no")
- Tax rate (User enters the percentage as a number; for example they enter 8.25 if the tax rate is 8.25%)

Program displays:

- Base price - the price before the discounts and taxes
- Price after discounts - the price after the buy one get one half off promotion and the member's discount, if applicable
- Total price - the amount of money the customer has to pay (after tax).

Your program should interact with the user **exactly** as it shows in the following example:

```
Enter price of first item: 10
Enter price of second item: 20
Does customer have a club card? (Y/N): y
Enter tax rate, e.g. 5.5 for 5.5% tax: 8.25
Base price: 30.0
Price after discounts: 22.5
Total price: 24.35625
```

Question 2:

Write a program that:

- Asks the user for their name.
- Asks the user to input their graduation year.
- Asks the user to input the current year.

Assume the student is in a four-year undergraduate program. Display the current status the student is in. Possible status include: not in college yet, freshman, sophomore, junior, senior, graduated.

Note: If graduation year equals to current year, status is 'Graduated'; if graduation year is four years after current year, status is 'Freshman', etc.

Your program should interact with the user **exactly** as it shows in the following example:

```
Please enter your name: Jessica
Please enter your graduation year: 2019
Please enter current year: 2015
Jessica, you are a Freshman
```

Question 3:

Write a program that does the following:

- Ask user to input three Real numbers a, b and c. They represent the parameters of a quadratic equation $ax^2 + bx + c = 0$
- Classify to one of the following:
 - 'Infinite number of solutions' (for example, $0x^2 + 0x + 0 = 0$ has infinite number of solutions)
 - 'No solution' (for example, $0x^2 + 0x + 4 = 0$ has no solution)
 - 'No real solution' (for example, $x^2 + 4 = 0$ has no real solutions)
 - 'One real solution'
 - 'Two real solutions'
- In cases there are 1 or 2 real solutions, also print the solutions.

Notes:

1. If $a \neq 0$ and there are real solutions to the equation, you can get these solutions using the following formula:

$$x_{1,2} = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

The number of solutions depends on whether $(b^2 - 4ac)$ is positive, zero, or negative.

2. In order to calculate the square root of a number (of type **double**), you should call the **sqrt** function, located in the **cmath** library.

Follow the syntax as demonstrated in the code below:

```
#include <iostream>
#include <cmath>
using namespace std;

int main() {
    double x = 2.0;
    double sqrtResult;

    sqrtResult = sqrt(x);
    cout<<sqrtResult<<endl;

    return 0;
}
```

Note that you first need to include the **cmath** library, and then you can call the **sqrt** function, passing the argument that you want to calculate the square root of, enclosed in parentheses.

Your program should interact with the user **exactly** as it shows in the following example:

Please enter value of a: 1

Please enter value of b: 4

Please enter value of c: 4

This equation has a single real solution x=-2.0

Question 4:

Define the following constants:

```
const int FLOOR_ROUND = 1;  
const int CEILING_ROUND = 2;  
const int ROUND = 3;
```

Write a program that asks the user to enter a Real number, then it asks the user to enter the method by which they want to round that number (floor, ceiling or to the nearest integer). The program will then print the rounded result.

Your program should interact with the user **exactly** as it shows in the following example:

Please enter a Real number:

4.78

Choose your rounding method:

1. Floor round
2. Ceiling round
3. Round to the nearest whole number

2

5

Implementation requirement: Use a **switch** statement.

Question 5:

Body mass index (BMI) is a number calculated from a person's weight and height using the following formula: $weight/height^2$. Where *weight* is in kilograms and *height* is in meters.

According to the Centers for Disease Control and Prevention, the BMI is a fairly reliable indicator of body fatness for most people. BMI does not measure body fat directly, but research has shown that BMI correlates to direct measures of body fat, such as underwater weighing and dual-energy X-ray absorptiometry.

The following table gives the weight status in respect to the BMI value:

BMI Range	Weight Status
Below 18.5	Underweight
[18.5, 25)	Normal
[25, 30)	Overweight
30 and above	Obese

Write a program that prompts for weight (in pounds) and height (in inches) of a person, and prints the weight status of that person.

Your program should interact with the user **exactly** as it shows in the following example:

Please enter weight (in pounds): 135

Please enter height (in inches): 71

The weight status is: Normal

Note: 1 pound is 0.453592 kilograms and 1 inch is 0.0254 meters.

Question 6:

Write a program that computes the cost of a long-distance call. The cost of the call is determined according to the following rate schedule:

- Any call started between 8:00 A.M. and 6:00 P.M., Monday through Friday, is billed at a rate of \$0.40 per minute.
- Any call starting before 8:00 A.M. or after 6:00 P.M., Monday through Friday, is charged at a rate of \$0.25 per minute.
- Any call started on a Saturday or Sunday is charged at a rate of \$0.15 per minute.

The input will consist of the day of the week, the time the call started, and the length of the call in minutes.

The output will be the cost of the call.

Notes:

1. The time is to be input in 24-hour notation, so the time 1:30 P.M. is input as 13:30
2. The day of the week will be read as one of the following two character string: Mo Tu We Th Fr Sa Su
3. The number of minutes will be input as a positive integer.

Question 7:

How many strings of eight uppercase English letters are there

- a) if letters can be repeated?
- b) if no letter can be repeated?
- c) that start with X, if letters can be repeated?
- d) that start with X, if no letter can be repeated?

Question 8:

How many one-to-one functions are there from a set with five elements to sets with the following number of elements?

- a) 4
- b) 5
- c) 6
- d) 7

Question 9:

How many subsets of a set with 100 elements have more than one element?

Question 10:

In how many ways can a photographer at a wedding arrange 6 people in a row from a group of 10 people, where the bride and the groom are among these 10 people, if

- a) the bride must be in the picture?
- b) both the bride and groom must be in the picture?
- c) exactly one of the bride and the groom is in the picture?

Question 11:

How many bit strings of length 12 contain

- a) exactly three 1s?
- b) at most three 1s?
- c) at least three 1s?

Question 12:

How many permutations of the letters ABCDEFGH

- a) contain the string DE?
- b) the letters E and D are not next to one another?
- c) contain either CD or DE?