

# The Theory of Computation

(Guidance)

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# CS327: The Theory of Computation (ToC)

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  - ◆ Answering class (optional): Will be announced.
- ♣ **QQ group**
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5/25/22

2

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# The Theory of Computation: What Is It and Why Study It?

- ♣ **The Theory of Computation (ToC): What is it?**
  - ◆ The ToC studies the nature of computation and various properties of computation.
  - ◆ It is the core theoretical foundation of Computer Science (CS), Intelligent Science (IS), and Artificial Intelligence (AI).
- ♣ **The Theory of Computation (ToC): Why study it?**
  - ◆ The ToC will let you know:
    - ◆ What can and cannot be computed in principle.
    - ◆ The computational time complexity, the computational space complexity, and the classification of computational difficulty.
  - ◆ You cannot be regarded as a professional in any area of CS, IS, and AI, if you have not studied the ToC.

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# The World of Computability and Complexity [SEP]

Arithmetic Hierarchy					
RE		FON(N)		E <sub>n</sub> -complete	
co-RE		FO(N)		E <sub>n</sub> , FO(N)	
Recursive					
Primitive Recursive					
				EXPTIME	
PSPACE		SO( $2^{poly(n)}$ )		PSPACE	
QST		PSPACE-complete			
FO( $2^{poly(n)}$ )		FO(PFP)		SOTC	
		SO		SO( $a^{poly(n)}$ )	
TIME Hierarchy					
co-NP-complete		SAT		NP-complete SAT	
co-NP		SOH		NP	
		NP ∩ co-NP		SOH	
FO( $a^{poly(n)}$ )		SAT		P-complete	
FO(LFP)		SO(Horn)		P	
FO(log n) <sup>[90]</sup>				NC	
FO(log n)				AC <sup>1</sup>	
FO(CFL)				sAC <sup>1</sup>	
FO(TC)		SO(Krom)		NL	
FO(DTC)		L		NL	
FO(REGULAR)		L <sub>LOCAL</sub>		L <sub>comp</sub>	
FO(COUNT)				TC <sup>(1)</sup>	
LOGTIME Hierarchy					
FC				AC <sup>0</sup>	

The World of Computability and Complexity

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4

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# Inclusion Relationships among Major Complexity Classes [SEP]

FIGURE 2. Inclusion relationships among major complexity classes. The only depicted inclusions which are currently known to be proper are  $L \subsetneq PSPACE$  and  $P \subsetneq EXP$ .

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5

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# CS327: The Theory of Computation


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- ◆ **Guidance**
- ◆ Enumerability and Diagonalization
- ◆ Finite Automata and Regular Languages
- ◆ Context-Free Languages
- ◆ Computation: Turing Machines
- ◆ Computation: Turing-Computability (Turing-Decidability)
- ◆ Computation: Reducibility (Turing-Reducibility)
- ◆ Computation: Recursive Functions
- ◆ Computation: Recursive Sets and Relations
- ◆ Equivalent Definitions of Computability
- ◆ Advanced Topics in Computability Theory
- ◆ Computational Complexity
- ◆ Time Complexity
- ◆ Space Complexity
- ◆ Intractability
- ◆ Advanced Topics in Complexity Theory

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6

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### Major Text Books

- ◆ M. Sipser, “Introduction to the Theory of Computation,” Cengage Learning, 2013 (3rd Edition).
- ◆ G. S. Boolos, J. P. Burgess, and R. C. Jeffrey, “Computability and Logic,” Cambridge University Press, 2007 (5th Edition).
- ◆ P. Linz, “An Introduction to Formal Languages and Automata,” Jones & Bartlett Learning, 2017 (6th Edition).

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7

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### Other Text and Reference Books

- ◆ R. Weber, “Computability Theory,” AMS, 2012. [W-12]
- ◆ C. Tourlakis, “Theory of Computation,” Wiley, 2012. [T-12]
- ◆ J. C. Martin, “Introduction to Languages and the Theory of Computation,” McGraw-Hill, 2011 (4th Edition). [M-11]
- ◆ S. Homer and A. L. Selman, “Computability and Complexity Theory,” Springer, 2011 (2nd Edition). [HS-11]
- ◆ C. Moore and S. Mertens, “The Nature of Computation,” Oxford University Press, 2011. [MM-11]
- ◆ M. Fernandez, “Models of Computation – An Introduction to Computability Theory,” Springer, 2009. [F-09]
- ◆ O. Goldreich, “Computational Complexity – A Conceptual Perspective,” Cambridge University Press, 2008. [G-08]
- ◆ J. R. Hindley and J. P. Seldin, “Lambda-Calculus and Combinators, An Introduction,” Cambridge University Press, 2008. [HS-08]
- ◆ J. E. Hopcroft, R. Motwani, and J. D. Ullman, “Introduction to Automata Theory, Languages, and Computation,” Pearson Education, 2007 (3rd Edition). [HMU-07]

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8

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### Other Text and Reference Books

- ◆ H. R. Lewis and C. H. Papadimitriou, “Elements of the Theory of Computation,” Prentice-Hall, 1998 (2nd Edition). [LP-98]
- ◆ D. S. Bridges, “Computability – A Mathematical Sketchbook,” Springer, 1994. [B-94]
- ◆ C. H. Papadimitriou, “Computational Complexity,” Addison-Wesley, 1994. [P-94]
- ◆ P. Odifreddi, “Classical Recursion Theory – The Theory of Functions and Sets of Natural Numbers,” Elsevier, 1992. [O-92]
- ◆ N. Cutland, “Computability – An Introduction to Recursive Function Theory,” Cambridge University Press, 1980. [C-80]
- ◆ M. R. Garey and D. S. Johnson, “Computers and Intractability – A Guide to the Theory of NP-Completeness,” 1979. [GJ-79]
- ◆ M. Davis, “Computability and Unsolvability,” McGraw-Hill, 1958. [D-58]
- ◆ T. H. Cormen, C. E. Leiserson, R. L. Rivest, and C. Stein, “Introduction to Algorithms,” 2009 (3rd Edition). [CLRS-12A-09]
- ◆ M. Davis, “Engines of Logic: Mathematicians and the Origin of the Computer,” Norton, 2000. [D-EoL-00]

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9

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### CS327: The Theory of Computation

#### ♣ Pre-requisites

- ◆ CS101(A/B): Introduction to Computer Science (A/B)
- ◆ CS104/CS108: Introduction to Mathematical Logic
- ◆ Those students who haven’t learned the naive Set Theory and Mathematical Logic should learn them by themselves in advance.

#### ♣ Notes

- ◆ Because of time limit, I do not answer any question about the naive Set Theory and Mathematical Logic in classes and QQ group.
- ◆ My courseware for the naive Set Theory and Mathematical Logic (and some other reading material) can be found in QQ group.

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10

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### My Hope/Statement and Your Attitude

#### ♣ My hope/statement

- ◆ I really like to teach and guide you to become world-class scientists and/or engineers in the future, by laying a good foundation for you.

#### ♣ Your attitude

- ◆ (I want you) to listen carefully, think deeply, ask questions actively, and read text books and reference materials carefully.

#### ♣ “青出于蓝而胜于蓝”

- ◆ “青，取之于蓝，而胜于蓝；冰，水为之，而寒于水。”  
– 荀子，“劝学”，约公元前230年
- ◆ 我将把你们视为清华的学生来教授你们知识和能力(但是按照南科大要求)；期待着你们 “青出于蓝而胜于蓝”。

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11

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### My Teaching Style

#### ♣ For important notions/concepts

- ◆ What is it?
- ◆ Why study it?

#### ♣ For important assumptions and/or principles

- ◆ Why ToC needs it?
- ◆ Why it is fundamental? / What is underlain by it?

#### ♣ For important problems

- ◆ What is its background?
- ◆ Why it is interesting?

#### ♣ Using QQ group

- ◆ Send various advices/materials/notices to you, and answer your questions.

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12

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### Some Rules You Should Follow

#### ♣ Preview

- ◆ I will distribute my courseware and some reading materials at least one week before class every week.
- ◆ You should preview my courseware and the reading materials before class every week.
- ◆ Note: It is very difficult to understand all the teaching contents at once just listening in class !!!

#### ♣ Ask questions in class but not break time

- ◆ I will give you time to ask questions in class.
- ◆ You should ask questions in class, but not break time, because my answers in class are beneficial to all students.

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13

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### Assessment Grading

#### ♣ Homework (50% of final score, 100/130 points)

- ◆ Answer questions, read materials, and submit reports
- ◆ You can (should!) get full points (100) if you do homework hard, and I will let you pass this course if you get full points of homework.
- ◆ Note: **The amount of homework is large !!!**

#### ♣ Final examination (50% of final score, 100/120 points)

- ◆ Open-book examination
- ◆ **Do not consider that the open-book examination is easy !!!**
- ◆ Only those students who have studied and reviewed the course contents very seriously can get full points (100).

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14

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- ◆ Enumerability and Diagonalization
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- ◆ Context-Free Languages
- ◆ Computation: Turing Machines
- ◆ Computation: Turing-Computability (Turing-Decidability)
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15

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