ICNPG 2023

Clase 9:

Álgebra lineal Densa, Rala y Grafos...



Algebra Lineal Numérica

- **CUFFT**: Una transformación lineal particular.
- **CUBLAS**: operaciones tipo I, II y III, optimizado para formatos de matriz densa.
- **NVBLAS**: si tu viejo programa C, octave, etc, usa BLAS, lo acelerás recompilando.
- **CUSPARSE**: operaciones de CUBLAS optimizadas para formatos ralos, etc.
- **CUSOLVER**: Resolución de Sistemas lineales, Autovalores, factorizaciones, etc.
- **NVGRAPH**/**CUGRAPH**: formatos y algoritmos para redes o grafos.
- **CUPY**: Python interfaces to many of the functions in the CUDA device/runtime, CUBLAS, CUFFT, and CUSOLVER.
- MAGMA: Como CUSOLVER+CUBLAS+CUSPARSE pero pensada para sistemas híbridos CPU/GPU.
- **Array-Fire**: librería de C++ library paralela con una API sencilla, para cpu, cuda y opencl! (y Python)

A Common Library Workflow

Many CUDA libraries share concepts, features, and a common workflow when being called from a host application. A common workflow while using NVIDIA libraries is as follows:

- Create a library-specific handle that manages contextual information useful for the library's operation.
- 2. Allocate device memory for inputs and outputs to the library function.
- **3.** If inputs are not already in a library-supported format, convert them to be accessible by the library.
- **4.** Populate the pre-allocated device memory with inputs in a supported format.
- **5.** Configure the library computation to be executed.
- **6.** Execute a library call that offloads the desired computation to the GPU.
- 7. Retrieve the results of that computation from device memory, possibly in a library-determined format.
- **8.** If necessary, convert the retrieved data to the application's native format.
- 9. Release CUDA resources. Si la librería es de alto nivel, esto se hace solo
- **10.** Continue with the remainder of the application.

CuBLAS: Basic Linear Algebra Subprograms

- Operaciones (números reales o complejos):
 - Level I: functions that perform scalar and vector based operations.
 - Level II: functions that perform matrix-vector operations.
 - Level III: functions that perform matrix-matrix operations.
- Cublas API: Mas control, pero hay que manejar memoria del host y del device.
- **CublasXt API:** Menos control, pero solo hace falta manejar memoria del host.
- **Paralelismo:** soporta streams y multi-gpu, útiles para "batchear". El precio a pagar es la comunicación entre las GPUs
- Compilación:

Es como un sistema de colas. Le mando muchos trabajos distintos a la GPU para que los paralelice

- nvcc myCublasApp.c -lcublas -o myCublasApp
 para linkear con la librería
- g++ myCublasApp.c -lcublas_static -lculibos -lcudart_static -lpthread -ldl -I <cuda-toolkit-path>/include -L
 <cuda-toolkit-path>/lib64 -o myCublasApp
- Ejemplo (level III):

/share/apps/icnpg/clases/Cuda_Basico/MultMat/soluciones/multmat_solucion.cu

Multiplicacion de Matrices de 1024x1024 en nuestro cluster

naive CPU: 6023.591623 ms (1x)

naive GPU: 120.343554 ms (50x) CUBLASXT: 17.587757 ms (300x) CUBLAS: 9.224054 ms (600x)

https://docs.nvidia.com/cuda/cublas/index.html

CuBLAS levels

scalar and vector based operations

▽ 2.5. cuBLAS Level-1 Function Reference
2.5.1. cublasI <t>amax()</t>
2.5.2. cublasI <t>amin()</t>
2.5.3. cublas <t>asum()</t>
2.5.4. cublas <t>axpy()</t>
2.5.5. cublas <t>copy()</t>
2.5.6. cublas <t>dot()</t>
2.5.7. cublas <t>nrm2()</t>
2.5.8. cublas <t>rot()</t>
2.5.9. cublas <t>rotg()</t>
2.5.10. cublas <t>rotm()</t>
2.5.11. cublas <t>rotmg()</t>
2.5.12. cublas <t>scal()</t>
2.5.13. cublas <t>swap()</t>

matrix-vector operations.

∇ 2.6. cuBLAS Level-2 Function Reference
2.6.1. cublas <t>gbmv()</t>
2.6.2. cublas <t>gemv()</t>
2.6.3. cublas <t>ger()</t>
2.6.4. cublas <t>sbmv()</t>
2.6.5. cublas <t>spmv()</t>
2.6.6. cublas <t>spr()</t>
2.6.7. cublas <t>spr2()</t>
2.6.8. cublas <t>symv()</t>
2.6.9. cublas <t>syr()</t>
2.6.10. cublas <t>syr2()</t>
2.6.11. cublas <t>tbmv()</t>
2.6.12. cublas <t>tbsv()</t>
2.6.13. cublas <t>tpmv()</t>
2.6.14. cublas <t>tpsv()</t>
2.6.15. cublas <t>trmv()</t>
2.6.16. cublas <t>trsv()</t>
2.6.17. cublas <t>hemv()</t>
2.6.18. cublas <t>hbmv()</t>
2.6.19. cublas <t>hpmv()</t>
2.6.20. cublas <t>her()</t>
2.6.21. cublas <t>her2()</t>
2.6.22. cublas <t>hpr()</t>
2.6.23. cublas <t>hpr2()</t>

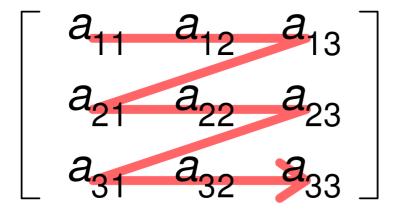
matrix-matrix operations.

∇ 2.7. cuBLAS Level-3 Function Reference
2.7.1. cublas <t>gemm()</t>
2.7.2. cublas <t>gemm3m()</t>
2.7.3. cublas <t>gemmBatched()</t>
2.7.4. cublas <t>gemmStridedBatched()</t>
2.7.5. cublas <t>symm()</t>
2.7.6. cublas <t>syrk()</t>
2.7.7. cublas <t>syr2k()</t>
2.7.8. cublas <t>syrkx()</t>
2.7.9. cublas <t>trmm()</t>
2.7.10. cublas <t>trsm()</t>
2.7.11. cublas <t>trsmBatched()</t>
2.7.12. cublas <t>hemm()</t>
2.7.13. cublas <t>herk()</t>
2.7.14. cublas <t>her2k()</t>
2.7.15. cublas <t>herkx()</t>

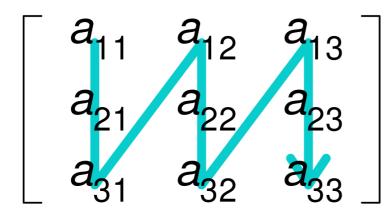
Data layout

Todas las librerías aceptan matrices ordenadas linealmente, solo hay que decirle si están ordenadas column major o row major. CuBLAS asume column major

Row-major order



Column-major order



1.1. Data layout

For maximum compatibility with existing Fortran environments, the cuBLAS library uses column-major storage, and 1-based indexing. Since C and C++ use row-major storage, applications written in these languages can not use the native array semantics for two-dimensional arrays. Instead, macros or inline functions should be defined to implement matrices on top of one-dimensional arrays. For Fortran code ported to C in mechanical fashion, one may chose to retain 1-based indexing to avoid the need to transform loops. In this case, the array index of a matrix element in row "i" and column "j" can be computed via the following macro

#define IDX2F(i,j,ld)
$$((((j)-1)*(ld))+((i)-1))$$

Here, ld refers to the leading dimension of the matrix, which in the case of column-major storage is the number of rows of the allocated matrix (even if only a submatrix of it is being used).

For natively written C and C++ code, one would most likely choose 0-based indexing, in which case the array index of a matrix element in row "i" and column "j" can be computed via the following macro

#define IDX2C(i,j,ld) (((j)*(ld))+(i))

CuSPARSE: cuBLAS para matrices ralas

The cuSPARSE library contains a set of GPU-accelerated basic linear algebra subroutines used for handling sparse matrices that perform significantly faster than CPU-only alternatives. Depending on the specific operation, the library targets matrices with sparsity ratios in the range between 70%-99.9%.

sparse matrix = matriz ralas

- > Operations between a sparse vector and a dense vector: sum, dot product, scatter, gather
- Operations between a dense matrix and a sparse vector: multiplication
 - > Operations between a sparse matrix and a dense vector: multiplication, triangular solver, tridiagonal solver, pentadiagonal solver
 - > Operations between a sparse matrix and a dense matrix: multiplication, triangular solver, tridiagonal solver, pentadiagonal solver
 - > Operations between a sparse matrix and a sparse matrix: sum, multiplication
 - > Operations between dense matrices with output a sparse matrix: multiplication
 - > Sparse matrix preconditioners: Incomplete Cholesky Factorization (level 0), Incomplete LU Factorization (level 0)
 - > Reordering and Conversion operations between different sparse matrix storage formats
- **Formateo**: operations that allow conversion between different matrix formats, and compression of **csr** matrices.

cimpressed-sparsed-rows

- Compilación:
 - nvcc myCusparseApp.c -lcusparse -o myCusparseApp
 - g++ myCusparseApp.c -lcusparse_static -lculibos -lcudart_static -lpthread -ldl -I <cuda-toolkit-path>/include -L <cuda-toolkit-path>/lib64 -o myCusparseApp
- **Ejemplos:** copiar del toolkit...

https://docs.nvidia.com/cuda/cusparse/index.html

CuSPARSE: Formatos de vectores

Vectores Densos

single data array that is stored linearly in memory 1.0 0.0 0.0 2.0 3.0 0.0 4.0

Se guarda todo, inclusive los valores nulos

Vectores Ralos

Se guardan los elementos distintos de cero y las posiciones

1.0 2.0 3.0 4.0

The data array has the nonzero values from the equivalent array in dense format.

The integer index array has the positions of the corresponding nonzero values in the equivalent array in dense format.

CuSPARSE: Formatos de Matrices

Matrices Densas

The dense matrix X is assumed to be stored in **column-major format in memory**

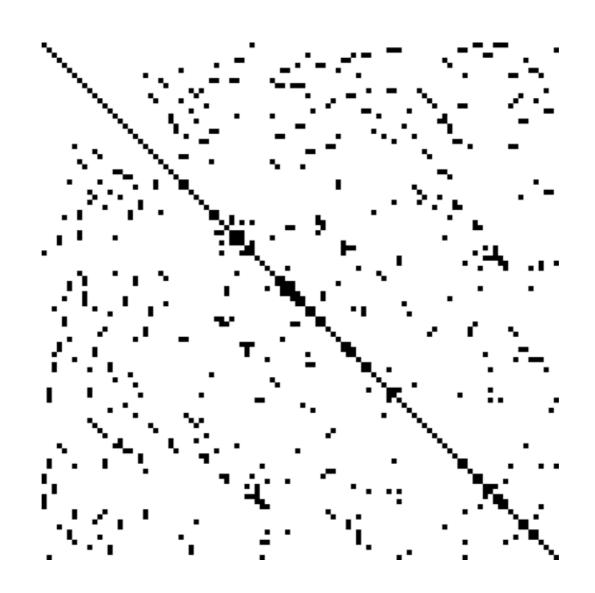
$$X_{1,1} \quad X_{2,1} \quad \cdots \quad X_{m,1} \quad \cdots \quad X_{ldX,1} \quad \cdots \quad X_{1,n} \quad X_{2,n} \quad \cdots \quad X_{m,n} \quad \cdots \quad X_{ldX,n}$$

and is represented by the following parameters.

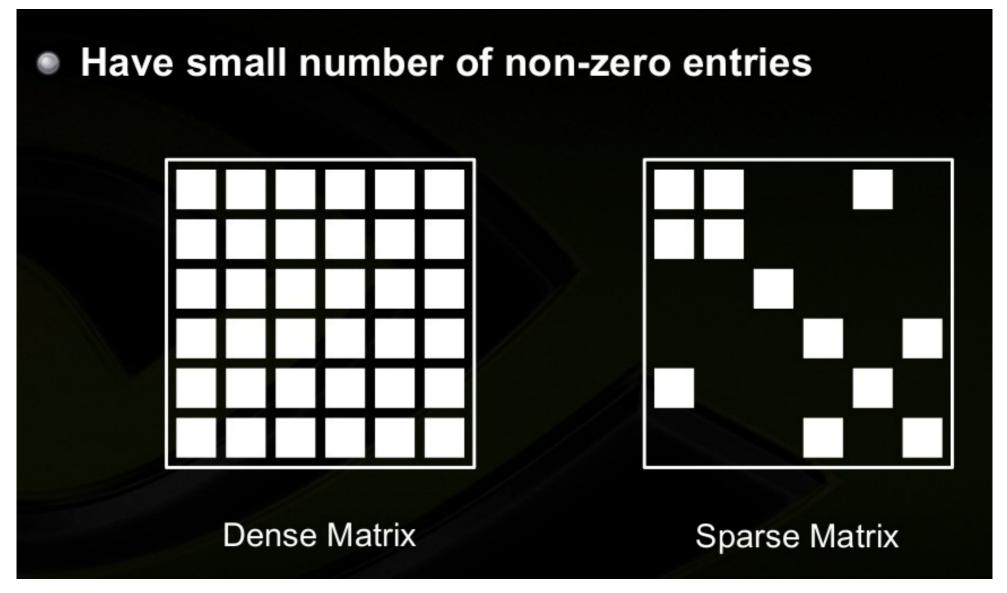
m	(integer)	The number of rows in the matrix.	
n	(integer)	The number of columns in the matrix.	
ldX	(integer)	The leading dimension of x , which must be greater than or equal to m . If $1dx$ is greater than m , then x represents a sub-matrix of a larger matrix stored in memory, es decir, uno podría trabajar con una submatriz	
Х	(pointer)	Points to the data array containing the matrix elements. It is assumed that enough storage is allocated for $\bar{\mathbf{x}}$ to hold all of the matrix elements and that cuSPARSE library functions may access values outside of the sub-matrix, but will never overwrite them.	

CuSPARSE: Formatos de Matrices

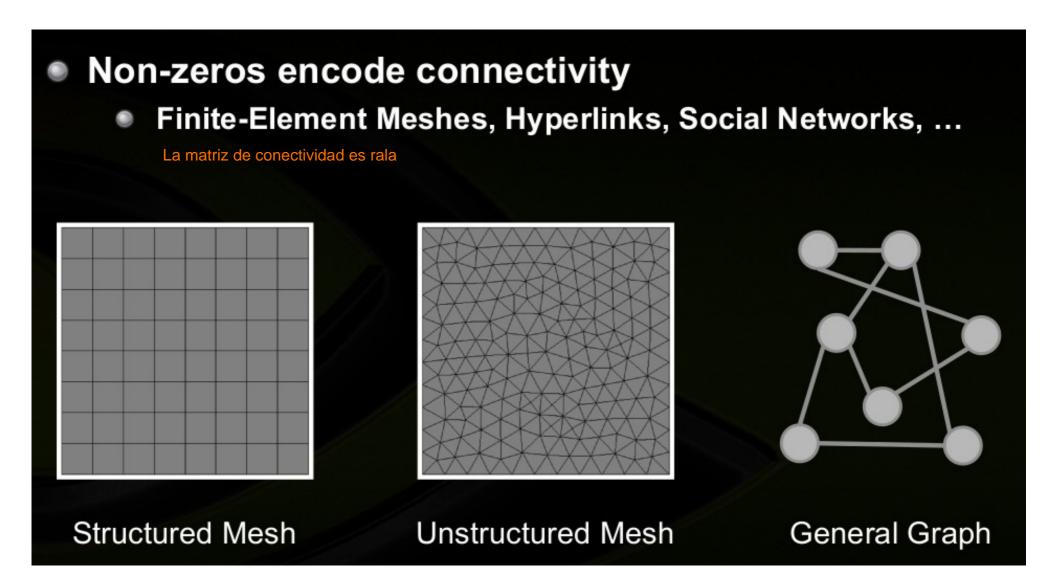
Matrices Ralas



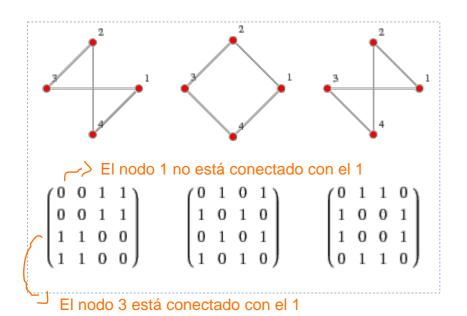
Que son las matrices ralas (sparse matrix)?

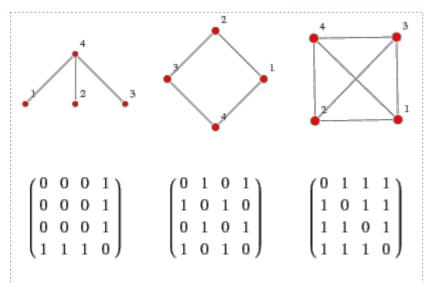


Donde aparecen las matrices ralas?



Matriz de conectividad o adyacencia





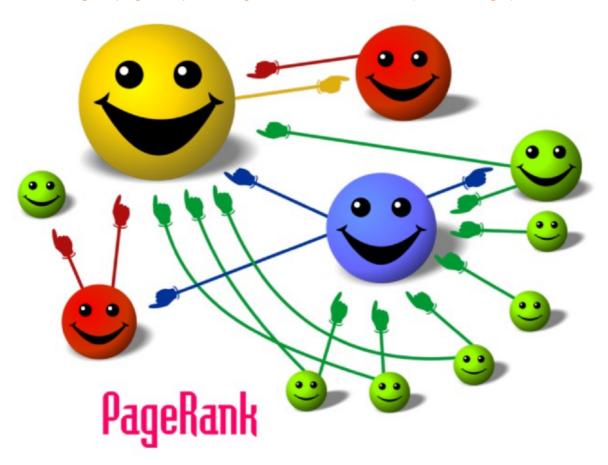
La matriz es basicamente una estructura de datos muy útil para representar y manipular grafos en programas de computadora.

The adjacency matrix, sometimes also called the connection matrix, of a simple labeled graph is a matrix with rows and columns labeled by graph vertices, with a 1 or 0 in position according to whether and are adjacent or not. For a simple graph with no self-loops, the adjacency matrix must have 0s on the diagonal. For an undirected graph, the adjacency matrix is symmetric.

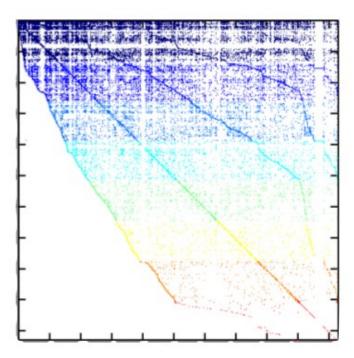
http://mathworld.wolfram.com/AdjacencyMatrix.html

Matrices: Page Rank (Brin, Page)

Ranking de páginas que da lugar a un buscador web (como Google)



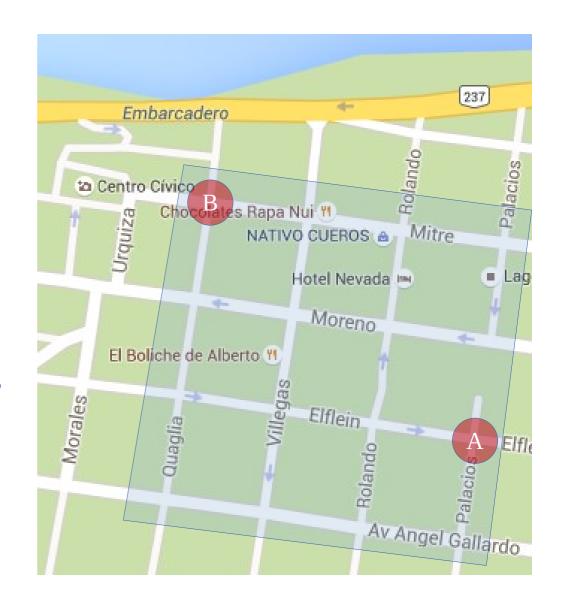
$$A_{ij}$$
=1 si i \longrightarrow j



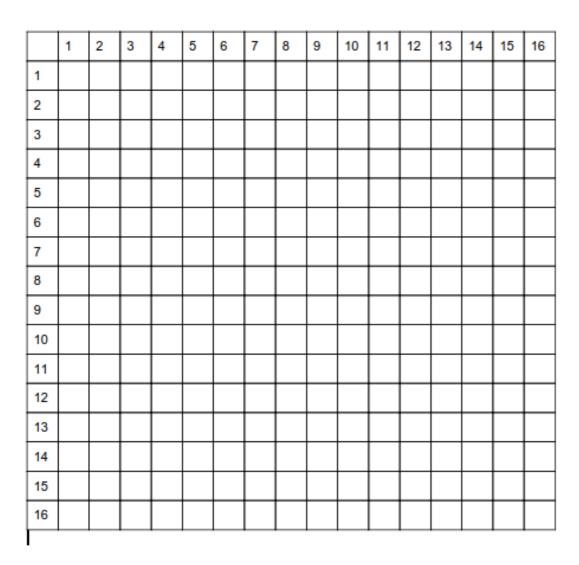
Ejercicio

- Mitre, Moreno, Elflein, Gallardo.
- Quaglia, Villegas, Rolando, Palacios.
- Salgo de (A) Elflein y Palacios
- Llego a (B) Mitre y Quaglia
- ¿camino mas corto?
- ¿cuantos caminos de n cuadras hay?
- ¿Cuantos caminos de hasta n cuadras?
- ¡A pie no es igual que en auto!
- Etc.

Todo esto se puede responder usando teoría de grafos



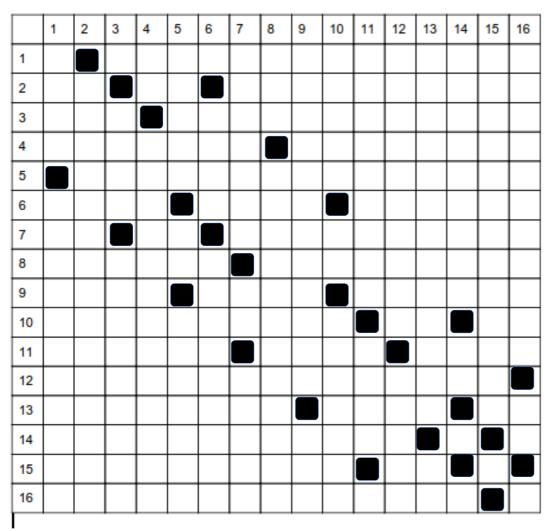
Matriz de conectividad en auto (2016!)





Matriz de conectividad en auto

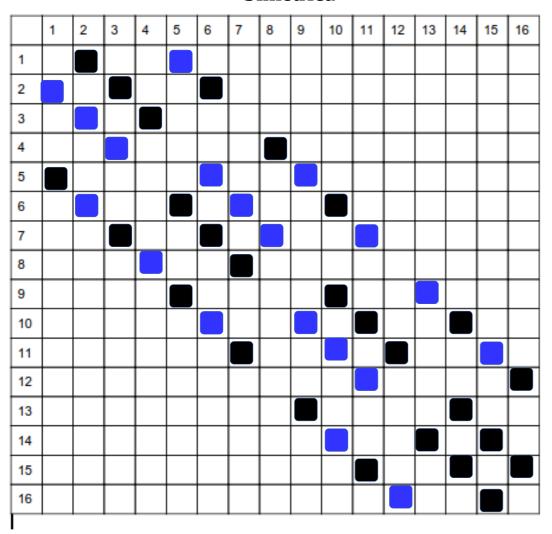
No simétrica





¿Matriz de conectividad a pie?

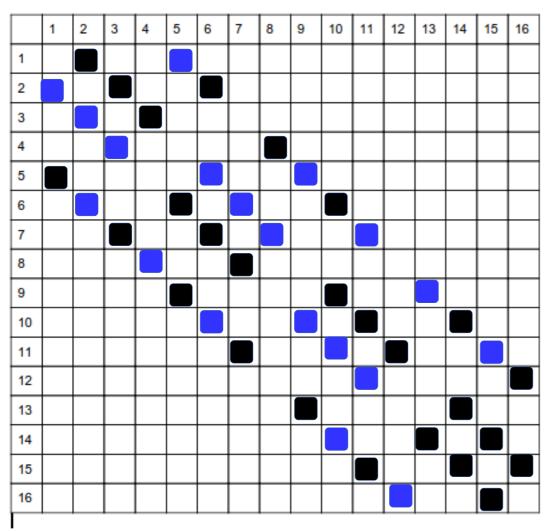
Simétrica





Test de vigilia ...

Simétrica





Conectividad a pie...











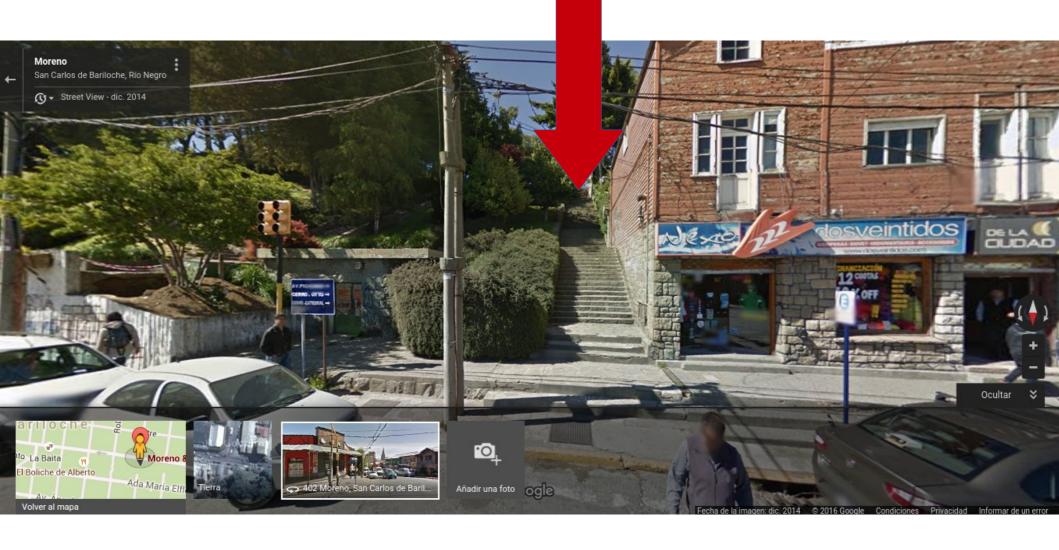






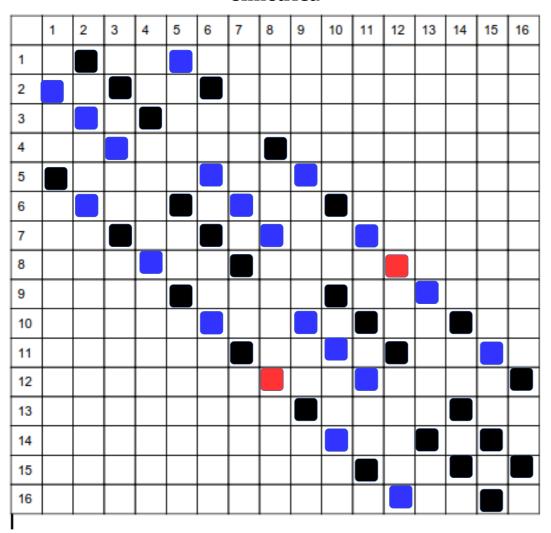


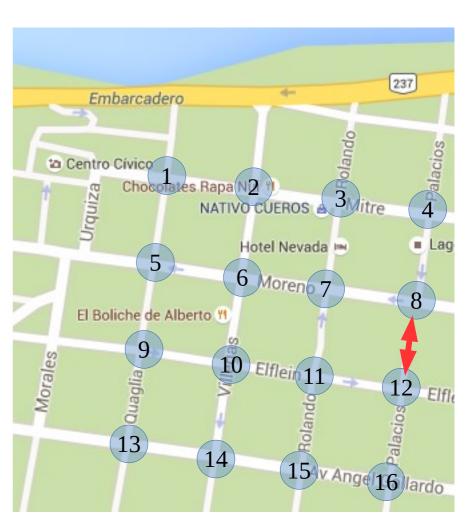




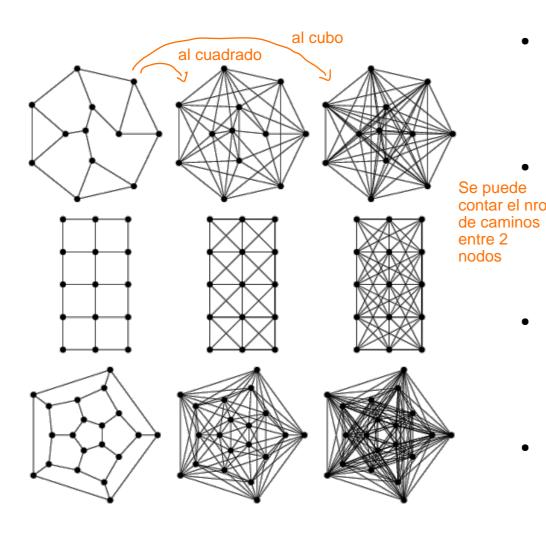
¿Matriz de conectividad a pie?

simétrica





Propiedades de la matriz de adyacencia



The kth power of a graph G is a graph with the same set of vertices as G and an edge between two vertices iff there is a path of length at most k between them.

Since a path of length two between vertices u and v exists for every vertex w such that {u,w} and {w,v} are edges in G, the square of the adjacency matrix of G counts the number of such paths.

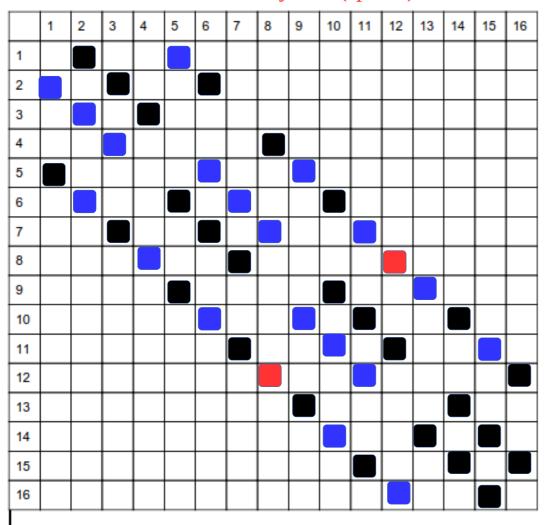
- Similarly, the (u,v)th element of the kth power of the adjacency matrix of G gives the number of paths of length k between vertices u and v.
- The graph kth power is then defined as the graph whose adjacency matrix given by the sum of the first k powers of the adjacency matrix,

 $adj(G^k)=sum_{i=1}^k[adj(G)]^i$, which counts all paths of length up to k.

http://mathworld.wolfram.com/GraphPower.html

Caminos mas cortos, entre uno o mas puntos, o número de caminos de k pasos entre dos puntos, etc, etc.

Simétrica y rala (sparse)





Ecuación de Laplace

- Ecuación de difusión
- Ecuación del calor
- Membrana elástica

 $V = f_O(y)$

- Electrostática...
- Etc.

$$V = f_N(x)$$

$$(\partial_x^2 + \partial_y^2)V = 0$$

$$V(x,y) = ?$$

$$V = f_E(y)$$

$$V = f_S(x)$$

Método de Jacobi

$$V_{i,j}^{n+1} = \frac{1}{4} (V_{i+1,j}^n + V_{i-1,j}^n + V_{i,j+1}^n + V_{i,j-1}^n)$$

	$V_{i,j+1}^n$	
$V_{i-1,j}^n$	$V_{i,j}^{n+1}$	$V_{i+1,j}^n$
	$V_{i,j-1}^n$	

Método de Jacobi

$$V_{i,j}^{n+1} = \frac{1}{4} (V_{i+1,j}^n + V_{i-1,j}^n + V_{i,j+1}^n + V_{i,j-1}^n)$$

En algebra lineal numérica toda matriz es un vector

$$\alpha(i,j) = i + jL = 0, 1, ..., L^2 - 1 \to V_{\alpha}^{n+1} = \sum_{\beta} A_{\alpha,\beta} V_{\beta}^n$$

Método de Jacobi

$$V_{i,j}^{n+1} = \frac{1}{4} (V_{i+1,j}^n + V_{i-1,j}^n + V_{i,j+1}^n + V_{i,j-1}^n)$$

$$V_{\alpha}^{n+1} = \sum_{\beta} A_{\alpha,\beta} V_{\beta}^n$$

$$\mathbf{V}^{n+1} = \mathbf{A}.\mathbf{V}^{\mathbf{n}}$$

¿Cuantos elementos distintos de cero tiene A?

A matriz real de $L^2 \times L^2$ rala

Convolución o Correlación

$$y_i = \sum_k h_k x_{k+i} \to \mathbf{y} = \mathbf{H}.\mathbf{x}$$

¿Cuantos elementos distintos de cero tiene H si el filtro es local?

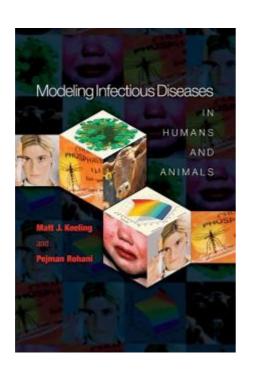
El filtro puede representar un operador diferencial discretizado

Por ejemplo en 1D Esto se llama un "extensil"
$$\mathbf{h} = \{1, -2, 1\}/\Delta x^2 \rightarrow$$

$$y_i = \sum_{k} h_k u_{k+i} = \frac{u_{i+1} + u_{i-1} - 2u_i}{\Delta x^2} \equiv \partial_x^2 u$$

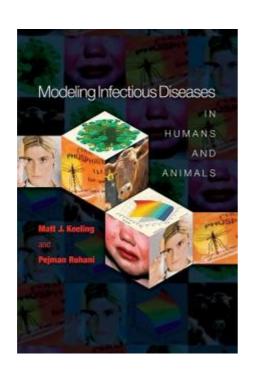
En general los operadores diferenciales locales dan una H rala.

Ejemplo: epidemias



$$\begin{split} \frac{dS}{dt} &= \mu - \beta SI - \mu S, \\ \frac{dI}{dt} &= \beta SI - \gamma I - \mu I, \\ \frac{dR}{dt} &= \gamma I - \mu R. \end{split}$$

Ejemplo: epidemias

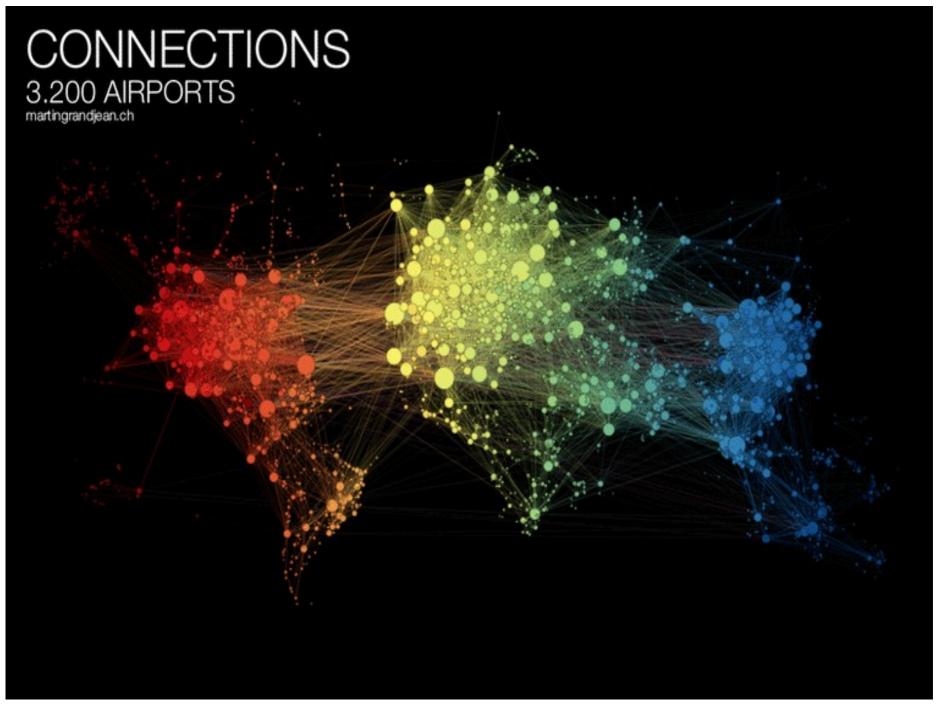


$$\frac{dX_i}{dt} = \nu_i N_i - \lambda_i X_i - \mu_i X_i,$$

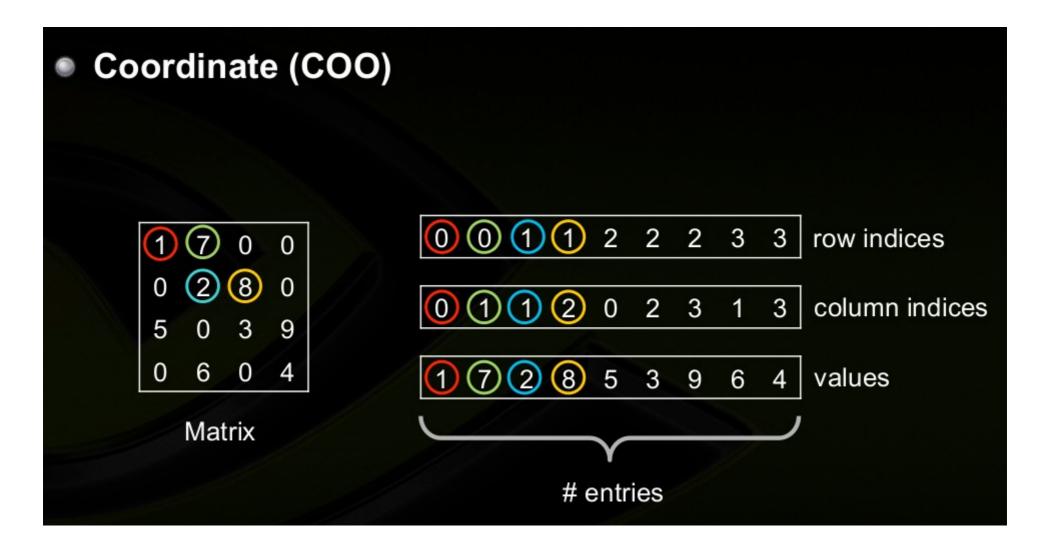
$$\frac{dY_i}{dt} = \lambda_i X_i - \gamma_i Y_i - \mu_i Y_i,$$

$$\lambda_i = \beta_i \sum_j \rho_{ij} \frac{X_j}{N_i},$$

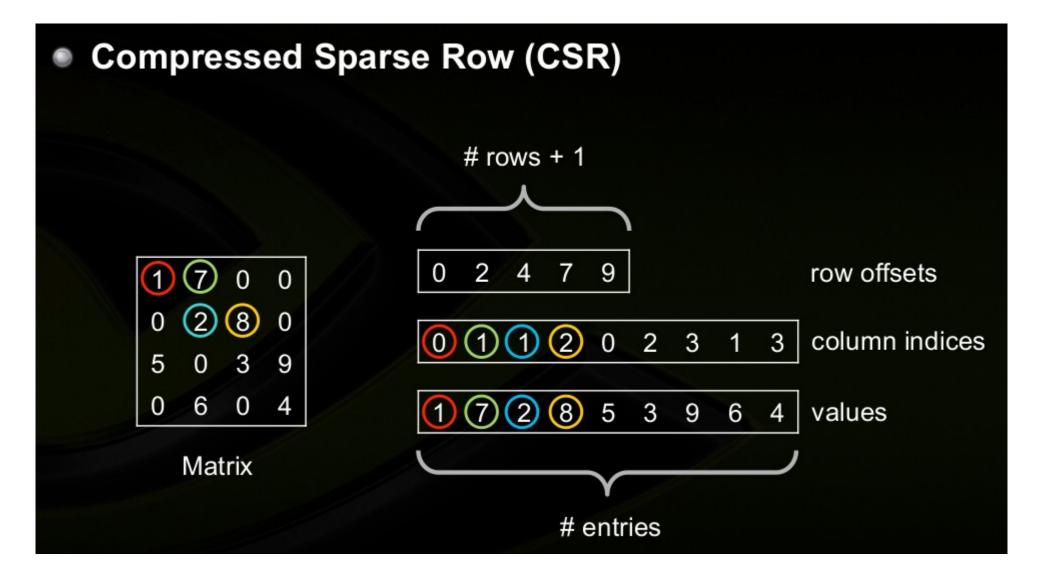
Elementos de matriz Típicamente rala

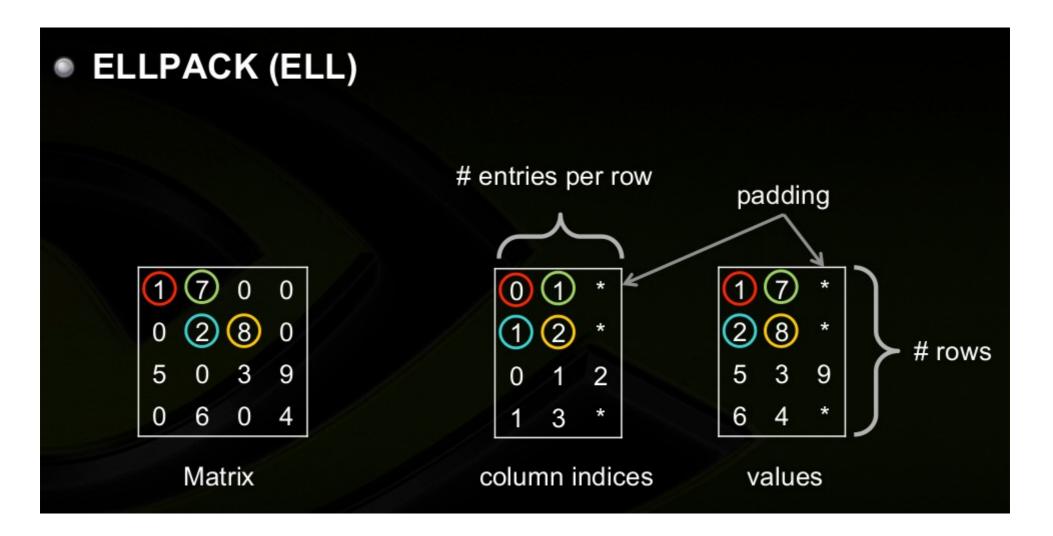


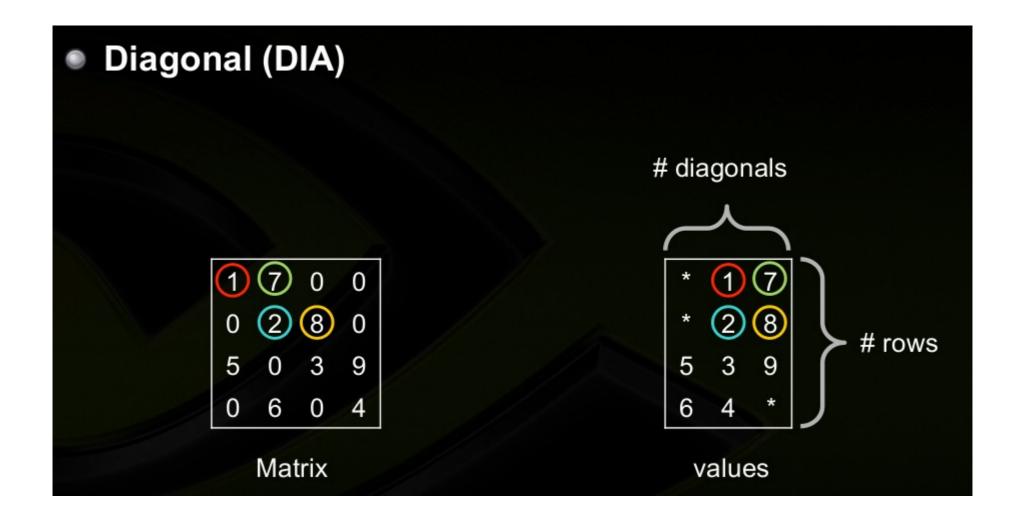
Matriz de adyacencia rala... *Viajan personas... portando enfermedades, mercancías, etc!*

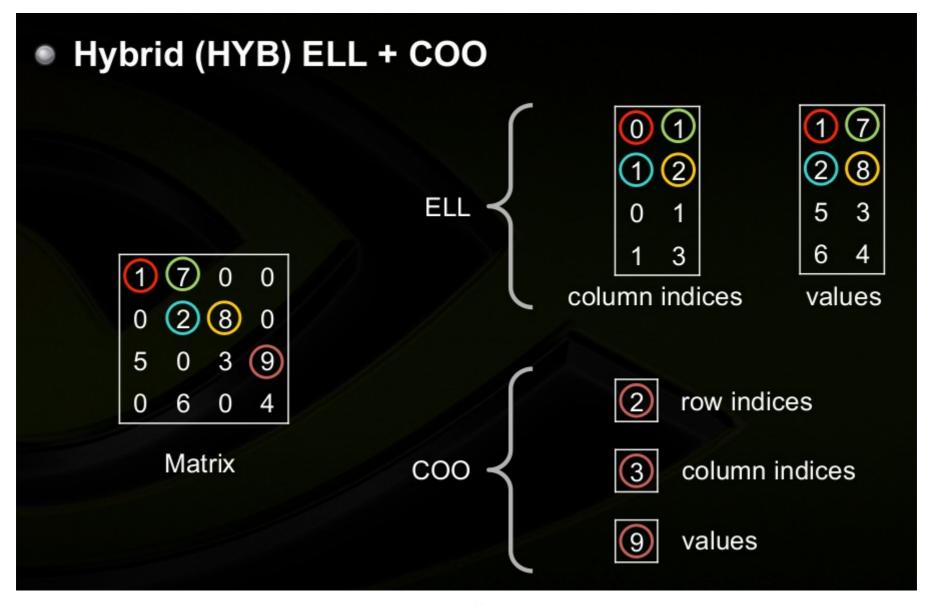


Formatos para matrices ralas

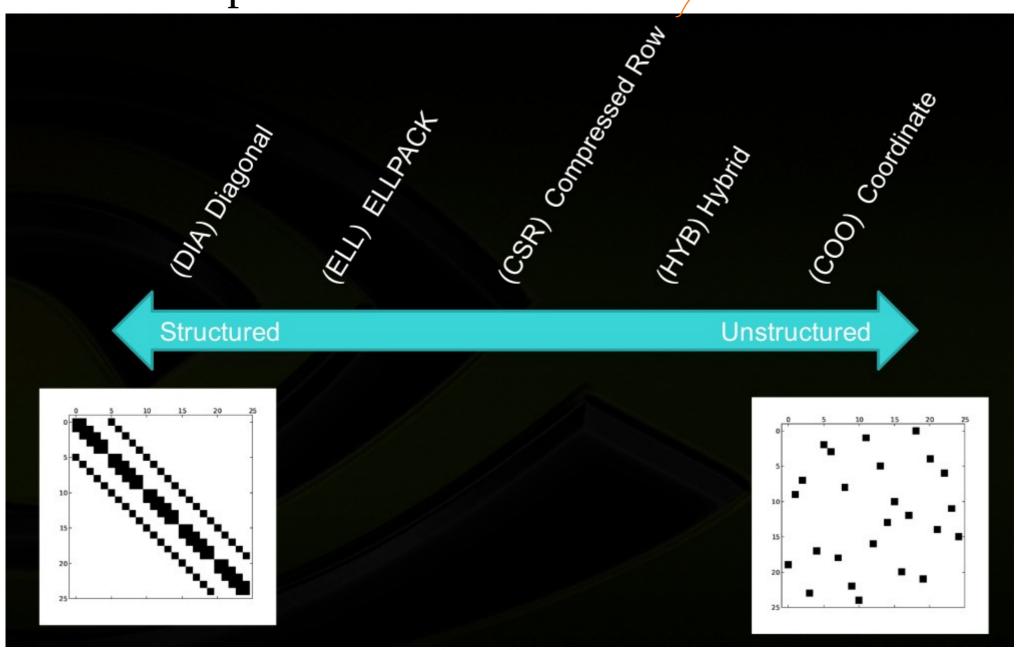




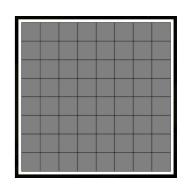


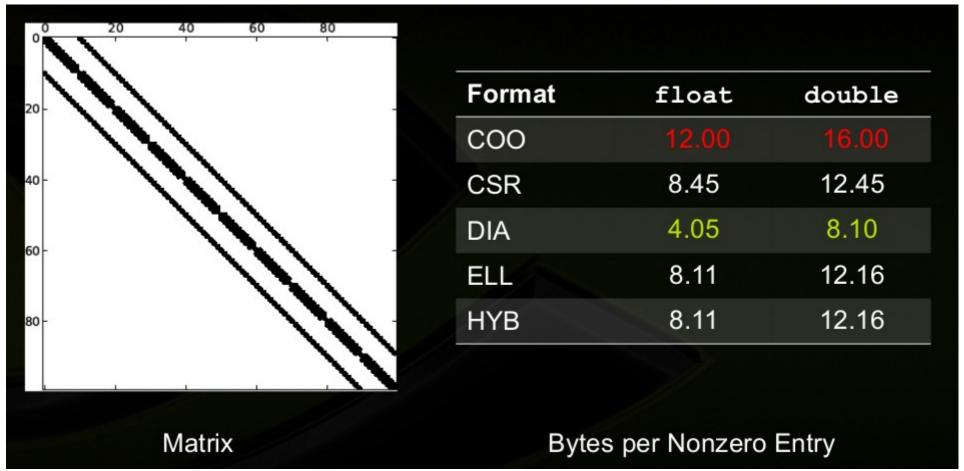


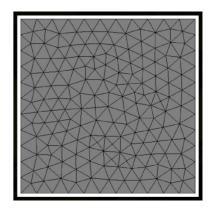
Nathan Bell, NVIDIA

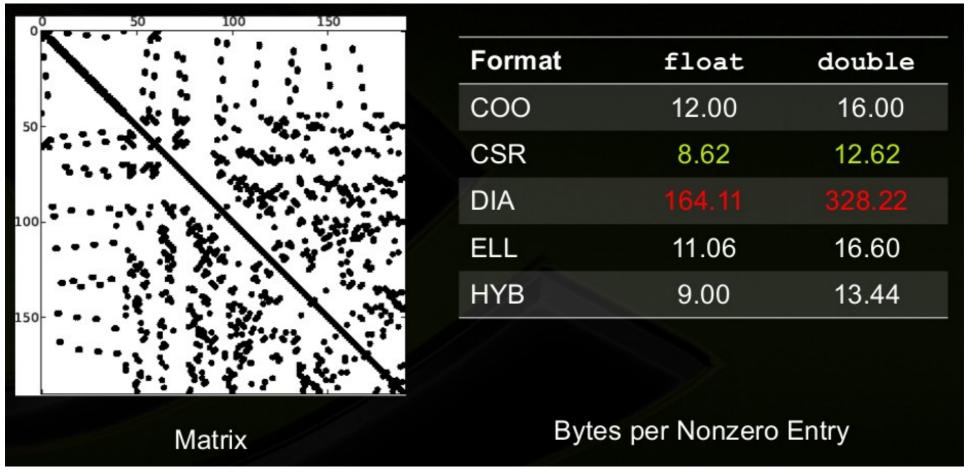


Nathan Bell, NVIDIA

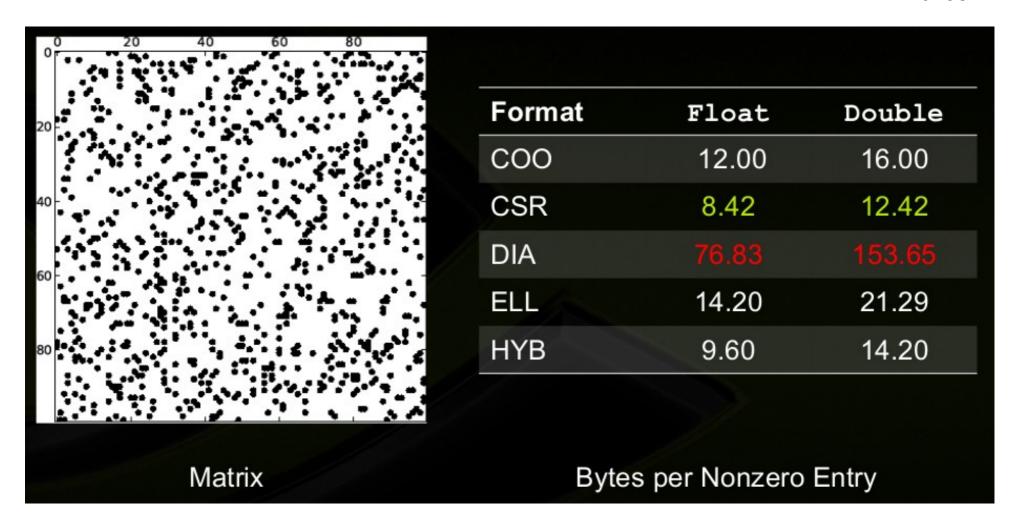




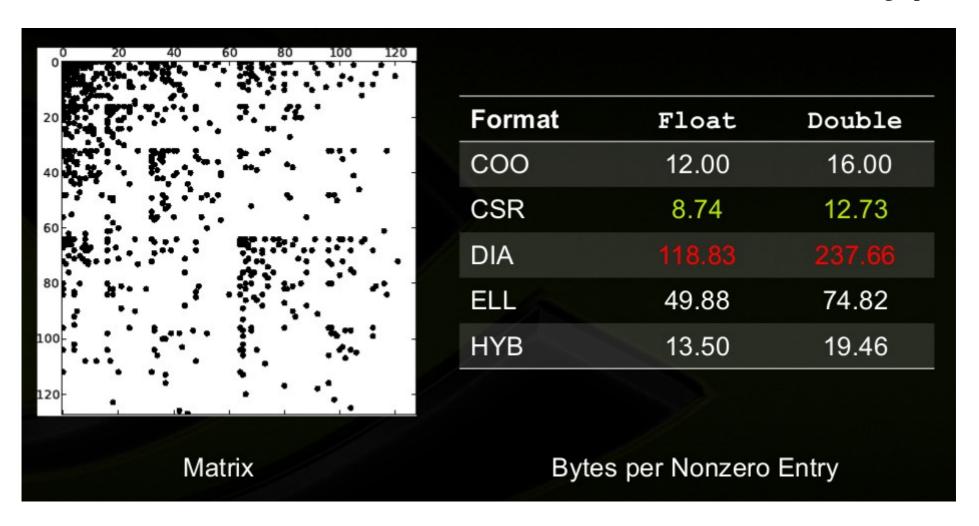




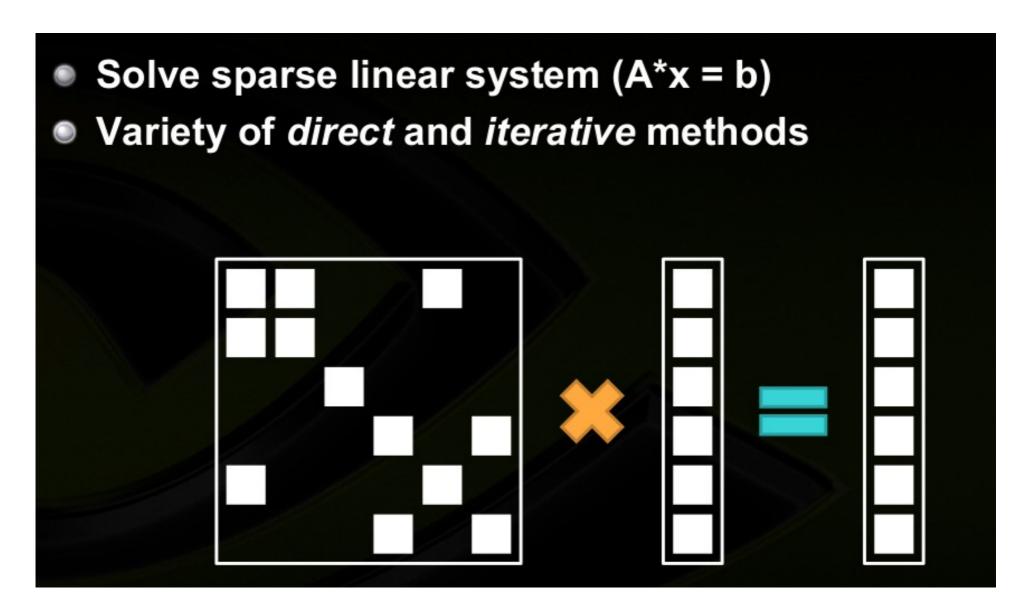
Random



Power law graph



Sistemas lineales ralos



CuSPARSE: Formatos de Matrices Ralas

Compressed Sparse Row Format (CSR)

The only way the CSR differs from the COO format is that the array containing the row indices is compressed in CSR format. The m×n sparse matrix A is represented in CSR format by the following parameters.

nnz	(integer)	The number of nonzero elements in the matrix.
csrValA	(pointer)	Points to the data array of length nnz that holds all nonzero values of A in row-major format.
csrRowPtrA	(pointer)	Points to the integer array of length m+1 that holds indices into the arrays csrColIndA and csrValA. The first m entries of this array contain the indices of the first nonzero element in the ith row for i=i,,m, while the last entry contains nnz+csrRowPtrA(0). In general, csrRowPtrA(0) is 0 or 1 for zero- and one-based indexing, respectively.
csrColIndA	(pointer)	Points to the integer array of length nnz that contains the column indices of the corresponding elements in array csrValA.

CuSPARSE: Formatos de Matrices Ralas

- 3.2.2. Coordinate Format (COO)
- 3.2.3. Compressed Sparse Row Format (CSR)
- 3.2.4. Compressed Sparse Column Format (CSC) Variante que en lugar de usar filas usa columnas
- 3.2.5. Block Compressed Sparse Row Format (BSR)
- 3.2.6. Extended BSR Format (BSRX)

▽ 13. cuSPARSE Format Conversion Reference	∇ 14.3. Sparse Matrix APIs
13.1. cusparse <t>bsr2csr()</t>	14.3.1. cusparseCreateCoo()
13.2. cusparse <t>gebsr2gebsc()</t>	14.3.2. cusparseCreateCooAoS() [DEPRECATED]
13.3. cusparse <t>gebsr2gebsr()</t>	14.3.3. cusparseCreateCsr()
13.4. cusparse <t>gebsr2csr()</t>	14.3.4. cusparseCreateCsc()
13.5. cusparse <t>csr2gebsr()</t>	14.3.5. cusparseCreateBlockedEll()
13.6. cusparse <t>coo2csr()</t>	14.3.6. cusparseDestroySpMat()
13.7. cusparse <t>csc2dense() [DEPRECATED]</t>	14.3.7. cusparseCooGet()
13.8. cusparse <t>csr2bsr()</t>	14.3.8. cusparseCooAosGet() [DEPRECATED]
13.9. cusparse <t>csr2coo()</t>	14.3.9. cusparseCsrGet()
13.10. cusparseCsr2cscEx2()	
13.11. cusparse <t>csr2dense() [DEPRECATED]</t>	14.3.10. cusparseCsrSetPointers()
13.12. cusparse <t>csr2csr_compress()</t>	14.3.11. cusparseCscSetPointers()
13.13. cusparse <t>dense2csc() [DEPRECATED]</t>	14.3.12. cusparseBlockedEllGet()
13.14. cusparse <t>dense2csr() [DEPRECATED]</t>	14.3.13. cusparseSpMatGetSize()
13.15. cusparse <t>nnz()</t>	14.3.14. cusparseSpMatGetFormat()
13.16. cusparseCreateIdentityPermutation()	14.3.15. cusparseSpMatGetIndexBase()
13.17. cusparseXcoosort()	14.3.16. cusparseSpMatGetValues()
13.18. cusparseXcsrsort()	14.3.17. cusparseSpMatSetValues()
13.19. cusparseXcscsort()	14.3.18. cusparseSpMatGetStridedBatch()
13.20. cusparseXcsru2csr()	14.3.19. cusparseSpMatSetStridedBatch() [DEPRECATED]
13.21. cusparseXpruneDense2csr()	
13.22. cusparseXpruneCsr2csr()	14.3.20. cusparseCooSetStridedBatch()
13.23. cusparseXpruneDense2csrPercentage()	14.3.21. cusparseCsrSetStridedBatch()
13.24. cusparseXpruneCsr2csrByPercentage()	14.3.22. cusparseSpMatGetAttribute()
13.25. cusparse <t>nnz_compress()</t>	14.3.23. cusparseSpMatSetAttribute()

Ejericicios CuSPARSE

/share/apps/icnpg/clases/Clases_cusparse/

// Copy the result vector back to the host

```
    // Create the cuSPARSE handle
    // Allocate device memory for vectors and the dense form of the matrix A
    // Construct a descriptor of the matrix A
    // Transfer the input vectors and dense matrix A to the device
    // Compute the number of non-zero elements in A
    // Allocate device memory to store the sparse CSR representation of A
    // Convert A from a dense formatting to a CSR formatting, using the GPU
    // Perform matrix-matrix multiplication with the CSR-formatted matrix A
```

Si uno hiciera el producto de matrices densas se estarían haciendo muchos productos por cero

ArrayFire



The Fastest Library for GPUs

also, hire us to accelerate your code

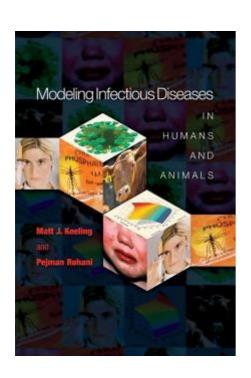
```
Get Started
            Easy-to-use API, like these examples
                                                           python
import arrayfire as af
                                                                                     Download Binaries
af.set backend('cuda')
                                 # choose cuda, opencl, or cpu
A = af.randu(2**15, 2**15) # create GPU data
A2 = af.matmul(A, A)
                                  # fast function calls
                                                                                        Github Project
B = af.fft2(A2)
                                  # ...
                                                 Open in Colab (Python)
                                                              C++
#include <arrayfire.h>
auto A = af::randu(2<<15, 2<<15); // create GPU data</pre>
                                                                                Talk to Us About Your Project
auto A2 = af::matmul(A, A);
                             // fast function calls
auto B = af::fft2(A2);
                                                                                  Learn abour Our Services
                                              Open in Codespace (C++
```

Mejor performance que cupy, y además corre en CUDA y OPENCL, y se puede usar en C++

(usa cuSOLVER para gpu de nvidia)

Ejericicios SPARSE con cupy y ArrayFire

• ICNPG_try-arrayfire-on-colab



$$\frac{dX_i}{dt} = \nu_i N_i - \lambda_i X_i - \mu_i X_i,$$

$$\frac{dY_i}{dt} = \lambda_i X_i - \gamma_i Y_i - \mu_i Y_i,$$

$$\lambda_i = \beta_i \sum_j \rho_{ij} \frac{X_j}{N_i},$$

Elementos de matriz Típicamente rala

$$Ax = b A_i x_i = b_i$$
$$Ax = \lambda x Ax = \lambda Bx$$

- ¿Qué es?: A high-level package based on the cuBLAS and cuSPARSE libraries... para resolver sistemas de ecuaciones lineales.
- **Operaciones:** matrix factorization and triangular solve routines for dense matrices, a sparse least-squares solver and an eigenvalue solver + a new refactorization library useful for solving sequences of matrices with a shared sparsity pattern.

• Tres sabores:

- CuSolverDN: matrices densas generales.
- CuSolverSP: formato CSR, matrices generales o especiales (simétricas/hermíticas, etc).
- CuSolverRF: refactorización, útil para sistemas "batcheados"

cuSOLVER D 1. Introduction D 2. Using the CUSOLVER API D 3. Using the CUSOLVERMG API D A. cuSolverRF Examples D B. CSR QR Batch Examples D C. QR Examples D LU Examples D LU Examples D E. Cholesky Examples D F. Examples of Dense Eigenvalue Solver D G. Examples of Singular Value Decomposition D H. Examples of multiGPU eigenvalue solver D I. Examples of multiGPU linear solver J. Acknowledgements K. Bibliography

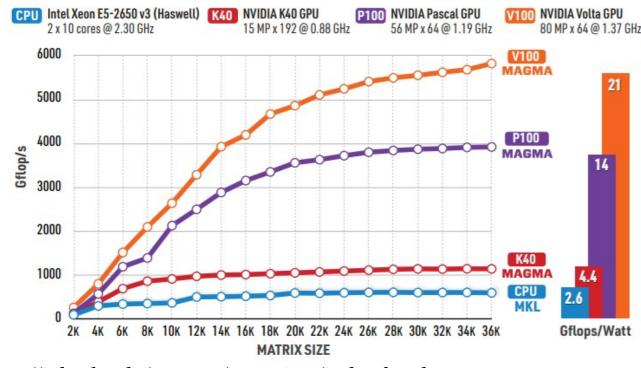
MAGMA

MAGMA

 Algebra lineal numérica para sistemas híbridos/heterogéneos: CPU-multicore + GPUs + ?

PERFORMANCE & ENERGY EFFICIENCY

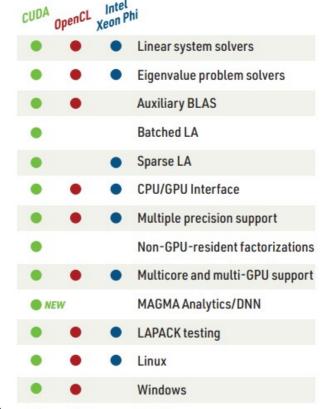
MAGMA LU factorization in double precision arithmetic





http://www.icl.utk.edu/files/print/2017/magma-sc17.pdf

(usa cuSOLVER para gpu de nvidia)



Mac OS

Ejercicios CuSolver

/share/apps/icnpg/clases/Clases_cusolver/

Linear algebra (cupy.linalg)

Hint NumPy API Reference: Linear algebra (numpy.linalg) See also Linear algebra (cupyx.scipy.linalg)

Linear algebra (cupyx.scipy.linalg)

Hint

SciPy API Reference: Linear algebra (scipy.linalg)

Linear algebra (cupyx.scipy.linalg)

cupyx.scipy.linalg.solve_triangular cupyx.scipy.linalg.tril cupyx.scipy.linalg.triu cupyx.scipy.linalg.lu cupyx.scipy.linalg.lu_factor cupyx.scipy.linalg.lu_solve cupyx.scipy.linalg.block_diag cupyx.scipy.linalg.circulant cupyx.scipy.linalg.companion cupyx.scipy.linalg.convolution_matrix cupyx.scipy.linalg.dft cupyx.scipy.linalg.fiedler cupyx.scipy.linalg.fiedler_companion cupyx.scipy.linalg.hadamard cupyx.scipy.linalg.hankel cupyx.scipy.linalg.helmert cupyx.scipy.linalg.hilbert cupyx.scipy.linalg.kron cupyx.scipy.linalg.leslie cupyx.scipy.linalg.toeplitz

cupyx.scipy.linalg.tri

Sparse matrices (cupyx.scipy.sparse

cupyx.scipy.sparse.coo_matrix cupyx.scipy.sparse.csc_matrix cupyx.scipy.sparse.csr_matrix cupyx.scipy.sparse.dia_matrix cupyx.scipy.sparse.spmatrix cupyx.scipy.sparse.eye cupyx.scipy.sparse.identity cupyx.scipy.sparse.kron cupyx.scipy.sparse.diags cupyx.scipy.sparse.spdiags cupyx.scipy.sparse.tril cupyx.scipy.sparse.triu cupyx.scipy.sparse.bmat cupyx.scipy.sparse.hstack cupyx.scipy.sparse.vstack cupyx.scipy.sparse.rand cupyx.scipy.sparse.random cupyx.scipy.sparse.find cupyx.scipy.sparse.issparse cupyx.scipy.sparse.isspmatrix cupyx.scipy.sparse.isspmatrix_csc cupyx.scipy.sparse.isspmatrix_csr cupyx.scipy.sparse.isspmatrix_coo cupyx.scipy.sparse.isspmatrix_dia

Linear algebra (cupy.linalg)

cupy.dot cupy.vdot cupy.inner cupy.outer cupy.matmul cupy.tensordot cupy.einsum cupy.linalg.matrix power cupy.kron cupy.linalg.cholesky cupy.linalg.qr cupy.linalg.svd cupy.linalg.eigh cupy.linalg.eigvalsh cupy.linalg.norm cupy.linalg.det cupy.linalg.matrix_rank cupy.linalg.slogdet cupy.trace cupy.linalg.solve cupy.linalg.tensorsolve cupy.linalg.lstsq cupy.linalg.inv

cupy.linalg.pinv

CUPY

CUPY

☐ Linear Algebra

Matrix and vector products

Decompositions

Matrix eigenvalues

Norms etc.

Solving linear equations

Logic Functions

Mathematical Functions

Padding

Random Sampling (cupy.random)

Sorting, Searching, and Counting

Statistical Functions

CuPy-specific Functions

SciPy-compatible Routines

Sparse matrices

Multi-dimensional image processing

NumPy-CuPy Generic Code Support

Memory Management

Low-Level CUDA Support

Docs » Reference Manual » Routines » Linear Algebra

C Edit on GitHub

Linear Algebra

Matrix and vector products

cupy.cross	Returns the cross product of two vectors.
cupy.dot	Returns a dot product of two arrays.
cupy.vdot	Returns the dot product of two vectors.
cupy.inner	Returns the inner product of two arrays.
cupy.outer	Returns the outer product of two vectors.
cupy.matmul	Returns the matrix product of two arrays and is the implementation
cupy.tensordot	Returns the tensor dot product of two arrays along specified axes.
cupy.einsum	Evaluates the Einstein summation convention on the operands.
cupy.linalg.matrix_power	Raise a square matrix to the (integer) power n.
cupy.kron	Returns the kronecker product of two arrays.

Matrix computations on the GPU

CUBLAS, CUSOLVER and MAGMA by example

Andrzej Chrzęszczyk

Jan Kochanowski University, Kielce, Poland

Jacob Anders

CSIRO, Canberra, Australia

Version 2017

Matrix Computations on GPU with ArrayFire - Python and ArrayFire - C/C++

Andrzej Chrzęszczyk

Jan Kochanowski University

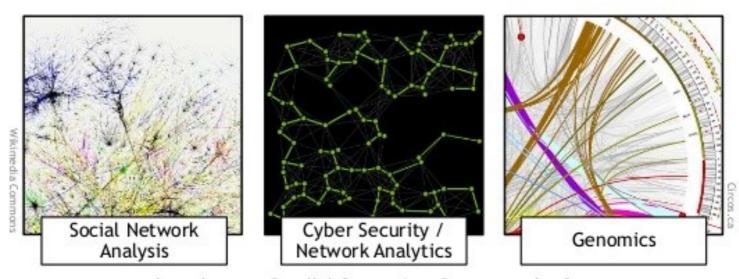
Version 2017

NVGRAPH (C) / CUGRAPH (python)

• graph construction and manipulation primitives, and a set of useful graph algorithms optimized for the GPU.

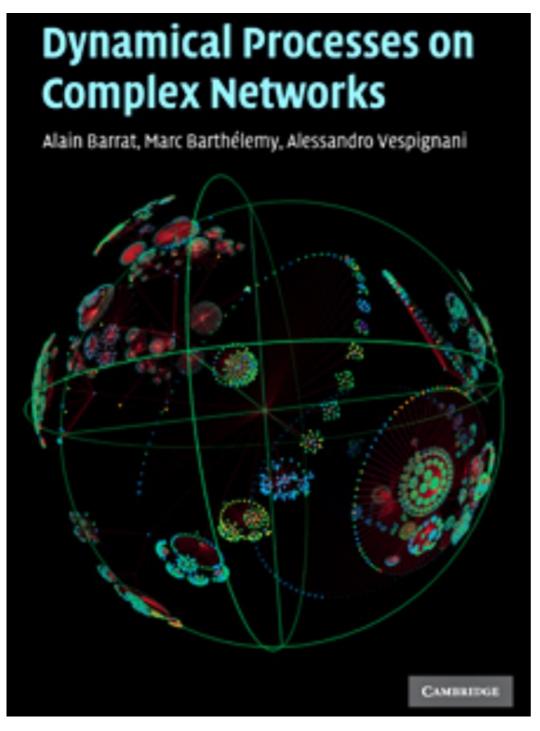
GRAPH ANALYTICS

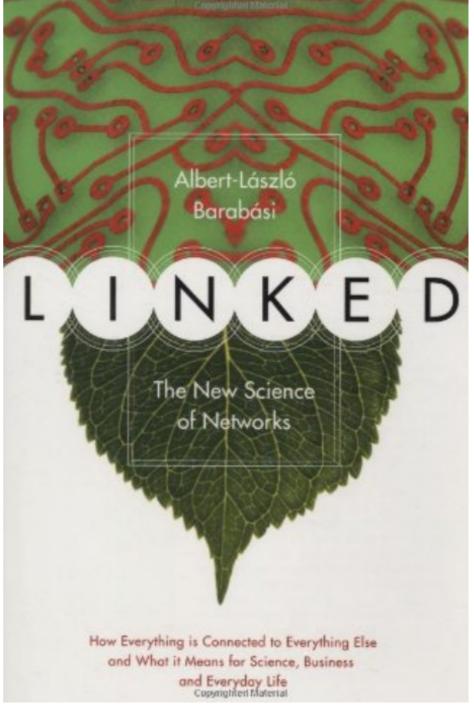
Insight from Connections in Big Data



... and much more: Parallel Computing, Recommender Systems, Fraud Detection, Voice Recognition, Text Understanding, Search







RAPIDS (python o C++)

DATA SCIENCE AT THE SPEED OF THOUGHT

DWHAT IS RAPIDS

RAPIDS provides unmatched speed with familiar APIs that match the most popular PyData libraries. Built on the shoulders of giants including **NVIDIA CUDA** and **Apache Arrow**, it unlocks the speed of GPUs with code you already know.

Learn more on the About Section **↗**

FASTER PANDAS WITH CUDF

cuDF is a near drop in replacement to pandas for most use cases and has greatly improved performance.

Run this benchmark yourself 7

₩HY USE RAPIDS

RAPIDS allows fluid, creative interaction with data for everyone from BI users to AI researchers on the cutting edge. GPU acceleration means less time and less cost moving data and training models.

Find out more from RAPIDS Use Cases **₹**

♣ OPEN SOURCE ECOSYSTEM

RAPIDS is Open Source and available on **GitHub**. Our mission is to empower and advance the open-source GPU data science data engineering ecosystem.

Jump to RAPIDS on GitHub ↗

FASTER SCIKIT-LEARN WITH CUML

cuML brings huge speedups to ML modeling with an API that matches scikit-learn.

Run this benchmark yourself 7

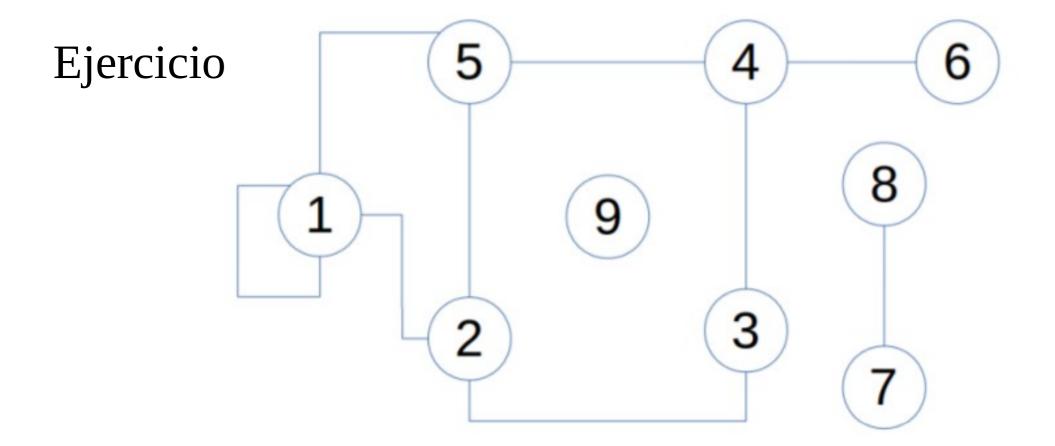
♥ FASTER NETWORKX WITH CUGRAPH

cuGraph makes migration from networkX easy, accelerates graph analytics, and allows scaling far beyond existing tools.

Run this benchmark yourself 7







Usando CUGRAPH

- Leer matriz de adyacencias csv.
- Número de caminos de exactamente 5 pasos que unen un vértice con cualquier otro.
- Número de componentes del grafo, y sus vértices miembros.
- Colorear, como si fuera un mapa, los vértices usando la mínima cantidad de colores.

ICNPG_ejemplocugraph.ipynb