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# Linear Regression

— Price of Used Cars Prediction —

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# Introduction

Linear Regression Model

Prediction Price of Used Cars Listing

# Methodology: Data

MSRP

<https://www.cars.com/research/>

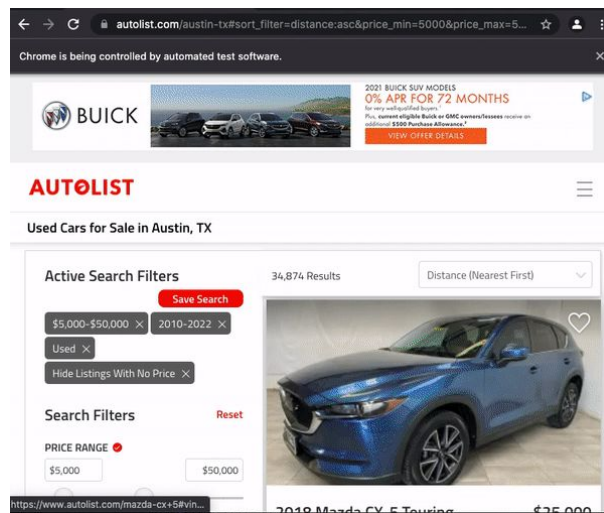
MSRP for latest model of 453 cars

Used Car Listings

<https://www.autolist.com/>

19 variables for 11809 used cars,  
including Price.

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 9129 entries, 0 to 9128
Data columns (total 11 columns):
#   Column          Non-Null Count  Dtype
---  -
0   Transmission    9128 non-null   object
1   Drivetrain      9129 non-null   object
2   Mileage         9129 non-null   float64
3   Body Style      9129 non-null   object
4   Price          9129 non-null   float64
5   Cylinders       9129 non-null   float64
6   Engine_Size     9129 non-null   float64
7   City_MPG       9129 non-null   float64
8   Hwy_MPG        9129 non-null   float64
9   Year           9129 non-null   float64
10  msrp           9129 non-null   float64
dtypes: float64(8), object(3)
memory usage: 784.6+ KB
```

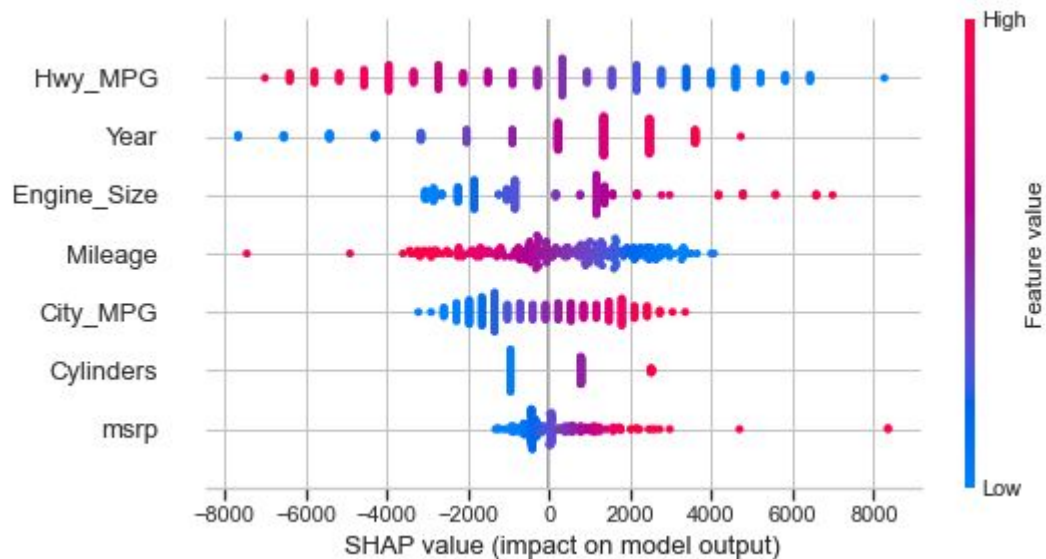


# Methodology: Libraries & Packages

- Selenium, requests & BeautifulSoup: Scrape and parse HTML
- sklearn.impute : Predictions to impute missing data
- Fuzzywuzzy - Search matches between different sources
- sklearn.linear\_model : Create regression models
- yellowbrick.regressor: Drop influential datapoints
- Shap: Visualization of influence of features in model.

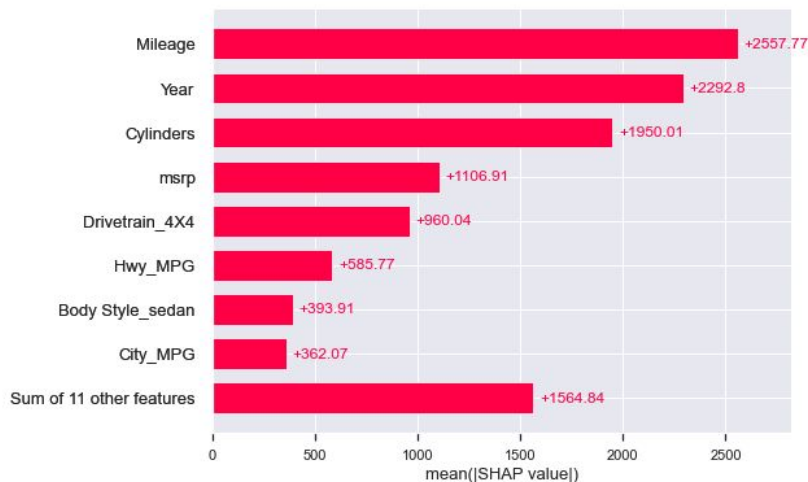
# Numerical Features

Numerical Features' SHAP Values

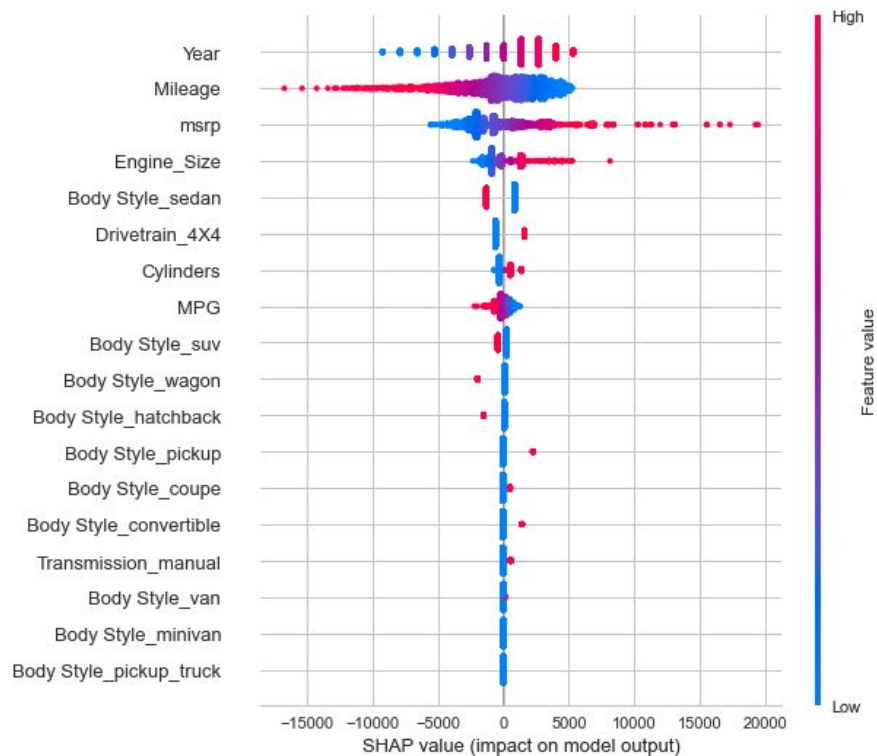


# All Features

Mean SHAP value of Features



SHAP Values of all Features



# Correlated Features & Regularization

Impute missing values

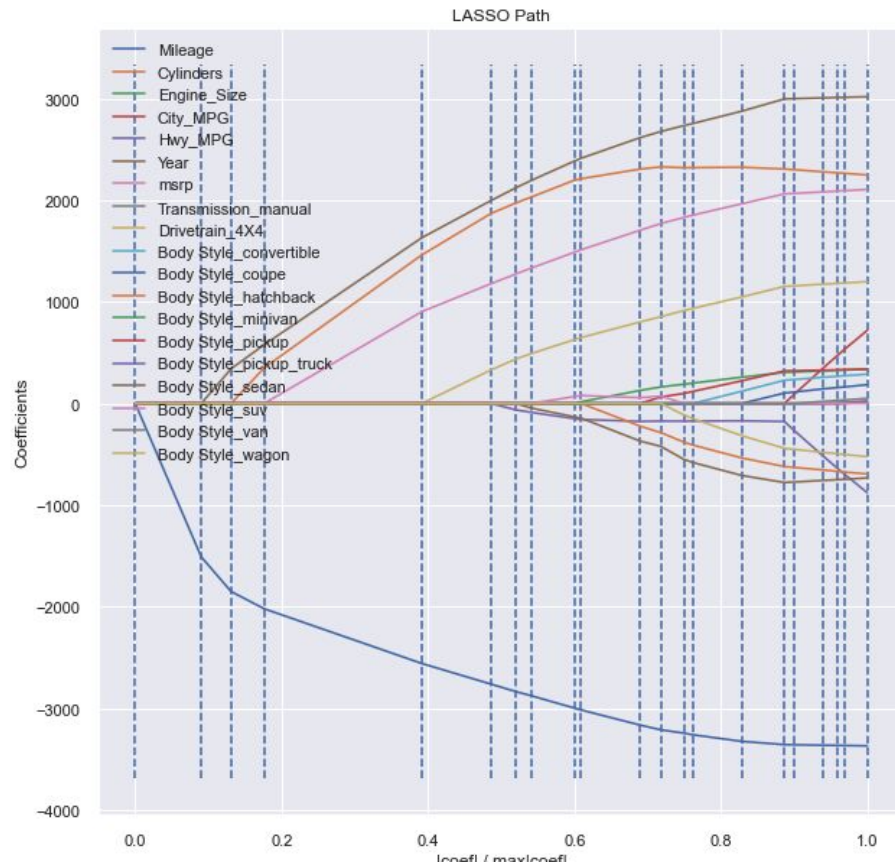
Imperfect Collinearity

Regularization

	variables	vif
0	Mileage	3.825799
1	Cylinders	40.772570
2	Engine_Size	7.444121
3	City_MPG	106.744936
4	Hwy_MPG	268.425848
5	Year	152.686841
6	msrp	6.901849

# Variables Dropped

- City MPG
- Manual Transmission
- Body Style - Minivan
- Body Style - Van
- Body Style - SUV
- Body Style - Pickup Truck
- Body Style Hatchback

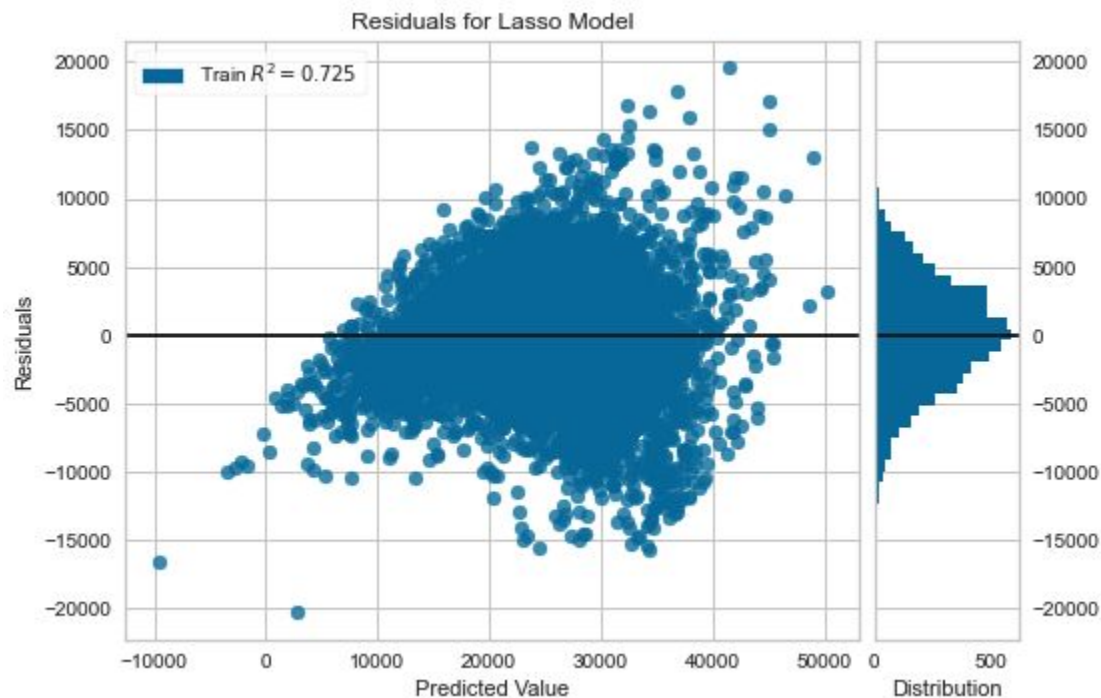




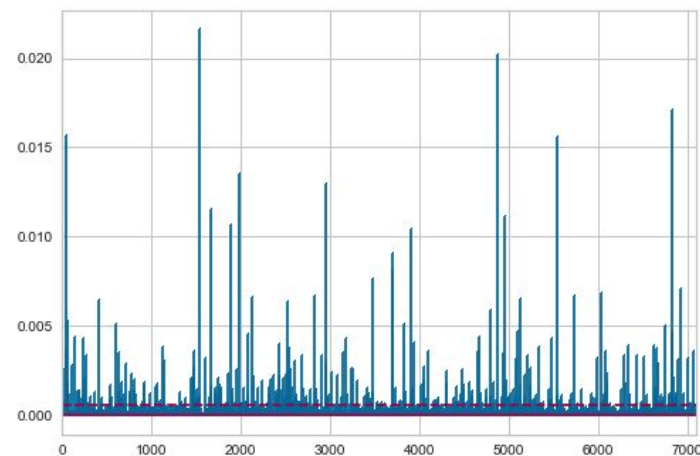
# Regularization Results

Model	Mean Squared Error	Mean Absolute Error	R^2 Score	Parameters
Ridge (L1)	1.837455e^07	3335.628	0.725271	Alpha: 12.9
Lasso (L2)	1.837435e^07	3335.626	0.725274	Alpha: 2.0
Elastic Net (L1 & L2)	1.83735e^07	3335.624	0.725274	Alpha:1.97 L1: 1

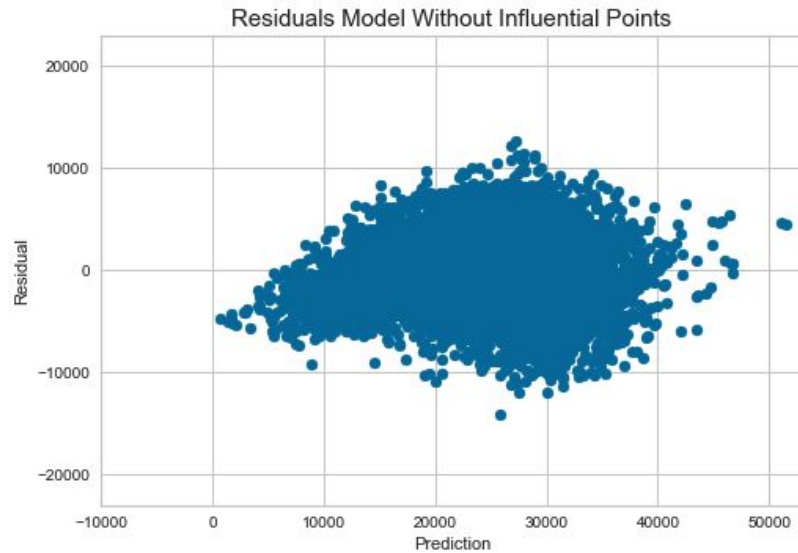
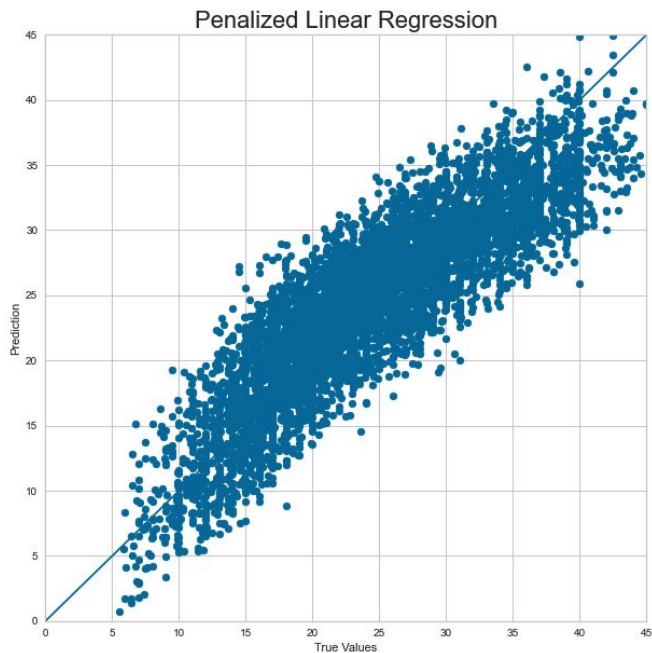
# Residual Analysis



399 Influential Points

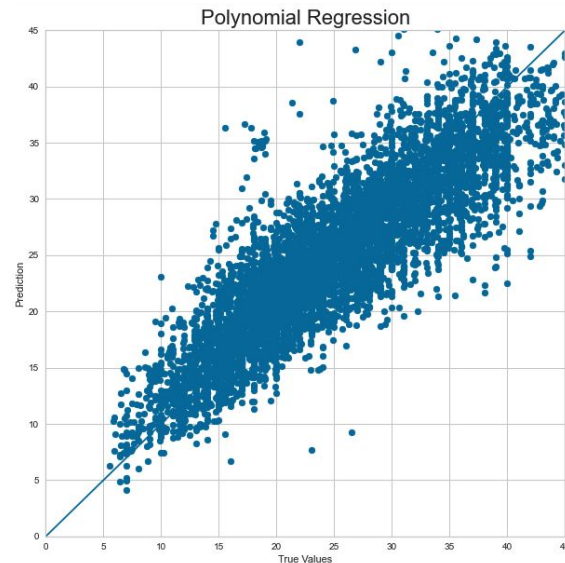
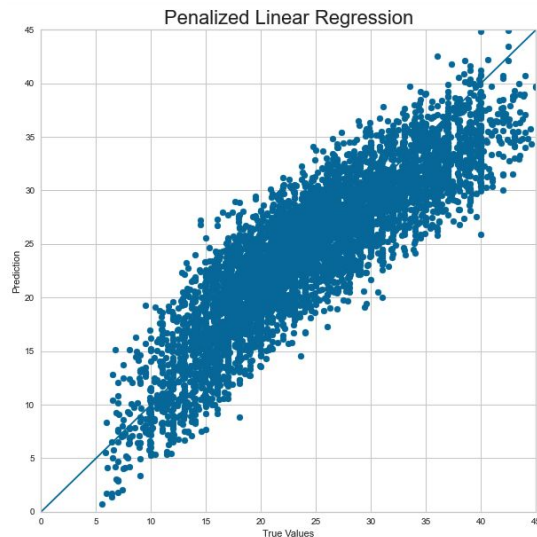


# Regression without Influential Points



Linear Model	Mean Absolute Error	Root Mean Squared Error	R^2 Score	Parameters
With Influential Points	1.837435e^07	3335.62	0.725	Alpha: 2.0 (L1)
Without Influential Points	1.357837e^07	2952.71	0.769	Alpha: 2.0 (L1)

# Polynomial Regression

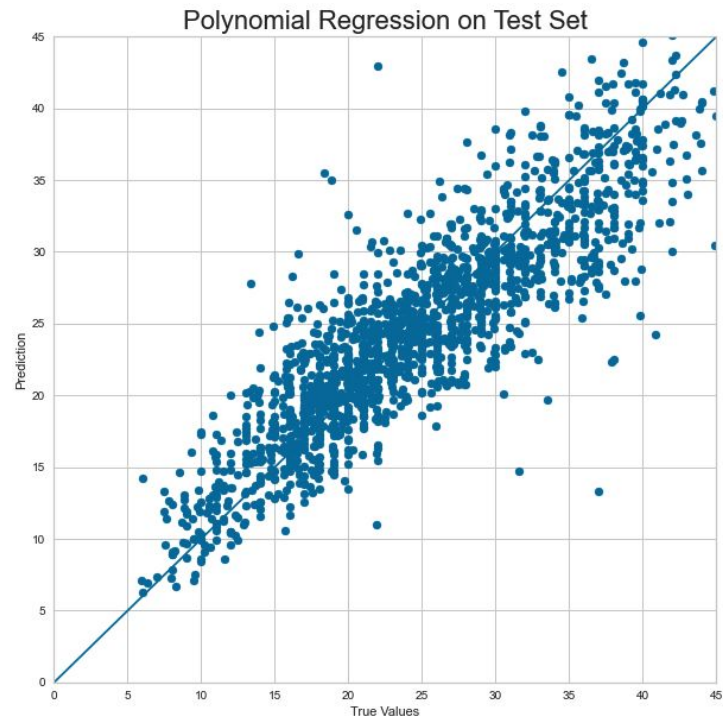
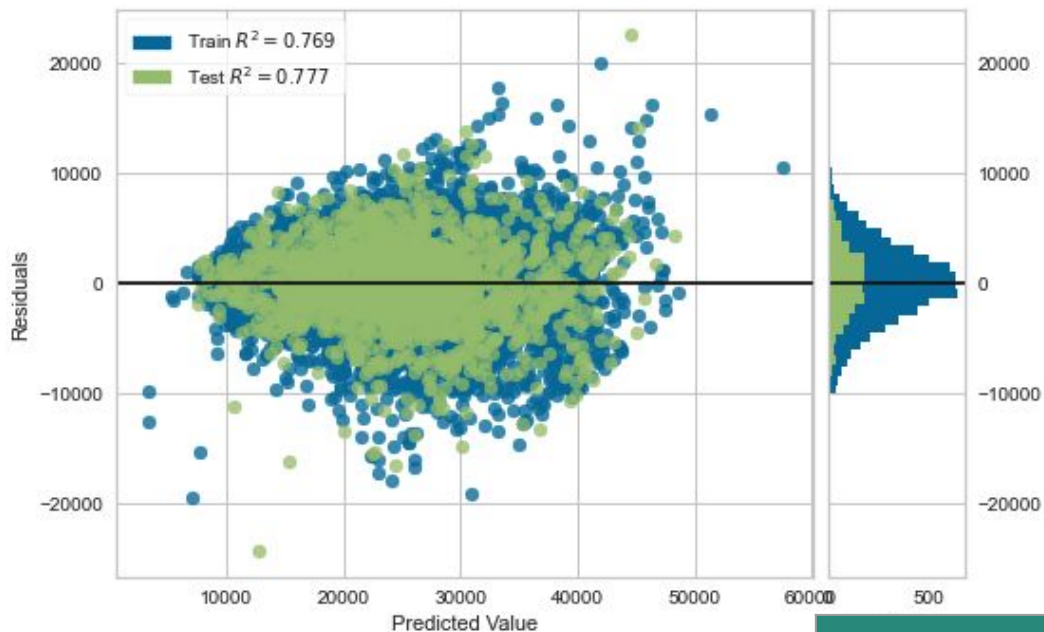


Linear Model	Mean Absolute Error	Root Mean Squared Error	R^2 Score	Parameters
Penalized Linear Model	1.357e^07	2953	0.769	Lambda 2.0 (L1)
Polynomial Model	1.201e^07	2714	0.796	

# Out of Sample Performance

Linear Model	Mean Squared Error	Root Mean Squared Error	R <sup>2</sup> Score
Polynomial Model	1.627e <sup>07</sup>	3016	0.770

# Results: Unseen Data



Linear Model	Mean Squared Error	Root Mean Squared Error	$R^2$ Score
Polynomial Model	$1.627e^07$	3016	0.770

# Conclusions

- Low Bias
- High Variance
- RMSE: ~\$3.000

# Future Work

Regularization in Polynomial Regression

Need features indicating level of car  
(basic/premium)

MSRP for individual car.

Remove influential datapoints from SHAP  
Summary Plot