NeuralNet_Eval copy

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1 Trabajo Práctico 2: Gradiente Descendente

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- 1.2 Importación de Librerías

```
[]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
from tqdm import tqdm
import networkx as nx
import itertools
import seaborn as sns
```

```
[]: import warnings

#suppress warnings
warnings.filterwarnings('ignore')
```

```
[]: # Display loss with all digits (not rounded)

pd.options.display.float_format = '{:,.20f}'.format
```

1.3 Lectura de Datos

```
2 2,013.58333330000004934845 13.300000000000071054 561.984500000000002546585
    3 2,013.50000000000000000000 13.300000000000071054 561.98450000000002546585
    4 2,012.83333330000004934845 5.00000000000000000 390.568399999999999690772
       Х4
                               Х5
                                                       Х6
                                                                                Y
    0 10 24.9829800000000129717 121.5402399999999716692 37.89999999999999857891
      9 24.9803400000000176556 121.5395100000000703949 42.2000000000000284217
      5 24.9874599999999867214 121.543909999999678494 47.299999999999715783
        5 24.9874599999999867214 121.5439099999999678494 54.799999999999715783
        5 24.979369999999940769 121.54245000000000231921 43.100000000000142109
[]: X_matrix: np.ndarray = np.array(real_estate.drop(['Y house price of unit_
     ⇔area'], axis=1))
    y_matrix: np.ndarray = np.array(real_estate['Y house price of unit area']).
      \rightarrowreshape(-1, 1)
    X_train: np.ndarray = X_matrix[0:315]
    y_train: np.ndarray = y_matrix[0:315]
    X_test: np.ndarray = X_matrix[315:]
    y_test: np.ndarray = y_matrix[315:]
    X_train.shape, y_train.shape, X_test.shape, y_test.shape
```

[]: ((315, 6), (315, 1), (99, 6), (99, 1))

1.4 Definición de clase NeuralNet

```
[]: from typing import List, Tuple, Callable
    from matplotlib import pyplot as plt
    import numpy as np
    from numpy import ndarray
    import networkx as nx

class NeuralNet:
    def __init__(self):
        """
        Inicializa los parámetros de la red neuronal.
        2 capas con 5 neuronas cada una.
        """

        self.W1: ndarray = np.random.random((5, 6))
        self.b1: ndarray = np.random.random((5, 1))

        self.W2: ndarray = np.random.random((1, 5))
        self.b2: ndarray = np.random.random((1, 1))
```

```
self.training_loss_acum: List[float] = []
    self.testing_loss_acum: List[float] = []
    self.activation = self.sigmoid
def sigmoid(self, x: ndarray) -> ndarray:
    Función de activación sigmoide.
    return 1 / (1 + np.exp(-x))
def relu(self, x: ndarray) -> ndarray:
    Función de activación ReLU.
    return np.maximum(0, x)
def leaky_relu(self, x: ndarray) -> ndarray:
    Función de activación Leaky ReLU.
    return np.maximum(0.01 * x, x)
def tanh(self, x: ndarray) -> ndarray:
    Función de activación tanh.
    return np.tanh(x)
def softmax(self, x: ndarray) -> ndarray:
    Función de activación softmax.
    return np.exp(x) / np.sum(np.exp(x))
def forward(
        self,
        x: ndarray,
        dropout: bool = False,
    ) -> ndarray:
    Calcula la salida de la red neuronal.
    11 11 11
    self.z1 = self.W1 @ x.T + self.b1.repeat(x.shape[0], axis=1)
    self.a1 = self.activation(self.z1)
```

```
# if dropout:
       # self.a1 = self.dropout(self.a1, 0.5)
      self.z2 = self.W2 @ self.a1 + self.b2.repeat(self.a1.shape[1], axis=1)
      self.a2 = self.z2
      return self.a2.reshape(-1, 1)
  def numerical_gradient(
      self, x: ndarray, y: ndarray, eps: float, dropout: bool = False,
       dropout_prob: float = 0.5
  ) -> Tuple[ndarray, ndarray, ndarray]:
       Una estrategia para calcular estas derivadas parciales,
       consiste en calcular el promedio de los cocientes incrementales
       a derecha e izquierda.
      Para obtener la siquiente aproximación, para
       cada parámetro de la red calculamos:
       $$
       \frac{1}{partial L}{partial p} \simeq \frac{L(\theta_t, p + \epsilon_t, p + \epsilon_t)}{-1}
\hookrightarrow L(\theta_t, p - \tension)){2 \ension}
       $$
       donde usamos $p$ de forma genérica para referirnos a cada elemento⊔
4 \cdot \$ w^1_{i,j}, \$ b^1_{j}, \$ w^2_{i,j}, \$ b^2_{i,j}
       11 11 11
      dW1 = np.zeros_like(self.W1)
      db1 = np.zeros_like(self.b1)
      dW2 = np.zeros_like(self.W2)
      db2 = np.zeros_like(self.b2)
      if dropout:
           temp_w1 = self.W1.copy()
           self.W1 = self.dropout(self.W1, dropout_prob)
           temp_b1 = self.b1.copy()
           self.b1 = self.dropout(self.b1, dropout_prob)
           temp_w2 = self.W2.copy()
           self.W2 = self.dropout(self.W2, dropout_prob)
           temp_b2 = self.b2.copy()
           self.b2 = self.dropout(self.b2, dropout_prob)
      for i in range(self.W1.shape[0]):
           for j in range(self.W1.shape[1]):
               if dropout:
                   if self.W1[i, j] == 0 and temp_w1[i, j] != 0:
                       continue
```

```
self.W1[i, j] += eps
        loss1 = self.loss(x, y)
        self.W1[i, j] -= 2 * eps
        loss2 = self.loss(x, y)
        dW1[i, j] = (loss1 - loss2) / (2 * eps)
        self.W1[i, j] += eps
for i in range(self.b1.shape[0]):
    for j in range(self.b1.shape[1]):
        if dropout:
            if self.b1[i, j] == 0 and temp_b1[i, j] != 0:
                continue
        self.b1[i, j] += eps
        loss1 = self.loss(x, y)
        self.b1[i, j] -= 2 * eps
        loss2 = self.loss(x, y)
        db1[i, j] = (loss1 - loss2) / (2 * eps)
        self.b1[i, j] += eps
for i in range(self.W2.shape[0]):
    for j in range(self.W2.shape[1]):
        if dropout:
            if self.W2[i, j] == 0 and temp_w2[i, j] != 0:
                continue
        self.W2[i, j] += eps
        loss1 = self.loss(x, y)
        self.W2[i, j] -= 2 * eps
        loss2 = self.loss(x, y)
        dW2[i, j] = (loss1 - loss2) / (2 * eps)
        self.W2[i, j] += eps
for i in range(self.b2.shape[0]):
    for j in range(self.b2.shape[1]):
        if dropout:
            if self.b2[i, j] == 0 and temp_b2[i, j] != 0:
                continue
        self.b2[i, j] += eps
        loss1 = self.loss(x, y)
        self.b2[i, j] -= 2 * eps
        loss2 = self.loss(x, y)
        db2[i, j] = (loss1 - loss2) / (2 * eps)
        self.b2[i, j] += eps
if dropout:
    self.W1 = temp_w1
    self.b1 = temp_b1
    self.W2 = temp_w2
```

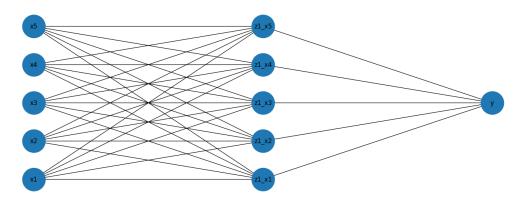
```
self.b2 = temp_b2
       return dW1, db1, dW2, db2
  def dropout(self, x: ndarray, p: float) -> ndarray:
      Aplica dropout a la capa de entrada.
      x: ndarray de entrada
      p: probabilidad de dropout
      mask = np.random.binomial(1, p, size=x.shape)
      return x * mask
  def update_weights(
      self,
      lr: float,
      dW1: ndarray,
      db1: ndarray,
      dW2: ndarray,
      db2: ndarray,
  ):
       .....
      Actualiza los pesos de la red neuronal usando
       numerical gradient descent.
       HHHH
      self.W1 -= lr * dW1
      self.b1 -= lr * db1
      self.W2 -= lr * dW2
      self.b2 -= lr * db2
  def loss(self, x: ndarray, y: ndarray, dropout: bool = False) -> float:
       Calcula el error cuadrático medio.
      return np.power((self.forward(x, dropout=dropout) - y), 2).mean(axis=0)_u
\hookrightarrow 2
  def record_metrics(self, x: ndarray, y: ndarray, x_test: ndarray, y_test:__
→ndarray):
      self.training_loss_acum.append(self.loss(x, y))
      self.test_loss_acum.append(self.loss(x_test, y_test))
  def fit(
      self,
```

```
x: ndarray,
      y: ndarray,
      x_test: ndarray,
      y_test: ndarray,
      lr: float = 0.01,
      epochs: int = 1000,
      eps: float = 1e-3,
      dropout: bool = False,
      dropout_prob: float = 0.5,
      custom_activation: Callable[[ndarray], ndarray] = None,
      verbose: bool = False,
  ) -> List[float]:
      Entrena la red neuronal usando gradient descent.
      if custom_activation:
          self.activation = custom_activation
      self.train_loss_acum = []
      self.test_loss_acum = []
      self.lr = lr
      self.epochs = epochs
      self.eps = eps
      self.with_dropout = dropout
      self.dropout_prob = dropout_prob
      for _ in tqdm(range(epochs)) if verbose else range(epochs):
          self.record_metrics(x, y, x_test, y_test)
          dW1, db1, dW2, db2 = self.numerical_gradient(x, y, eps,_
→dropout=dropout, dropout_prob=dropout_prob)
          self.update_weights(lr, dW1, db1, dW2, db2)
      self.activation = self.sigmoid
      return self.train_loss_acum
  def predict(self, x: ndarray) -> ndarray:
      Infiere la salida de la red neuronal.
      return self.forward(x)
  def get_weights(self) -> Tuple[ndarray, ndarray, ndarray, ndarray]:
```

```
Devuelve los pesos de la red neuronal.
      return self.W1, self.b1, self.W2, self.b2
  def get_training_loss(self) -> List[float]:
      Devuelve el error cuadrático medio acumulado.
      return self.training_loss_acum
  def get_test_loss(self) -> List[float]:
      return self.test_loss_acum
  def plot_loss(self, ax: plt.Axes = None) -> plt.Axes:
      if ax is None:
          _, ax = plt.subplots()
      ax.plot(
          range(len(self.training_loss_acum)),
          self.training_loss_acum,
          label="Training Loss",
      )
      ax.plot(range(len(self.test_loss_acum)), self.test_loss_acum,_
⇔label="Test Loss")
      ax.legend()
      ax.set_xlabel("Epoch")
      ax.set_ylabel("Loss")
      ax.set_title("Loss vs Epoch, lr = {}, $\epsilon$ = {}".format(self.lr,_
⇔self.eps))
      # If dropout is used, add it to the title
      if self.with_dropout:
          ax.set_title(
              "Loss vs Epoch, lr = {}, $\epsilon$ = {}, dropout_prob = {}".
→format(
                  self.lr, self.eps, self.dropout_prob
              )
          )
      return ax
  def mse(self, y_true: ndarray, x_test: ndarray) -> float:
```

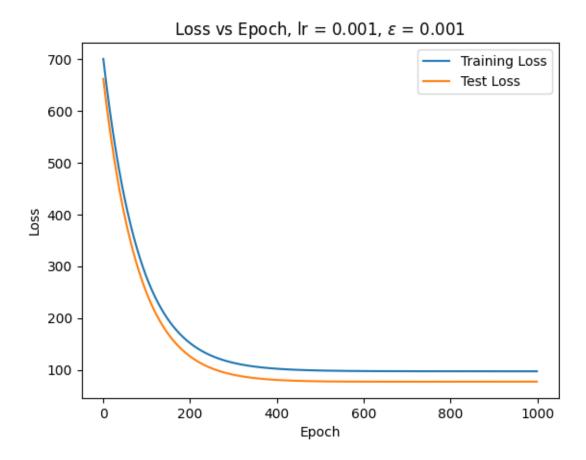
```
Calcula el error cuadrático medio.
      y_pred = self.predict(x_test)
      return np.mean(np.power(y_true - y_pred, 2))
  def plot_network_graph(self, ax: plt.Axes):
      Visualiza la red neuronal y sus conexiones
      G = nx.DiGraph()
      G.add_nodes_from(["x1", "x2", "x3", "x4", "x5"])
      G.add_nodes_from(["z1_x1", "z1_x2", "z1_x3", "z1_x4", "z1_x5"])
      G.add_nodes_from(["y"])
      # Add edges with weights
      for i in range(5):
          for j in range(5):
              G.add\_edge(f"x{i+1}", f"z1_x{j+1}", weight=self.W1[i, j])
              G.add_edge(f"z1_x{j+1}", f"y", weight=1)
      pos = {
          "x1": (0, 0),
          "x2": (0, 1),
          x3: (0, 2),
          x4: (0, 3),
          x5: (0, 4),
          z1_x1: (1, 0),
          "z1_x2": (1, 1),
          "z1_x3": (1, 2),
          "z1_x4": (1, 3),
          "z1_x5": (1, 4),
          "y": (2, 2),
      }
      # Edge labels with weights
      nx.draw_networkx_nodes(G, pos, cmap=plt.get_cmap("jet"),__
⇒node size=2000, ax=ax)
      nx.draw_networkx_labels(G, pos, ax=ax)
      nx.draw_networkx_edges(
          G, pos, edgelist=G.edges(), edge_color="k", arrows=True, ax=ax
      )
```

/Users/nacho/opt/anaconda3/envs/coding/lib/python3.8/sitepackages/networkx/drawing/nx_pylab.py:433: UserWarning: No data for colormapping provided via 'c'. Parameters 'cmap' will be ignored node_collection = ax.scatter(



1.5 Experimentación Manual

[]: <Axes: title={'center': 'Loss vs Epoch, lr = 0.001, \$\epsilon\$ = 0.001'},
 xlabel='Epoch', ylabel='Loss'>



```
[]: nn = NeuralNet()
     nn.fit(X_train, y_train, x_test=X_test, y_test=y_test, epochs=1000, lr=0.001,_

¬custom_activation=nn.tanh, verbose=True)
     display(pd.Series(
         y_test[0][0],
             nn.predict(X_test[0].reshape(1, -1))[0][0],
             nn.get_training_loss()[-1][0],
             nn.get_test_loss()[-1][0],
         ],
         index=["y_true", "y_pred", "train_loss", "test_loss"]
     ))
    nn.plot_loss()
    100%|
               | 1000/1000 [00:04<00:00, 248.22it/s]
                 27.3000000000000071054
    y_true
```

38.02122515605474006861

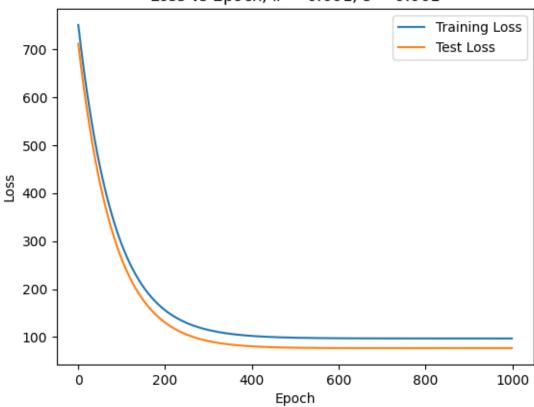
y_pred

```
train_loss 97.12112880050391083842
test_loss 77.15022996002481647793
```

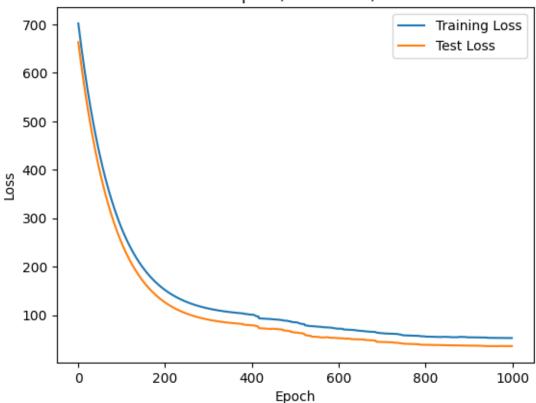
dtype: float64

[]: <Axes: title={'center': 'Loss vs Epoch, lr = 0.001, \$\epsilon\$ = 0.001'},
 xlabel='Epoch', ylabel='Loss'>

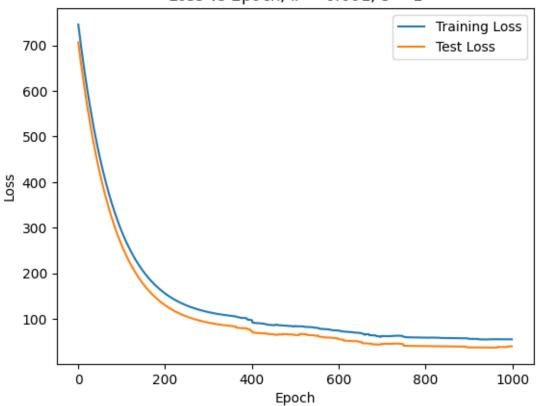


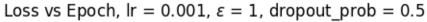


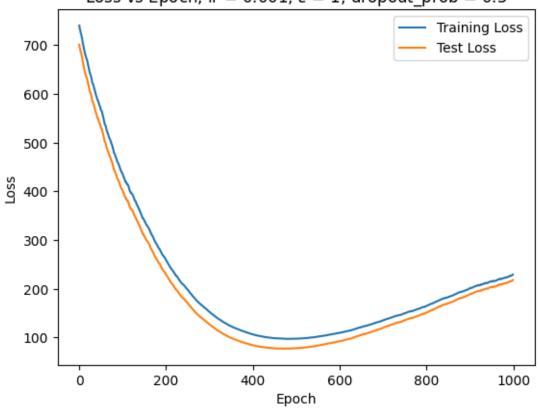
Loss vs Epoch, lr = 0.001, $\varepsilon = 1$



Loss vs Epoch, lr = 0.001, $\varepsilon = 1$







```
[]: nn_dropout = NeuralNet()
```

```
nn_dropout.fit(X_train, y_train, x_test=X_test, y_test=y_test, epochs=1000,_u
 →lr=0.001, eps=1, dropout=True, dropout_prob=0.5, custom_activation=nn.tanh,
 →verbose=True)
display(pd.Series(
    y test[0][0],
        nn_dropout.predict(X_test[0].reshape(1, -1))[0][0],
        nn_dropout.get_training_loss()[-1][0],
        nn_dropout.get_test_loss()[-1][0],
        min(nn_dropout.get_training_loss())[0],
        min(nn_dropout.get_test_loss())[0],
    ],
    index=["y_true", "y_pred", "train_loss", "test_loss", "min_train_loss", "
 _ = nn_dropout.plot_loss()
100%|
          | 1000/1000 [00:02<00:00, 461.19it/s]
                 27.3000000000000071054
y_true
y_pred
                 54.65448618360453281184
```

233.43453540371953636168

222.41958081889217169191

97.11738405032269838557

77.04853250241073681082

train_loss

test loss

min_train_loss

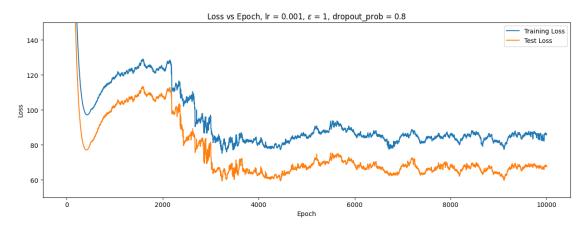
min_test_loss

```
Loss vs Epoch, lr = 0.001, \varepsilon = 1, dropout_prob = 0.5
700
                                                             Training Loss
                                                             Test Loss
600
500
400
300
200
100
                                400
       0
                   200
                                            600
                                                         800
                                                                      1000
                                     Epoch
```

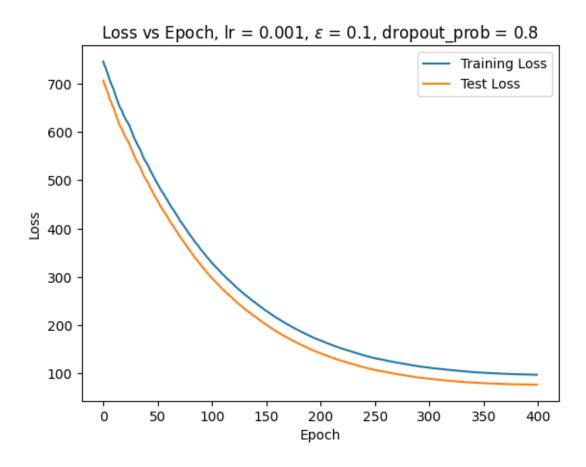
```
[]: nn_dropout = NeuralNet()
     nn_dropout.fit(X_train, y_train, x_test=X_test, y_test=y_test, epochs=10000,__
      →lr=0.001, eps=1, dropout=True, dropout_prob=0.8, verbose=True)
    100%|
              | 10000/10000 [00:38<00:00, 259.49it/s]
[]:[]
[]: display(pd.Series(
             y_test[0][0],
             nn_dropout.predict(X_test[0].reshape(1, -1))[0][0],
             nn_dropout.get_training_loss()[-1][0],
             nn_dropout.get_test_loss()[-1][0],
         ],
         index=["y_true", "y_pred", "train_loss", "test_loss"]
     ))
                 27.3000000000000071054
    y_true
                 33.30453404740335798806
    y_pred
    train_loss
                 85.91754731507950282321
```

```
test_loss 67.61037497622338321435
dtype: float64
```

```
[]: fig, ax = plt.subplots(1, 1, figsize=(15, 5))
ax.set_ylim(50, 150)
_ = nn_dropout.plot_loss(ax=ax)
```

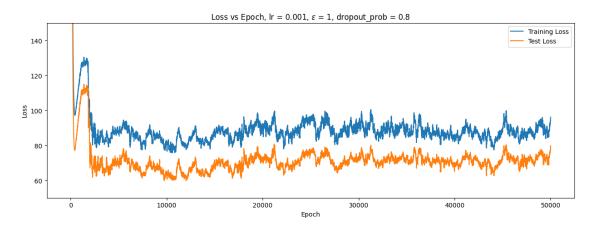


y_true 27.300000000000000071054
y_pred 37.03763934176618022320
train_loss 97.69831781165335371497
test_loss 77.19354891780324123829



```
[]: hyper_nn = NeuralNet()
     hyper_nn.fit(X_train, y_train, x_test=X_test, y_test=y_test, epochs=50000, lr=0.
      ⇔001, eps=1, dropout=True, dropout_prob=0.8)
    /var/folders/5j/7b3w3dw95qdcl187vxc3yn300000gn/T/ipykernel_1661/2190381686.py:28
    : RuntimeWarning: overflow encountered in exp
      return 1 / (1 + np.exp(-x))
[]:[]
[]: display(pd.Series(
         y_test[0][0],
            hyper_nn.predict(X_test[0].reshape(1, -1))[0][0],
            hyper_nn.get_training_loss()[-1][0],
            hyper_nn.get_test_loss()[-1][0],
        ],
        index=["y_true", "y_pred", "train_loss", "test_loss"]
     ))
```

/var/folders/5j/7b3w3dw95qdcl187vxc3yn300000gn/T/ipykernel_1661/2190381686.py:28



1.6 Mascara sobre los pesos: Dropout

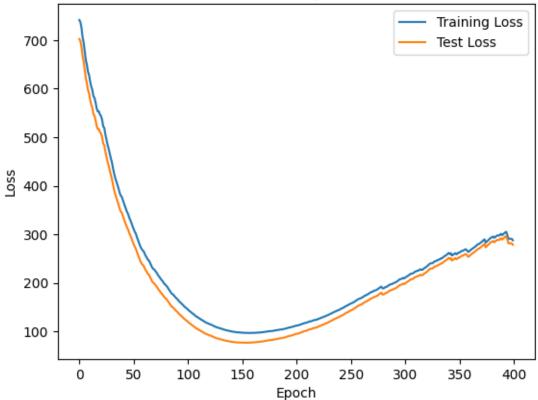
[]: # Epoch en el que se obtuvo la menor Loss

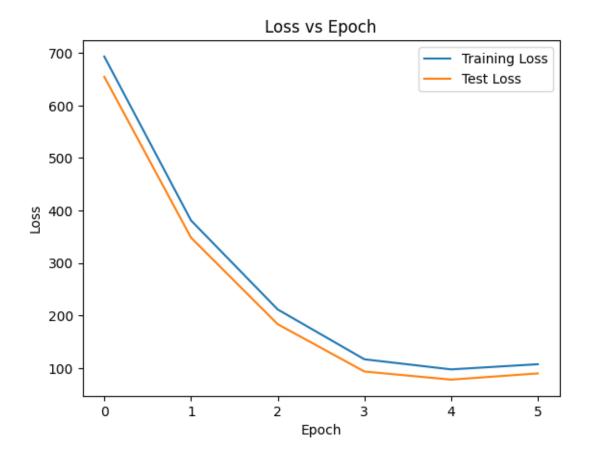
Otras dos cuestiones que probamos fueron cambiar la función de activación, y aplicar una mascara a los pesos de entrenamiento de la red con cierta probabilidad en cada epoch.

Para la función de activación probamos con la función sigmoide como indicaba la consigna, y ademas con la funciones ReLU y Tanh.

$$\operatorname{ReLU}(x) = \max(0, x) \operatorname{Tanh}(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$





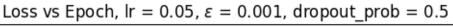


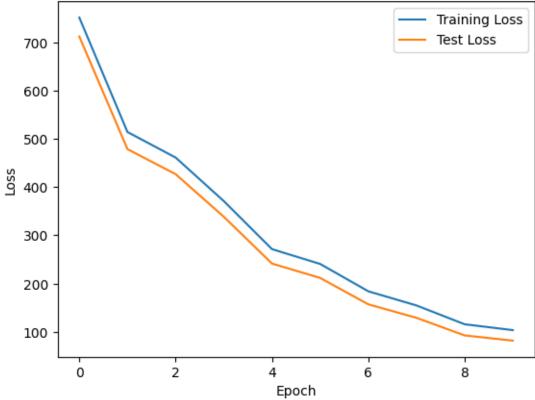
```
[ ]: nn = NeuralNet()
```

 y_true
 27.300000000000000071054

 y_pred
 38.24117112246570826528

 train_loss
 103.20305378438199284119





1.7 Otras funciones de activación

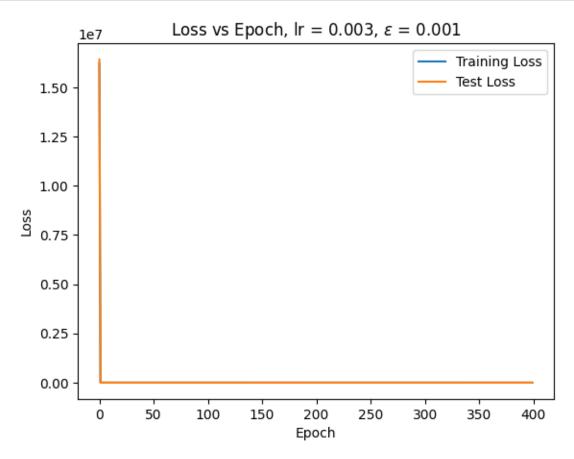
Para la función de activación probamos con la función sigmoide como indicaba la consigna, y ademas con la funciones ReLU, Leaky Relu y Tanh.

$$\operatorname{ReLU}(x) = \max(0, x) \operatorname{LeakyReLU}(x) = \max(0.01x, x) \operatorname{Tanh}(x) = \frac{e^x - e^{-x}}{e^x + e^{-x}}$$

1.7.1 ReLu y Leaky ReLu

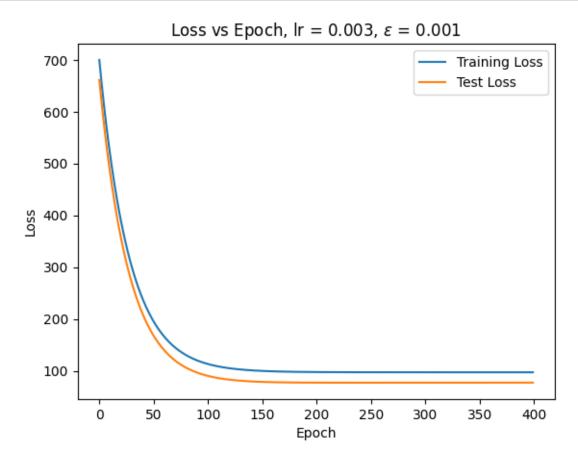
Con las función ReLU y Leaky ReLU no logramos convergencia.

```
[]: nn_relu = NeuralNet()
    nn_relu.fit(X_train, y_train, x_test=X_test, y_test=y_test, lr=0.003,
    epochs=400, custom_activation=nn.relu)
    nn_relu.plot_loss()
```



```
[]: nn_leaky = NeuralNet()
nn_leaky.fit(X_train, y_train, x_test=X_test, y_test=y_test, lr=0.003,
epochs=400, custom_activation=nn.leaky_relu)
nn_leaky.plot_loss()
```

Sin Embargo para la función Tanh si vimos convergencia en nuestras pruebas.

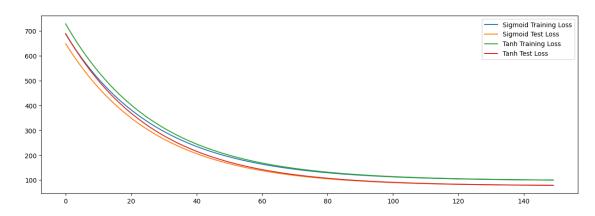


Aca una comparación entre las funciones de activación sigmoide y tanh. En este caso la función de activación tanh hasta converge mas rápido y a una loss menor que la sigmoide.

```
fig, ax = plt.subplots(figsize=(15, 5))
nn = NeuralNet()
nn.fit(X_train, y_train, x_test=X_test, y_test=y_test, lr=0.003, epochs=150)
nn_tanh = NeuralNet()
nn_tanh.fit(X_train, y_train, x_test=X_test, y_test=y_test, lr=0.003, u_tepochs=150, custom_activation=nn.tanh)
ax.plot(nn.get_training_loss(), label="Sigmoid Training Loss")
```

```
ax.plot(nn.get_test_loss(), label="Sigmoid Test Loss")
ax.plot(nn_tanh.get_training_loss(), label="Tanh Training Loss")
ax.plot(nn_tanh.get_test_loss(), label="Tanh Test Loss")
ax.legend()
```

[]: <matplotlib.legend.Legend at 0x7faeb6ae5d30>



1.8 Distintos valores de Learning Rate para distintos Epochs

```
[]: # Brute force para encontrar el mejor número de epochs y learning rate

lrs = np.linspace(0.001, 0.5, 10).round(3)
eps = list(range(1, 1000, 50))

train_losses = {}

test_losses = {}

for lr, ep in tqdm(list(itertools.product(lrs, eps))):
    nn = NeuralNet()
    nn.fit(X_train, y_train, x_test=X_test, y_test=y_test, lr=lr,u=epochs=int(ep))

train_losses[(lr, int(ep))] = nn.get_training_loss()[-1][0]
test_losses[(lr, int(ep))] = nn.get_test_loss()[-1][0]
```

```
100% | 200/200 [06:15<00:00, 1.88s/it]
```

```
[]: train_losses_arr = []
test_losses_arr = []

for (lr, ep), loss in train_losses.items():
    train_losses_arr.append((lr, int(ep), loss))
```

```
for (lr, ep), loss in test_losses.items():
         test_losses_arr.append((lr, int(ep), loss))
     train_losses_df = pd.DataFrame(train_losses_arr, columns=['lr', 'epochs', __

¬'loss'])
     test_losses_df = pd.DataFrame(test_losses_arr, columns=['lr', 'epochs', 'loss'])
     # merge dataframes
     losses_df = pd.merge(train_losses_df, test_losses_df, on=['lr', 'epochs'],
      ⇔suffixes=('_train', '_test'))
     losses df
[]:
                                  epochs
         0.001000000000000000002
     0
                                       1
     1
         0.001000000000000000002
                                      51
     2
         0.001000000000000000002
                                     101
     3
         0.001000000000000000002
                                     151
         0.00100000000000000002
                                     201
     195 0.50000000000000000000
                                     751
     196 0.500000000000000000000
                                     801
     197 0.50000000000000000000
                                     851
     198 0.50000000000000000000
                                     901
     199 0.50000000000000000000
                                     951
                                                   loss_train \
     0
                                    712.35544408202019894816
     1
                                    438.10390531169031191894
     2
                                    277.70827155145241249556
     3
                                    204.45153606491405184897
     4
                                    152.95659639606813584578
     195 10,064,873,608,080,629,039,315,616,564,842,070,...
     196 38,883,928,850,905,498,030,357,258,510,008,320...
     197 1,964,394,829,934,937,164,113,258,741,760.00000...
     198 161,643,292,004,524,220,750,446,944,777,003,859...
     199 5,408,037,911,253,026,769,260,384,748,568,576.0...
                                                    loss_test
     0
                                    673.50730859418263207772
     1
                                    404.09167713681171107964
     2
                                    247.53186235583663687976
     3
                                    176.62372830443592874872
     4
                                    127.33201401750525860734
     195 10,064,873,608,080,626,678,132,375,130,019,463,...
```

```
198 161,643,292,004,524,220,750,446,944,777,003,859...
     199 5,408,037,911,253,026,769,260,384,748,568,576.0...
     [200 rows x 4 columns]
    losses_df.sort_values(by='loss_test', ascending=True).head(10)
Г1:
                                  epochs
                                                      loss train
                              lr
         0.001000000000000000002
                                     701 97.24997849157063001257
         0.00100000000000000002
                                     651 97.36517063828993912011
     13
     15
         0.001000000000000000002
                                     751 97.18700042019692375561
     16
         0.001000000000000000002
                                     801 97.15765470153172600476
     17
         0.001000000000000000002
                                     851 97.13886442836047763194
         0.00100000000000000002
     12
                                     601 97.53729094639008678769
     18
         0.001000000000000000002
                                     901 97.12979841319094020946
         0.001000000000000000002
                                     951 97.12443781084131444459
     148 0.38900000000000001243
                                     401 97.11721857464502249968
     182 0.500000000000000000000
                                     101 97.11721191618177329019
                       loss_test
     14
         77.04882381592535978143
         77.06209465460953822458
     13
     15
         77.06229356767643423609
         77.08106987569057366727
     17
         77.10344679716750704301
     12
        77.11963007880184761689
     18
        77.12105310560889392946
        77.13643326268517341759
     148 77.19205646245166008157
     182 77.19363039787369018541
[]: losses_df.sort_values(by='loss_train', ascending=True).head(10)
[]:
                              lr
                                  epochs
                                                      loss_train
     81
         0.2230000000000000377
                                      51 97.11721158982109614044
        0.2230000000000000377
                                     901 97.11721158982109614044
     98
     118 0.27800000000000002487
                                     901 97.11721158982109614044
        0.05600000000000000117
                                     301 97.11721158982109614044
     95
         0.2230000000000000377
                                     751 97.11721158982109614044
     45
         0.11200000000000000233
                                     251 97.11721158982109614044
     42
        0.11200000000000000233
                                     101 97.11721158982109614044
     44
        0.11200000000000000233
                                     201 97.11721158982109614044
                                     401 97.11721158982109614044
     28
         0.05600000000000000117
     71
        0.16700000000000000955
                                     551 97.11721158982109614044
```

196 38,883,928,850,905,493,418,671,240,082,620,416... 197 1,964,394,829,934,938,571,488,142,295,040.0000...

```
loss_test
81 77.19406594744638994143
98 77.19406594746409666641
118 77.19406594745940708435
26 77.19406594745862548734
95 77.19406594745851180051
45 77.19406594745805705315
42 77.19406594745773020350
44 77.19406594745751704068
28 77.19406594745743177555
71 77.19406594745981919914
```

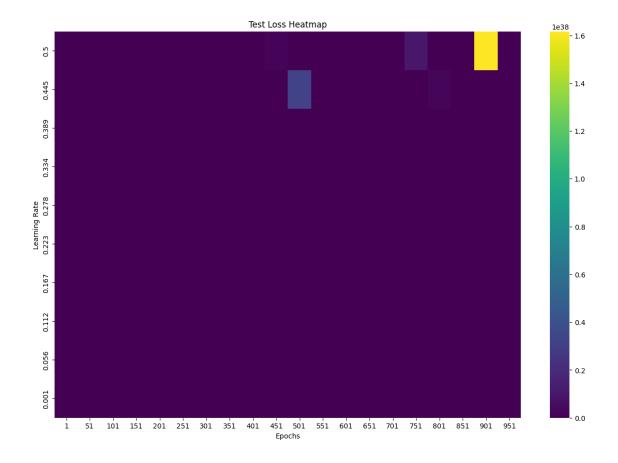
Muchos de los valores de la convergen a la misma loss minima \sim (97.117), pero algunos lo hacen mas rapido que otros. En nuestra experimentación con el Learning Rate, obtuvimos que para lr=0.05 y epoch=20, la Loss alcanzaba \sim (97.118).

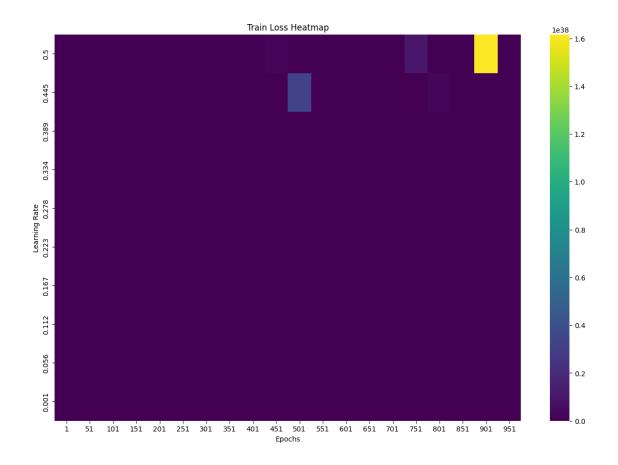
En estos gráficos de calor podemos ver como la mayoría de los learning rates para cierto epoch logran converger a este mismo valor.

```
[]: losses_df_hm = losses_df.pivot(index='lr', columns='epochs', values='loss_test')

fig, ax = plt.subplots(figsize=(15, 10))

sns.heatmap(losses_df_hm, ax=ax, cmap='viridis')
ax.set_xlabel('Epochs')
ax.set_ylabel('Learning Rate')
ax.set_title('Test Loss Heatmap')
ax.invert_yaxis()
plt.show()
```



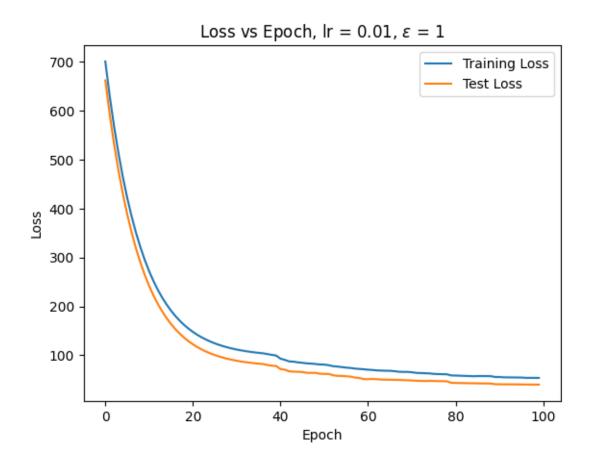


Para lograr obtener una menor Loss, probamos modificando el valor de Epsilon

 y_true
 27.30000000000000000071054

 y_pred
 28.85025195570380773802

 train_loss
 53.80364135528142099929

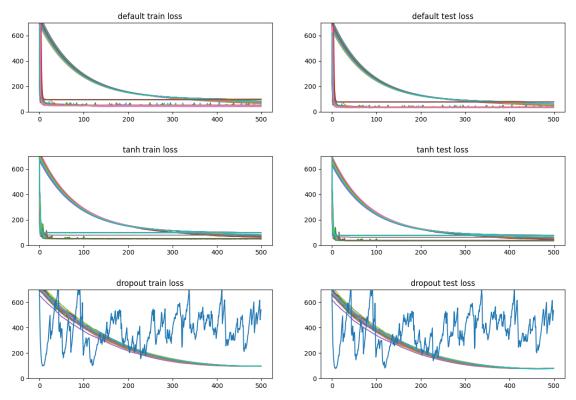


1.9 Combinaciones de Learning Rate y Epsilon

Buscamos ver como variando el Epsilon junto al Learning Rate para una cantidad fija arbitraria de epochs podemos encontrar un valor de la que converja mas rápido sobre los modelos con las funciones de activación Tanh y Sigmoide, esta última con y sin Dropout de pesos. Ademas, vamos a ver como cambia la loss minima para cuando finalice el entrenamiento.

```
[]: 200
[]: losses = {
         'default': {
             'train': {},
             'test': {}
         },
         'tanh': {
             'train': {},
             'test': {}
         },
         'dropout': {
             'train': {},
             'test': {}
         },
     }
[]: for lr, ep, eps in tqdm(list(itertools.product(lrs, epochs, epsilons))):
         nn = NeuralNet()
         nn.fit(X_train, y_train, x_test=X_test, y_test=y_test, lr=lr,_
      ⇔epochs=int(ep), eps=eps)
         losses['default']['train'][lr, ep, eps] = nn.get_training_loss()
         losses['default']['test'][lr, ep, eps] = nn.get_test_loss()
         nn_drop = NeuralNet()
         nn_drop.fit(X_train, y_train, x_test=X_test, y_test=y_test, lr=lr,_
      ⇔epochs=int(ep), eps=eps, dropout=True)
         losses['dropout']['train'][lr, ep, eps] = nn_drop.get_training_loss()
         losses['dropout']['test'][lr, ep, eps] = nn_drop.get_test_loss()
         nn_tanh = NeuralNet()
         nn_tanh.fit(X_train, y_train, x_test=X_test, y_test=y_test, lr=lr,_
      →epochs=int(ep), eps=eps, custom_activation=nn_tanh.tanh)
         losses['tanh']['train'][lr, ep, eps] = nn_tanh.get_training_loss()
         losses['tanh']['test'][lr, ep, eps] = nn_tanh.get_test_loss()
      1%1
                   | 2/200 [00:10<17:29, 5.30s/it]/var/folders/5j/7b3w3dw95qdcll87v
    xc3yn30000gn/T/ipykernel_64997/343068776.py:30: RuntimeWarning: overflow
    encountered in exp
      return 1 / (1 + np.exp(-x))
              | 200/200 [17:34<00:00, 5.27s/it]
    100%|
[]: fig, axs = plt.subplots(len(losses.keys()), 2, figsize=(15, 10))
     for i, (variation, train test) in enumerate(losses.items()):
         for (lr, ep, eps), loss in train_test['train'].items():
```

```
# De forma empírica observamos que con pesos aleatorios, la loss⊔
 ⇔comienza al rededor de ~700
        # Evitamos en el gráfico aquellos que superen en algún momento esa loss_{f \sqcup}
 ⇔para limpiar
        if any([1 > 800 for 1 in loss]):
            continue
        axs[i, 0].plot(loss, label=f'lr={lr}, ep={ep}, eps={eps}')
    for (lr, ep, eps), loss in train_test['test'].items():
        if any([1 > 800 for 1 in loss]):
            continue
        axs[i, 1].plot(loss, label=f'lr={lr}, ep={ep}, eps={eps}')
    axs[i, 0].set_title(f'{variation} train loss')
    axs[i, 1].set_title(f'{variation} test loss')
    axs[i, 0].set_ylim(0, 700)
    axs[i, 1].set_ylim(0, 700)
# Add space between subplots
fig.subplots_adjust(hspace=0.5)
```



Podemos observar como para ciertas combinaciones de Learning Rate y Epochs la convergencia es

mas rápida.

Para la función de activación ReLU observamos que la convergencía no ocurre directamente por lo que se dejo de evaluar, la función Tanh sin embargo si converge, pero no logra alcanzar la misma loss minima que la función sigmoide.

Para la mascara de pesos, probamos con una probabilidad de 0.5. En todos los casos la convergencia fue o mas lenta, y la loss minima alcanzada mayor que la obtenida sin aplicar la mascara, o directamente esporádico sin convergencia.

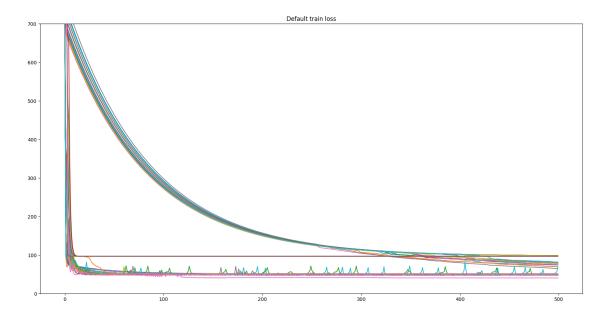
```
[]: # Large Default Training Loss Plot
fig, ax = plt.subplots(figsize=(20, 10))

for (lr, ep, eps), loss in losses['default']['train'].items():
    if any([1 > 800 for 1 in loss]):
        continue
    ax.plot(loss, label=f'lr={lr}, ep={ep}, eps={eps}')

ax.set_title(f'Default train loss')
#ax.legend()

ax.set_ylim(0, 700)
```

[]: (0.0, 700.0)

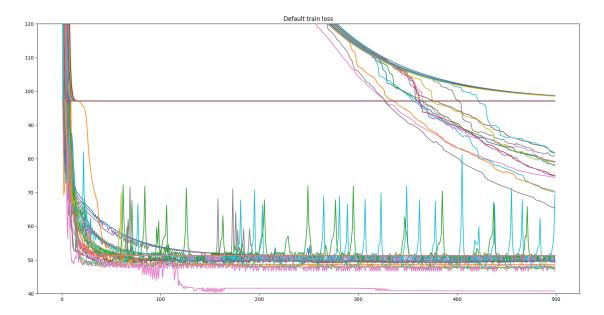


```
[]: # Large Default Training Loss Plot
fig, ax = plt.subplots(figsize=(20, 10))
```

```
for (lr, ep, eps), loss in losses['default']['train'].items():
    if any([l > 800 for l in loss]):
        continue
    ax.plot(loss, label=f'lr={lr}, ep={ep}, eps={eps}')

ax.set_title(f'Default train loss')
ax.set_ylim(40, 120)
```

[]: (40.0, 120.0)

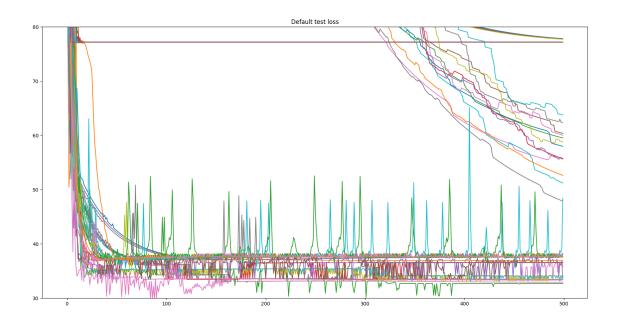


```
[]: # Large Default Test Loss Plot
fig, ax = plt.subplots(figsize=(20, 10))

for (lr, ep, eps), loss in losses['default']['test'].items():
    if any([l > 800 for l in loss]):
        continue
    ax.plot(loss, label=f'lr={lr}, ep={ep}, eps={eps}')

ax.set_title(f'Default test loss')
ax.set_ylim(30, 80)
```

[]: (30.0, 80.0)

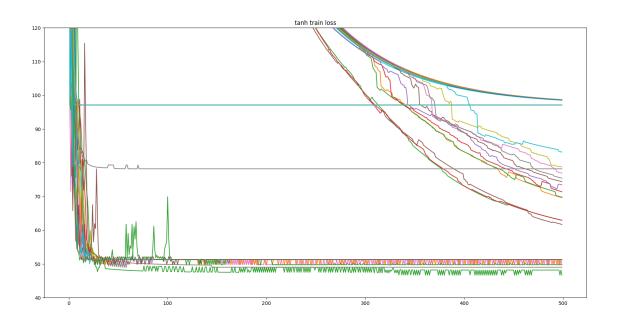


```
[]: # Large Default Training Loss Plot
fig, ax = plt.subplots(figsize=(20, 10))

for (lr, ep, eps), loss in losses['tanh']['train'].items():
    if any([1 > 800 for 1 in loss]):
        continue
    ax.plot(loss, label=f'lr={lr}, ep={ep}, eps={eps}')

ax.set_title(f'tanh train loss')
ax.set_ylim(40, 120)
```

[]: (40.0, 120.0)



```
[]: # Filter out the best learning rate - epsilons combinations for the Default NN
    # The 20 lowest training loss by epoch 200

# Sort by the loss at epoch 250

train_loss = losses['default']['train'].items()

train_loss = sorted(train_loss, key=lambda x: x[1][250])

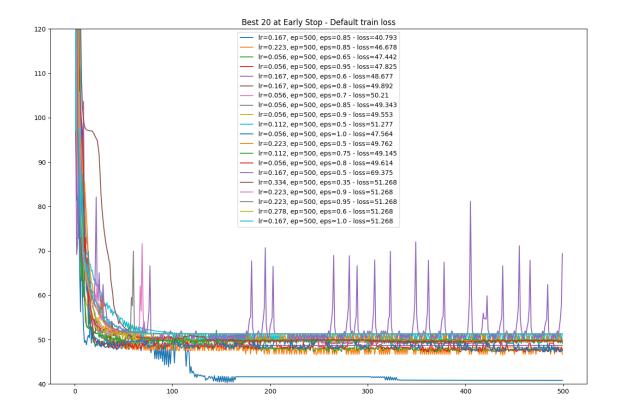
# Plot every train_loss[:20]

fig, ax = plt.subplots(figsize=(15, 10))

for (lr, ep, eps), loss in train_loss[:20]:
    ax.plot(loss, label=f'lr={lr}, ep={ep}, eps={eps} - loss={loss[-1].
    -round(3)[0]}')

ax.set_title(f'Best 20 at Early Stop - Default train loss')
ax.set_ylim(40, 120)
ax.legend()
```

[]: <matplotlib.legend.Legend at 0x7faec6a079a0>



```
[]: # Filter out the best learning rate - epsilons combinations for the Default NN
    # The 20 lowest training loss by epoch 200

# Sort by the loss at epoch 250

train_loss = losses['tanh']['train'].items()

train_loss = sorted(train_loss, key=lambda x: x[1][250])

# Plot every train_loss[:20]

fig, ax = plt.subplots(figsize=(15, 10))

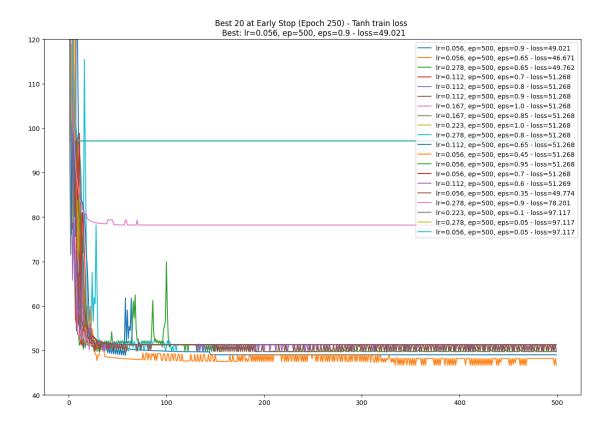
for (lr, ep, eps), loss in train_loss[:20]:
    ax.plot(loss, label=f'lr={lr}, ep={ep}, eps={eps} - loss={loss[-1].
    -round(3)[0]}')

(min_250_lr, min_250_ep, min_250_eps), min_250_loss = train_loss[0]

ax.set_title(f'Best 20 at Early Stop (Epoch 250) - Tanh train loss \n Best:
    -lr={min_250_lr}, ep={min_250_ep}, eps={min_250_eps} - loss={min_250_loss[-1].
    -round(3)[0]}')
```

```
ax.set_ylim(40, 120)
ax.legend()
```

[]: <matplotlib.legend.Legend at 0x7faec6e9d310>



```
fig, ax = plt.subplots(figsize=(15, 10))

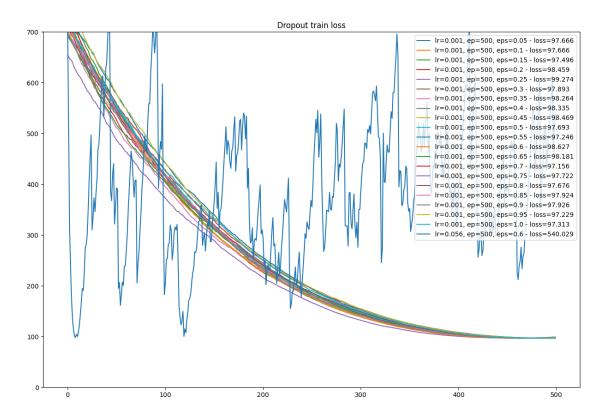
for (lr, ep, eps), loss in losses['dropout']['train'].items():

    # If loss has any value > 800, skip
    if any([1 > 800 for l in loss]):
        continue

    ax.plot(loss, label=f'lr={lr}, ep={ep}, eps={eps} - loss={loss[-1].
        -round(3)[0]}')

ax.set_title(f'Dropout train loss')
ax.set_ylim(0, 700)
ax.legend()
```

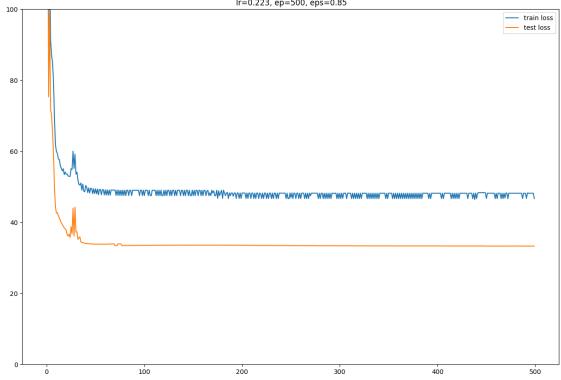
[]: <matplotlib.legend.Legend at 0x7faea3223520>



[]: (0.0, 100.0)

Best train loss at epoch 100

Final Loss=46.678 Loss ep100 = 47.525 Ir=0.223, ep=500, eps=0.85



```
[]: # Filter dropout losses, if any > 800

less_dropout_train_loss = {}
less_dropout_test_loss = {}

for (lr, ep, eps), loss in losses['dropout']['train'].items():
    if any([1 > 800 for 1 in loss]):
        continue
    less_dropout_train_loss[(lr, ep, eps)] = loss
    less_dropout_test_loss[(lr, ep, eps)] = losses['dropout']['test'][(lr, ep, useps)]

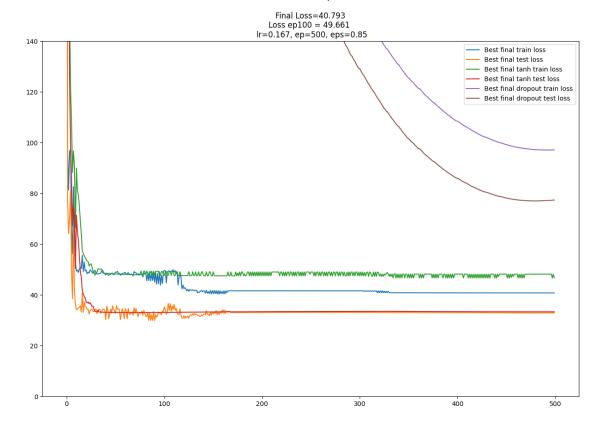
deps)]
```

```
min_tanh_test_loss = losses['tanh']['test'][(min_tanh_lr, min_tanh_ep,_u

→min_tanh_eps)]
(min_dropout_lr, min_dropout_ep, min_dropout_eps), min_dropout_train_loss = __
 →min(less_dropout_train_loss.items(), key=lambda x: x[1][-1])
min_dropout_test_loss = less_dropout_test_loss[(min_dropout_lr, min_dropout_ep,_
 →min_dropout_eps)]
fig, ax = plt.subplots(figsize=(15, 10))
ax.plot(min_train_loss, label=f'Best final train loss')
ax.plot(min_test_loss, label=f'Best final test loss')
ax.plot(min_tanh_train_loss, label=f'Best final tanh train loss')
ax.plot(min_tanh_test_loss, label=f'Best final tanh test loss')
ax.plot(min_dropout_train_loss, label=f'Best final dropout train loss')
ax.plot(min_dropout_test_loss, label=f'Best final_dropout_test_loss')
ax.set_title(f'Best train loss at epoch 500 \n\n Final Loss={min_train_loss[-1].
 \neground(3)[0]} \n Loss ep100 = {min_train_loss[100].round(3)[0]} \n_\[ \n_\]
 coltr={min_lr}, ep={min_ep}, eps={min_eps}')
ax.legend()
ax.set_ylim(0, 140)
```

[]: (0.0, 140.0)

Best train loss at epoch 500



```
values_df = pd.DataFrame({
    'learning rate': [min_lr, min_tanh_lr, min_dropout_lr],
    'epsilon': [min_eps, min_tanh_eps, min_dropout_eps],
    'epochs': [min_ep, min_tanh_ep, min_dropout_ep],
    'train_loss': [min_train_loss[-1].round(3)[0], min_tanh_train_loss[-1].
    'round(3)[0], min_dropout_train_loss[-1].round(3)[0]],
    'test_loss': [min_test_loss[-1].round(3)[0]],
    'train_loss_ep100': [min_train_loss[100].round(3)[0]],
    'min_tanh_train_loss[100].round(3)[0], min_dropout_train_loss[100].
    'round(3)[0]],
    'test_loss_ep100': [min_test_loss[100].round(3)[0], min_tanh_test_loss[100].
    'cound(3)[0], min_dropout_test_loss[100].round(3)[0]],
    'tound(3)[0], min_dropout_test_loss[100].round(3)[0]],
}, index=['default', 'tanh', 'dropout'])
```

```
[]: learning rate epsilon epochs \
default 0.167000000000000000055 0.84999999999999997780 500
tanh 0.0560000000000000117 0.6500000000000002220 500
```

```
train_loss test_loss \
default 40.79299999999999926104 32.90899999999999999891998
tanh 46.67099999999999937472 33.3459999999999653255
dropout 97.15600000000000591172 77.38200000000000500222

train_loss_ep100 test_loss_ep100
default 49.6610000000000136424 35.2610000000000278533
tanh 47.7259999999999999951 33.1349999999999901048
dropout 428.0169999999999590727 394.21499999999997498890
```

1.10 Conclusiones

En este trabajo práctico pudimos ver como el gradiente descendente nos permite entrenar una red neuronal. Pudimos ver como la función de activación sigmoide es la mas adecuada para este tipo de problemas, y como el learning rate y la cantidad de epochs afectan la convergencia de la red.

También pudimos ver como la mascara de pesos no es una buena opción para este tipo de problemas, ya que no logra converger a una loss minima menor que la obtenida sin aplicar la mascara.

```
[]: nn final = NeuralNet()
     nn_final.fit(X_train, y_train, x_test=X_test, y_test=y_test, epochs=1000,_u
      →lr=min_lr, eps=min_eps, verbose=True)
     display(pd.Series(
         y test[0][0],
             nn_final.predict(X_test[0].reshape(1, -1))[0][0],
             nn_final.get_training_loss()[-1][0]
         ],
         index=["y_true", "y_pred", "train_loss"]
     ))
     fig, ax = plt.subplots(figsize=(15, 10))
     nn_final.plot_loss(ax=ax)
     _{-} = ax.set_ylim(0, 100)
    100%|
               | 1000/1000 [00:04<00:00, 219.65it/s]
```

y_true 27.3000000000000001054 y_pred 27.23155726721838831850 train_loss 40.78857608365985498722

