Analytical Geometry and Linear Algebra I, Class #7

Innopolis University, October 2022

- 1. Find the centroid of the triangle formed by the lines given by the equations $12x^2 - 20xy + 7y^2 = 0$ and 2x - 3y + 4 = 0. And draw the picture.
- 2. Find the condition that one of the lines given by $ax^2 + 2hxy + by^2 = 0$ may be perpendicular to one of the lines given by $a_1x^2 + 2h_1xy + by^2 = 0$. And draw the picture.
- 3. Find the equation of the plane passing through the point (2, -3, 4) and parallel to the plane 2x - 5y - 7z + 15 = 0. And draw the picture.
- 4. Find the equation of the plane passing through the point (-1,3,2) and perpendicular to the planes x + 2y + 2z = 5 and 3x + 3y + 2z = 8. And draw the picture.
- 5. Find the ratio in which the line joining the points (2, -1, 4) and (6, 2, 4)is divided by the plane x + 2y + 3z + 5 = 0. And draw the picture.
- 6. Find the equation of the plane which passes through the intersection of the planes 2x+3y+10z-8=0, 2x-3y+7z-2=0 and is perpendicular to the plane 3x - 2y + 4z - 5 = 0. And draw the picture.
- 7. Find the equations of the line passing through the point (1,2,3) and perpendicular to the planes x - 2y - z + 5 = 0 and x + y + 3z + 6 = 0. And draw the picture.
- 8. Find the perpendicular distance from the point (1,3,-1) to the line $\frac{x-13}{5} = \frac{y+8}{-8} = \frac{z-31}{1}$. And draw the picture.
- 9. Find the distance of the points (2,3,-5), (3,4,7) from the plane x+2y-2z = 9 and prove that these points lie on the opposite sides of the plane. And draw the picture.
- 10. Find the distance of the point (1, -2, 3) from the plane x y + z = 5measured parallel to the line $\frac{x}{2} = \frac{y}{3} = \frac{z}{-6}$. And draw the picture.
- 11. Draw the following three cases and find how much solutions does the systems have.

(a)
$$\begin{cases} 2x + 3y - z = 1, \\ x - 2y + z = 2, \\ x + y + z = 1 \end{cases}$$
(b)
$$\begin{cases} 2x - 3y + z = 3, \\ x - 2y + 2z = 2, \\ x - y - z = 1 \end{cases}$$
(c)
$$\begin{cases} 2x - 3y + z = 3, \\ x - 2y + 2z = 0, \\ x - y - z = 1 \end{cases}$$

(b)
$$\begin{cases} 2x - 3y + z = 3, \\ x - 2y + 2z = 2, \\ x - y - z = 1 \end{cases}$$

(c)
$$\begin{cases} 2x - 3y + z = 3, \\ x - 2y + 2z = 0, \\ x - y - z = 1 \end{cases}$$