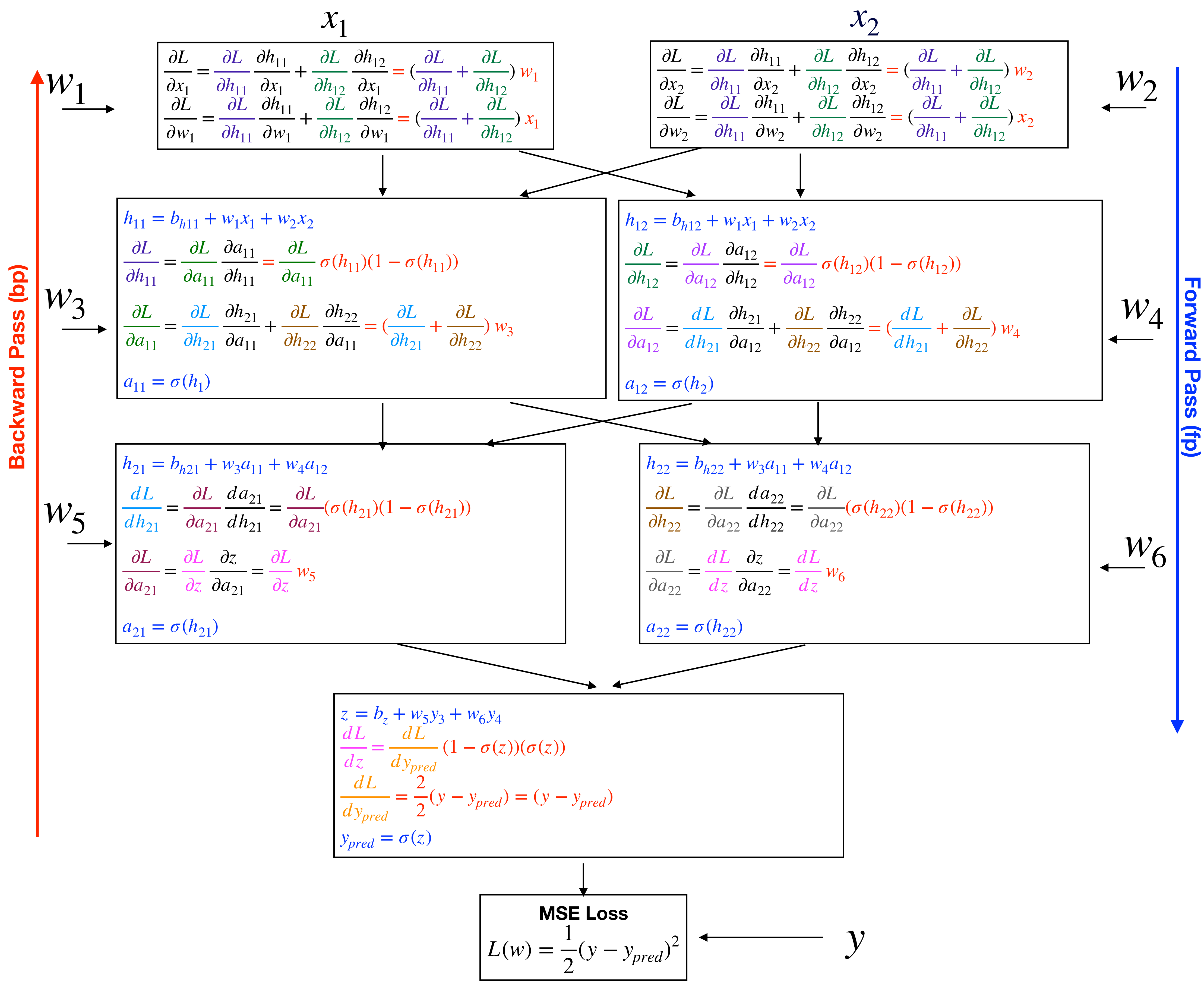
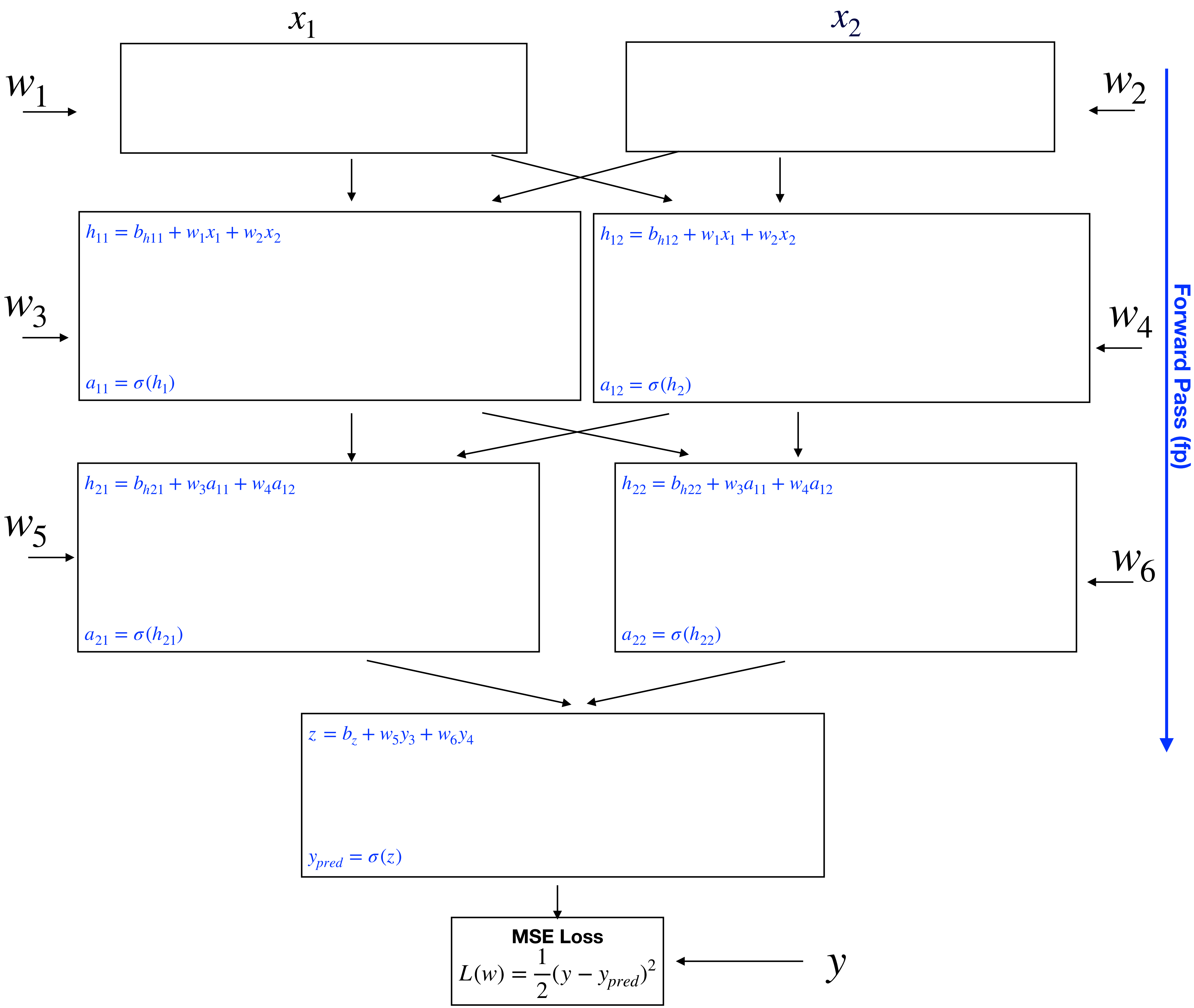
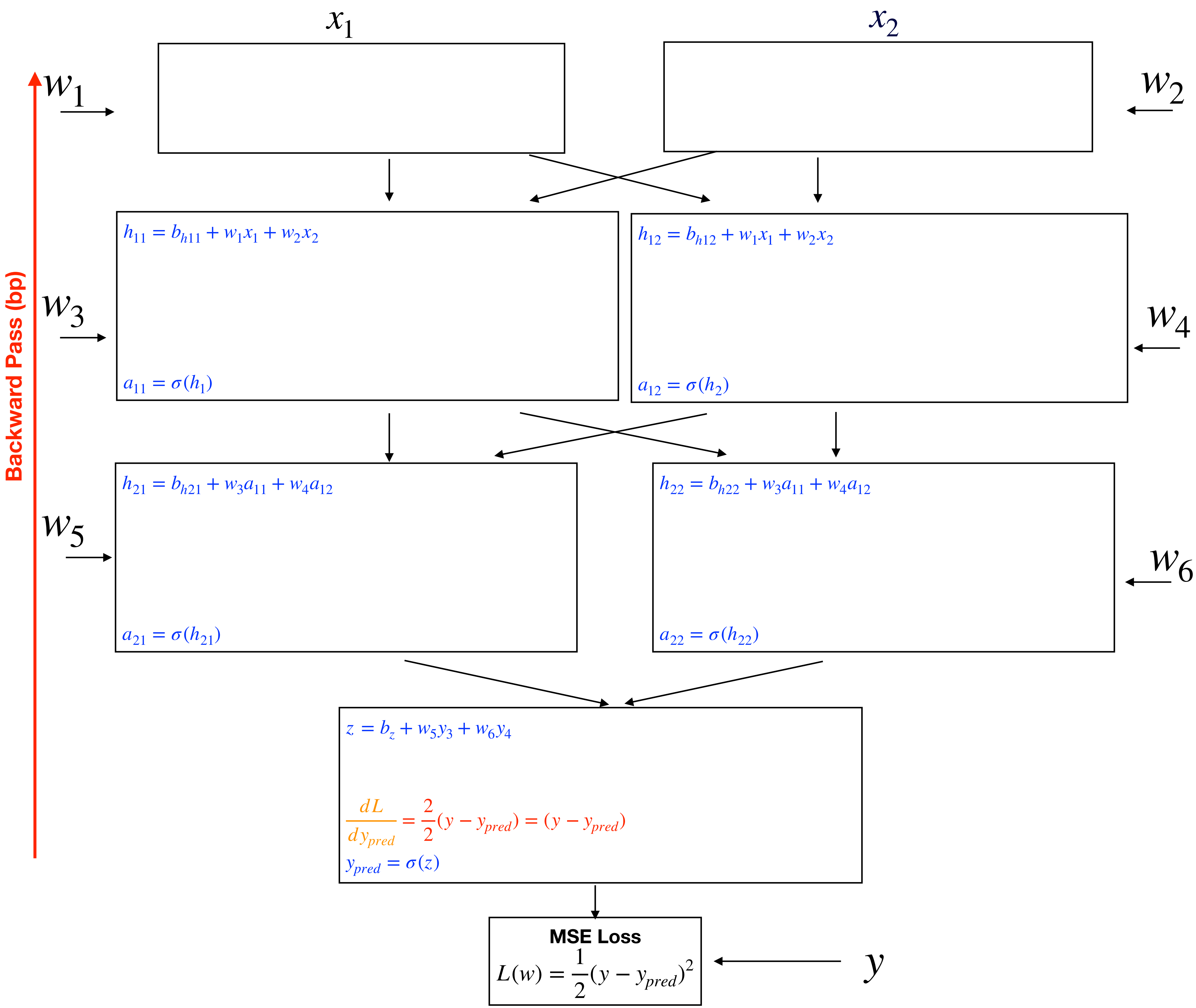
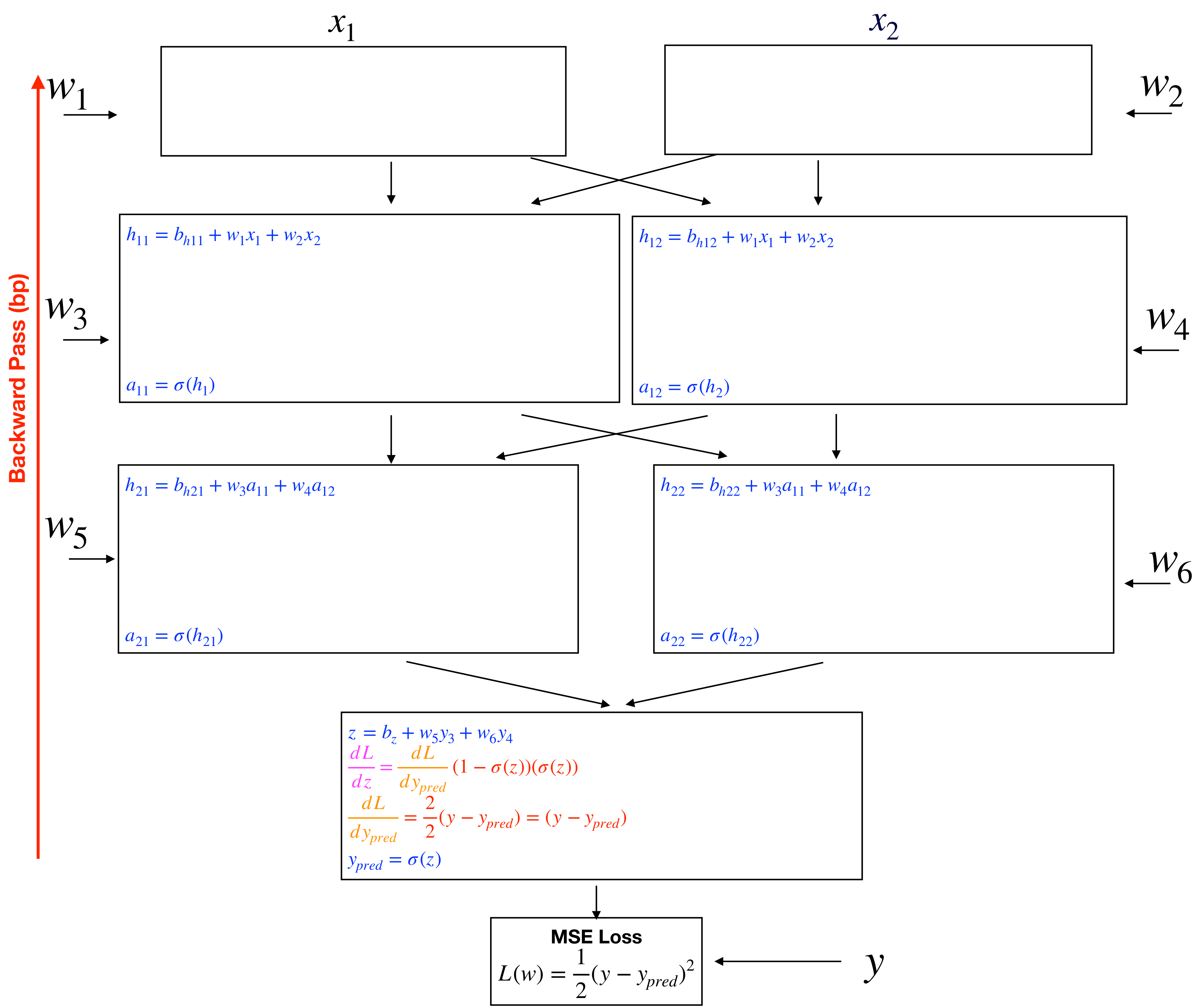


x_1
$\frac{\partial L}{\partial x_1} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial x_1} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial x_1} = (\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}})\, w_1$
$\frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial w_1} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial w_1} = (\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}})\, x_1$
x_2
$\frac{\partial L}{\partial x_2} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial x_2} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial x_2} = (\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}})\, w_2$
$\frac{\partial L}{\partial w_2} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial w_2} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial w_2} = (\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}})\, x_2$
w_1
w_2
Backward Pass (bp)
Forward Pass (fp)
w_3
$h_{11} = b_{h11} + w_1x_1 + w_2x_2$
$\frac{\partial L}{\partial h_{11}} = \frac{\partial L}{\partial a_{11}}\frac{\partial a_{11}}{\partial h_{11}} = \frac{\partial L}{\partial a_{11}}\sigma(h_{11})(1-\sigma(h_{11}))$
$\frac{\partial L}{\partial a_{11}} = \frac{\partial L}{\partial h_{21}}\frac{\partial h_{21}}{\partial a_{11}} + \frac{\partial L}{\partial h_{22}}\frac{\partial h_{22}}{\partial a_{11}} = (\frac{\partial L}{\partial h_{21}} + \frac{\partial L}{\partial h_{22}})\, w_3$
$a_{11} = \sigma(h_1)$
w_4
$h_{12} = b_{h12} + w_1x_1 + w_2x_2$
$\frac{\partial L}{\partial h_{12}} = \frac{\partial L}{\partial a_{12}}\frac{\partial a_{12}}{\partial h_{12}} = \frac{\partial L}{\partial a_{12}}\sigma(h_{12})(1-\sigma(h_{12}))$
$\frac{\partial L}{\partial a_{12}} = \frac{dL}{dh_{21}}\frac{\partial h_{21}}{\partial a_{12}} + \frac{\partial L}{\partial h_{22}}\frac{\partial h_{22}}{\partial a_{12}} = (\frac{dL}{dh_{21}} + \frac{\partial L}{\partial h_{22}})\, w_4$
$a_{12} = \sigma(h_2)$
w_5
$h_{21} = b_{h21} + w_3a_{11} + w_4a_{12}$
$\frac{dL}{dh_{21}} = \frac{\partial L}{\partial a_{21}}\frac{da_{21}}{dh_{21}} = \frac{\partial L}{\partial a_{21}}(\sigma(h_{21})(1-\sigma(h_{21}))$
$\frac{\partial L}{\partial a_{21}} = \frac{\partial L}{\partial z}\frac{\partial z}{\partial a_{21}} = \frac{\partial L}{\partial z}\, w_5$
$a_{21} = \sigma(h_{21})$
w_6
$h_{22} = b_{h22} + w_3a_{11} + w_4a_{12}$
$\frac{\partial L}{\partial h_{22}} = \frac{\partial L}{\partial a_{22}}\frac{da_{22}}{dh_{22}} = \frac{\partial L}{\partial a_{22}}(\sigma(h_{22})(1-\sigma(h_{22}))$
$\frac{\partial L}{\partial a_{22}} = \frac{dL}{dz}\frac{\partial z}{\partial a_{22}} = \frac{dL}{dz}\, w_6$
$a_{22} = \sigma(h_{22})$
$z = b_z + w_5y_3 + w_6y_4$
$\frac{dL}{dz} = \frac{dL}{dy_{pred}}(1-\sigma(z))(\sigma(z))$
$\frac{dL}{dy_{pred}} = \frac{2}{2}(y - y_{pred}) = (y - y_{pred})$
$y_{pred} = \sigma(z)$
MSE Loss
$L(w) = \frac{1}{2}(y - y_{pred})^2$
y

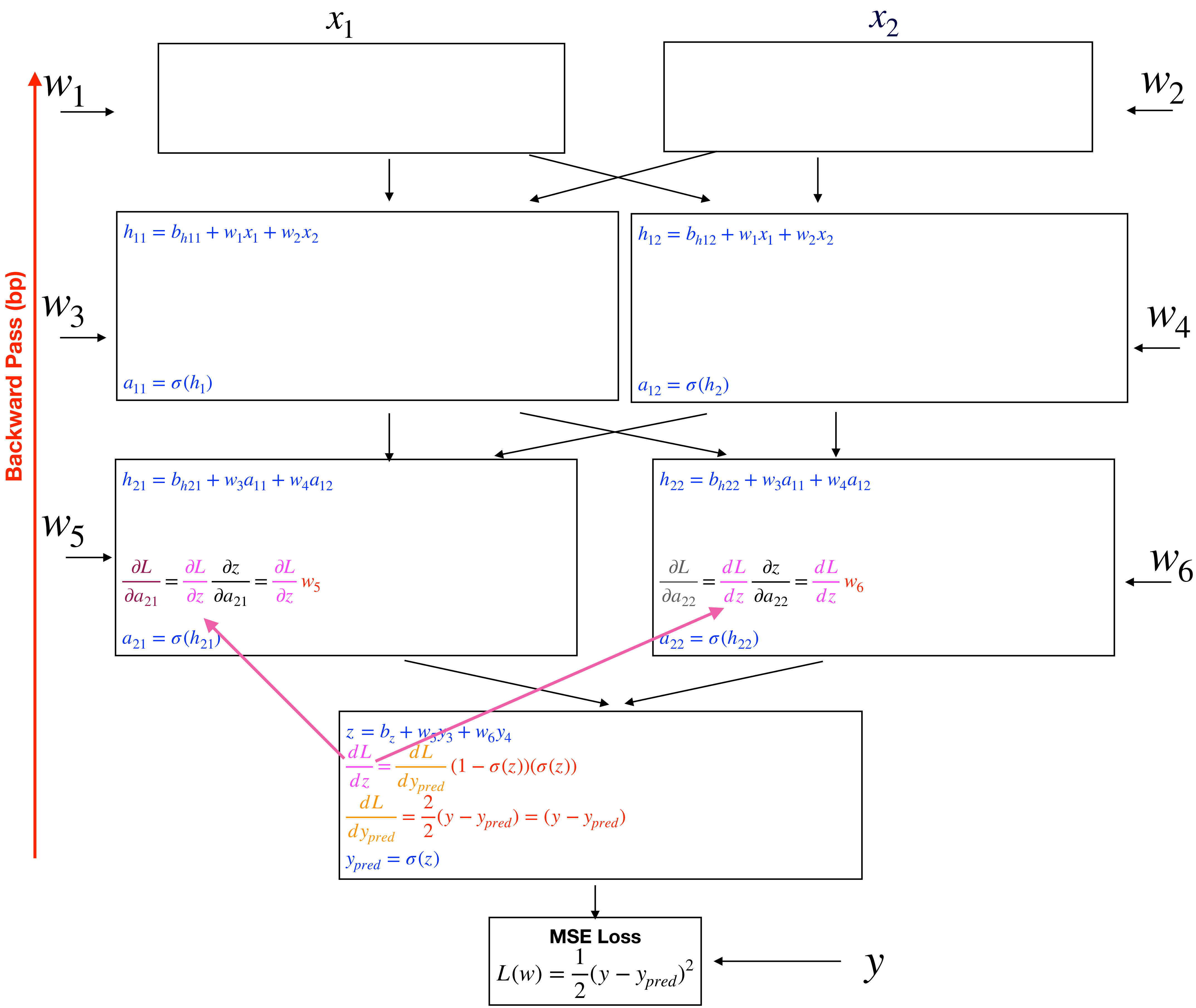


x_1
x_2
w_1
w_2
$h_{11} = b_{h11} + w_1 x_1 + w_2 x_2$
$a_{11} = \sigma(h_1)$
$h_{12} = b_{h12} + w_1 x_1 + w_2 x_2$
$a_{12} = \sigma(h_2)$
w_3
w_4
Forward Pass (fp)
$h_{21} = b_{h21} + w_3 a_{11} + w_4 a_{12}$
$a_{21} = \sigma(h_{21})$
$h_{22} = b_{h22} + w_3 a_{11} + w_4 a_{12}$
$a_{22} = \sigma(h_{22})$
w_5
w_6
$z = b_z + w_5 y_3 + w_6 y_4$
$y_{pred} = \sigma(z)$
MSE Loss
$L(w) = \frac{1}{2}(y - y_{pred})^2$
y

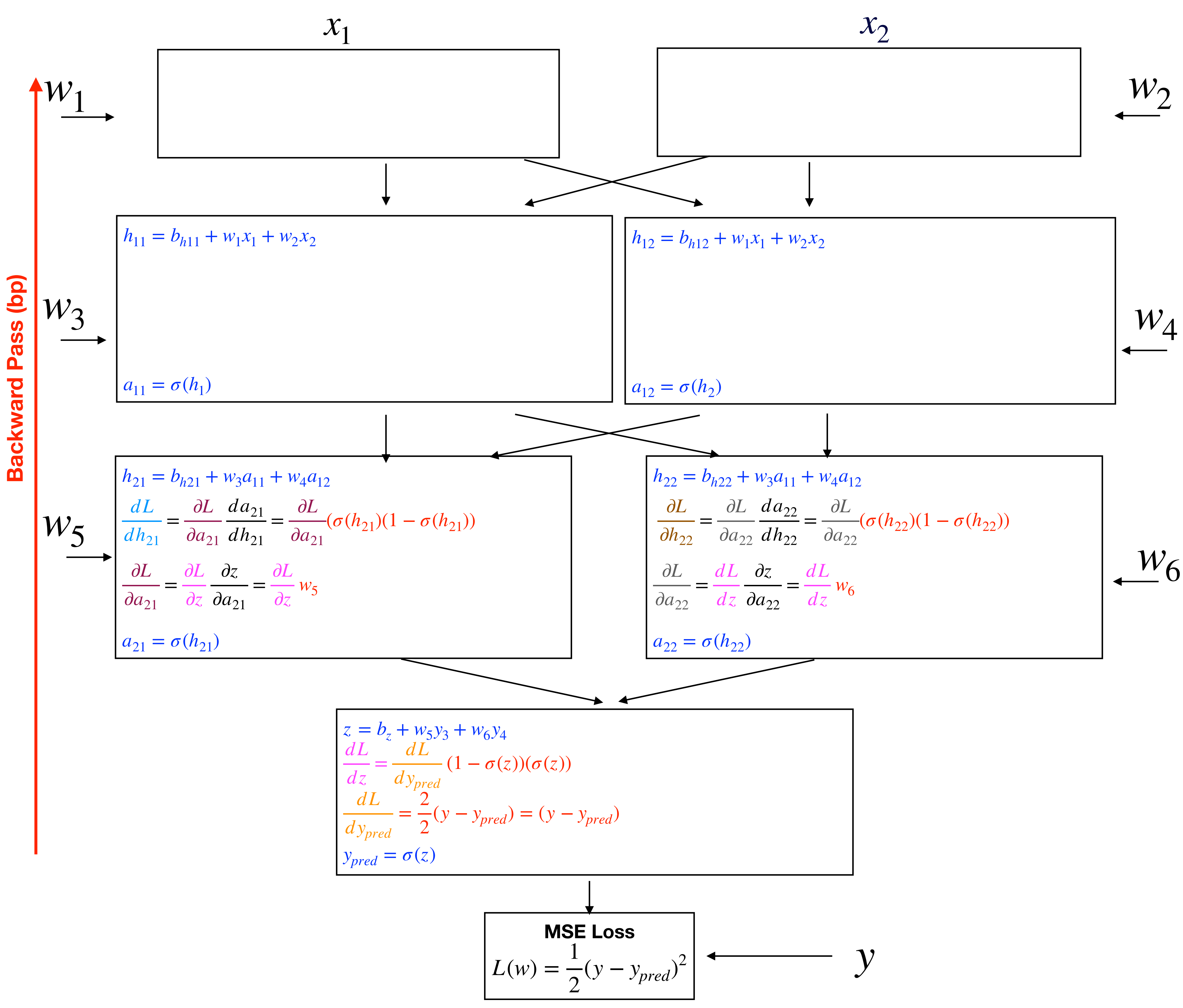

x_1
x_2
w_1
w_2
Backward Pass (bp)
w_3
$h_{11} = b_{h11} + w_1x_1 + w_2x_2$
$a_{11} = \sigma(h_1)$
$h_{12} = b_{h12} + w_1x_1 + w_2x_2$
$a_{12} = \sigma(h_2)$
w_4
w_5
$h_{21} = b_{h21} + w_3a_{11} + w_4a_{12}$
$a_{21} = \sigma(h_{21})$
$h_{22} = b_{h22} + w_3a_{11} + w_4a_{12}$
$a_{22} = \sigma(h_{22})$
w_6
$z = b_z + w_5y_3 + w_6y_4$
$\frac{dL}{dy_{pred}} = \frac{2}{2}(y - y_{pred}) = (y - y_{pred})$
$y_{pred} = \sigma(z)$
MSE Loss
$L(w) = \frac{1}{2}(y - y_{pred})^2$
y



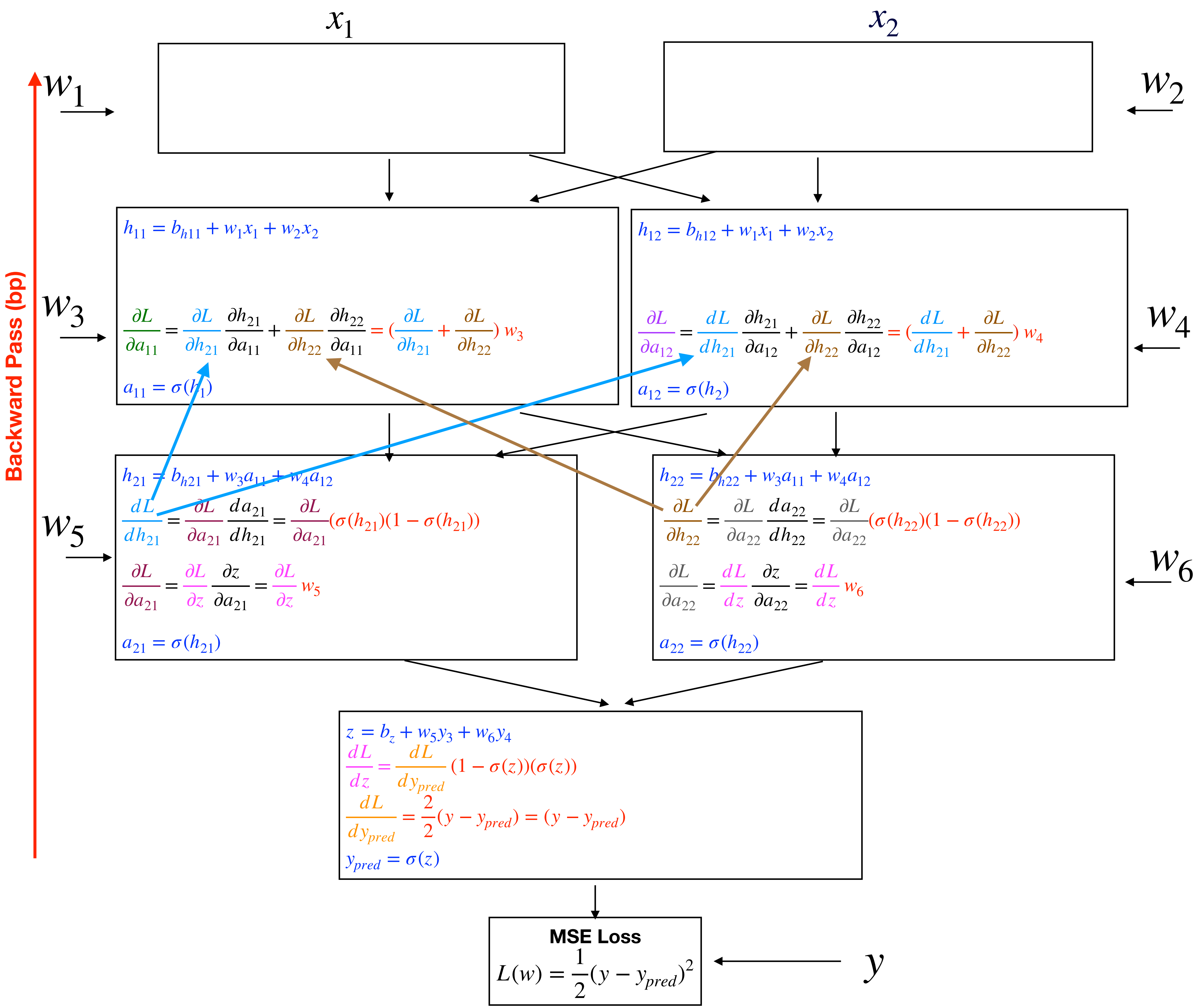
x_1
x_2
w_1
w_2
Backward Pass (bp)
$h_{11} = b_{h11} + w_1 x_1 + w_2 x_2$
$a_{11} = \sigma(h_1)$
$h_{12} = b_{h12} + w_1 x_1 + w_2 x_2$
$a_{12} = \sigma(h_2)$
w_3
w_4
$h_{21} = b_{h21} + w_3 a_{11} + w_4 a_{12}$
$a_{21} = \sigma(h_{21})$
$h_{22} = b_{h22} + w_3 a_{11} + w_4 a_{12}$
$a_{22} = \sigma(h_{22})$
w_5
w_6
$z = b_z + w_5 y_3 + w_6 y_4$
$\frac{dL}{dz} = \frac{dL}{dy_{pred}}(1 - \sigma(z))(\sigma(z))$
$\frac{dL}{dy_{pred}} = \frac{2}{2}(y - y_{pred}) = (y - y_{pred})$
$y_{pred} = \sigma(z)$
MSE Loss
$L(w) = \frac{1}{2}(y - y_{pred})^2$
y



Backward Pass (bp)
x_1
x_2
w_1
w_2
w_3
w_4
w_5
w_6
$h_{11} = b_{h11} + w_1 x_1 + w_2 x_2$
$a_{11} = \sigma(h_1)$
$h_{12} = b_{h12} + w_1 x_1 + w_2 x_2$
$a_{12} = \sigma(h_2)$
$h_{21} = b_{h21} + w_3 a_{11} + w_4 a_{12}$
$\frac{\partial L}{\partial a_{21}} = \frac{\partial L}{\partial z}\frac{\partial z}{\partial a_{21}} = \frac{\partial L}{\partial z} w_5$
$a_{21} = \sigma(h_{21})$
$h_{22} = b_{h22} + w_3 a_{11} + w_4 a_{12}$
$\frac{\partial L}{\partial a_{22}} = \frac{dL}{dz}\frac{\partial z}{\partial a_{22}} = \frac{dL}{dz} w_6$
$a_{22} = \sigma(h_{22})$
$z = b_z + w_5 y_3 + w_6 y_4$
$\frac{dL}{dz} = \frac{dL}{dy_{pred}}(1 - \sigma(z))(\sigma(z))$
$\frac{dL}{dy_{pred}} = \frac{2}{2}(y - y_{pred}) = (y - y_{pred})$
$y_{pred} = \sigma(z)$
MSE Loss
$L(w) = \frac{1}{2}(y - y_{pred})^2$
y



x_1
x_2
w_1
w_2
Backward Pass (bp)
$h_{11} = b_{h11} + w_1 x_1 + w_2 x_2$
$a_{11} = \sigma(h_1)$
w_3
$h_{12} = b_{h12} + w_1 x_1 + w_2 x_2$
$a_{12} = \sigma(h_2)$
w_4
w_5
$h_{21} = b_{h21} + w_3 a_{11} + w_4 a_{12}$
$\frac{dL}{dh_{21}} = \frac{\partial L}{\partial a_{21}} \frac{da_{21}}{dh_{21}} = \frac{\partial L}{\partial a_{21}} (\sigma(h_{21})(1 - \sigma(h_{21}))$
$\frac{\partial L}{\partial a_{21}} = \frac{\partial L}{\partial z} \frac{\partial z}{\partial a_{21}} = \frac{\partial L}{\partial z} w_5$
$a_{21} = \sigma(h_{21})$
$h_{22} = b_{h22} + w_3 a_{11} + w_4 a_{12}$
$\frac{\partial L}{\partial h_{22}} = \frac{\partial L}{\partial a_{22}} \frac{da_{22}}{dh_{22}} = \frac{\partial L}{\partial a_{22}} (\sigma(h_{22})(1 - \sigma(h_{22}))$
$\frac{\partial L}{\partial a_{22}} = \frac{dL}{dz} \frac{\partial z}{\partial a_{22}} = \frac{dL}{dz} w_6$
$a_{22} = \sigma(h_{22})$
w_6
$z = b_z + w_5 y_3 + w_6 y_4$
$\frac{dL}{dz} = \frac{dL}{dy_{pred}} (1 - \sigma(z))(\sigma(z))$
$\frac{dL}{dy_{pred}} = \frac{2}{2}(y - y_{pred}) = (y - y_{pred})$
$y_{pred} = \sigma(z)$
MSE Loss
$L(w) = \frac{1}{2}(y - y_{pred})^2$
y



x_1
x_2
w_1
w_2
Backward Pass (bp)
$h_{11} = b_{h11} + w_1 x_1 + w_2 x_2$
w_3
$\frac{\partial L}{\partial a_{11}} = \frac{\partial L}{\partial h_{21}} \frac{\partial h_{21}}{\partial a_{11}} + \frac{\partial L}{\partial h_{22}} \frac{\partial h_{22}}{\partial a_{11}} = (\frac{\partial L}{\partial h_{21}} + \frac{\partial L}{\partial h_{22}})\, w_3$
$a_{11} = \sigma(h_1)$
$h_{12} = b_{h12} + w_1 x_1 + w_2 x_2$
w_4
$\frac{\partial L}{\partial a_{12}} = \frac{dL}{dh_{21}} \frac{\partial h_{21}}{\partial a_{12}} + \frac{\partial L}{\partial h_{22}} \frac{\partial h_{22}}{\partial a_{12}} = (\frac{dL}{dh_{21}} + \frac{\partial L}{\partial h_{22}})\, w_4$
$a_{12} = \sigma(h_2)$
w_5
$h_{21} = b_{h21} + w_3 a_{11} + w_4 a_{12}$
$\frac{dL}{dh_{21}} = \frac{\partial L}{\partial a_{21}} \frac{da_{21}}{dh_{21}} = \frac{\partial L}{\partial a_{21}} (\sigma(h_{21})(1 - \sigma(h_{21}))$
$\frac{\partial L}{\partial a_{21}} = \frac{\partial L}{\partial z} \frac{\partial z}{\partial a_{21}} = \frac{\partial L}{\partial z} w_5$
$a_{21} = \sigma(h_{21})$
w_6
$h_{22} = b_{h22} + w_3 a_{11} + w_4 a_{12}$
$\frac{\partial L}{\partial h_{22}} = \frac{\partial L}{\partial a_{22}} \frac{da_{22}}{dh_{22}} = \frac{\partial L}{\partial a_{22}} (\sigma(h_{22})(1 - \sigma(h_{22}))$
$\frac{\partial L}{\partial a_{22}} = \frac{dL}{dz} \frac{\partial z}{\partial a_{22}} = \frac{dL}{dz} w_6$
$a_{22} = \sigma(h_{22})$
$z = b_z + w_5 y_3 + w_6 y_4$
$\frac{dL}{dz} = \frac{dL}{dy_{pred}} (1 - \sigma(z))(\sigma(z))$
$\frac{dL}{dy_{pred}} = \frac{2}{2}(y - y_{pred}) = (y - y_{pred})$
$y_{pred} = \sigma(z)$
MSE Loss
$L(w) = \frac{1}{2}(y - y_{pred})^2$
y

Backward Pass (bp)

x_1 — w_1

$$\frac{\partial L}{\partial x_1} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial x_1} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial x_1} = \left(\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}}\right) w_1$$

$$\frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial w_1} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial w_1} = \left(\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}}\right) x_1$$

x_2 — w_2

$$\frac{\partial L}{\partial x_2} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial x_2} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial x_2} = \left(\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}}\right) w_2$$

$$\frac{\partial L}{\partial w_2} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial w_2} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial w_2} = \left(\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}}\right) x_2$$

w_3

$$h_{11} = b_{h11} + w_1x_1 + w_2x_2$$

$$\frac{\partial L}{\partial h_{11}} = \frac{\partial L}{\partial a_{11}}\frac{\partial a_{11}}{\partial h_{11}} = \frac{\partial L}{\partial a_{11}}\sigma(h_{11})(1-\sigma(h_{11}))$$

$$\frac{\partial L}{\partial a_{11}} = \frac{\partial L}{\partial h_{21}}\frac{\partial h_{21}}{\partial a_{11}} + \frac{\partial L}{\partial h_{22}}\frac{\partial h_{22}}{\partial a_{11}} = \left(\frac{\partial L}{\partial h_{21}} + \frac{\partial L}{\partial h_{22}}\right) w_3$$

$$a_{11} = \sigma(h_1)$$

w_4

$$h_{12} = b_{h12} + w_1x_1 + w_2x_2$$

$$\frac{\partial L}{\partial h_{12}} = \frac{\partial L}{\partial a_{12}}\frac{\partial a_{12}}{\partial h_{12}} = \frac{\partial L}{\partial a_{12}}\sigma(h_{12})(1-\sigma(h_{12}))$$

$$\frac{\partial L}{\partial a_{12}} = \frac{dL}{dh_{21}}\frac{\partial h_{21}}{\partial a_{12}} + \frac{\partial L}{\partial h_{22}}\frac{\partial h_{22}}{\partial a_{12}} = \left(\frac{dL}{dh_{21}} + \frac{\partial L}{\partial h_{22}}\right) w_4$$

$$a_{12} = \sigma(h_2)$$

w_5

$$h_{21} = b_{h21} + w_3a_{11} + w_4a_{12}$$

$$\frac{dL}{dh_{21}} = \frac{\partial L}{\partial a_{21}}\frac{da_{21}}{dh_{21}} = \frac{\partial L}{\partial a_{21}}(\sigma(h_{21})(1-\sigma(h_{21})))$$

$$\frac{\partial L}{\partial a_{21}} = \frac{\partial L}{\partial z}\frac{\partial z}{\partial a_{21}} = \frac{\partial L}{\partial z} w_5$$

$$a_{21} = \sigma(h_{21})$$

w_6

$$h_{22} = b_{h22} + w_3a_{11} + w_4a_{12}$$

$$\frac{\partial L}{\partial h_{22}} = \frac{\partial L}{\partial a_{22}}\frac{da_{22}}{dh_{22}} = \frac{\partial L}{\partial a_{22}}(\sigma(h_{22})(1-\sigma(h_{22})))$$

$$\frac{\partial L}{\partial a_{22}} = \frac{dL}{dz}\frac{\partial z}{\partial a_{22}} = \frac{dL}{dz} w_6$$

$$a_{22} = \sigma(h_{22})$$

$$z = b_z + w_5y_3 + w_6y_4$$

$$\frac{dL}{dz} = \frac{dL}{dy_{pred}}(1-\sigma(z))(\sigma(z))$$

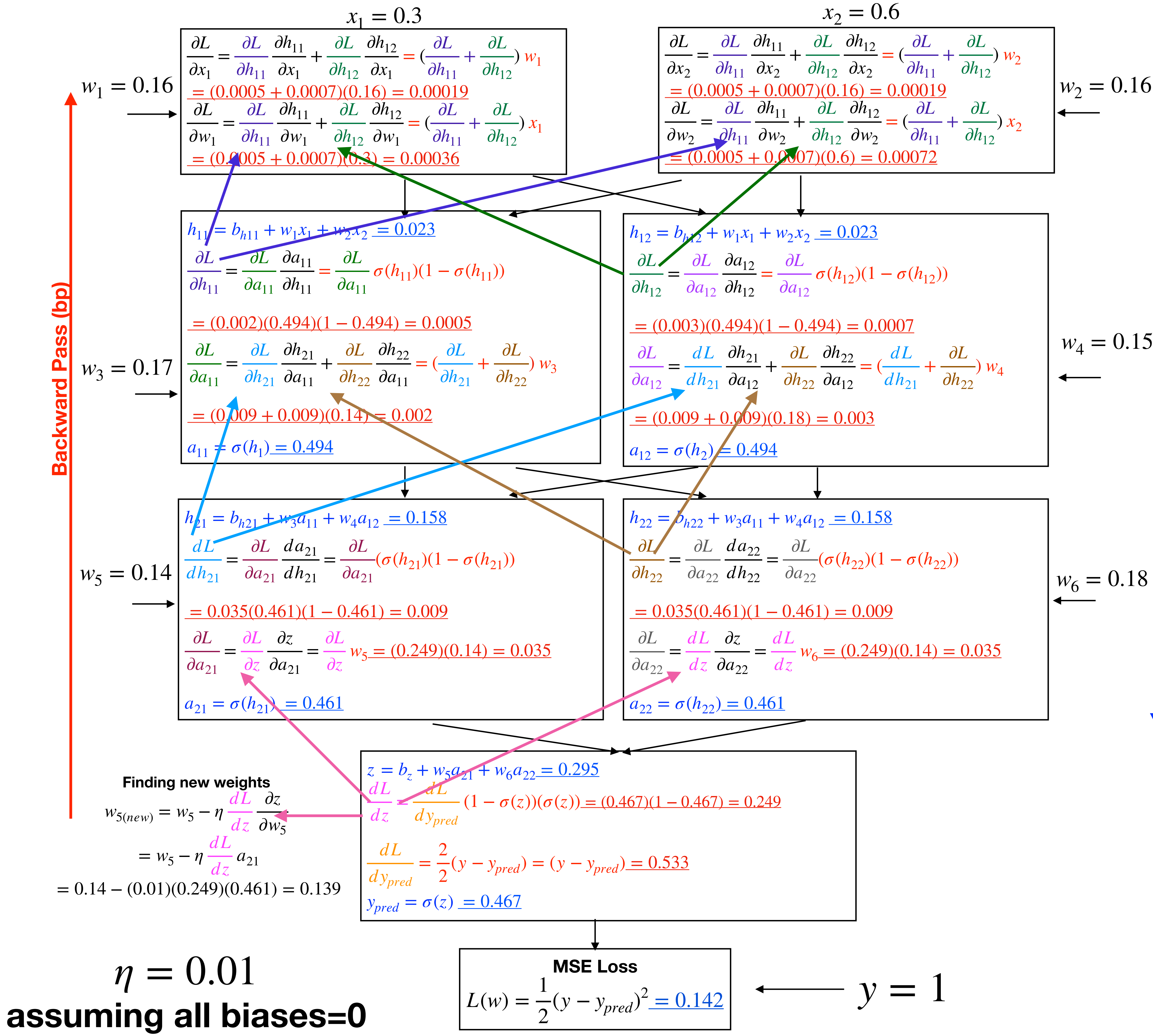
$$\frac{dL}{dy_{pred}} = \frac{2}{2}(y-y_{pred}) = (y-y_{pred})$$

$$y_{pred} = \sigma(z)$$

MSE Loss

$$L(w) = \frac{1}{2}(y-y_{pred})^2$$

y



$x_1 = 0.3$
$\frac{\partial L}{\partial x_1} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial x_1} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial x_1} = (\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}})\, w_1$
$= (0.0005 + 0.0007)(0.16) = 0.00019$
$\frac{\partial L}{\partial w_1} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial w_1} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial w_1} = (\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}})\, x_1$
$= (0.0005 + 0.0007)(0.3) = 0.00036$
$x_2 = 0.6$
$\frac{\partial L}{\partial x_2} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial x_2} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial x_2} = (\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}})\, w_2$
$= (0.0005 + 0.0007)(0.16) = 0.00019$
$\frac{\partial L}{\partial w_2} = \frac{\partial L}{\partial h_{11}}\frac{\partial h_{11}}{\partial w_2} + \frac{\partial L}{\partial h_{12}}\frac{\partial h_{12}}{\partial w_2} = (\frac{\partial L}{\partial h_{11}} + \frac{\partial L}{\partial h_{12}})\, x_2$
$= (0.0005 + 0.0007)(0.6) = 0.00072$
$w_1 = 0.16$
$w_2 = 0.16$
$h_{11} = b_{h11} + w_1x_1 + w_2x_2 = 0.023$
$\frac{\partial L}{\partial h_{11}} = \frac{\partial L}{\partial a_{11}}\frac{\partial a_{11}}{\partial h_{11}} = \frac{\partial L}{\partial a_{11}}\sigma(h_{11})(1-\sigma(h_{11}))$
$= (0.002)(0.494)(1-0.494) = 0.0005$
$\frac{\partial L}{\partial a_{11}} = \frac{\partial L}{\partial h_{21}}\frac{\partial h_{21}}{\partial a_{11}} + \frac{\partial L}{\partial h_{22}}\frac{\partial h_{22}}{\partial a_{11}} = (\frac{\partial L}{\partial h_{21}} + \frac{\partial L}{\partial h_{22}})\, w_3$
$= (0.009 + 0.009)(0.14) = 0.002$
$a_{11} = \sigma(h_1) = 0.494$
$h_{12} = b_{h12} + w_1x_1 + w_2x_2 = 0.023$
$\frac{\partial L}{\partial h_{12}} = \frac{\partial L}{\partial a_{12}}\frac{\partial a_{12}}{\partial h_{12}} = \frac{\partial L}{\partial a_{12}}\sigma(h_{12})(1-\sigma(h_{12}))$
$= (0.003)(0.494)(1-0.494) = 0.0007$
$\frac{\partial L}{\partial a_{12}} = \frac{dL}{dh_{21}}\frac{\partial h_{21}}{\partial a_{12}} + \frac{\partial L}{\partial h_{22}}\frac{\partial h_{22}}{\partial a_{12}} = (\frac{dL}{dh_{21}} + \frac{\partial L}{\partial h_{22}})\, w_4$
$= (0.009 + 0.009)(0.18) = 0.003$
$a_{12} = \sigma(h_2) = 0.494$
$w_3 = 0.17$
$w_4 = 0.15$
$h_{21} = b_{h21} + w_3a_{11} + w_4a_{12} = 0.158$
$\frac{dL}{dh_{21}} = \frac{\partial L}{\partial a_{21}}\frac{da_{21}}{dh_{21}} = \frac{\partial L}{\partial a_{21}}(\sigma(h_{21})(1-\sigma(h_{21}))$
$= 0.035(0.461)(1-0.461) = 0.009$
$\frac{\partial L}{\partial a_{21}} = \frac{\partial L}{\partial z}\frac{\partial z}{\partial a_{21}} = \frac{\partial L}{\partial z} w_5 = (0.249)(0.14) = 0.035$
$a_{21} = \sigma(h_{21}) = 0.461$
$h_{22} = b_{h22} + w_3a_{11} + w_4a_{12} = 0.158$
$\frac{\partial L}{\partial h_{22}} = \frac{\partial L}{\partial a_{22}}\frac{da_{22}}{dh_{22}} = \frac{\partial L}{\partial a_{22}}(\sigma(h_{22})(1-\sigma(h_{22}))$
$= 0.035(0.461)(1-0.461) = 0.009$
$\frac{\partial L}{\partial a_{22}} = \frac{dL}{dz}\frac{\partial z}{\partial a_{22}} = \frac{dL}{dz} w_6 = (0.249)(0.14) = 0.035$
$a_{22} = \sigma(h_{22}) = 0.461$
$w_5 = 0.14$
$w_6 = 0.18$
Backward Pass (bp)
Forward Pass (fp)
$z = b_z + w_5a_{21} + w_6a_{22} = 0.295$
$\frac{dL}{dz} = \frac{dL}{dy_{pred}}(1-\sigma(z))(\sigma(z)) = (0.467)(1-0.467) = 0.249$
$\frac{dL}{dy_{pred}} = \frac{2}{2}(y - y_{pred}) = (y - y_{pred}) = 0.533$
$y_{pred} = \sigma(z) = 0.467$
Finding new weights
$w_{5(new)} = w_5 - \eta \frac{dL}{dz}\frac{\partial z}{\partial w_5}$
$= w_5 - \eta \frac{dL}{dz} a_{21}$
$= 0.14 - (0.01)(0.249)(0.461) = 0.139$
MSE Loss
$L(w) = \frac{1}{2}(y - y_{pred})^2 = 0.142$
$y = 1$
$\eta = 0.01$
assuming all biases=0

Backpropagation- forward pass and Gradient calculations

- As seen in the previous slide we perform the forward pass to calculate
    - linear combination(or a function) of inputs
    - sigmoid (activation function) of the above function
- We use the value from the output layer to predict the value of y
- we calculate loss function Using MSE or Cross entropy
- to update weights$w_t = w_{t-1} + \nabla L$, we need to find gradient of L w.r.t all weights

Backpropagation-backward pass

- during backward pass we propagate the gradient through all nodes
  - first, we take a sum of products of all incoming gradient from the next nodes and weights of current node
    - $\sum_{i=1}^{NodesInNextLayer} \frac{\partial L}{\partial h_{layer,i}} w_{layer})$
    - e.g. $(\frac{\partial L}{\partial h_{21}} + \frac{\partial L}{\partial h_{22}})\ w_3$
      - where h_{21}, h_{22} are nodes in the next layer in MLP connect to current node h_{11}
      - w_3 is the weight of the current layer h_{11}
  - multiply this sum with the derivative of the sigmoid function
    - $[\ \ (\frac{\partial L}{\partial h_{21}} + \frac{\partial L}{\partial h_{22}})\ w_3\ ]\ \ \ [\ \sigma(h_{11})(1 - \sigma(h_{11}))\ \ ]$
  - pass this value to previous node as gradient

Backpropagation - weight calculations

- using the new gradient we find the new weights as
  $$w_{new} = w_{old} - \eta(\frac{dL}{dNode}\sigma(Node))$$
- $\frac{dL}{dNode}$ the node gets from the previous node during back propogation
- $\sigma(Node)$ is its own output
- w_{old} is the node's current weight
- η is the learning rate