

Lab4 Questions

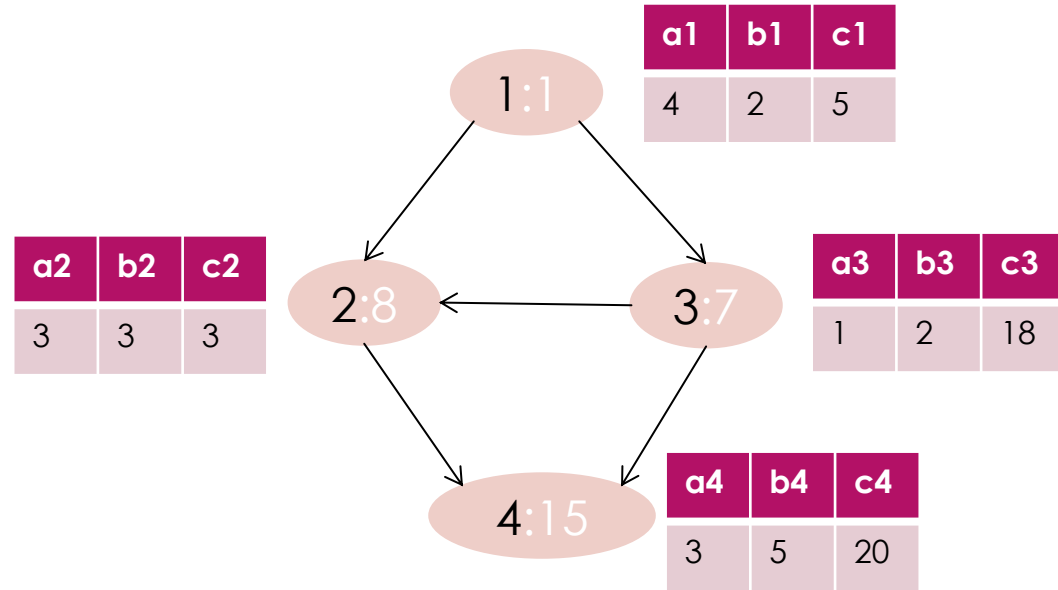
YAO ZHAO

Lab4.A: Brknight

- ▶ Recently Andrea is obsessed with a Roguelike game named Brknight.
- ▶ The map of Brknight can be seen as a directed acyclic graph (DAG) with N points and M edges, in which there exists one single starting point and multiple terminal points. A point is a terminal point iff Andrea can go nowhere from it.
- ▶ Andrea's squad is at point 1 (the starting point) and has Combat Effectiveness (CE) C initially. At point i , she would encounter a stage with dangerous level h_i , and if Andrea's CE is less than h_i , she would lose immediately. Otherwise, she would complete the stage successfully and can choose one reward among the three below:
 - ▶ Recruit an operator: Andrea's current CE would increase by a_i
 - ▶ Obtain a powerful collection: Andrea's current CE would multiply by b_i
 - ▶ Reset her squad: Andrea's current CE would become c_i
- ▶ After that, if this point is a terminal point, Andrea will fight against a BOSS. Otherwise, she would choose an edge from point i to another point j and move to j .
- ▶ If Andrea can make her way to the BOSS, tell her the maximum possible CE module $10^9 + 7$ when she fights the BOSS.

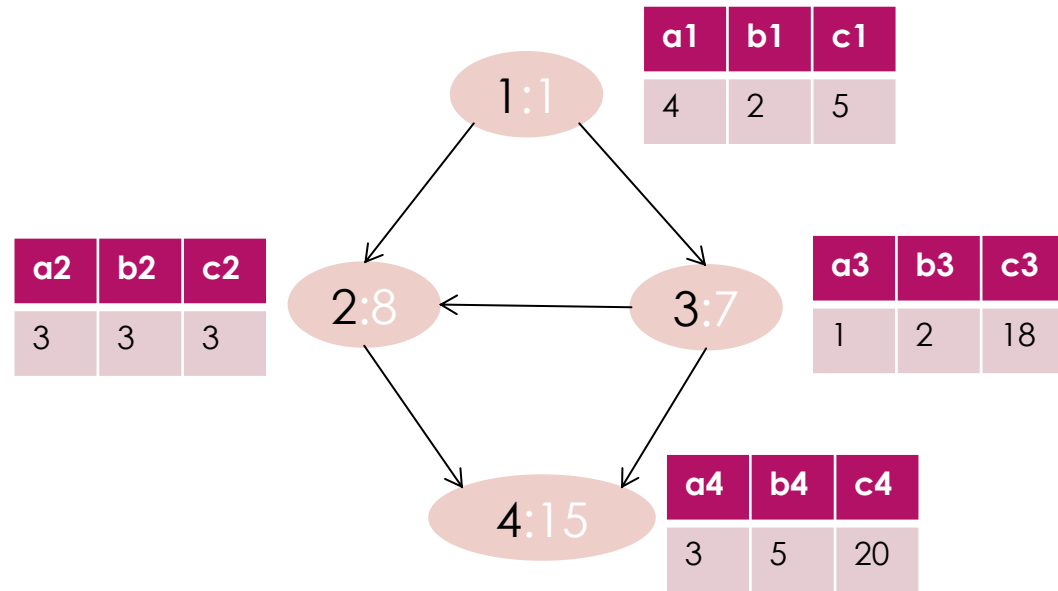
Sample Input

4 5 3
1 4 2 5
8 3 3 3
7 1 2 18
15 3 5 20
1 2
2 4
1 3
3 2
3 4



Sample Input

4 5 3
1 4 2 5
8 3 3 3
7 1 2 18
15 3 5 20
1 2
2 4
1 3
3 2
3 4



Initial $c = 3$

Point 1: $c \geq h_1$
 $c=3 \rightarrow c=3+a_1=7$

Move to Point 3: $c \geq h_3$
 $c=7 \rightarrow c=c_3=18$

Move to Point 2: $c \geq h_2$
 $c=18 \rightarrow c=18*b_2=54$

Move to Point 4: $c \geq h_4$
 $c=54 \rightarrow c=54*b_4=270$



Sample Output 1

270

Lab4.B: Precarious Computing

- ▶ Sky has N expendable computers $1, 2, \dots, N$ lining up from left to right.
- ▶ The i^{th} computer can only be powered up for a_i seconds and generates b_i income per second when powered. If the total workload exceeds a_i seconds, the computer will blow up Sky's bedroom. It is guaranteed that a_i is unique.
- ▶ Sky has a special cable. He can only power up a consecutive interval of computers at a time. Sky can change the powered interval at anytime.
- ▶ Unfortunately, the cable is also expendable and can only function for M seconds. How much income can Sky obtain if he operates optimally? Sky does not want any splendid explosion since he still needs the bedroom to sleep.

Sample Input 1

5 3
1 3 5 2 4
3 5 5 3 1

1 3 5 2 4
3 5 5 3 1

1s, computer 1..5 income:17

0 2 4 1 3
3 5 5 3 1

1s, computer 2..5 income:14

0 2 4 1 3
3 5 5 3 1

1s, computer 2..3 income:10

0 1 3 0 2
3 5 5 3 1

Total: 41

Sample Output 1
41

Sample Input 2

10 30

44 32 6 1 7 18 27 21 40 48

97 39 32 23 18 32 34 34 21 5

44 32 6 1 7 18 27 21 40 48

97 39 32 23 18 32 34 34 21 5

1s, computer 1..10, income:335

43 31 5 0 6 17 26 20 39 47

97 39 32 23 18 32 34 34 21 5

5s, computer 1..3, income:168*5

38 26 0 0 6 17 26 20 39 47

97 39 32 23 **18 32 34 34 21 5**

6s, computer 5..10, income:144*6

38 26 0 0 0 11 20 14 33 41

97 39 32 23 18 32 34 34 21 5

18s, computer 1..2, income:136*18

20 8 0 0 0 11 20 14 33 41

97 39 32 23 18 32 34 34 21 5

$1s + 5s + 6s + 18s = 30s$

Total income: 4487

Sample Output 2
4487

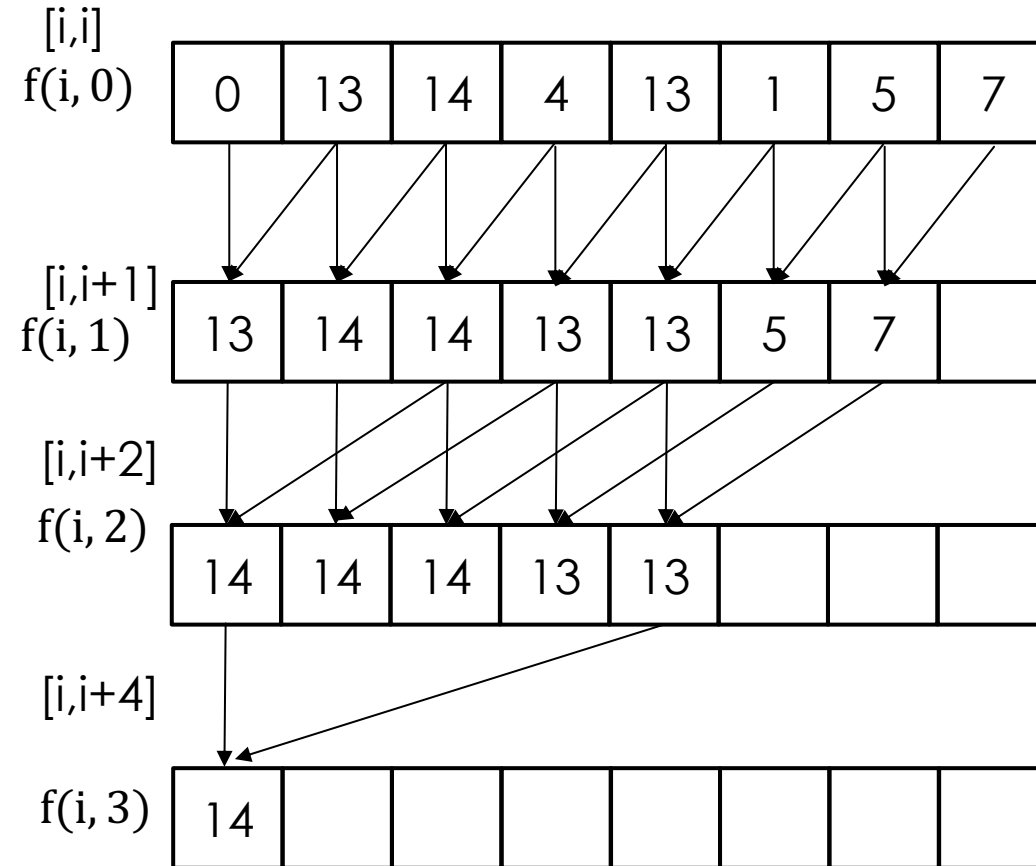
ST table

Data:

0	13	14	4	13	1	5	7
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Creating ST table:

$$\log_2 8 = 3$$



Query:

Data:

0	13	14	4	13	1	5	7
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Maximum Query:

Range: [2,7]

$$S = \lfloor \log_2(7 - 2 + 1) \rfloor = 2$$

$$L = 2, \text{index1} = 2$$

$$R = 7, \text{index2} = 7 - 2^2 + 1 = 4$$

$$\text{Max}(14, 13) = \mathbf{14}$$

