

Activation function

المركب

$$\text{net} = \sum_{i=1}^n x_i w_i + \theta \beta$$

$$= \omega_1 x_1 + \omega_2 x_2 + \omega_3 x_3 + \dots + \theta$$

in/out des:

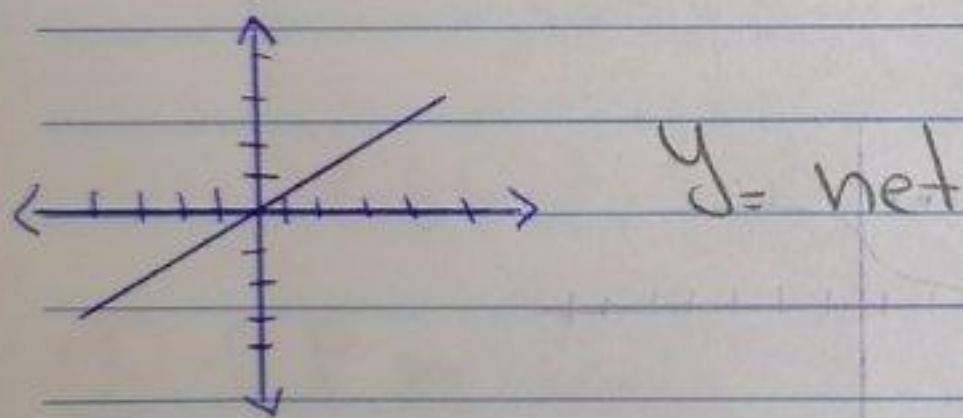
* إذا اذعنا
بالسؤال

نموده و اذا
لم تمشي في
O=

θ : threshold, β : bias, w : weight

Type of activation function:

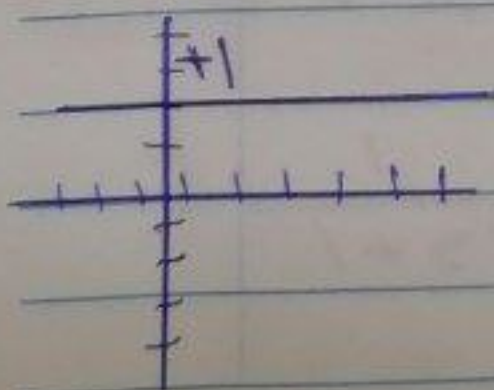
1) linear \Rightarrow identity function $\boxed{y = net}$ (Ramp)



2) hard limiter

a) binary hard limiter \Rightarrow Unit Step Function

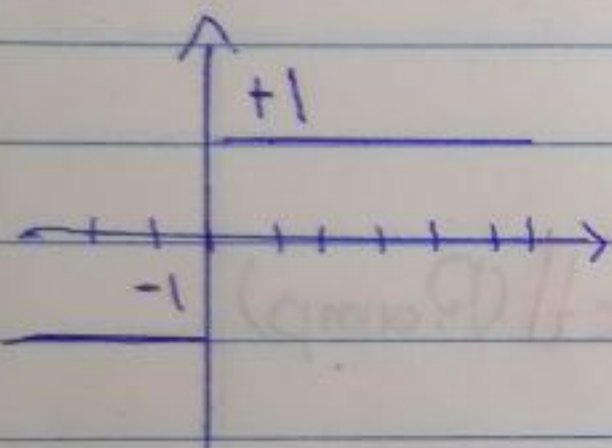
$$y_d = \begin{cases} 0 & \text{if net} < 0 \\ 1 & \text{if net} \geq 0 \end{cases}$$



b) Symmetric hard limiter (SHL) \Rightarrow double Side

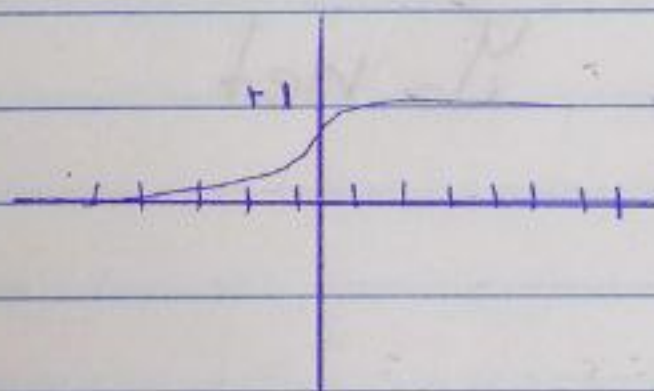
$$y = \begin{cases} -1 & \text{if net} < 0 \\ 0 & \text{if net} = 0 \\ +1 & \text{if net} > 0 \end{cases}$$

أكبر من
وإلا
عند الصفر
عند السالب
عند الموجب



3) Sigmoid

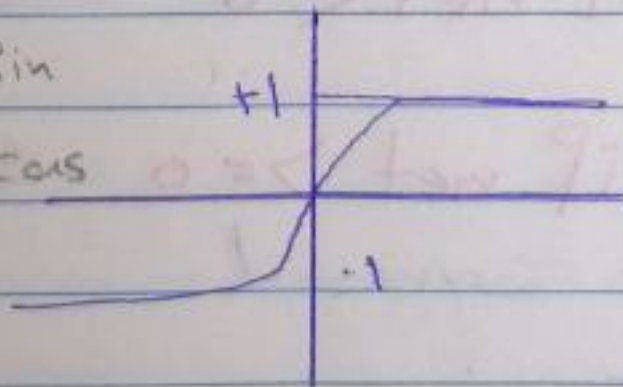
$$y = \frac{1}{1 + e^{-net}}$$



4) Hyperbolic tangent (tanh)

$$y = \frac{e^{net} - e^{-net}}{e^{net} + e^{-net}}$$

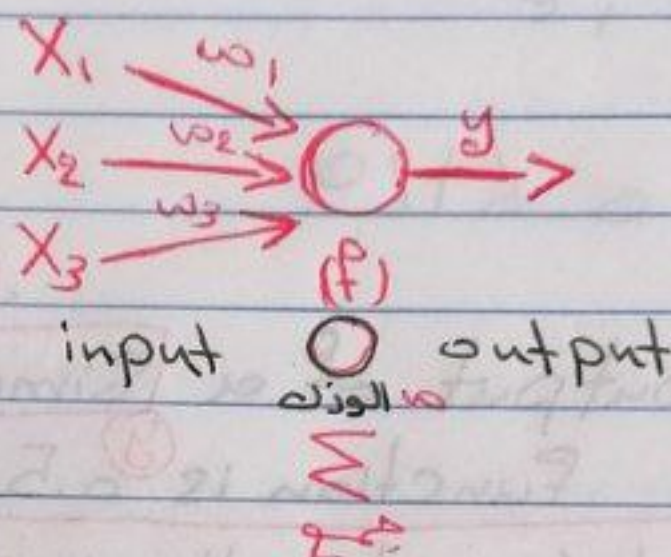
sin
cos



Ex 1- find y for the following neuron if :-

$$X_1 = 0.5, X_2 = 1, X_3 = -0.7$$

$$w_1 = 0, w_2 = -0.3, w_3 = 0.6$$



Sol:

$$\begin{aligned} \text{net} &= X_1 w_1 + X_2 w_2 + X_3 w_3 + \theta \\ &= (0.5 * 0) + (1 * -0.3) + (-0.7 * 0.6) + 0 \\ &= -0.3 - 0.42 \\ &= -0.72 \end{aligned}$$

إذا كان الوزن θ فنعوضه
وزنه هنا وإذا من هنا فنعوضه

1- if f is linear

$$y = \text{net} \Rightarrow y = -0.72$$

2- if f is hard limiter
(Symmetric)

إذا كان الوزن θ فنعوضه

أما

$$\text{if net} < 0 \Rightarrow -1$$

$$y = -1$$

3- if f is Sigmoid

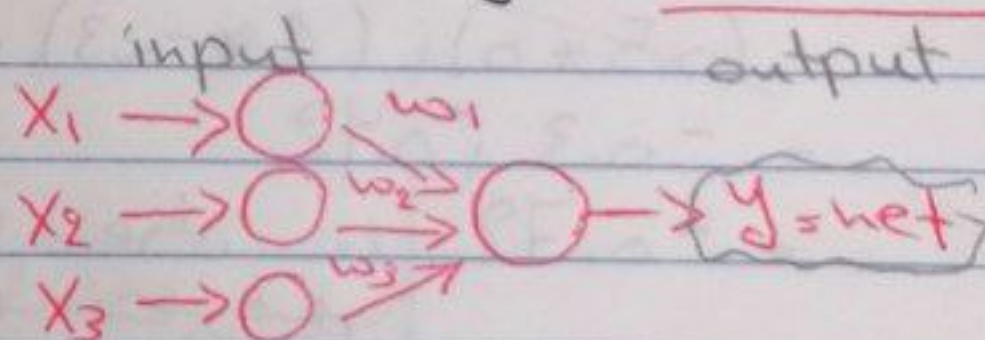
$$y = \frac{1}{1 + e^{-\text{net}}} \Rightarrow y = \frac{1}{1 + e^{-0.72}} = 0.39$$

4- if f is tanh

$$y = \frac{e^{\text{net}} - e^{-\text{net}}}{e^{\text{net}} + e^{-\text{net}}} \Rightarrow y = \frac{e^{0.72} - e^{-0.72}}{e^{0.72} + e^{-0.72}}$$

$$y = -0.6169$$

EX2: The output of a Simulated neural using a Sigmoidal Function is 0.5 Find the value of threshold when the input $X_1=1$, $X_2=1.5$, $X_3=2.5$ and have initial weights values 0.2



Sol: $y = 0.5$, $\theta = ?$

$$y = \frac{1}{1 + e^{-\text{net}}} \quad \text{Sigmoidal Function}$$

$$\text{net} = w_1 X_1 + w_2 X_2 + w_3 X_3 + \theta$$

$$\text{net} = (1 * 0.2) + (1.5 * 0.2) + (2.5 * 0.2)$$

$$\text{net} = 0.2 + 0.30 + 0.50$$

$$\text{net} = 1$$

$$0.5 = \frac{1}{1 + e^{-(1+\theta)}} \Rightarrow 0.5(1 + e^{-(1+\theta)}) = 1$$

$$0.5 + 0.5e^{-(1+\theta)} = 1 \Rightarrow 0.5e^{-(1+\theta)} = 0.5$$

$$e^{-(1+\theta)} = 1 \Rightarrow -(1+\theta) = \ln 1 \Rightarrow -1 - \theta = 0$$

$$-\theta = 1 \Rightarrow \theta = -1$$

CLEAR