

# Lab 8: Discrete Fourier Transform

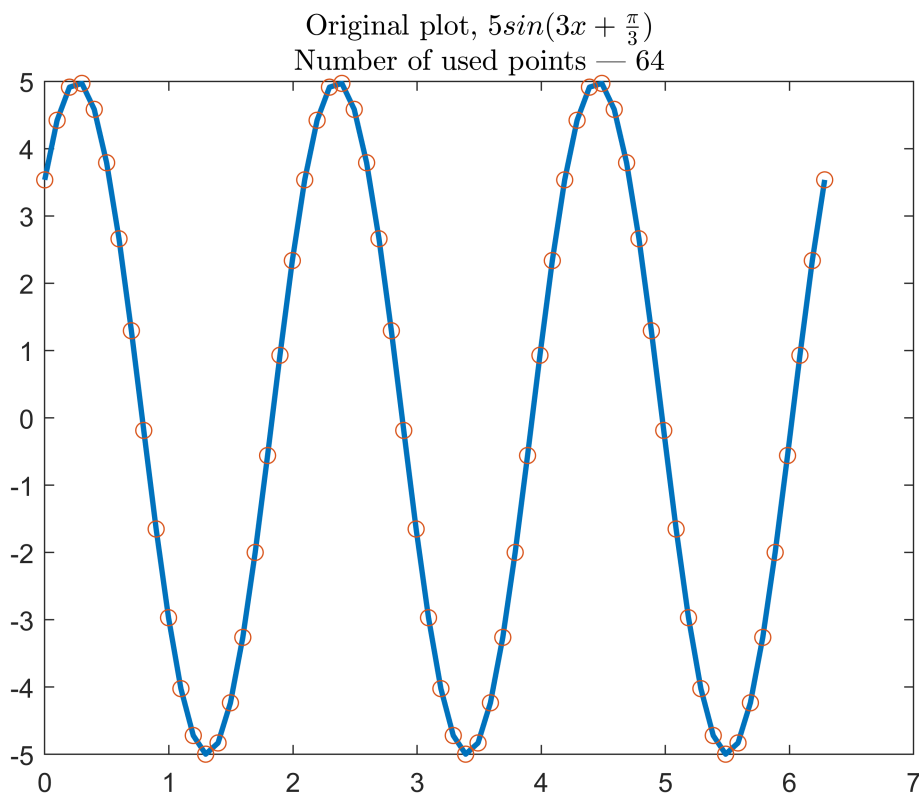
## Simple periodic function

Let's choose the function:  $5\sin(3x + \frac{\pi}{3})$

```
n = 2^6
```

```
n = 64
```

```
x = linspace(0,2*pi,n);  
y = 5*sin(3*x+pi/4);  
plot(x,y,"LineWidth",2)  
title(["Original plot,  $5\sin(3x+\frac{\pi}{3})$ ", "Number of used points --- " + num2str(n)], "In"  
hold on  
scatter(x,y)  
hold off
```



## Interpolation, using Fourier Transform

```
% Let's make F_4 for checking that it is what we need
```

```
F_4 = conj(dftmtx(4)) % because they use different formula inside
```

```
F_4 = 4x4 complex  
1.0000 + 0.0000i 1.0000 + 0.0000i 1.0000 + 0.0000i 1.0000 + 0.0000i
```

```

1.0000 + 0.0000i    0.0000 + 1.0000i   -1.0000 + 0.0000i    0.0000 - 1.0000i
1.0000 + 0.0000i   -1.0000 + 0.0000i    1.0000 + 0.0000i   -1.0000 + 0.0000i
1.0000 + 0.0000i    0.0000 - 1.0000i   -1.0000 + 0.0000i    0.0000 + 1.0000i

```

```

F_64 = conj(dftmtx(n));

% Let's find our args of functions
C = linsolve(F_64,y');

Y_new = zeros(n,1);
for t=1:n
    temp = 0;
    for j=1:n
        temp = C(j)*exp(2*pi/n*(t-1)*(j-1)*1i);
        Y_new(t) = Y_new(t) + temp;
    end
end
error_interpolation = rms(y'-Y_new)

```

```

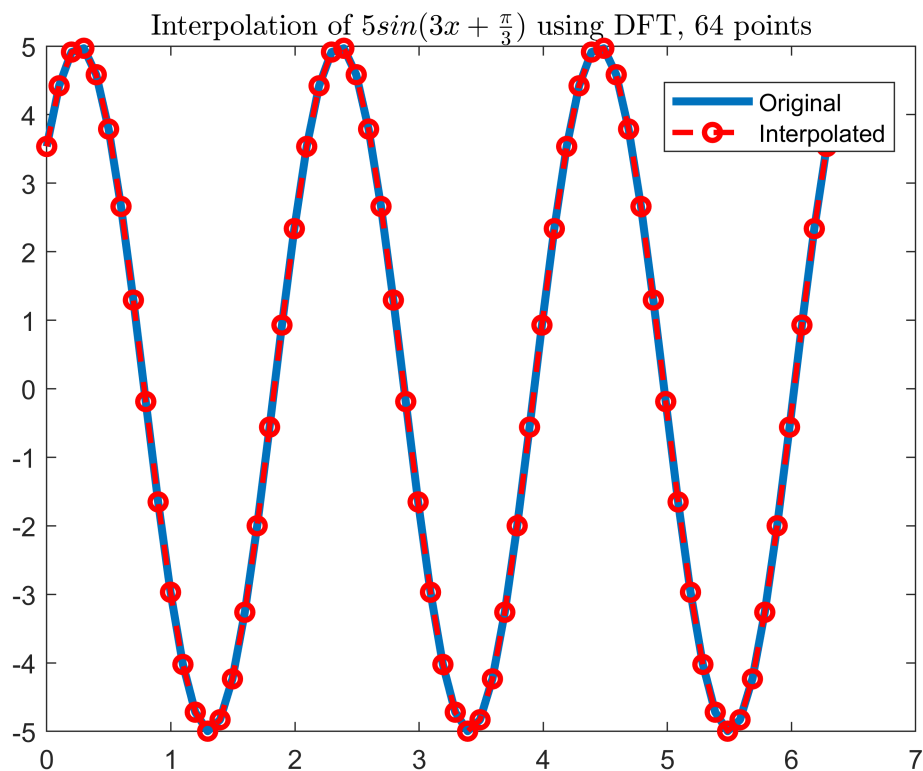
error_interpolation = 4.2429e-14

```

```

p=plot(x,y,x,real(Y_new),'r--o');
p(1).LineWidth = 3;
p(2).LineWidth = 2;
title("Interpolation of  $5\sin(3x + \frac{\pi}{3})$  using DFT, " + num2str(n) + " points",'interpol');
legend("Original","Interpolated")

```

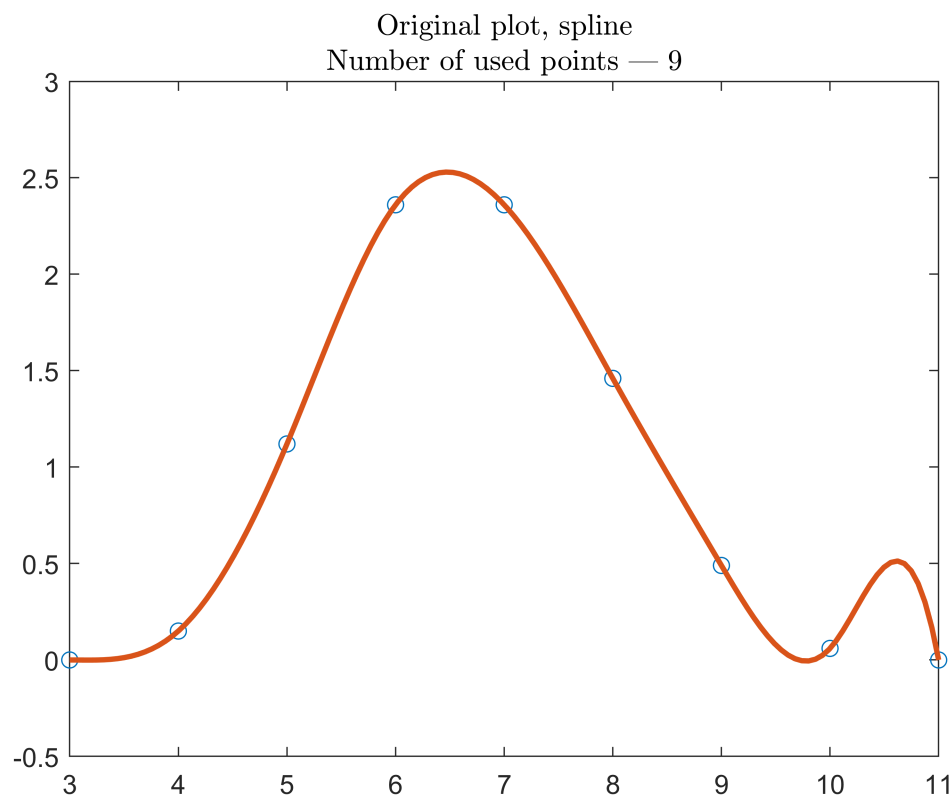


## Interpolation, complex example

```
% boundaries
a = 3;
b = 11;
x_exp2 = a:b;
y_exp2 = [0 .15 1.12 2.36 2.36 1.46 .49 .06 0];
cs = spline(x_exp2,[0 y_exp2 -3]);
n_spline = 128
```

```
n_spline = 128
```

```
xx_spline = linspace(a,b,n_spline);
yy_spline = ppval(cs,xx_spline);
p_spline = plot(x_exp2,y_exp2,'o',xx_spline,yy_spline,'-');
p_spline(2).LineWidth=2;
title(["Original plot, spline", "Number of used points --- 9"], "Interpreter", "latex")
```



```
% Transform from a-b to 0-2pi
mapping = linspace([0 1;2*pi 1],[a;b])
```

```
mapping = 2x1
1.2732
3.0000
```

```

F_128 = conj(dftmtx(n_spline));

% Let's find our args of functions
C_spline = linsolve(F_128,yy_spline');

Y_new_spline = zeros(n_spline,1);
for t=1:n_spline
    temp = 0;
    for j=1:n_spline
        temp = C_spline(j)*exp(2*pi/n_spline*(t-1)*(j-1)*1i);
        Y_new_spline(t) = Y_new_spline(t) + temp;
    end
end
error_interpolation_spline = rms(y'-Y_new)

```

```
error_interpolation_spline = 4.2429e-14
```

```

p=plot(xx_spline,yy_spline,xx_spline,real(Y_new_spline),'r--o');
p(1).LineWidth = 3;
p(2).LineWidth = 1;
title("Interpolation of the spline using DFT, " + num2str(n_spline) + " points",'interpreter', 'none');
legend("Original","Interpolated")

```

