

Lab 12: SVD

Dimension reduction, toy example

```
A = [1 2 3;4 5 6; 7 8 9]
```

```
A = 3x3
     1     2     3
     4     5     6
     7     8     9
```

```
Rank = rank(A)
```

```
Rank = 2
```

```
[U,S,V] = svd(A)
```

```
U = 3x3
    -0.2148    0.8872    0.4082
    -0.5206    0.2496   -0.8165
    -0.8263   -0.3879    0.4082
S = 3x3
    16.8481     0     0
     0    1.0684     0
     0     0    0.0000
V = 3x3
    -0.4797   -0.7767   -0.4082
    -0.5724   -0.0757    0.8165
    -0.6651    0.6253   -0.4082
```

```
% Find full A again
```

```
A_full = U*S*V'
```

```
A_full = 3x3
     1.0000     2.0000     3.0000
     4.0000     5.0000     6.0000
     7.0000     8.0000     9.0000
```

```
% Reduce 3 el from S
```

```
A_2 =U(:,1:2)*S(1:2,1:2)*V(:,1:2)'
```

```
A_2 = 3x3
     1.0000     2.0000     3.0000
     4.0000     5.0000     6.0000
     7.0000     8.0000     9.0000
```

```
% reduce all columns exept 1 one
```

```
A_1=U(:,1)*S(1,1)*V(:,1)'
```

```
A_1 = 3x3
     1.7362     2.0717     2.4073
     4.2072     5.0202     5.8332
     6.6781     7.9686     9.2592
```

```
%result - dim the same, but info and rank changes
```

```
Rank_new = rank(A_1)
```

```
Rank_new = 1
```