



STUDENT PLAGIARISM: COURSE WORK - POLICY AND PROCEDURE COMPLIANCE STATEMENT

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CONTENTS

	d Based Robot Motion Planning	1
1.1	Introduction	1
1.2	Martian Terrain Map	1
1.3	Gridded Map	1
	1.3.1 Generate Grid	1
1.4		1
		1
1.5		$\overline{2}$
1.0		2
	•	2
	•	$\frac{2}{2}$
	1	$\frac{2}{2}$
		3
1.6		ა 3
1.0		
		3
		3
1.7		3
	1.7.1 A* Implementation	3
0,,,	action 2	4
•		4
		4
		4
2.4	Methodology	5
App	pendix A: Grid Based Robot Motion Planning	6
App	pendix B: Question 2	12
IST	OF FIGURES	
3.1	Output from Section 1.3.1 Generate Grid. The start node is in blue and the goal node	
	is in red	6
3.2	Output from Section 1.4.1 Generate Obstacles. The start node is in blue, the goal node	
	is in red and obstacles are black	7
3.3	Output from Section ?? ??. Traversability map: Darker colours indicate a higher cost	
	to travel over. White indicates the rover is unable to travel over	7
3.4	Output from Section 1.6.2 Dijkstra Implementation. The start node is in blue, the goal	
	node is in red and obstacles are black	8
3.5	A* Euclidean Distance	9
3.6	A* Manhattan Distance	10
3.7		11
ICT	OF TARIES	
19 1	OF TABLES	
2.1	text	5
	1.2 1.3 1.4 1.5 1.6 1.7 Que 2.1 2.2 2.3 2.4 Apr Apr 3.1 3.2 3.3 3.4 3.5 3.6 3.7	1.2 Martian Terrain Map 1.3 Gridded Map 1.3.1 Generate Grid 1.4 Configuration Space 1.4.1 Generate Obstacles 1.5 GESTALT 1.5.1 Footprint Points 1.5.2 Least Squares Fit of Plane 1.5.3 Step Hazard Evaluation 1.5.4 Pitch Hazard Evaluation 1.5.5 Roughness Hazard Evaluation 1.5.6 Roughness Hazard Evaluation 1.6.1 Identify Neighbours 1.6.2 Dijkstra Algorithm 1.6.1 A* Algorithm 1.7.1 A* Implementation 1.7 A* Algorithm 1.7.1 A* Implementation 2.2 Cost and Constraints 2.3 Local frame of satellite 2.4 Methodology Appendix A: Grid Based Robot Motion Planning Appendix B: Question 2 IST OF FIGURES 3.1 Output from Section 1.3.1 Generate Grid. The start node is in blue and the goal node is in red 3.2 Output from Section 1.4.1 Generate Obstacles. The start node is in blue, the goal node is in red and obstacles are black 3.3 Output from Section 1.6.2 Dijkstra Implementation. The start node is in blue, the goal node node is in red and obstacles are black 3.4 Output from Section 1.6.2 Dijkstra Implementation. The start node is in blue, the goal node is in red and obstacles are black 3.5 A* Euclidean Distance 3.6 A* Manhattan Distance 3.7 Output from Section ?? ??.

1. GRID BASED ROBOT MOTION PLANNING

1.1 Introduction

presents the output of each function discussion of your understanding of each section how you implemented the relevant algorithms.

1.2 Martian Terrain Map

nothing

1.3 Gridded Map

1.3.1 Generate Grid

The function **generateGrid** calculates the size of the matrix that reflects the discretised map by mapDim/cellDim and creates the matrix as map. The start and end node are calculated using the provided function pos2cell and set in map. The map is displayed by the predefined function **showmap**, see Figure 3.1.

Inputs:

- mapDim: The width and height of the map in meters.
- cellDim: The required width and height of each cell on the grid.
- startPos: The x and y position of the start point in meters from the centre of the grid.
- goalPos: The x and y position of the goal point in meters from the centre of the grid.

Outputs:

• map: The discretised global map with start and goal node defined

1.4 Configuration Space

1.4.1 Generate Obstacles

The function **generateObstacles** defines the cells on the map where the rover cannot travel due to predefined obstacles. The map reflects the configuration space of the rover, therefore the radius of the rovers footprint was added to the radius of each obstacle. The x domain of each obstacle was defined in meters discretised by . Using the conic equation for a circle Eq(1), the x domain was to calculate the upper and lower edge of the obstacle in meters.

$$y_i = y_c \pm \sqrt{r^2 - (x_i - x_c)^2} \tag{1}$$

Where x_i is the discretised domain, (x_c, y_c) is the centre of the obstacle, r is the new radius of the obstacle and y_i is the discretised upper and lower edge of the obstacle. The coordinates (x_i, y_i) were converted to indices in map by **pos2cell**. For each x_i index, the coordinates between y_i^+ and y_i^- were set as an obstacle in map. The output map is displayed using **showmap**, see Figure 3.2.

Inputs:

- map: The discretised global map from **generategrid**.
- obstacles: The x,y coordinates and the radius of each obstacle

- cellDim: The required width and height of each cell on the grid.
- mapDim: The width and height of the map in meters.
- ullet global $ROVER_FOOTPRINT_RADIUS$: The radius of the footprint of the rover in meters.

Outputs:

• map: The discretised global map with start node, goal node and obstacles defined.

1.5 GESTALT

1.5.1 Footprint Points

The function **getRoverFootprintPoints** uses the built-in function **rangesearch** to identify points in *pointCloud* that fall within the rover's footprint radius from the centre of a cell.

1.5.2 Least Squares Fit of Plane

The function **fitplane** fits a plane using least squares method with all the points in the current cell. The mean average vector \vec{p} was calculated from the point cloud *points* and the residuals R were found. The first eigenvector of R'R is the unit vector normal to the plane.

Inputs:

• points:

Outputs:

- n: vector normal to the plane
- p: average vector

1.5.3 Step Hazard Evaluation

The function **stepHazardEval** assigns a cost associated with how much of a step hazard the current cell is.

Algorithm 1 Step Hazard Evaluation

```
\begin{array}{l} \text{max step} \leftarrow \text{max z - min z} \\ \textbf{if max step} < \text{threshold/3 then} \\ \text{step hazard} \leftarrow 0 \\ \textbf{else} \\ \text{step hazard} \leftarrow 255 \times \% \text{ max step from threshold} \\ \textbf{return step hazard} \end{array}
```

1.5.4 Pitch Hazard Evaluation

The function pitchHazardEval

The pitch angle θ is calculated using the vector normal n to the plane of best fit as returned from **fitplane** using Eq(2).

$$\theta = \frac{\pi}{2} - \tan^{-1} \left(\frac{n_z}{\sqrt{n_x^2 + n_y^2}} \right) \tag{2}$$

Algorithm 2 Pitch Hazard Evaluation

```
pitch angle \leftarrow Eq(2)

if pitch angle > threshold then

pitch hazard \leftarrow 255

else

pitch hazard \leftarrow 255 \times % angle from threshold

return pitch hazard
```

1.5.5 Roughness Hazard Evaluation

The function **roughnessHazardEval** evaluates how rough the current cell is by calculating the standard deviation of the residuals,

1.6 Dijkstra Algorithm

The purpose of implementing Dijkstra's Algorithm was to find the path of least cost without having to test every possible combination. It operates by storing the path of minimum cost from a start node to each point on a grid. Dijkstra moves outwards from the start node as a breadth search, regardless of the direction the goal node is in.

1.6.1 Identify Neighbours

The function **getNeighbours** identifies the valid neighbours around the current node based on information from *map*, *mapTraversability* and size of the gridded map. A neighbour is considered invalid if it is outside the global map indices, if it has already been visited or if it was above the traversability threshold. There are two options for how each node is connected to its neighbours; four connections (up,down,left,right) or eight connections (including diagonals). The indices of the valid neighbours are returned from the function and set as 'on list' in *map*.

1.6.2 Dijkstra Implementation

The function **dijkstraBody** identifies if going from the current node to a neighbour is better than any previous calculated paths.

Algorithm 3 Dijkstra Body

```
for each neighbour around node do

if cost from start(neighbour) > cost from start(node) + traversability(neighbour) then

cost from start(neighbour) \leftarrow cost from start(node) + traversability(neighbour)

best path so far \leftarrow node

nodes to do \leftarrow neighbour
```

1.7 A* Algorithm

The A* algorithm follows the Dijkstra structure, except that it searches towards the goal node first. This was done using a heuristic and implementing cost-to-go and cost-from-start metrics.

1.7.1 A* Implementation

The function **aStarBody** identifies if going from the current node to a neighbour is better than any previous calculated paths.

Heuristic	Weighting factor	numExpanded	Cost increase	% Cost Increase
Dijstra reference	0	1743	60306	-
Euclidean distance	1	1731	0	0%
Euclidean distance	10	1612	0	0%
Euclidean distance	25	1366	587	0.97%
Euclidean distance	50	957	8020	13.30%
Euclidean distance	75	159	15156	25.13%
Euclidean distance	100	67	22644	37.55%
Manhattan distance	1	1730	0	0%
Manhattan distance	10	1573	0	0%
Manhattan distance	25	1235	324	0.54%
Manhattan distance	50	306	7891	13.08%
Manhattan distance	75	74	26397	43.77%
Manhattan distance	100	53	28143	46.67%

Algorithm 4 A* Body

for each neighbour around node do

```
if cost from start(neighbour) > cost from start(node) + traversability(neighbour) then cost from start(neighbour) \leftarrow cost from start(node) + traversability(neighbour) cost to go(neighbour) \leftarrow cost to come(node) + heuristic to goal(neighbour) best path so far \leftarrow node
```

nodes to do \leftarrow neighbour

2. Question 2

2.1 Introduction

The final GEO orbit is defined as having a period of one sidereal day, 23 hours 56 minutes 4.0916 seconds. Using Kepler's third law Eq(3) and the vis-viva law Eq(4) the semi-major axis and velocity of the circular orbit were calculated, see Table 2.1.

$$a = \sqrt[1/3]{\frac{\mu \mathbb{P}^2}{4\pi^2}} \tag{3}$$

$$v = \sqrt{\frac{\mu}{a}} \tag{4}$$

The satellite parameters in the park orbit are

2.2 Cost and Constraints

What are constraints - why are they important.

The constraints on this optimisation problem defines the final GEO orbit. They are The radius and velocity are enforced by requiring the ratio between the

$$J = |\Delta v_1| + |\Delta v_2| \tag{5}$$

2.3 Local frame of satellite

The local frame of the satellite where the burn is applied

Table 2.1: text

Orbital Parameter	Initial Value	Final Value
Semi-major axis	6655937 m	
Period		86164.0916 s
Velocity		
Eccentricity	0	0
Inclination angle	-28.5°	0 \circ
RAAN	0°	
Argument of Perigee	0°	
Mean Anomaly	0°	free
Epoch	0 s	free

2.4 Methodology

The Hessian of the Lagrangian $H_{\mathcal{L}} = \nabla_{xx}^2 \mathcal{L}$ BFGS method. Approximation of the Hessian update

$$\boldsymbol{H}_{k+1} = \boldsymbol{H}_k - \frac{\boldsymbol{H}_k s_k s_k^T \boldsymbol{H}_k}{s_k^T \boldsymbol{H}_k s_k} + \frac{\boldsymbol{y}_k \boldsymbol{y}_k^T}{\boldsymbol{y}_k^T s_k}$$
(6)

$$s_k = x_{k+1} - x_k \tag{7}$$

$$y_k = \nabla f_{k+1} - \nabla f_k \tag{8}$$

3. APPENDIX A: GRID BASED ROBOT MOTION PLANNING

Figure 3.1: Output from Section 1.3.1 Generate Grid. The start node is in blue and the goal node is in red

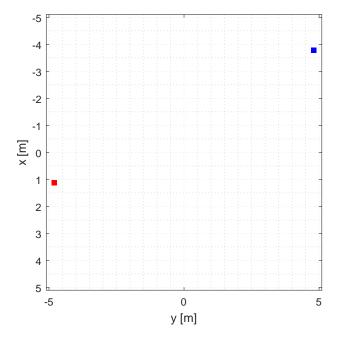


Figure 3.2: Output from Section 1.4.1 Generate Obstacles. The start node is in blue, the goal node is in red and obstacles are black

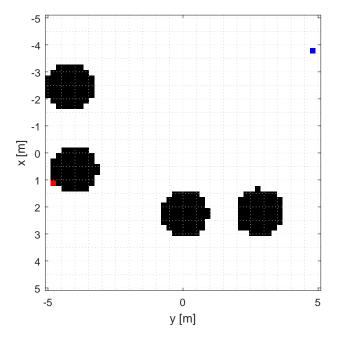


Figure 3.3: Output from Section ?? ??. Traversability map: Darker colours indicate a higher cost to travel over. White indicates the rover is unable to travel over.

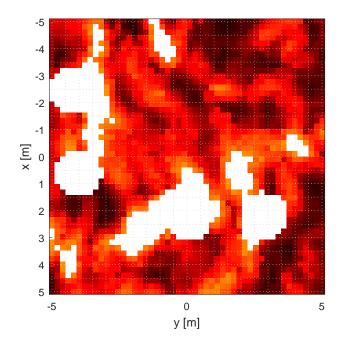


Figure 3.4: Output from Section 1.6.2 Dijkstra Implementation. The start node is in blue, the goal node is in red and obstacles are black

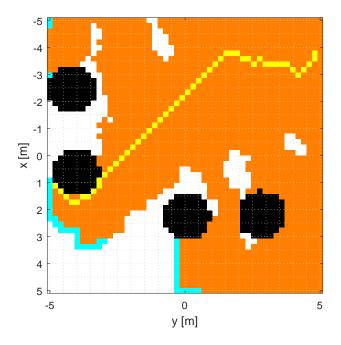
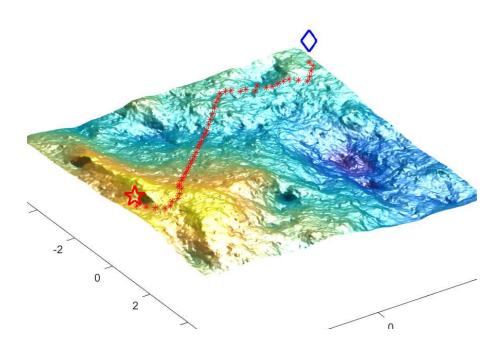


Figure 3.5: Output from Section ?? ??.



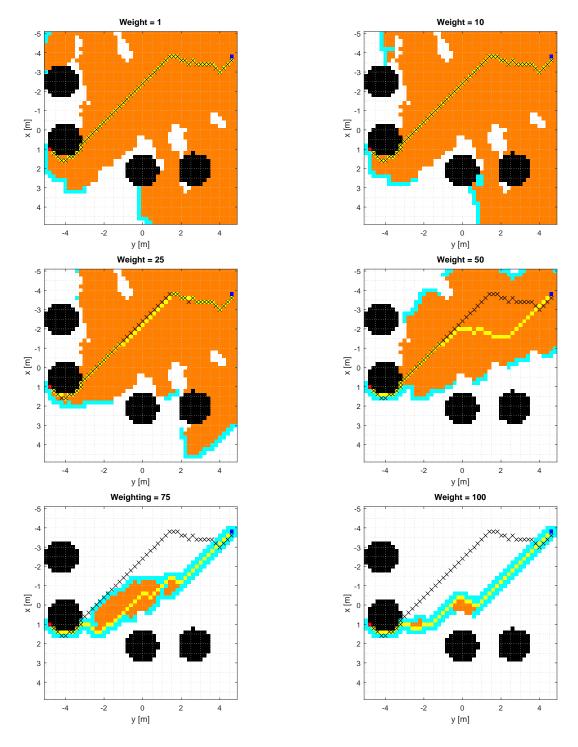


Figure 3.6: A* Euclidean Distance

Weight = 1 Weight = 10 Œ ₀ 0 y [m] 0 y [m] 2 4 Weight = 25 Weight = 50 Ξ₀ 3 0 y [m] 0 y [m] -4 Weight = 75 Weight = 100 <u>E</u> 0 Ξ₀ 0 y [m] 0 y [m] 2 2

Figure 3.7: A* Manhattan Distance

4. APPENDIX B: QUESTION 2