





Generate Admissible Heuriscics O from Relaxed Problems For 8-puzzle problem: • Real Rule: A tile can only move to the adjacent empty square. • Relaxed rules: h_{mis} and h_{1stp} are admissible • R1: A tile can move **anywhere** $\Rightarrow h_{mis}(s) = \#(\text{misplaced titles}).$ • R2: A tile can move one step in any direction regardless of an occupied neighbour $\Rightarrow h_{1stp}(s) = \#(1\text{-step move})$ to reach goal. · Optimal solutions to problems with R1, R2 are easier to find. Relaxed Problem • Relaxed problem: a problem with relaxed rules on the action. • E.g. 8-puzzle problems with R1 and R2. • Theorem: The cost of an optimal solution to a relaxed problem is an admissible heuristic for the original problem. • No wonder h_{mis} and h_{1stp} are admissible. 2 from sub-problems Subproblem • Task: get tiles 1, 2, 3 and 4 into their correct positions. • Relaxation: move them disregarding the others. Theory: cost*(subproblem)<cost*(original). • cost*(subproblem): the cost of the optimal solution of this subproblem. Subproblem and Addmissible Heuristics • Admissible $h_{sub}^*(s)$: estimate the cost from s to the subproblem • E.g. $h_{sub}^{(1,2,3,4)}$ is the cost to solve the 1-2-3-4 subproblem. • Theorem: $h_{sub}(s)$ dominates $h_{1stp}(s)$, • $h_{sub}(s) = max\{h_{sub}^{(1,2,3,4)}(s), h_{sub}^{(2,3,4,5)}(s), \cdots\}$ Disjoint Subproblems • Question: Will the addition of heuristics from subproblem (1-2-3-4) and (5-6-7-8) give an admissible heuristic, considering the two subproblems are not overlapped? Answer: No, since they always share some moves. • Question: What if not count those shared moves? • Answer: $h_{sub}^{(1,2,3,4)}(s) + h_{sub}^{(5,6,7,8)}(s) \le c^*(s) \Rightarrow \text{admissible}.$ Disjoint pattern database For 8-puzzle problem: • Solve many 8-puzzles to obtain many examples. • Each example consists of a state from the solution path and the actual cost of the solution from that point. • These examples are our 'experience' for this problem. • Question: How to learn h(s) from these experience?

