

NOTE : ANSWER FOUR QUESTION

Time: 3 hours

Q1: A multiple-input neuron has a weight matrix  $= [1.2 \ -1.2 \ -1]$  and a bias  $b = [-0.1]$ , do the

following:

[15 marks]

- 1- Plot an abbreviated notation for neuron showing numeric values.
- 2- Calculate the net input net if input is  $p = [-1.0 \ -3.1 \ -0.1]$ .
- 3- For the result in (2), find the network output  $a$  for each of the transfer function.

A-hardlim . B- logsig.

Q2: Calculate the thresholds and weight for Hopfield Network that is to learn the following three input vector:

$$X1 = [-1 \ -1 \ 1] \quad X2 = [1 \ -1 \ -1] \quad X3 = [-1 \ 1 \ 1]$$

[15 marks]

Q3: Determine the neural network weight matrices using perceptron rule after applying first iteration on the prototype vector:

[15 marks]

$$\left\{ p_1 = \begin{bmatrix} 2 \\ 2 \end{bmatrix}, t_1 = 0 \right\} \left\{ p_2 = \begin{bmatrix} 1 \\ -2 \end{bmatrix}, t_2 = 1 \right\} \left\{ p_3 = \begin{bmatrix} -2 \\ 2 \end{bmatrix}, t_3 = 0 \right\} \left\{ p_4 = \begin{bmatrix} -1 \\ 1 \end{bmatrix}, t_4 = 1 \right\}$$

And

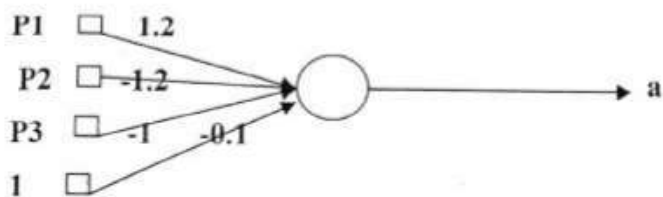
$$W(0) = \begin{bmatrix} 0 & 0 \end{bmatrix} \quad b(0) = 0$$

Q4: A kohonen self-organization map(SOM) to be cluster two vectores  $V_{octer1} = (1 \ 1 \ 0)$  and  $V_{octer2} = (0 \ 0 \ 0)$ . the maximum number of cluster to be formed is  $m=2$  with learning rate  $\alpha=0.6$  and the initial waite matrex are:

[15 marks]

Q1:

1:



2:

$$\text{Net} = W * p(\text{vectors Transpose}) + b$$

$$\text{Net} = [1.2 \ -1.2 \ -1] * \begin{bmatrix} 1.0 \\ -3.1 \\ -0.1 \end{bmatrix} + [-0.1] = 2.52$$

3:

A: $a = \text{hardlim}(2.52) = 1$ Net > 0	B: $a = 1 / (1 + \exp -(\text{Net})) = 0.9255$
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Q2:

<p>1- The vectors</p> <p>(-1 -1 1)      (1 -1 -1)      (-1 1 1)</p> <p>The matrix</p> <p>-1 -1 1</p> <p>1 -1 -1</p> <p>-1 1 1</p> <p>The transpose of matrix</p> <p>-1    1    -1      1    -1</p> <p>-1    -1    1    *    1    =    -1    = W0</p> <p>1    -1    1      1      1</p> <p><math>T_j = -W0 = 1</math> (T1)</p> <p>                  1 (T2)</p> <p>                  -1 (T3)</p>	<p>2- The weight matrix</p> <p>The vectors</p> <p>(-1 -1 1)      (1 -1 -1)      (-1 1 1)</p> <p><math>w_{1,1} = 0</math></p> <p><math>w_{1,2} = (-1) \times (-1) + 1 \times (-1) + (-1) \times 1 = -1</math></p> <p><math>w_{1,3} = (-1) \times 1 + 1 \times (-1) + (-1) \times 1 = -3</math></p> <p><math>w_{2,2} = 0</math></p> <p><math>w_{2,1} = w_{1,2}</math></p> <p><math>w_{2,3} = (-1) \times 1 + (-1) \times (-1) + 1 \times 1 = 1</math></p> <p><math>w_{3,3} = 0</math></p> <p><math>w_{3,1} = w_{1,3}</math></p> <p><math>w_{3,2} = w_{2,3}</math></p>
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Q3:

$$\left\{ \mathbf{p}_1 = \begin{bmatrix} 2 \\ 2 \end{bmatrix}, t_1 = 0 \right\} \left\{ \mathbf{p}_2 = \begin{bmatrix} 1 \\ -2 \end{bmatrix}, t_2 = 1 \right\} \left\{ \mathbf{p}_3 = \begin{bmatrix} -2 \\ 2 \end{bmatrix}, t_3 = 0 \right\} \left\{ \mathbf{p}_4 = \begin{bmatrix} -1 \\ 1 \end{bmatrix}, t_4 = 1 \right\}$$

Use the initial weights and bias:

$$\mathbf{W}(0) = \begin{bmatrix} 0 & 0 \end{bmatrix} \quad b(0) = 0.$$

We start by calculating the perceptron's output  $a$  for the first input vector  $\mathbf{p}_1$ , using the initial weights and bias.

$$\begin{aligned} a &= \text{hardlim}(\mathbf{W}(0)\mathbf{p}_1 + b(0)) \\ &= \text{hardlim}\left(\begin{bmatrix} 0 & 0 \end{bmatrix} \begin{bmatrix} 2 \\ 2 \end{bmatrix} + 0\right) = \text{hardlim}(0) = 1 \end{aligned}$$

The output  $a$  does not equal the target value  $t_1$ , so we use the perceptron rule to find new weights and biases based on the error.

$$\begin{aligned} e &= t_1 - a = 0 - 1 = -1 \\ \mathbf{W}(1) &= \mathbf{W}(0) + e\mathbf{p}_1^T = \begin{bmatrix} 0 & 0 \end{bmatrix} + (-1) \begin{bmatrix} 2 & 2 \end{bmatrix} = \begin{bmatrix} -2 & -2 \end{bmatrix} \\ b(1) &= b(0) + e = 0 + (-1) = -1 \end{aligned}$$

We now apply the second input vector  $\mathbf{p}_2$ , using the updated weights and bias.

$$\begin{aligned} a &= \text{hardlim}(\mathbf{W}(1)\mathbf{p}_2 + b(1)) \\ &= \text{hardlim}\left(\begin{bmatrix} -2 & -2 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \end{bmatrix} - 1\right) = \text{hardlim}(1) = 1 \end{aligned}$$

This time the output  $a$  is equal to the target  $t_2$ . Application of the perceptron rule will not result in any changes.

$$\begin{aligned} \mathbf{W}(2) &= \mathbf{W}(1) \\ b(2) &= b(1) \end{aligned}$$

We now apply the third input vector.

$$a = \text{hardlim}(W(2)p_3 + b(2))$$

$$= \text{hardlim}\left(\begin{bmatrix} -2 & -2 \end{bmatrix} \begin{bmatrix} -2 \\ 2 \end{bmatrix} - 1\right) = \text{hardlim}(-1) = 0$$

The output in response to input vector  $p_3$  is equal to the target  $t_3$ , so there will be no changes.

$$W(3) = W(2)$$

$$b(3) = b(2)$$

We now move on to the last input vector  $p_4$ .

$$a = \text{hardlim}(W(3)p_4 + b(3))$$

$$= \text{hardlim}\left(\begin{bmatrix} -2 & -2 \end{bmatrix} \begin{bmatrix} -1 \\ 1 \end{bmatrix} - 1\right) = \text{hardlim}(-1) = 0$$

This time the output  $a$  does not equal the appropriate target  $t_4$ . The perceptron rule will result in a new set of values for  $W$  and  $b$ .

$$e = t_4 - a = 1 - 0 = 1$$

$$W(4) = W(3) + e p_4^T = \begin{bmatrix} -2 & -2 \end{bmatrix} + (1) \begin{bmatrix} -1 & 1 \end{bmatrix} = \begin{bmatrix} -3 & -1 \end{bmatrix}$$

$$b(4) = b(3) + e = -1 + 1 = 0$$

After making one pass through all of the two inputs, get the value :  $w = [-3 \ -1]$ , and  $b=0$ .

**Q4:**

$$\begin{array}{l} \text{1- for the first vector} \\ \begin{array}{ccc} x_1 & x_2 & x_3 \\ (1 & 1 & 0) \end{array} \end{array}$$

$$D(1) = (1 - 0.2)^2 + (1 - 0.6)^2 + (0 - 0.5)^2 = 1.05$$

$$D(2) = (1 - 0.8)^2 + (1 - 0.4)^2 + (0 - 0.7)^2 = 0.89 \text{ (Minimum)}$$

$\therefore J = 2$  (The input vector) is closest to output node 2)

$\therefore$  The weight on the winning unit is update:-

$$\begin{aligned} W_{21}(\text{new}) &= W_{21}(\text{old}) + 0.6(x_1 - W_{21}(\text{old})) \\ &= 0.8 + 0.6(1 - 0.8) = 0.92 \end{aligned}$$

$$\begin{aligned} W_{22}(\text{new}) &= 0.4 + 0.6(1 - 0.4) \\ &= 0.4 + 0.36 = 0.76 \end{aligned}$$

Step 1: for each I/p training vector    target o/p

Pair,  $S : t$  do steps 2- 4.

Step 2 : Set activations for I/P units:

$$x_i = s_i \text{ (i =1 to n )}$$

Step 3 : set activation for O/P unit :

$$y=t$$

Step 4 : Adjust the weights for

$$w_i \text{ (new)} = w_i \text{ (old)} + x_i y \text{ (i =1 to n )}$$

Adjust the bias:

$$b \text{ (new)} = b \text{ (old)} + y$$