Lab: Logistic Regression for Gene Expression Data

In this lab, we use logistic regression to predict biological characteristics ("phenotypes") from gene expression data. In addition to the concepts in <u>breast cancer demo (./breast_cancer.ipynb)</u>, you will learn to:

- Handle missing data
- · Perform multi-class logistic classification
- · Create a confusion matrix
- Use L1-regularization for improved estimation in the case of sparse weights (Grad students only)

Background

Genes are the basic unit in the DNA and encode blueprints for proteins. When proteins are synthesized from a gene, the gene is said to "express". Micro-arrays are devices that measure the expression levels of large numbers of genes in parallel. By finding correlations between expression levels and phenotypes, scientists can identify possible genetic markers for biological characteristics.

The data in this lab comes from:

https://archive.ics.uci.edu/ml/datasets/Mice+Protein+Expression (https://archive.ics.uci.edu/ml/datasets/Mice+Protein+Expression)

In this data, mice were characterized by three properties:

- Whether they had down's syndrome (trisomy) or not
- · Whether they were stimulated to learn or not
- Whether they had a drug memantine or a saline control solution.

With these three choices, there are 8 possible classes for each mouse. For each mouse, the expression levels were measured across 77 genes. We will see if the characteristics can be predicted from the gene expression levels. This classification could reveal which genes are potentially involved in Down's syndrome and if drugs and learning have any noticeable effects.

Load the Data

We begin by loading the standard modules.

```
In [1]: import pandas as pd
   import numpy as np
   import matplotlib
   import matplotlib.pyplot as plt
   %matplotlib inline
   from sklearn import linear_model, preprocessing
```

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Use the pd.read excel command to read the data from

https://archive.ics.uci.edu/ml/machine-learning-databases/00342/Data_Cortex_Nuclear.xls (https://archive.ics.uci.edu/ml/machine-learning-databases/00342/Data_Cortex_Nuclear.xls)

into a dataframe df. Use the index_col option to specify that column 0 is the index. Use the df.head() to print the first few rows.

```
In [2]: # TODO
# df = ...
df = pd.read_excel('https://archive.ics.uci.edu/ml/machine-learning-databases/
00342/Data_Cortex_Nuclear.xls',index_col=0)
df.head()
```

Out[2]:

	DYRK1A_N	ITSN1_N	BDNF_N	NR1_N	NR2A_N	pAKT_N	pBRAF_N	pCAI
MouseID								
309_1	0.503644	0.747193	0.430175	2.816329	5.990152	0.218830	0.177565	2.373
309_2	0.514617	0.689064	0.411770	2.789514	5.685038	0.211636	0.172817	2.292
309_3	0.509183	0.730247	0.418309	2.687201	5.622059	0.209011	0.175722	2.283
309_4	0.442107	0.617076	0.358626	2.466947	4.979503	0.222886	0.176463	2.152
309_5	0.434940	0.617430	0.358802	2.365785	4.718679	0.213106	0.173627	2.134

5 rows × 81 columns

This data has missing values. The site:

http://pandas.pydata.org/pandas-docs/stable/missing_data.html (http://pandas.pydata.org/pandas-docs/stable/missing_data.html)

has an excellent summary of methods to deal with missing values. Following the techniques there, create a new data frame df1 where the missing values in each column are filled with the mean values from the non-missing values.

```
In [3]: # TODO
    # df1 = ...
    df1=df.fillna(df.mean())
    df.isnull().values.any()
    df1.isnull().values.any()
Out[3]: False
```

Binary Classification for Down's Syndrome

We will first predict the binary class label in df1['Genotype'] which indicates if the mouse has Down's syndrome or not. Get the string values in df1['Genotype'].values and convert this to a numeric vector y with 0 or 1. You may wish to use the np.unique command with the return inverse=True option.

```
In [4]: # TODO
# y = ...
u,y=np.unique(df1['Genotype'].values,return_inverse=True)
print(y)

[0 0 0 ..., 1 1 1]
```

As predictors, get all but the last four columns of the dataframes. Standardize the data matrix and call the standardized matrix Xs. The predictors are the expression levels of the 77 genes.

```
In [5]: # TODO
        \# Xs = ...
        Xs = preprocessing.scale(df1.values[:,:-4])
        print(Xs.shape)
        print(df1.shape)
        print(Xs)
        (1080, 77)
        (1080, 81)
        [[ 0.31271112  0.5179336
                                   2.2536689 ..., -1.41662394 -1.60789061
           1.06590091]
         [ 0.35679793  0.28650133  1.8802795  ..., -1.32521803 -1.54684392
           1.28029118]
         [ 0.33496588  0.45046461  2.01292763  ..., -1.37325709  -1.62359464
           1.85703831]
         [-0.79192771 -0.88354273 -1.72382963 ..., 1.27078193 3.11724261
           0.29352469]
         [-0.82188815 -0.8130138 -1.52387571 ..., 1.88117889 3.32828966
           0.2089962 ]
         [-0.49491588 -0.62125474 -1.26845332 ..., 1.92748438 3.32672533
           0.10478825]]
        /home/ky935/anaconda3/lib/python3.6/site-packages/sklearn/utils/validation.p
        y:429: DataConversionWarning: Data with input dtype object was converted to f
        loat64 by the scale function.
          warnings.warn(msg, _DataConversionWarning)
```

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Create a LogisticRegression object logreg and fit the training data.

```
In [6]: # TODO
    logreg = linear_model.LogisticRegression(C=1e5)
    logreg.fit(Xs, y)
```

Measure the accuracy of the classifer. That is, use the logreg.predict function to predict labels yhat and measure the fraction of time that the predictions match the true labels. Below, we will properly measure the accuracy on cross-validation data.

```
In [7]: # TODO
  yhat = logreg.predict(Xs)
  acc = np.mean(yhat == y)
  print("Accuracy on training data = %f" % acc)
```

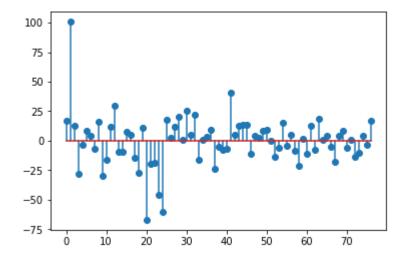
Accuracy on training data = 1.000000

Interpreting the weight vector

Create a stem plot of the coefficients, W in the logistic regression model. You can get the coefficients from logreg.coef_, but you will need to reshape this to a 1D array.

```
In [8]: # TODO
    logreg_coef=logreg.coef_.reshape(77)
    plt.stem(logreg_coef)
```

Out[8]: <Container object of 3 artists>



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You should see that W[i] is very large for a few components i. These are the genes that are likely to be most involved in Down's Syndrome. Although, we do not discuss it in this class, there are ways to force the logistic regression to return a sparse vector W.

Find the names of the genes for two components i where the magnitude of W[i] is largest.

```
In [9]:
        # TODO
         W = np.zeros(77)
         W=np.argsort(abs(logreg coef))[::-1]
         print(W[:2])
         colname = df.columns[W[:2]]
         print(colname)
         data = {'feature': colname, 'slope': logreg_coef[W[:2]]}
         dfslope = pd.DataFrame(data=data)
         dfslope
         [ 1 20]
        Index(['ITSN1_N', 'BRAF_N'], dtype='object')
Out[9]:
             feature
                          slope
           ITSN1_N | 100.753125
           BRAF N
                     -67.053533
```

Cross Validation

The above measured the accuracy on the training data. It is more accurate to measure the accuracy on the test data. Perform 10-fold cross validation and measure the average precision, recall and f1-score. Note, that in performing the cross-validation, you will want to randomly permute the test and training sets using the shuffle option. In this data set, all the samples from each class are bunched together, so shuffling is essential. Print the mean precision, recall and f1-score and error rate across all the folds.

```
In [10]: # TODO
         from sklearn.model selection import KFold
         from sklearn.metrics import precision recall fscore support
         nfold = 10
         kf = KFold(n splits=nfold, shuffle=True)
         prec = []
         rec = []
         f1 = []
         acc = []
         for train, test in kf.split(Xs):
             # Get training and test data
             Xtr = Xs[train,:]
             ytr = y[train]
             Xts = Xs[test,:]
             yts = y[test]
             # Fit a model
             logreg.fit(Xtr, ytr)
             yhat = logreg.predict(Xts)
             # Measure performance
             preci, reci, f1i, _= precision_recall_fscore_support(yts, yhat, average='binar
         y')
             prec.append(preci)
             rec.append(reci)
             f1.append(f1i)
             acci = np.mean(yhat == yts)
             acc.append(acci)
         # Take average values of the metrics
         precm = np.mean(prec)
         recm = np.mean(rec)
         f1m = np.mean(f1)
         accm= np.mean(acc)
         # Compute the standard errors
         prec se = np.std(prec)/np.sqrt(nfold-1)
         rec se = np.std(rec)/np.sqrt(nfold-1)
         f1 se = np.std(f1)/np.sqrt(nfold-1)
         acc_se = np.std(acc)/np.sqrt(nfold-1)
         print('Precision = {0:.4f}, SE={1:.4f}'.format(precm,prec_se))
                             {0:.4f}, SE={1:.4f}'.format(recm, rec se))
         print('Recall =
         print('f1 =
                             {0:.4f}, SE={1:.4f}'.format(f1m, f1 se))
         print('Accuracy = {0:.4f}, SE={1:.4f}'.format(accm, acc se))
         Precision = 0.9405, SE=0.0154
         Recall =
                     0.9635, SE=0.0055
                     0.9510, SE=0.0072
```

Accuracy = 0.9537, SE=0.0063

Multi-Class Classification

Now use the response variable in df1['class']. This has 8 possible classes. Use the np.unique funtion as before to convert this to a vector y with values 0 to 7.

```
In [11]: # TODO
# y = ...
u,y=np.unique(df1['class'].values,return_inverse=True)
print(y)
[0 0 0 ..., 7 7 7]
```

Fit a multi-class logistic model by creating a LogisticRegression object, logreg and then calling the logreg.fit method.

Measure the accuracy on the training data.

command

```
In [13]: # TODO
   yhat = logreg.predict(Xs)
   acc = np.mean(yhat == y)
   print("Accuracy on training data = %f" % acc)

Accuracy on training data = 1.000000
```

Now perform 10-fold cross validation, and measure the confusion matrix C on the test data in each fold. You can use the confustion_matrix method in the sklearn package. Add the confusion matrix counts across all folds and then normalize the rows of the confusion matrix so that they sum to one. Thus, each element C[i,j] will represent the fraction of samples where yhat==j given ytrue==i. Print the confusion matrix. You can use the

```
print(np.array_str(C, precision=4, suppress_small=True))
```

to create a nicely formatted print. Also print the overall mean and SE of the test error rate across the folds.

```
In [14]: from sklearn.metrics import confusion_matrix
from sklearn.model_selection import KFold
# TODO
```

```
from sklearn.metrics import precision_recall_fscore_support
C = np.zeros((8,8))
nfold = 10
kf = KFold(n splits=nfold, shuffle=True)
prec = []
rec = []
f1 = []
acc = []
mse = []
for train, test in kf.split(Xs):
    # Get training and test data
   Xtr = Xs[train,:]
   ytr = y[train]
   Xts = Xs[test,:]
   yts = y[test]
   # Fit a model
    logreg.fit(Xtr, ytr)
   yhat = logreg.predict(Xts)
   C=C+confusion_matrix(yts, yhat)
     print(np.array_str(C, precision=4, suppress_small=True))
#
    print(C.shape)
    # Measure performance
    preci,reci,f1i,_= precision_recall_fscore_support(yts,yhat,average='weight
ed')
   prec.append(preci)
    rec.append(reci)
    f1.append(f1i)
    acci = np.mean(yhat == yts)
   acc.append(acci)
#
  msei = np.mean((yts-yhat)**2)
    mse.append(msei)
    print(mse)
    print(np.mean((yts-yhat)**2))
# Take average values of the metrics
precm = np.mean(prec)
recm = np.mean(rec)
f1m = np.mean(f1)
accm= np.mean(acc)
# Compute the standard errors
prec se = np.std(prec)/np.sqrt(nfold-1)
rec_se = np.std(rec)/np.sqrt(nfold-1)
f1_se = np.std(f1)/np.sqrt(nfold-1)
acc_se = np.std(acc)/np.sqrt(nfold-1)
print('Precision = {0:.4f}, SE={1:.4f}'.format(precm,prec_se))
print('Recall =
                  {0:.4f}, SE={1:.4f}'.format(recm, rec se))
                   {0:.4f}, SE={1:.4f}'.format(f1m, f1_se))
print('f1 =
print('Accuracy(Overall mean) = {0:.4f}, SE={1:.4f}'.format(accm, acc_se))
print(np.array_str(C, precision=4, suppress_small=True))
```

acc_se_12=acc_se

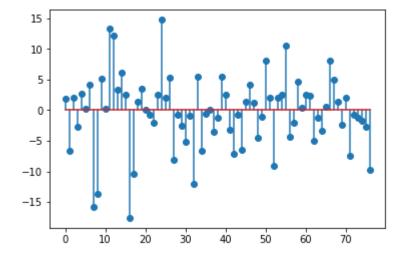
```
C_Normalized = C.astype('float') / C.sum(axis=1)[:, np.newaxis]
           print(np.array_str(C_Normalized, precision=4, suppress_small=True))
Precision = 0.9898, SE=0.0024
           Recall =
                          0.9889, SE=0.0027
                          0.9890, SE=0.0026
           Accuracy(Overall mean) = 0.9889, SE=0.0027
           [[ 147.
                         2.
                                1.
                                       0.
                                               0.
                                                      0.
                                                                     0.]
                 3.
                      131.
                                0.
                                       0.
                                               1.
                                                      0.
                                                              0.
                                                                     0.1
                 0.
                         1.
                              148.
                                       0.
                                               1.
                                                      0.
                                                              0.
                                                                     0.1
                 1.
                         0.
                                0.
                                     134.
                                               0.
                                                      0.
                                                              0.
                                                                     0.]
                                0.
                                       0.
                                            134.
                                                      0.
                                                              0.
                                                                     0.]
                 0.
                         1.
                 0.
                         0.
                                0.
                                       0.
                                               0.
                                                    105.
                                                              0.
                                                                     0.1
                                               0.
                         0.
                                        1.
                                                      0.
                                                           134.
                 0.
                                0.
                                                                     0.1
                 0.
                         0.
                                0.
                                       0.
                                               0.
                                                      0.
                                                                  135.]]
           [[ 0.98
                         0.0133
                                                                0.
                                                                                    0.
                                  0.0067
                                            0.
                                                      0.
                        0.9704
               0.0222
                                                      0.0074
                                  0.
                                            0.
                                                                0.
                                                                          0.
                                                                                    0.
               0.
                         0.0067
                                  0.9867
                                            0.
                                                      0.0067
                                                                0.
                                                                          0.
                                                                                    0.
                                            0.9926
               0.0074
                        0.
                                  0.
                                                      0.
                                                                0.
                                                                          0.
                                                                                    0.
               0.
                        0.0074
                                  0.
                                            0.
                                                      0.9926
                                                                0.
                                                                          0.
                                                                                    0.
               0.
                         0.
                                  0.
                                            0.
                                                      0.
                                                                1.
                                                                          0.
                                                                                    0.
                                                                          0.9926
               0.
                                  0.
                                            0.0074
                                                                0.
                                                                                    0.
                         0.
                                                      0.
                                                                                           1
                         0.
                                  0.
                                            0.
                                                      0.
                                                                0.
                                                                          0.
                                                                                    1.
                                                                                           ]]
               0.
           accm 12=accm
In [15]:
```

Re-run the logistic regression on the entire training data and get the weight coefficients. This should be a 8 x 77 matrix. Create a stem plot of the first row of this matrix to see the coefficients on each of the genes.

```
In [16]: # TODO
    logreg.fit(Xs, y)
    yhat = logreg.predict(Xs)
    logreg_coef=logreg.coef_
    print(logreg_coef.shape)
    print(np.squeeze(logreg_coef[:1,:]))
    plt.stem(np.squeeze(logreg_coef[:1,:]))
(8, 77)
```

```
1.93411546
             -6.69333707
                            2.02773919
                                         -2.73093125
                                                       2,72967662
 0.19812115
              4.25653068 -15.88271771 -13.628345
                                                       5.12012653
 0.19704198
             13.34139923
                           12.25845629
                                          3.39361786
                                                       6.21072996
 2.5490988
            -17.59319577 -10.41553735
                                          1.37597033
                                                       3.45368891
 0.11449641
             -0.71706134
                           -2.04410987
                                          2.5162673
                                                      14.78130419
 2.05861518
              5.38335755
                           -8.11319162
                                         -0.81440863
                                                      -2.56172783
-5.22834959
             -0.97982776 -12.02870904
                                          5.42675847
                                                      -6.66341825
-0.58915819
              0.12324367
                           -3.60076254
                                         -1.25289946
                                                       5.55724645
 2.55750522
             -3.22542083
                           -7.17376484
                                         -0.65956484
                                                      -6.42091461
 1.42622082
              4.11355009
                            1.28925078
                                         -4.58497929
                                                      -1.08660756
 8.11370387
              2.09724106
                           -9.05510725
                                          2.03550112
                                                       2.57987223
10.61037076
             -4.30479664
                           -2.09949263
                                         4.71012373
                                                       0.40773661
 2.6169485
              2.39580391
                           -5.07010688
                                         -1.17309264
                                                      -3.33687232
 0.64811757
              8.07997694
                            4.96647674
                                          1.44871333
                                                      -2.30383111
 2.03550112
             -7.43982129
                           -0.69749528
                                         -1.18171322
                                                      -1.74338271
-2.62507383
             -9.72176294]
```

Out[16]: <Container object of 3 artists>



L1-Regularization

Graduate students only complete this section.

In most genetic problems, only a limited number of the tested genes are likely influence any particular attribute. Hence, we would expect that the weight coefficients in the logistic regression model should be sparse. That is, they should be zero on any gene that plays no role in the particular attribute of interest. Genetic analysis commonly imposes sparsity by adding an I1-penalty term. Read the sklearn documentation (http://scikit-learn.org/stable/modules/generated/sklearn.linear_model.LogisticRegression.html) on the LogisticRegression class to see how to set the I1-penalty and the inverse regularization strength, C.

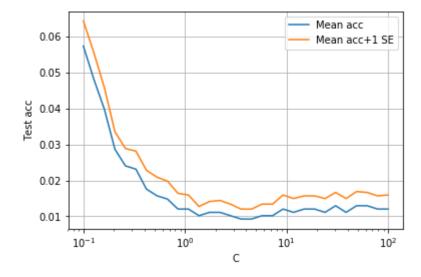
Using the model selection strategies from the <u>prostate cancer analysis demo (../model_sel/prostate.ipynb)</u>, use K-fold cross validation to select an appropriate inverse regularization strength.

- · Use 10-fold cross validation
- You should select around 20 values of C. It is up to you find a good range.
- · Make appropriate plots and print out to display your results
- How does the accuracy compare to the accuracy achieved without regularization.

```
In [17]: # TODO
         import sklearn.model selection
         # Create a k-fold cross validation object
         nfold = 10
         kf = sklearn.model_selection.KFold(n_splits=nfold,shuffle=True)
         nC=30
         C = np.logspace(-1,2,nC)
         preci = np.zeros(nC)
         reci = np.zeros(nC)
         f1i = np.zeros(nC)
         acci = np.zeros(nC)
         prec = np.zeros((nC,nfold))
         rec = np.zeros((nC,nfold))
         f1 = np.zeros((nC,nfold))
         acc = np.zeros((nC,nfold))
             # Get the training data in the split
         for ifold, ind in enumerate(kf.split(Xs)):
             train, test=ind
             Xtr = Xs[train,:]
             ytr = y[train]
             Xts = Xs[test,:]
             yts = y[test]
             # Compute the lasso path for the split
             for ic, c in enumerate(C):
                 # Fit the model on the training data
                 clf_l1_LR = linear_model.LogisticRegression(C=c, penalty='l1', tol=0.0
         1)
```

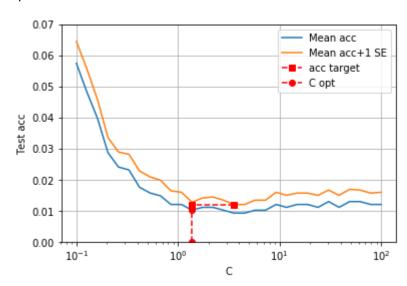
lab_gene_partial

```
clf_l1_LR.fit(Xtr, ytr)
        coef_l1_LR = clf_l1_LR.coef_.ravel()
        sparsity l1 LR = np.mean(coef l1 LR == 0) * 100
        print("C=%.2f" % c)
#
        print("Sparsity with L1 penalty: %.2f%%" % sparsity L1 LR)
#
        print("score with L1 penalty: %.4f" % clf_L1_LR.score(Xtr, ytr))
        # Compute the prediction error on the test data
        yhat = clf_l1_LR.predict(Xts)
        prec[ic,ifold],rec[ic,ifold],f1[ic,ifold],_= precision_recall_fscore_s
upport(yts,yhat,average='weighted')
        acc[ic,ifold] = np.mean(yhat == yts)
# Take average values of the metrics
precm = np.mean(prec,axis=1)
recm = np.mean(rec,axis=1)
f1m = np.mean(f1,axis=1)
accm= np.mean(acc,axis=1)
# Compute the standard errors
prec_se = np.std(prec,axis=1)/np.sqrt(nfold-1)
rec_se = np.std(rec,axis=1)/np.sqrt(nfold-1)
f1 se = np.std(f1,axis=1)/np.sqrt(nfold-1)
acc se = np.std(acc,axis=1)/np.sqrt(nfold-1)
```



```
# Find the minimum MSE and MSE target
In [19]:
         imin = np.argmax(accm)
         acc_tgt = 1-accm[imin] + acc_se[imin]
         C min = C[imin]
         # Find the least complex model with mse_mean < mse_tgt
         I = np.where(1-accm < acc tgt)[0]</pre>
         iopt = I[0]
         C opt = C[iopt]
         print("Optimal C = %f" % C_opt)
         # Plot the mean MSE and the mean MSE + 1 std dev
         plt.semilogx(C, 1-accm)
         plt.semilogx(C, 1-accm+acc_se)
         # Plot the MSE target
         plt.semilogx([C_min,C_opt], [acc_tgt,acc_tgt], 'rs--')
         # Plot the optimal alpha line
         plt.semilogx([C opt,C opt], [0.00,1-accm[iopt]], 'ro--')
         plt.legend(['Mean acc', 'Mean acc+1 SE', 'acc target','C opt'],loc='upper righ
         t')
         plt.xlabel('C')
         plt.ylabel('Test acc')
         plt.ylim([0,0.07])
         plt.grid()
         plt.show()
```

Optimal C = 1.373824



For the optimal C, fit the model on the entire training data with I1 regularization. Find the resulting weight matrix, W_11. Plot the first row of this weight matrix and compare it to the first row of the weight matrix without the regularization. You should see that, with I1-regularization, the weight matrix is much more sparse and hence the roles of particular genes are more clearly visible.