

Analyzing Semantic Correctness with Symbolic Execution: A Case Study on PKCS#1 v1.5 Signature Verification

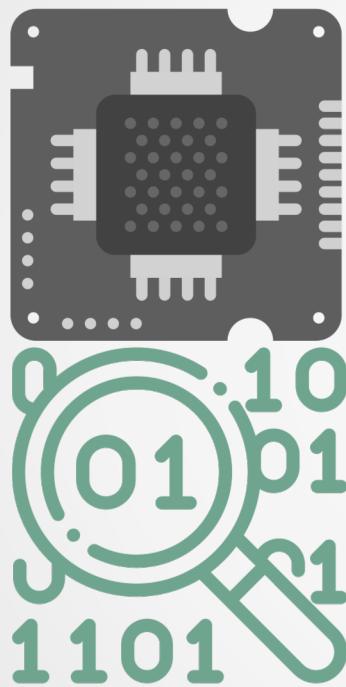
Sze Yiu Chau

Purdue University

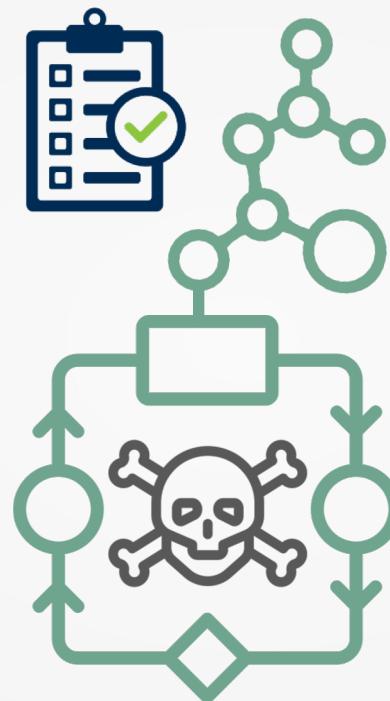
Joint work with Moosa Yahyazadeh, Omar Chowdhury,
Aniket Kate, Ninghui Li



Software Testing



Low-level
Errors



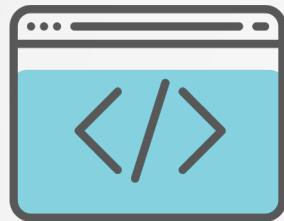
Logical Errors



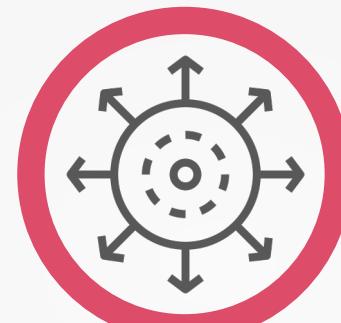
Attacks
e.g. libssh auth. bypass,
crypto. attacks

This work

- Symbolic execution for analyzing semantic correctness



Code
Coverage



Scalability
Challenges

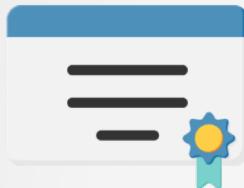


Domain
Knowledge

- Case study: Implementing PKCS#1 v1.5 signature verification

Motivation

- PKCS#1 v1.5 RSA signature is widely used



...



- Previous work on X.509 testing neglect to analyze RSA signature verifications
(Brubaker et al. 2014, Chen et al. 2015, Chau et al. 2017)

Motivation

- Implementations need to verify signatures robustly
- Logical errors may allow **signature forgery**
 - e.g. Bleichenbacher 2006, Kühn et al. 2008



Textbook RSA signature

- Signing message m :



- Given (S, m, e, n) , verifying S is a valid signature of m



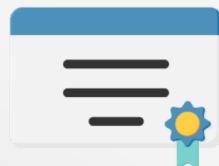
Beyond textbook RSA

- Reality is more complex than that
1. Which $H()$ to use?
 - SHA-1, SHA-2 family, SHA-3 family ...
 2. n is usually much longer than $H(m)$
 - $|n| \geq 2048\text{-bit}$
 - $|\text{SHA-1}| = 160\text{-bit}, |\text{SHA-256}| = 256\text{-bit}$
 - Need padding and meta-data



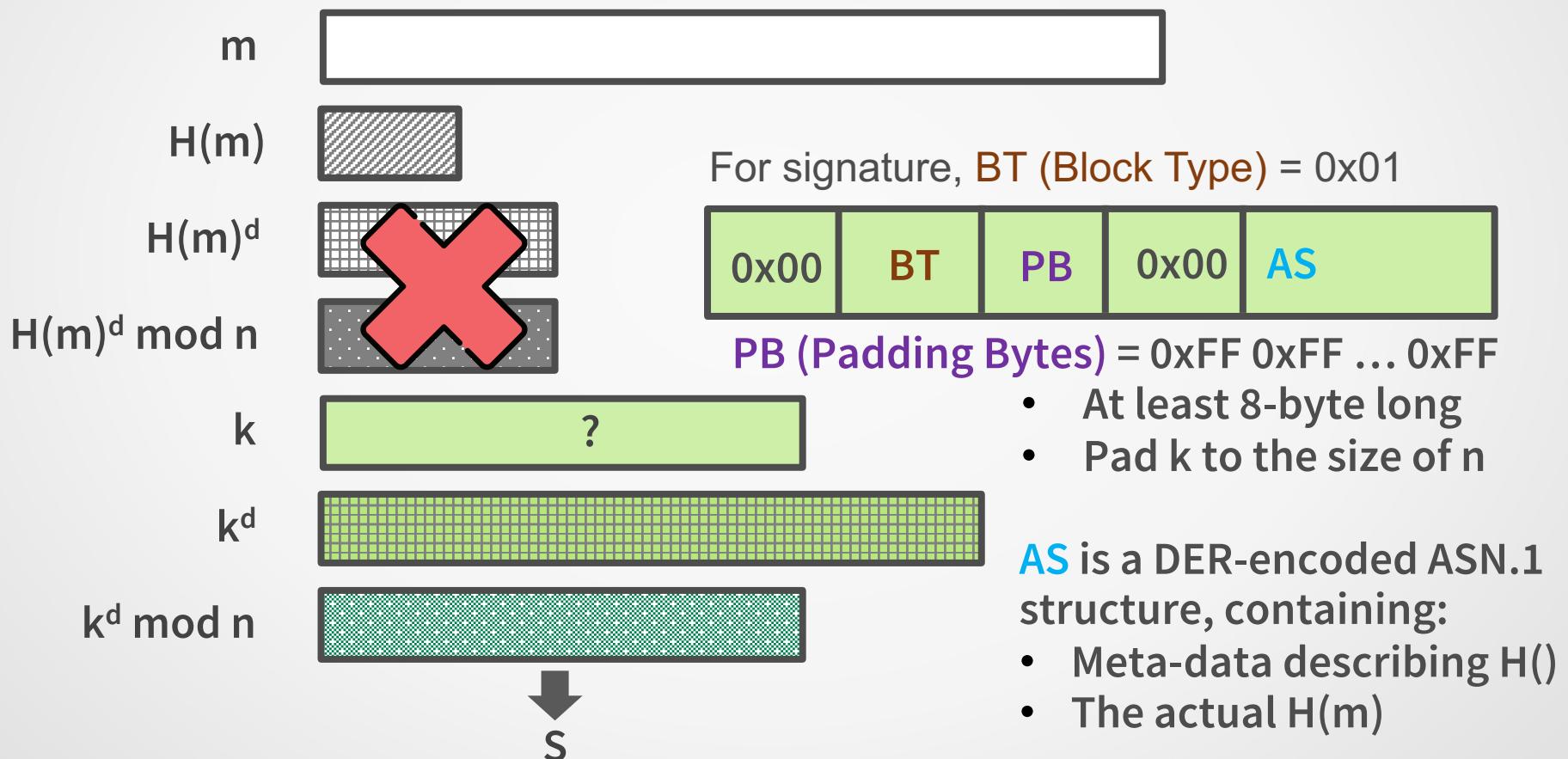
Beyond textbook RSA

- The PKCS#1 family of standards
 - Published by RSA (the company)
 - Both encryption and signature schemes
 - version 2+ adapted schemes from Bellare et al.
 - For signatures, **version 1.5 most widely used**
 - e.g. certificates of Google, Wikipedia



PKCS#1 v1.5 Signature Scheme

- **Signing:**



PKCS#1 v1.5 Signature Scheme

- DER encoded object is a tree of <T,L,V> triplets
- AS looks like this when encoded:

```
/** all numbers below are hexadecimals **/
/* [AS.DigestInfo] */
30 w          // ASN.1 SEQUENCE, length = w = 0x21
/* [AlgorithmIdentifier] */
30 x          // ASN.1 SEQUENCE, length = x = 0x09
  06 u 2B 0E 03 02 1A    // ASN.1 OID, length = u = 0x05
  05 y          // ASN.1 NULL parameter, length = y = 0x00
/* [Digest] */
04 z          // ASN.1 OCTET STRING, length = z = 0x14
/* H(m), H()=SHA-1(), m = "hello world" */
2A AE 6C 35 C9 4F CF B4 15 DB
E9 5F 40 8B 9C E9 1E E8 46 ED
```

- altogether 35 bytes if $H() = \text{SHA-1}()$

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PKCS#1 v1.5 Signature Scheme

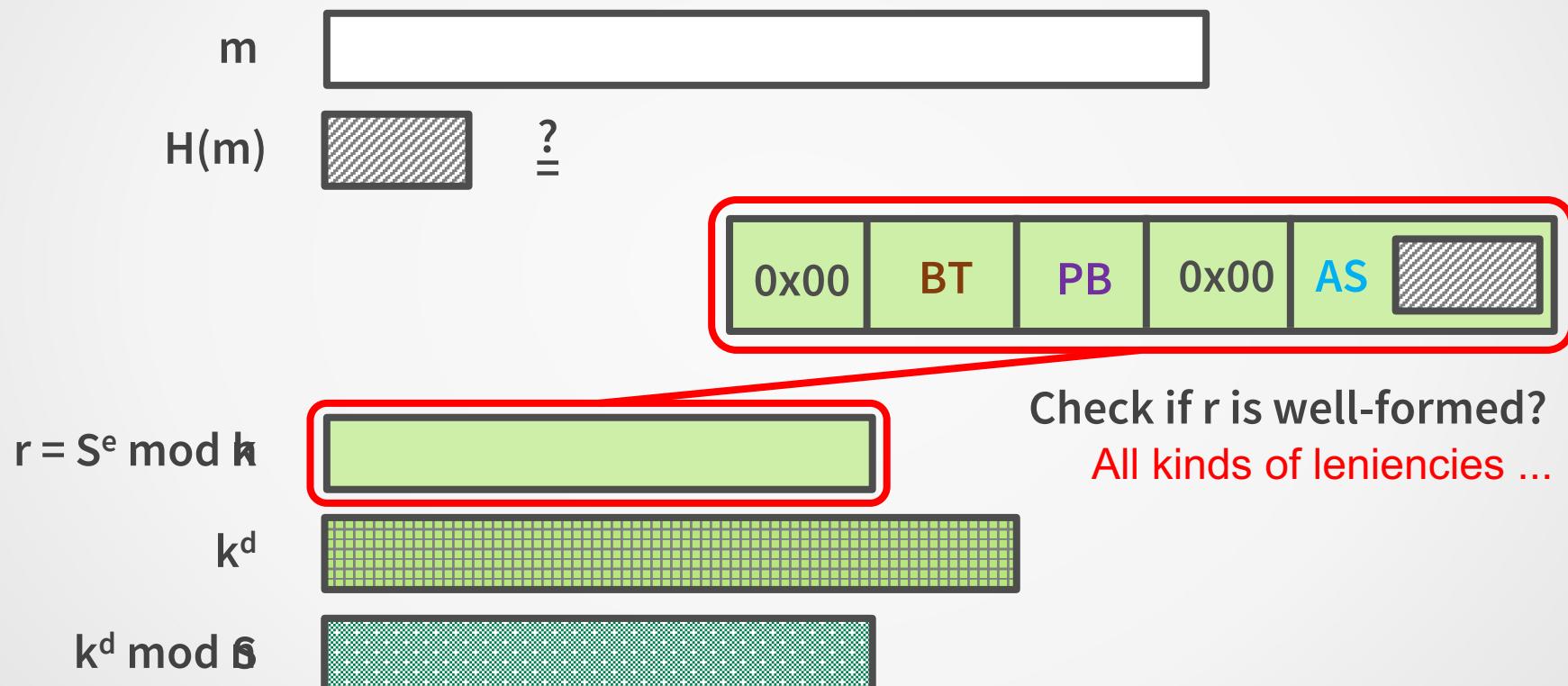
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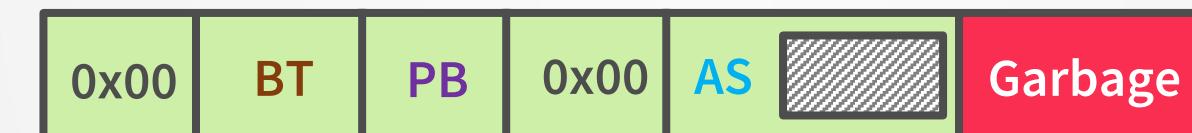
PKCS#1 v1.5 Signature Scheme

- Given (S, m, e, n) , verifier computes $H(m)$ and $r = S^e \bmod n$



Bleichenbacher's low exponent attack

- Yet another crypto attack attributed to D. Bleichenbacher
- CRYPTO 2006 rump session
- Some implementations accept malformed r'



- Existential forgery possible when e is small
 - Generate signatures for arbitrary m without d



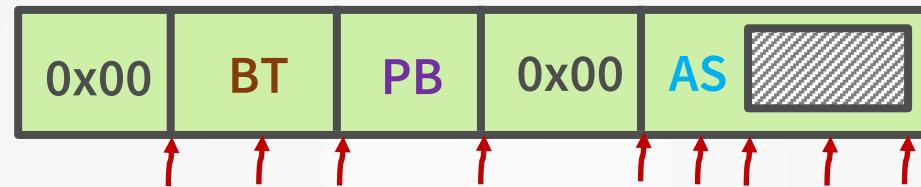
Bleichenbacher's low exponent attack

- A contributing factor to the push for bigger e (e.g. 65537)
- Smaller e more efficient for signature verifier
 - $e = 3$ prescribed in some protocols
 - (e.g. DNSSEC [RFC3110, Sect. 4])



Why was the attack possible?

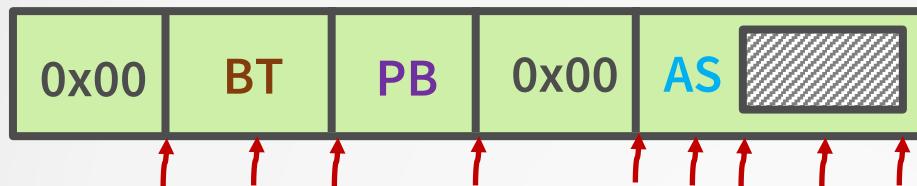
- Problem: accept malformed input w/ **GARBAGE** unchecked
 - Can be in many different locations, not only at the end



- Longer modulus makes forgery easier
 - More **GARBAGE** bits to use
 - Can handle longer hashes / **slightly larger e**

To find these attacks

- Want to see how input bytes are being checked

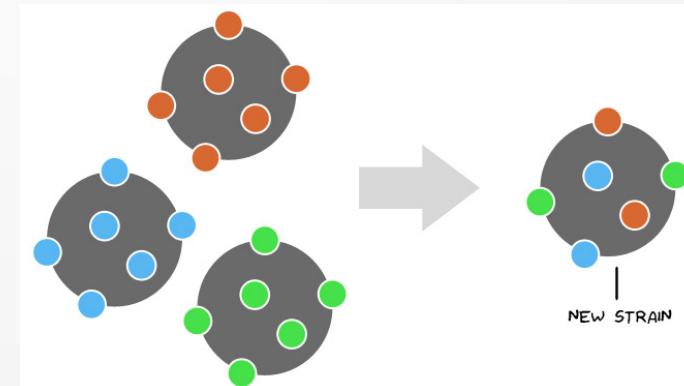
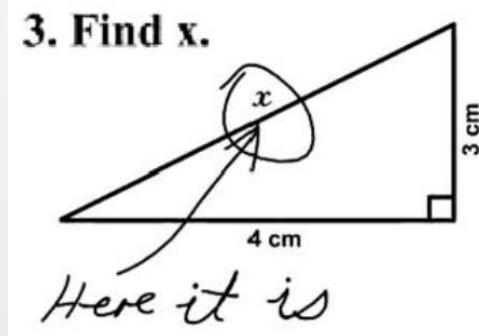
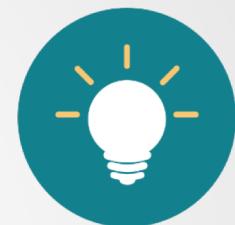


- If enough unchecked **GARBAGE** then



Automatically generate concolic test cases

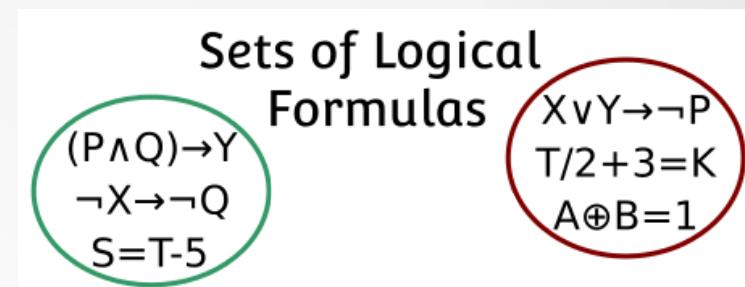
- Observation: size of components exhibit linear relations
 - e.g. $\sum \text{length(components)} = |n|$; ASN.1 DER
 - Programmatically capture such linear constraints
 - Ask Symbolic Execution to find satisfiable solutions



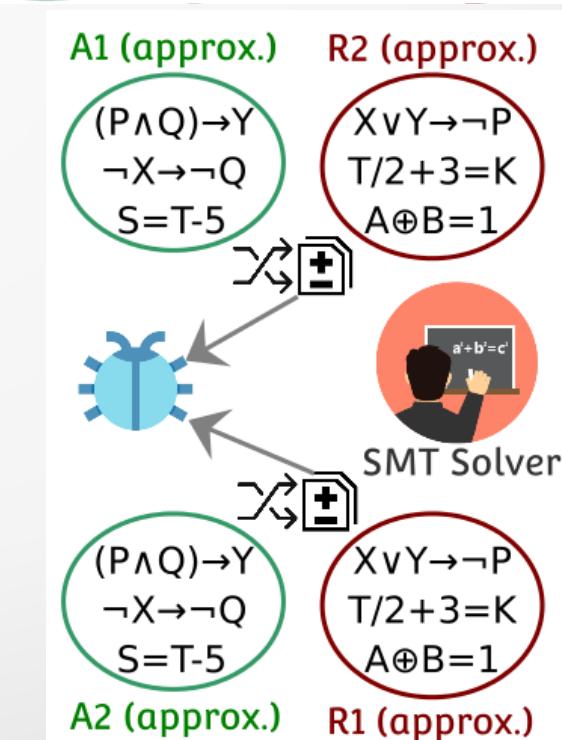
- Based on that, automatically pack symbolic/concrete components into test buffers

Testing with Symbolic Execution

- Symbolic Execution with concolic test cases

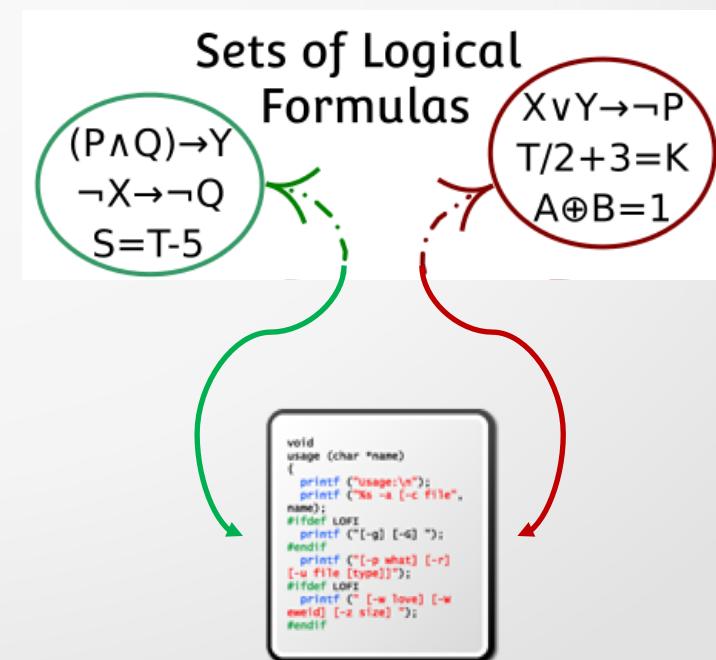


- Very useful abstraction
 - What and how things are being checked in code?
- Formulas can help cross-validate implementations



Finding root causes

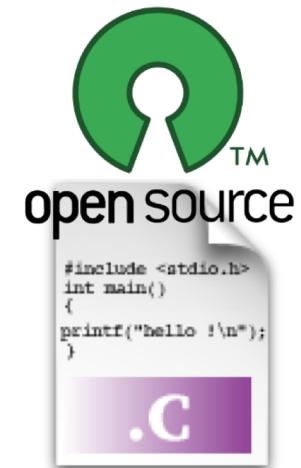
- Locate the piece of code that imposes wrong constraints
- Can we go from formula abstraction back to code?
- Constraint Provenance Tracking
 - Keep a mapping of <clause, source-level origin>
 - Tiny space & time overhead



Implementations Tested

Discussion of signature forgery
assumes e = 3 and SHA-1,
attacks also applicable to
newer hash algorithms

<u>Name - Version</u>	<u>Overly lenient</u>	<u>Practical exploit under small e</u>
axTLS - 2.1.3	YES	YES
BearSSL - 0.4	No	-
BoringSSL - 3112	No	-
Dropbear SSH – 2017.75	No	-
GnuTLS – 3.5.12	No	-
LibreSSL – 2.5.4	No	-
libtomcrypt – 1.16	YES	YES
MatrixSSL – 3.9.1 (Certificate)	YES	No
MatrixSSL – 3.9.1 (CRL)	YES	No
mbedTLS – 2.4.2	YES	No
OpenSSH – 7.7	No	-
OpenSSL – 1.0.2l	No	-
Openswan – 2.6.50 *	YES	YES
PuTTY – 0.7	No	-
strongSwan – 5.6.3 *	YES	YES
wolfSSL – 3.11.0	No	-



* configured to use
their own internal
implementations of
PKCS#1 v1.5

Leniency in Openswan 2.6.50

- Ignoring padding bytes (CVE-2018-15836)
- Simple oversight, severe implications
 - Exploitable for signature forgery
- Use this r' */** all numbers below are hexadecimals **/*

- Want: $(a + b)^3 = a^3 + 3a^2b + 3b^2a + b^3$, s.t.
 - MSBs of a^3 give what is before GARBAGE
 - LSBs of b^3 give what is after GARBAGE
 - LSBs of $a^3 + 3a^2b + 3b^2a + b^3$ stay in GARBAGE
 - fake signature $S' = (a+b)$

```
/* check signature contents */
/* verify padding (not including
any DER digest info!      */
padlen = sig_len - 3 - hash_len;
...
...
/* skip padding */
if(s[0] != 0x00 || s[1] != 0x01
|| s[padlen+2] != 0x00)
{ return "3""SIG padding does not ";
s += padlen + 3;
```



New unit test in Openswan

xelerance / Openswan

Code Issues 95 Pull requests 0 Projects 0 Wiki Insights

wo#7449 . test case for Bleichenbacher-style signature forgery

Special thanks to Sze Yiu Chau of Purdue University (schau@purdue.edu) who reported the issue, and made major contributions towards defining this test case.

master (#330) v2.6.51.2 ... v2.6.50.1

 bartman committed on Aug 20 1 parent 9eaa6c2

Showing 6 changed files with 218 additions and 0 deletions.

1 tests/unit/libosswan/Makefile

		@@ -23,6 +23,7 @@ clean check:
23	23	@@ \${MAKE} -C lo04-verifypubkeys \$@
24	24	@@ \${MAKE} -C lo05-datatot \$@
25	25	@@ \${MAKE} -C lo06-verifybadsigs \$@
26	+	@@ \${MAKE} -C lo07-bleichenbacher-attack \$@
27		

Leniency in strongSwan 5.6.3

1. Not checking AlgorithmParameter (CVE-2018-16152)

- classical flaw found in others like GnuTLS, Firefox years ago
- **Exploitable** for signature forgery
 - hide **GARBAGE** in **AlgorithmParameter**
 - follow the Openswan attack algorithm
 - adjust what a^3 and b^3 represent, **fake signature** $S' = (a+b)$



Leniency in strongSwan 5.6.3

2. Accept trailing bytes after Algorithm OID (CVE-2018-16151)

- interestingly, **Algorithm OID** is not matched exactly
- a variant of longest prefix match

```
/* [AlgorithmIdentifier] */  
30 09  
 06 05 2B 0E 03 02 1A  
 05 00
```

```
/* [AlgorithmIdentifier] */  
30 0C  
 06 08 2B 0E 03 02 1A AB CD EF  
 05 00
```

both would be recognized as OID of SHA-1

- knowing this, one can hide **GARBAGE** there
- follow the Openswan attack algorithm
 - adjust what a^3 and b^3 represent, **fake signature** $S' = (a+b)$



strongSwan Security Update

<input checked="" type="checkbox"/>	StrongSwan daemon starter and configuration file parser	742 kB
<input checked="" type="checkbox"/>	StrongSwan Internet Key Exchange daemon	56 kB
<input checked="" type="checkbox"/>	StrongSwan utility and crypto library	1.4 MB
<input checked="" type="checkbox"/>	StrongSwan utility and crypto library (standard plugins)	267 kB
<input checked="" type="checkbox"/>	Virtual Linux kernel tools	3 kB

▼ Technical description

[Changes](#) [Description](#)

src/libstrongswan/plugins/gmp/gmp_rsa_private_key.c
- [CVE-2018-17540](#)

Version 5.3.5-1ubuntu3.7:

* SECURITY UPDATE: Insufficient input validation in gmp plugin
- debian/patches/strongswan-5.3.1-5.6.0_gmp-pkcs1-verify.patch: don't
parse PKCS1 v1.5 RSA signatures to verify them in
src/libstrongswan/plugins/gmp/gmp_rsa_private_key.c,
src/libstrongswan/plugins/gmp/gmp_rsa_public_key.c.
- [CVE-2018-16151](#)
- [CVE-2018-16152](#)

+ SECURITY UPDATE.....+-----+-----+-----+-----+

Some key generation programs still forces $e = 3$

e.g., ipsec_rsasigkey on Ubuntu

NAME

ipsec_rsasigkey - generate RSA signature key

SYNOPSIS

```
ipsec rsasigkey [--verbose] [--seeddev device] [--seed numbits] [--nssdir nssdir]
                 [--password nsspassword] [--hostname hostname] [nbits]
```

DESCRIPTION

rsasigkey generates an RSA public/private key pair, suitable for digital signatures, of (exactly) nbets bits (that is, two primes each of exactly nbets/2 bits, and related numbers) and emits it on standard output as ASCII (mostly hex) data. nbets must be a multiple of 16.

The public exponent is forced to the value **3**, which has important speed advantages for signature checking. Beware that the resulting keys have known weaknesses as encryption keys **and should not be used for that purpose**.

Leniency in axTLS 2.1.3

1. Accepting trailing GARBAGE (CVE-2018-16150)
 - original Bleichenbacher '06 forgery also works



Leniency in axTLS 2.1.3

2. Ignoring AS.AlgorithmIdentifier (CVE-2018-16253)

```
/** all numbers below are hexadecimals */
/* [AS.DigestInfo] */
30 21
/* [AlgorithmIdentifier] */
30 09
06 05 2B 0E 03 02 1A
05 00
/* [Digest] */
04 14
/* H(m), H()=SHA-1(), m = "hello world" */
2A AE 6C 35 C9 4F CF B4 15 DB
E9 5F 40 8B 9C E9 1E E8 46 ED
```

this whole chunk
is skipped ...

```
if (asn1_next_obj(asn1_sig, &offset,
ASN1_SEQUENCE) < 0 ||
asn1_skip_obj(asn1_sig, &offset,
ASN1_SEQUENCE)) goto end_get_sig;

if (asn1_sig[offset++] != ASN1_OCTET_STRING)
goto end_get_sig;
*len = get_asn1_length(asn1_sig, &offset);
ptr = &asn1_sig[offset]; /* all ok */

end_get_sig:
return ptr;
```

Certificate Fields
Authority Information Access
Certificate Subject Key ID
Certificate Basic Constraints
Certificate Authority Key Identifier
Certificate Policies
CRL Distribution Points
Certificate Signature Algorithm
Certificate Signature Value

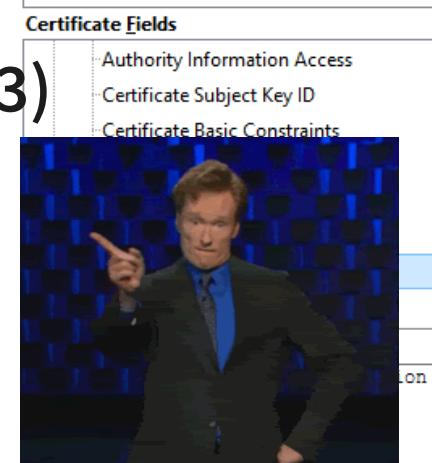
Field Value
PKCS #1 SHA-256 With RSA Encryption

- Probably because certificates have an explicit signature algorithm field, which gives H()

Leniency in axTLS 2.1.3

2. Ignoring AS.AlgorithmIdentifier (CVE-2018-16253)

- Just because $H()$ is known from outside
- Doesn't mean it can be skipped
- Use this r' `/** all numbers below are hexadecimals **/`
`00 01 FF FF FF FF FF FF FF FF 00`
`30 5D 30 5B GARBAGE 04 16 SHA-1(m')`
- hide **GARBAGE** in **AlgorithmIdentifier**
- follow the Openswan attack algorithm
 - adjust what a^3 and b^3 represent, **fake signature** $S' = (a+b)$



Leniency in axTLS 2.1.3

3. Trusting the declared ASN.1 DER lengths w/o sanity checks [CVE-2018-16149]

```
/** all numbers below are hexadecimals */
/* [AS.DigestInfo] */
30 w
/* [AlgorithmIdentifier] */
30 x
06 u 2B 0E 03 02 1A
05 y
/* [Digest] */
04 z
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```

put absurdly large values to trick verifier
into reading from illegal addresses



- DoS PoC: making z exceptionally large crashed the verifier

patching axTLS (ESP8266 port)

igrr / [axtls-8266](#)

Code Issues 8 Pull requests 1 Projects 0 Insights

Apply CVE fixes for X509 parsing

Apply patches developed by Sze Yiu which correct a vulnerability in X509 parsing. See CVE-2018-16150 and CVE-2018-16149 for more info.

master (#60)

 **earlephilhower** authored and **igrr** committed on Oct 22

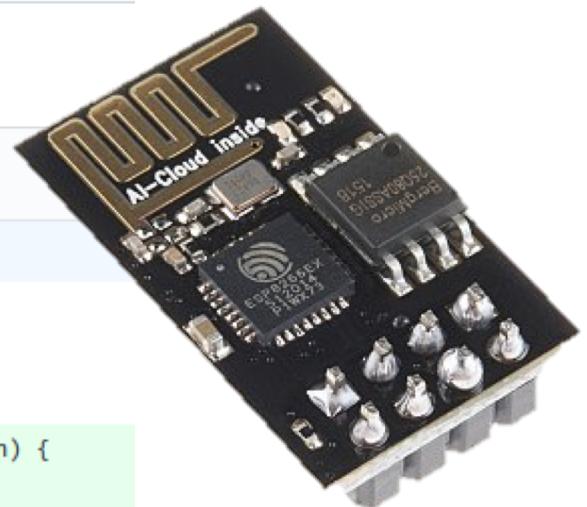
1 parent e634adf

ESP8266

Showing 2 changed files with 76 additions and 38 deletions.

12  ssl/os_port.h

```
@@ -142,6 +142,18 @@ static inline int strlen_P(const char *str) {  
142    142        while (pgm_read_byte(str++)) cnt++;  
143    143        return cnt;  
144    144    }  
145    + static inline int memcmp_P(const void *a1, const void *b1, size_t len) {  
146    +     const uint8_t* a = (const uint8_t*)(a1);  
147    +     uint8_t* b = (uint8_t*)(b1);
```



Other leniencies

- Lax checks on ASN.1 DER lengths in MatrixSSL(CRL)

```
/** all numbers below are hexadecimals */
/* [AS.DigestInfo] */
30 w
  /* [AlgorithmIdentifier] */
30 x
  06 u 2B 0E 03 02 1A
  05 y
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  04 z
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```

many possible values
will be accepted

- Some bits in the middle of AS can take any values
- Doesn't seem to be numerous enough for practical attacks
- Variants of this leniency also found in *mbedTLS*, *libtomcrypt*, *MatrixSSL (Certificate)*

Leniency in MatrixSSL 3.9.1

MatrixSSL 4.x changelog

Changes between 4.0.0 and 4.0.1 [November 2018]

This version improves the security of RSA PKCS #1.5 signature verification and adds better support for run-time security configuration.

- Crypto:
 - Changed from a parsing-based to a comparison-based approach in DigestInfo validation when verifying RSA PKCS #1.5 signatures. There are no known practical attacks against the old code, but the comparison-based approach is theoretically more sound. Thanks to Sze Yiu Chau from Purdue University for pointing this out.
 - (MatrixSSL FIPS Edition only:) Fix DH key exchange when using DH parameter files containing optional privateValueLength argument.
 - psX509AuthenticateCert now uses the common psVerifySig API for signature verification. Previously, CRLs and certificates used different code paths for signature verification.

Conclusion

- RSA signature verification should be robust regardless of the choice of e
 - Flawed verification can break authentication in different scenarios
 - To analyze this, we extend symbolic execution with
 - Automatic generation of concolic test cases
 - Constraint Provenance Tracking
 - Found new variants of Bleichenbacher '06 attacks after more than a decade, 6 new CVEs
 - And many other unwarranted leniencies



Q&A

Thank You

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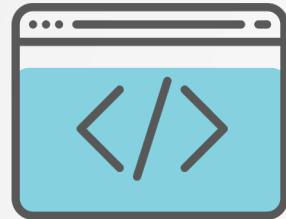
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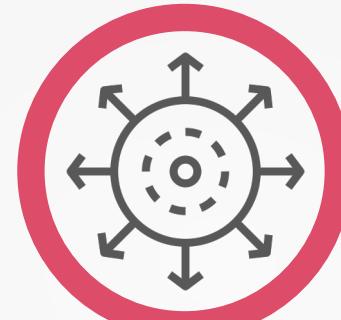
Additional Slides

This work

- Symbolic execution for analyzing semantic correctness



Code
Coverage



Scalability
Challenges



Domain
Knowledge

- Case study: Implementing PKCS#1 v1.5 signature verification
 - Flaws in TLS and crypto libraries, and IPSec software
 - Exploitable for **signature forgery** and **DoS** attacks



Bleichenbacher's low exponent attack

- $r' = 0x00 \parallel BT \parallel PB \parallel 0x00 \parallel AS \parallel GARBAGE$
- Assuming $e = 3$
- Construct $t = 00\ 01\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ 00 \parallel AS \parallel FF..FF$
 - if $(\text{floor}(\sqrt[3]{t}))^3$ match r' before **GARBAGE** then
 - **fake signature** $S' = \text{floor}(\sqrt[3]{t})$
 - if necessarily, tweak m to get a different **AS**, try again



Bleichenbacher's low exponent attack

- $r' = 0x00 \parallel BT \parallel PB \parallel 0x00 \parallel AS \parallel GARBAGE$
 - $= 00\ 01\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ 00 \parallel AS \parallel GARBAGE$
 - assuming $e = 3$, $|n| = 1024$ bits, $r' < 2^{1009}$
 - want to find S' s.t. $S'^3 = r'$
- construct $t = 00\ 01\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ 00 \parallel AS \parallel FF..FF$
 - if $(\text{floor}(\sqrt[3]{t}))^3$ match r' before GARBAGE then we're done
 - fake signature $S' = \text{floor}(\sqrt[3]{t})$
 - if necessarily, tweak m to get a different AS , try again

Bleichenbacher's low exponent attack

- $r' = 00\ 01\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ FF\ 00 \parallel AS \parallel \text{GARBAGE}$
 - assuming $e = 3$, $|n| = 1024$ bits, $r' < 2^{1009}$
 - want to find S' s.t. $S'^3 = r'$
 - distance between two consecutive perfect cubes:
 - $b^3 - (b - 1)^3 = 3b^2 - 3b + 1 < 3 \cdot 2^{673} - 3 \cdot 2^{337} + 1 < 2^{675} \quad (\because b^3 < 2^{1009})$
 - assuming $H() = \text{SHA-1}()$, max length of GARBAGE is:
 - $1024/8 - (2 + 8 + 1 + 35) = 82$ bytes = 656 bits
 - roughly 19 bits less than $b^3 - (b - 1)^3$, so around 2^{19} trials to find a working S'

Over-permissiveness in Openswan 2.6.50

- Use this r' :

```
/** all numbers below are hexadecimals */
00 01 GARBAGE 00 30 21 ... ... 04 16 SHA-1(m')
```
- Want: $(a + b)^3 = a^3 + 3a^2b + 3b^2a + b^3$
- Finding 'a' is similar to the original attack algorithm
- construct $t = 00 01 00 00 .. 00$
 - compute $\alpha = \text{ceil}(\sqrt[3]{t})$
 - sequentially find the largest 'c' s.t. $((\alpha / 2^c + 1) 2^c)^3$ match r' before GARBAGE
 - then $a = (\alpha / 2^c + 1) 2^c$
 - this is to make as many LSBs of 'a' zeros
 - to avoid overlapping terms

Over-permissiveness in Openswan 2.6.50

- Use this r' : $\text{/** all numbers below are hexadecimals **/}$
 $\boxed{00\ 01\ \text{GARBAGE}\ 00\ 30\ 21\ \dots\ \dots\ 04\ 16\ \text{SHA-1}(m')}$
- Want: $(a + b)^3 = \boxed{a^3 + 3a^2b + 3b^2a + b^3}$
- Finding ' b ' is a little more complex
- let $r_b = \boxed{00\ 30\ 21\ \dots\ \dots\ 04\ 16\ \text{SHA-1}(m')}$, and $n' = 2^{|r_b|}$
 - r_b can be considered as $(b^3 \bmod n')$
 - since n' is a power of 2, $\phi(n') = 2^{|r_b|-1}$
 - we can guarantee r_b and n' are coprime w/ an odd $\text{SHA-1}(m')$
 - use Extended Euclidean Algorithm to find f , s.t.
 - $ef = 1 \pmod{2^{|r_b|-1}}$
that is, f is the multiplicative inverse of $e \bmod \phi(n')$
 - finally $b = r_b^f \bmod n'$

Leniency in strongSwan 5.6.3

3. Accepting less than 8 bytes of padding

- Can be used to make the other attacks easier
 - Use no padding, gain more bytes for **GARBAGE**



Leniency in axTLS 2.1.3

2. Ignoring prefix bytes

```
i = 10;  
/* start at the first possible non-padded byte */  
while (block[i++] && i < sig_len);  
size = sig_len - i;  
/* get only the bit we want */  
if (size > 0) {... ...}
```

- First 10 bytes are not checked at all



Leniency in axTLS 2.1.3

2. Ignoring prefix bytes

- First 10 bytes directly skipped
- Make forgery easier, use this r' (first 90 bits are all zeros)

```
/** all numbers below are hexadecimals */
00 00 00 00 00 00 00 00 00 00
30 21 ... ... 04 16 SHA-1(m') GARBAGE
```

- Reduce the distance between two consecutive perfect cubes
 - Easier to find S'

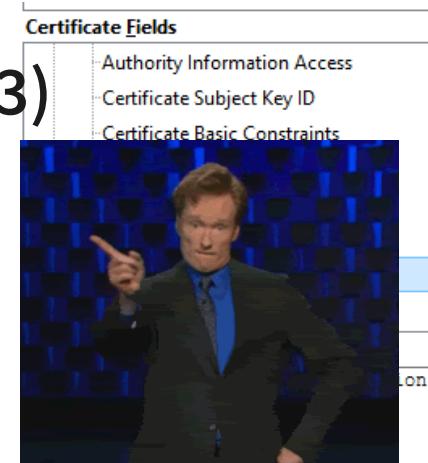


Leniency in axTLS 2.1.3

3. Ignoring AS.AlgorithmIdentifier (CVE-2018-16253)

- Just because $H()$ is known from outside
- Doesn't mean it does not need to be checked
- This can be exploit together with the previous 2 flaws
- Use this r'

```
/** all numbers below are hexadecimals */
00 00 00 00 00 00 00 00 00 00
30 00 30 00 04 H().size H(m') GARBAGE++
```
- shorten the AlgorithmIdentifier to allow more GARBAGE
- useful with shorter modulus and longer hashes



Leniency in axTLS 2.1.3

4. Trusting the declared ASN.1 DER lengths w/o sanity checks [CVE-2018-16149]

- DoS PoC: making z exceptionally large crashed the verifier
- Particularly damaging
 - axTLS does certificate chain validation bottom-up
 - even if no **small e** in the wild
 - any MITM can inject a fake certificate with $e = 3$
 - **crash verifier** before the whole chain is verified against some trusted root anchors



Leniency in MatrixSSL 3.9.1 (CRL)

1. Mishandling Algorithm OID

```
/** all numbers below are hexadecimals */
/* [AS.DigestInfo] */
30 w
/* [AlgorithmIdentifier] */
30 x
06 u 2B 0E 03 02 1A ← can take arbitrarily
05 y
/* [Digest] */
04 z
/* H(m), H()=SHA-1(), m = "hello world" */
2A AE 6C 35 C9 4F CF B4 15 DB
E9 5F 40 8B 9C E9 1E E8 46 ED
```

- Some bytes in the middle of AS can take any values
 - Depends on choice of H(), SHA-1: 5 bytes, SHA-256: 9 bytes
 - Doesn't seem to be numerous enough for practical attacks

Discussion

- Parsing is hard!
- What robustness means depends on the context
 - Parser robustness (e.g. handling malformed inputs) is bad for security-critical scenarios
- Better way: construction-based verification
 - Many libraries have code for signing
 - for verifiers, instead of parsing, compute $H(m)$, prepare AS and construct r_v
 - then see if $r_v == S^e \text{ mod } n$