

§ 8.1

1. 设电阻值为  $X$  ( $\Omega$ ), 则  $X \sim N(2.64, 0.06^2)$ , 样本容量  $n=36$ , 均值  $\bar{X}=2.61$ ,  $\alpha=0.01$

假设  $H_0: \mu = \mu_0 = 2.64$ ,  $H_1: \mu \neq \mu_0$ .

$$\frac{\bar{X} - \mu}{\sigma/\sqrt{n}} \sim N(0, 1)$$

$$H_0 \text{ 的拒绝域: } \left\{ \frac{|\bar{X} - \mu_0|}{\sigma/\sqrt{n}} > u_{1-\frac{\alpha}{2}} \right\}$$

$$\therefore \frac{|\bar{X} - \mu_0|}{\sigma/\sqrt{n}} \approx 3 > u_{1-\frac{\alpha}{2}} = 2.575$$

$\therefore$  拒绝  $H_0$

$\therefore$  有显著性影响.

2.  $X \sim N(\mu, \sigma^2)$ ,  $\sigma=40$ ,  $n=9$ ,  $\bar{X}=\mu+20$ ,  $\alpha=0.01$

假设  $H_0: \mu \leq \mu_0$ ,  $H_1: \mu > \mu_0$ .

$$\therefore \frac{\bar{X} - \mu}{\sigma/\sqrt{n}} \sim N(0, 1)$$

$$\therefore H_0 \text{ 的拒绝域为 } \left\{ \frac{|\bar{X} - \mu_0|}{\sigma/\sqrt{n}} > u_{1-\frac{\alpha}{2}} \right\}$$

$$\therefore \frac{|\bar{X} - \mu_0|}{\sigma/\sqrt{n}} \approx 1.5 < u_{1-\frac{\alpha}{2}} = 2.575$$

$\therefore$  接受  $H_0$

$\therefore$  无显著提高.

3.