



CSE5014 CRYPTOGRAPHY AND NETWORK SECURITY

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Stream ciphers

- As we defined, PRGs are *limited*
 - They have fixed-length output
 - They produce output in “one shot”
- In practice, PRGs are based on *stream ciphers*
 - Can be viewed as producing an “infinite” stream of pseudorandom bits, on demand
 - More flexible, more efficient

Stream ciphers

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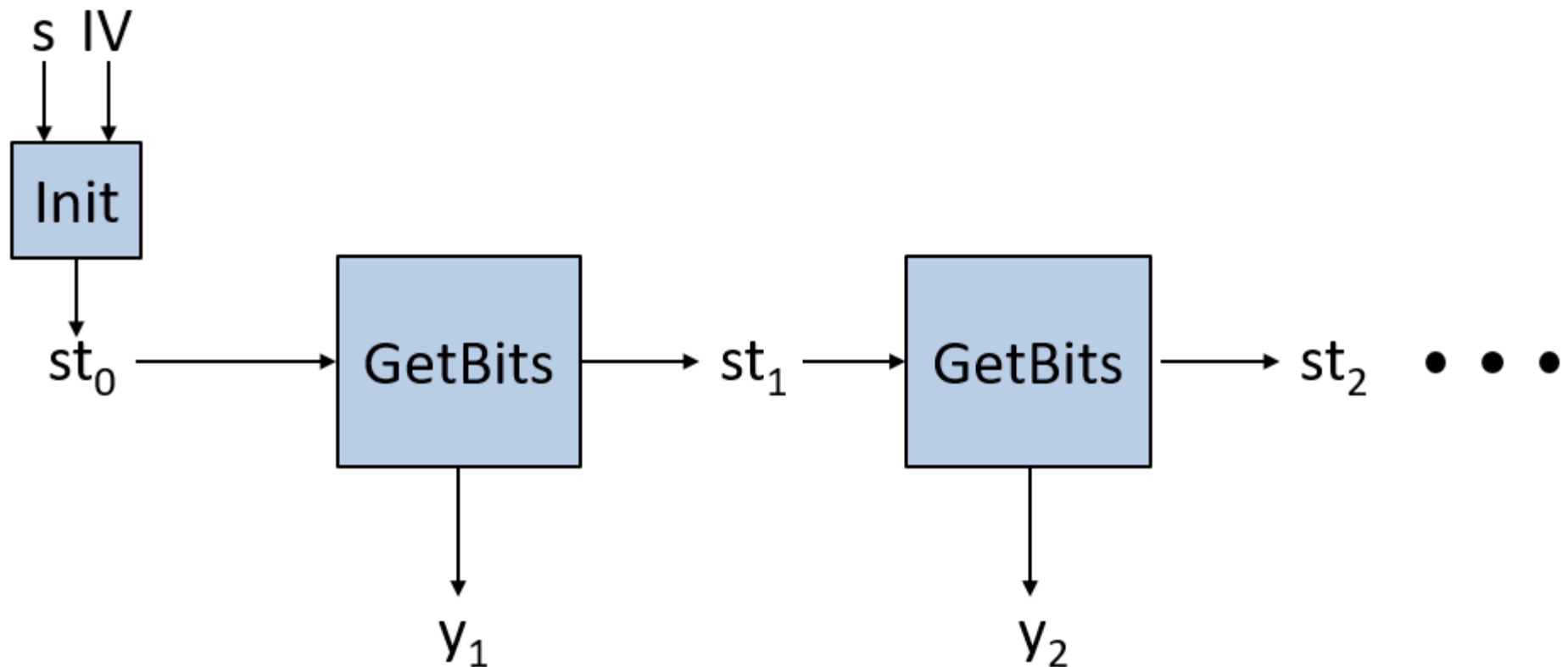
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 - In practice, y would be a block rather than a bit



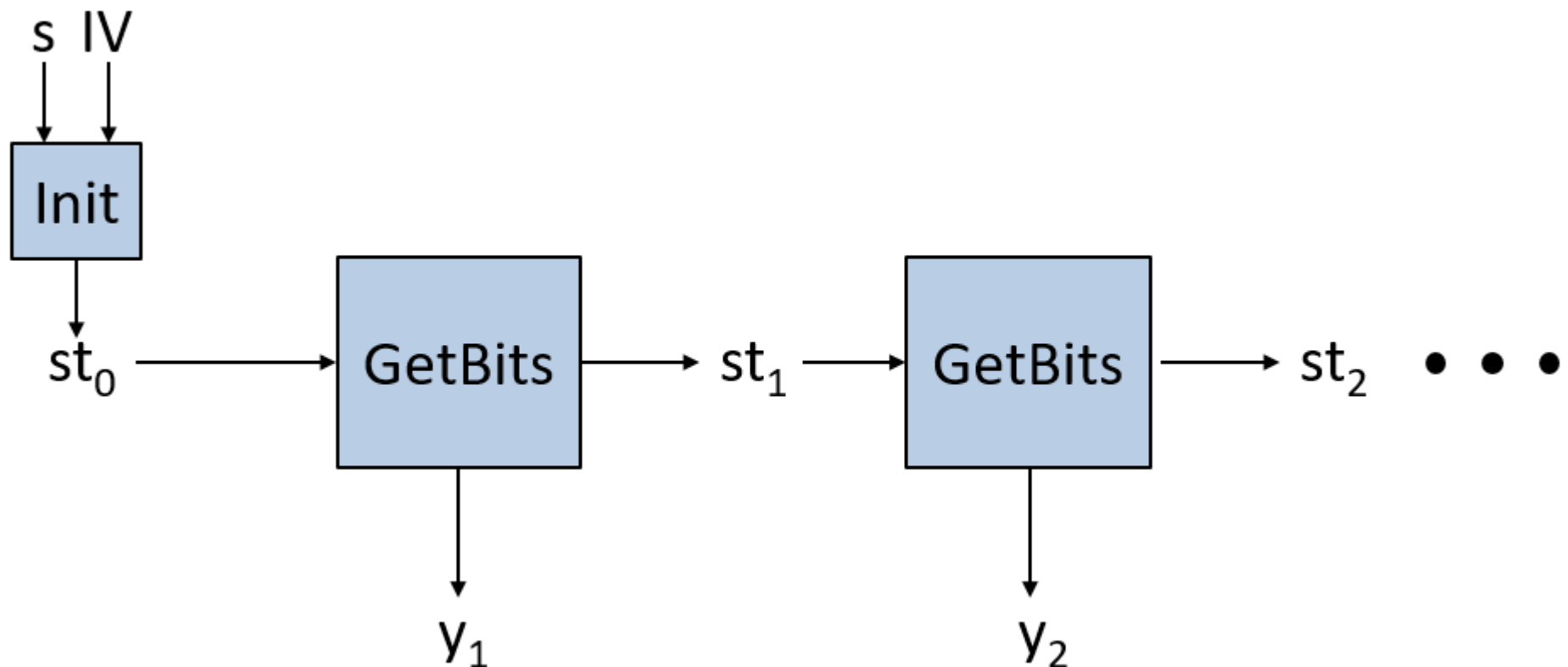
Stream ciphers

- Can use (**Init**, **GetBits**) to generate **any** desired number of output bits from an initial seed



Stream ciphers

- A *stream cipher* is *secure* (*informally*) if the output stream generated from a uniform seed is *pseudorandom*
 - I.e., regardless of how long the output stream is (so long as it is polynomial)



Modes of operation

- Stream-cipher modes of operation
 - Synchronized
 - Unsynchronized

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 - Sender and receiver maintain state (they are *stateful*), and must be *synchronized*

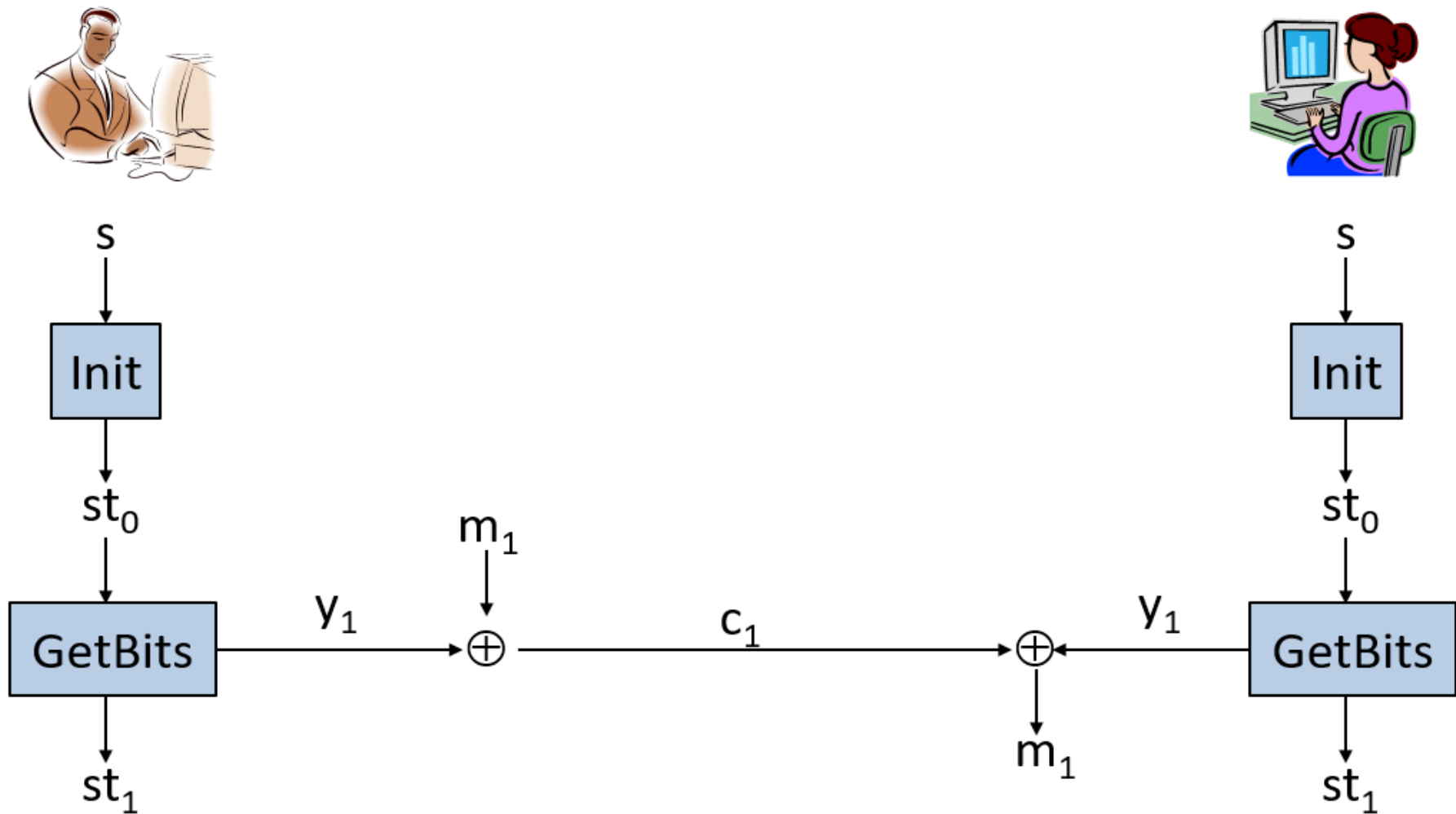


Modes of operation

- Stream-cipher modes of operation
 - Synchronized
 - Unsynchronized
- Synchronized mode
 - Sender and receiver maintain state (they are *stateful*), and must be *synchronized*
 - Makes sense in the context of a *limited-time* communication session where messages are received *in order*, without being lost



Synchronized mode



Unsynchronized mode

- Choose **random IV** to encrypt next message

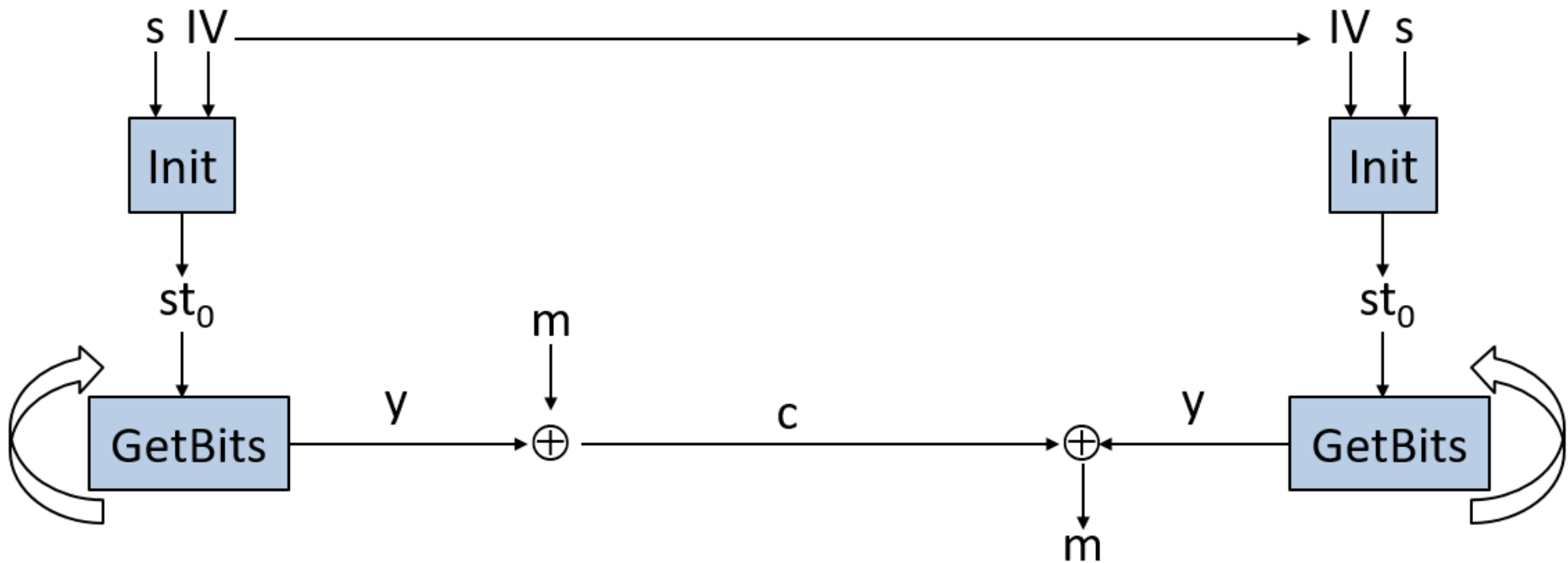
Unsynchronized mode

- Choose **random IV** to encrypt next message
- Similar to the first CPA-secure scheme we have seen
 - But “natively” handles **arbitrary-length** messages with better ciphertext expansion



Unsynchronized mode

- Choose **random IV** to encrypt next message



Unsynchronized mode

- Note that for security, we require the stream cipher to be a *PRF*
 - I.e., for fixed seed s , the output of the stream cipher when using *different IVs* should all look *uniform* and *independent*
 - The ciphertext $\langle IV, G_\infty(s, IV, 1^{|m|}) \oplus m \rangle$
 $F_k(IV) := G_\infty(k, IV, 1^\ell)$ is a *PRF*



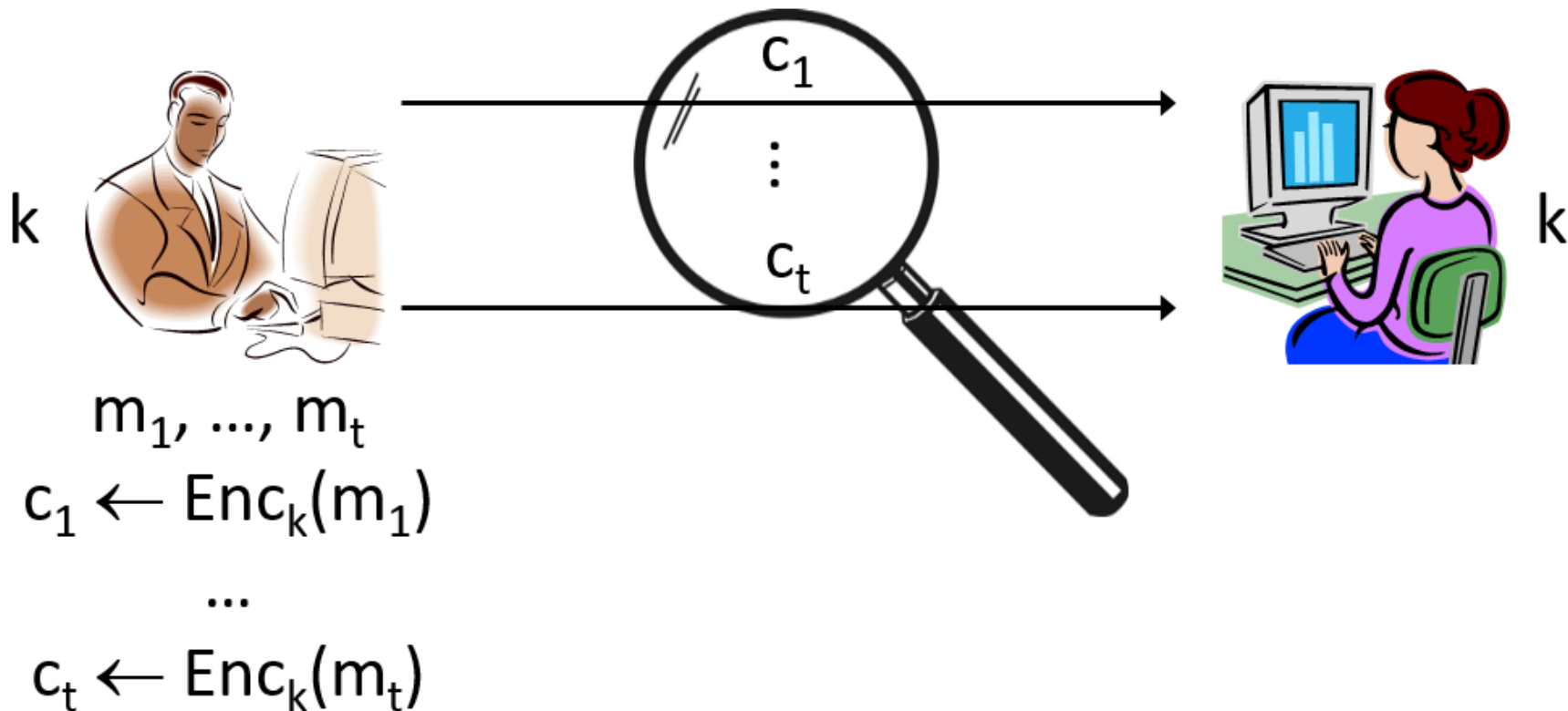
Passive & active attack

- So far, we have been assuming **only** a *passive, eavesdropping* attacker
 - Even if it can carry out *chosen-plaintext attacks* (CPA)



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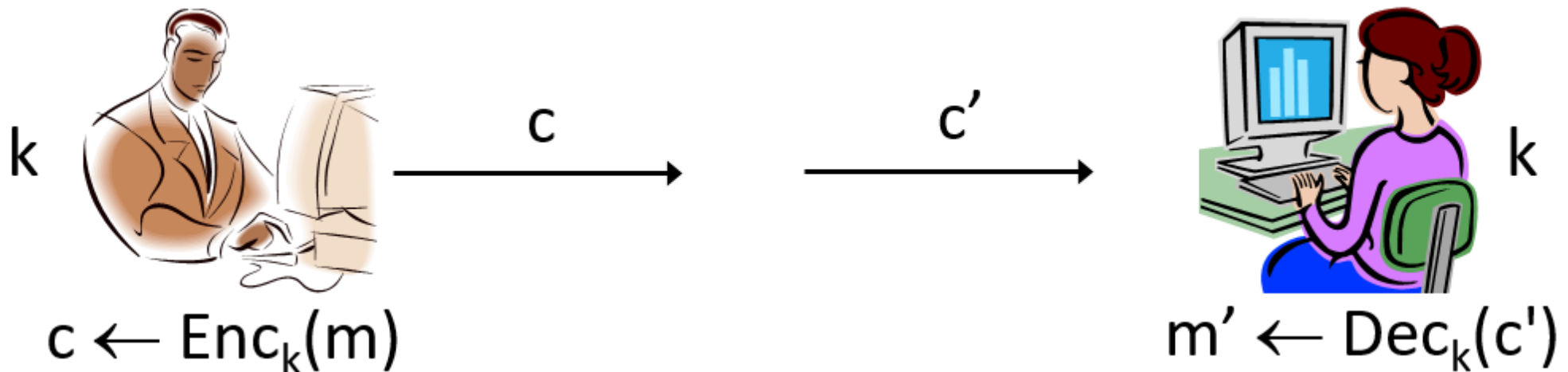
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Malleability

- (Informal): A scheme is *malleable* if it is possible to modify a ciphertext and thereby cause a *predictable* change to the plaintext

Malleability

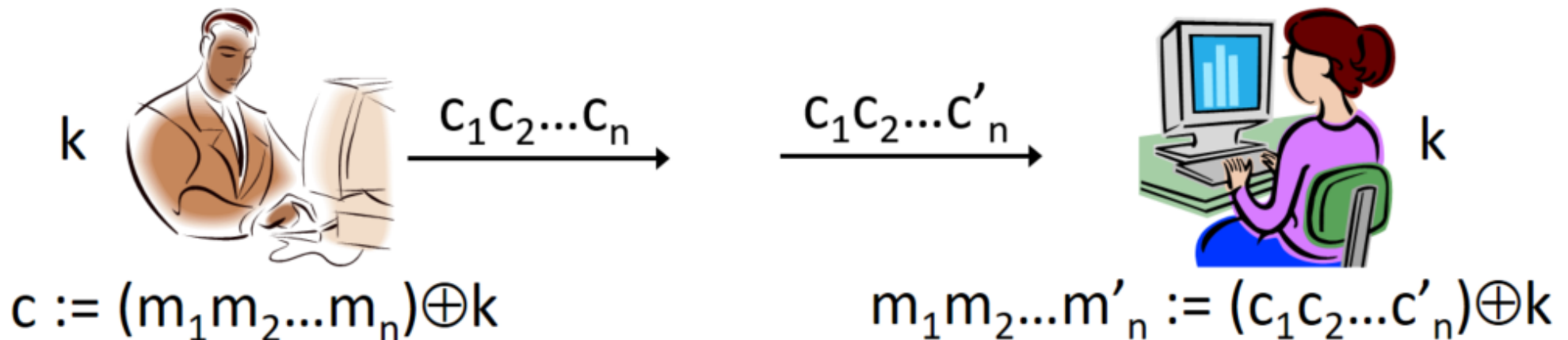
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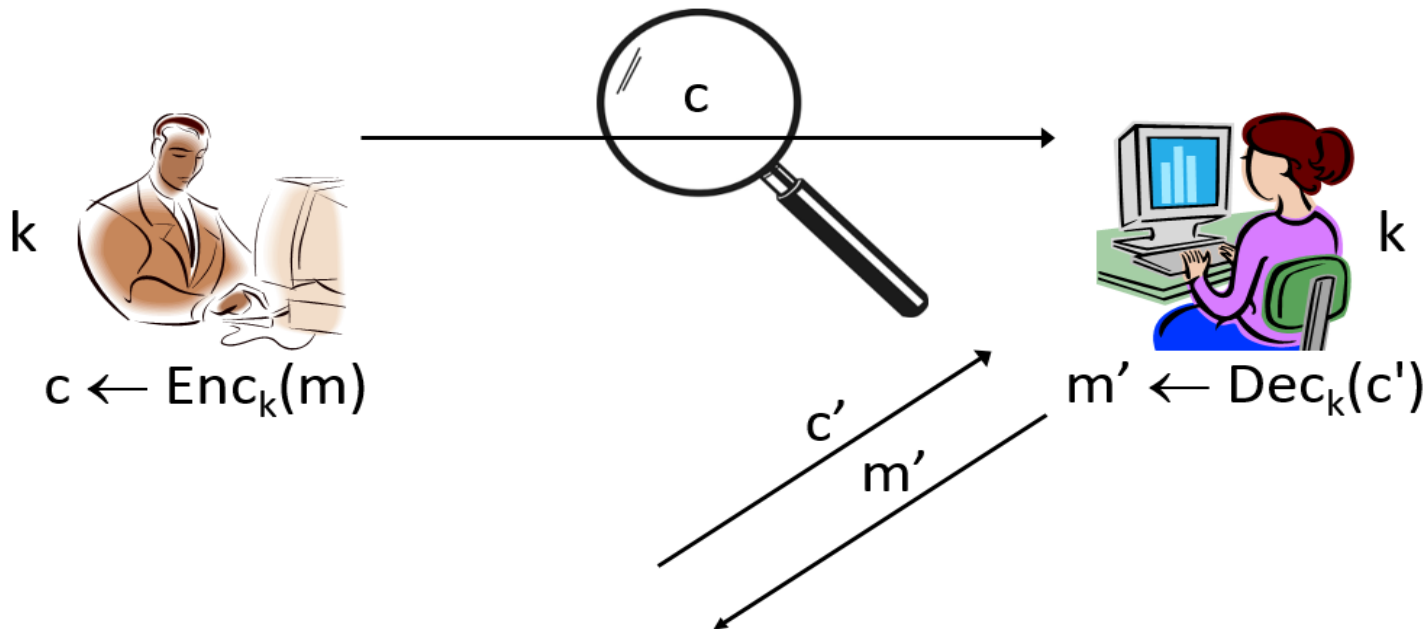
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Chosen-ciphertext attacks

- Models settings in which the attacker can **influence** what gets *decrypted*, and observe the effects
 - How to model?



Chosen-ciphertext attacks

- Models settings in which the attacker can **influence** what gets *decrypted*, and observe the effects
 - How to model?
- Allow attackers to submit ciphertexts of its choice (with **one restriction**) to the receiver, and learn the corresponding plaintext
 - In addition to being able to carry out a *chosen-plaintext attack*



CCA-security

- Define a randomized experiment $\text{PrivCCA}_{A,\Pi}(n)$:
 1. $k \leftarrow \text{Gen}(1^n)$
 2. $A(1^n)$ **interacts** with an *encryption oracle* $\text{Enc}_k(\cdot)$, and a *decryption oracle* $\text{Dec}_k(\cdot)$, and then outputs m_0, m_1 of the same length
 3. $b \leftarrow \{0, 1\}$, $c \leftarrow \text{Enc}_k(m_b)$, give c to A
 4. A can **continue** to interact with $\text{Enc}_k(\cdot)$, $\text{Dec}_k(\cdot)$,
but may **not** request decryption of c
 5. A outputs b' ; A succeeds if $b = b'$, and experiment evaluates to 1 in this case



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Definition 6.1 Π is *secure against chosen-ciphertext attacks (CCA-secure)* if for **all PPT** attackers A , there is a *negligible* function ϵ such that

$$\Pr[\text{PrivCCA}_{A,\Pi}(n) = 1] \leq 1/2 + \epsilon(n)$$



Chosen-ciphertext attacks and malleability

- If a scheme is *malleable*, then it cannot be *CCA-secure*
 - Modify c , submit the modified ciphertext c' to the decryption oracle and determine original message based on the result



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- *CCA-security* implies *non-malleability*

$Gen(1^n)$: choose a uniform key $k \in \{0, 1\}^n$

$Enc_k(m)$, for $|m| = |k|$

- Choose **uniform** $r \in \{0, 1\}^n$ (*nonce/ initialization vector*)

- Output ciphertext $\langle r, F_k(r) \oplus m \rangle$

$Dec_k(c_1, c_2)$: output $c_2 \oplus F_k(c_1)$

Theorem 5.1 If F is a pseudorandom function, then this scheme is *CPA-secure*.



CCA-security

- In the definition of *CCA-security*, the attacker can obtain the **decryption** of any ciphertext of its choice (besides the challenge ciphertext)
 - Is this realistic?

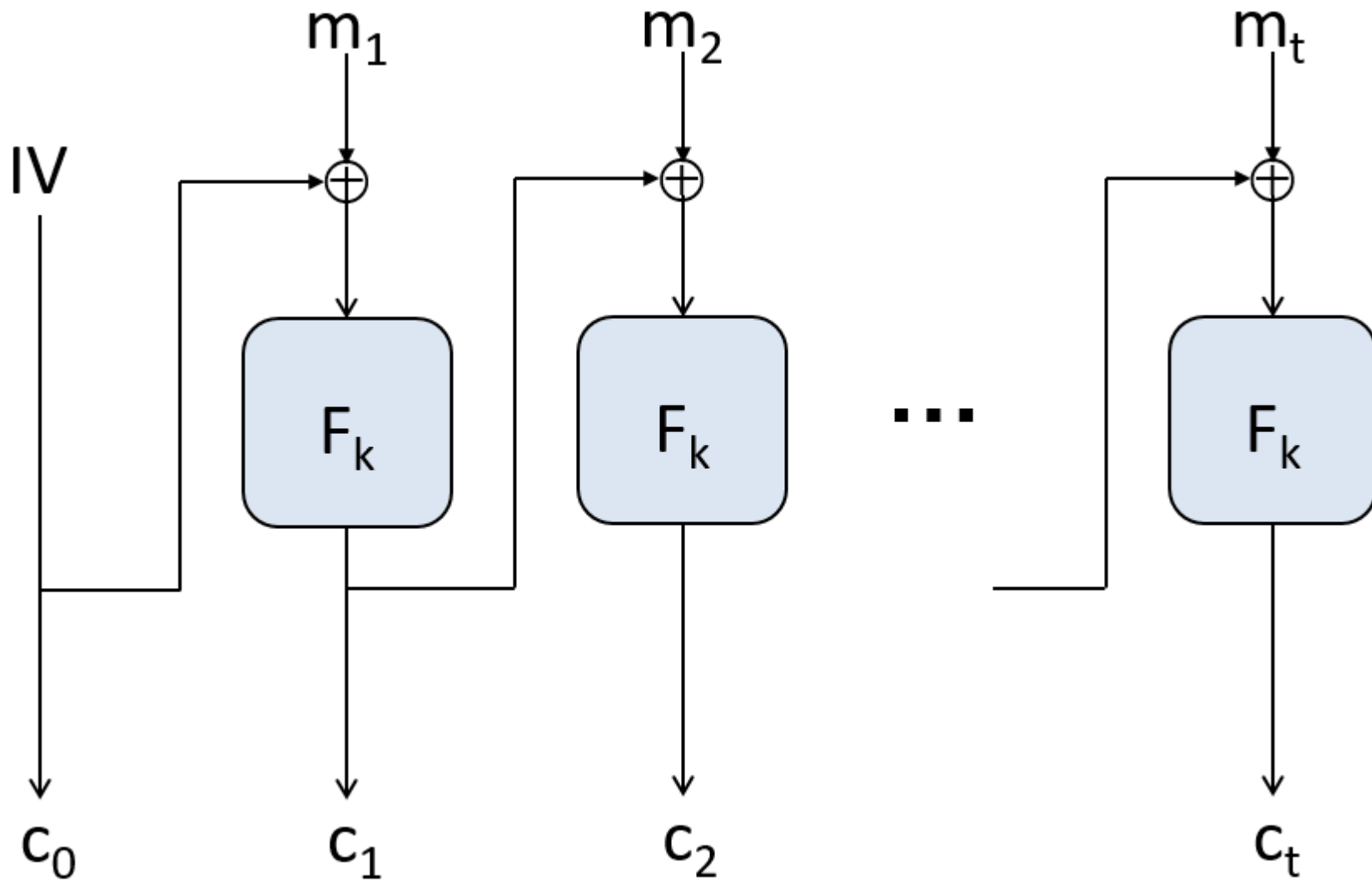


CCA-security

- In the definition of *CCA-security*, the attacker can obtain the **decryption** of any ciphertext of its choice (besides the challenge ciphertext)
 - Is this realistic?
- We show a scenario where:
 - *One bit* about decrypted ciphertexts is leaked
 - The scenario occurs in the real world!
 - This can be exploited to learn the **entire** plaintext



CBC mode



Arbitrary-length messages

- Message \rightarrow encoded data \rightarrow ciphertext

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- Message \rightarrow encoded data \rightarrow ciphertext
- PKCS #5 encoding:
 - Assume message is an integral # of bytes
 - Let L be the block length (in bytes) of the cipher
 - Let $b \geq 1$ be # of bytes that need to be appended to the message to get length a multiple of L
 - $1 \leq b \leq L$; note $b \neq 0$
 - Append b (encoded in 1 byte), b times
 - I.e., if 3 bytes of padding are needed, append 0x030303



Decryption?

- To Decrypt:
 - Use **CBC-mode** decryption to obtain encoded data
 - Say, the final byte of encoded data has value b



Decryption?

- To Decrypt:
 - Use **CBC-mode** decryption to obtain encoded data
 - Say, the final byte of encoded data has value b
 - If $b = 0$ or $b > L$, return “error”
 - If final b bytes of encoded data are not all equal to b , return “error”
 - Otherwise, strip off the final b bytes of the encoded data, and output what remains as the message

Example ($L = 8$)

<i>AB</i>	01	4 <i>F</i>	21	00	7 <i>C</i>
-----------	----	------------	----	----	------------

Example ($L = 8$)

<i>AB</i>	01	4 <i>F</i>	21	00	7 <i>C</i>	02	02
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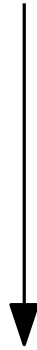
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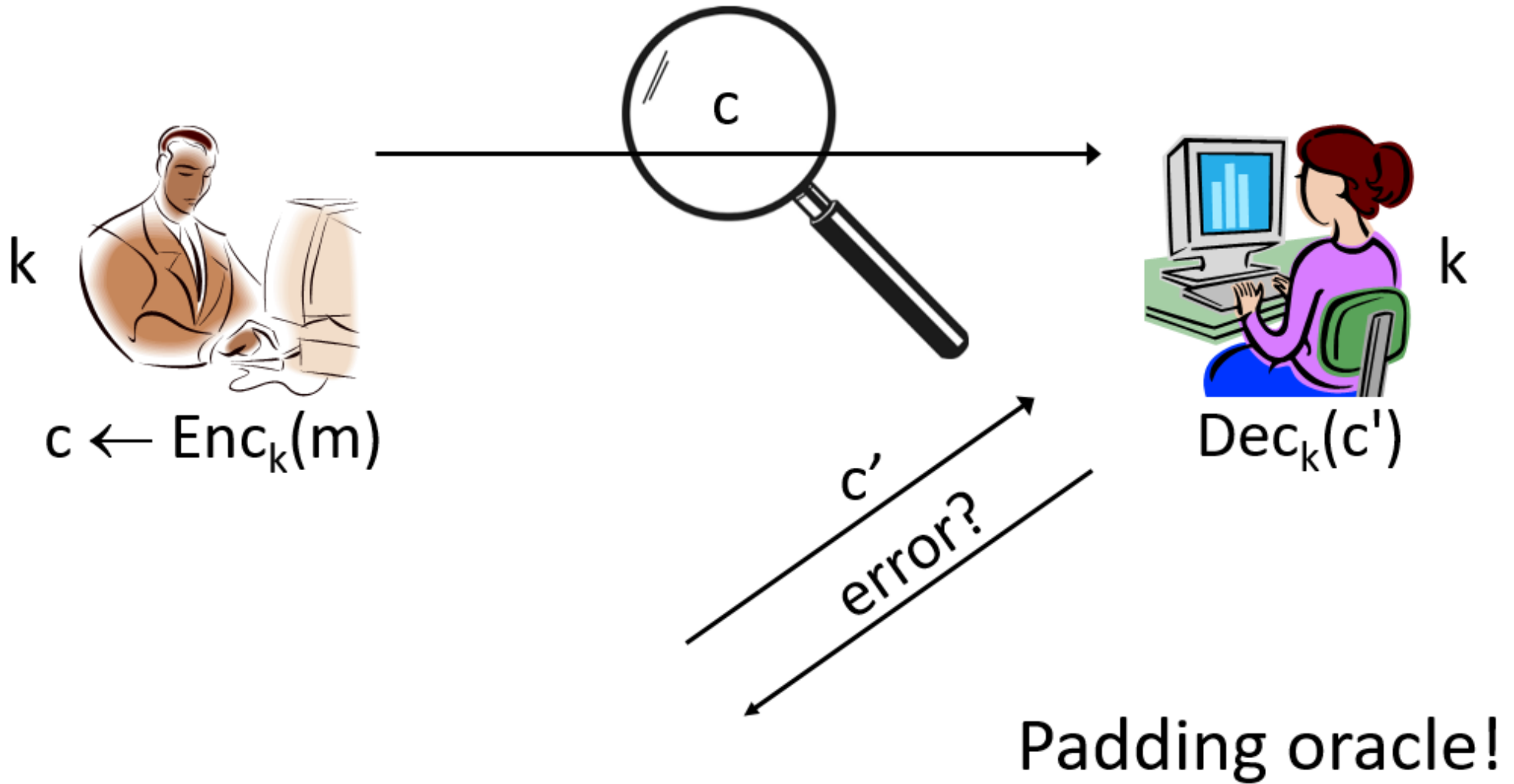
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Padding oracles



Padding oracles

- Padding oracles are frequently present in, e.g., web applications
- Even if an error is not explicitly returned, an attacker might be able to detect differences in timing, behavior, etc.



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- Main idea of the attack
 - Consider a two-block ciphertext IV, c
 - Encoded data = $F_k^{-1}(c) \oplus IV$



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- Main idea of the attack
 - Consider a two-block ciphertext IV, c
 - Encoded data = $F_k^{-1}(c) \oplus IV$
 - Main observation: If an attacker modifies the i th byte of IV , this causes a predictable change (**only**) to the i th byte of the encoded data



Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	XX
----	----	----	----	----	----	----	----

\oplus

IV :

AB	01	4F	21	00	7C	02	9E
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	XX	XX	XX	XX	XX	XX
----	----	----	----	----	----	----	----

“Success”

Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	XX
----	----	----	----	----	----	----	----

\oplus

IV :

	01	4F	21	00	7C	02	9E
--	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	XX	XX	XX	XX	XX	XX
----	----	----	----	----	----	----	----

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----	----	----	----	----	----	----	----

\oplus

IV :

	01	4F	21	00	7C	02	9E
--	----	----	----	----	----	----	----

$=$

Encoded data:

	XX	XX	XX	XX	XX	XX	XX
--	----	----	----	----	----	----	----

“Success”

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XX	XX	XX	XX	XX	XX	XX	XX
----	----	----	----	----	----	----	----

\oplus

IV :

		4F	21	00	7C	02	9E
--	--	----	----	----	----	----	----

$=$

Encoded data:

		XX	XX	XX	XX	XX	XX
--	--	----	----	----	----	----	----

“Success”

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XX	XX	XX	XX	XX	XX	XX	XX
----	----	----	----	----	----	----	----

\oplus

IV :

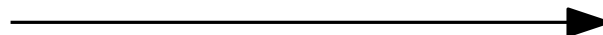
			21	00	7C	02	9E
--	--	--	----	----	----	----	----

$=$

Encoded data:

			XX	XX	XX	XX	XX
--	--	--	----	----	----	----	----

“Success”



“Error”

Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	XX
----	----	----	----	----	----	----	----

\oplus

IV :

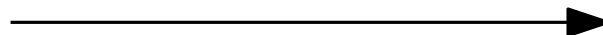
			21	00	7C	02	9E
--	--	--	----	----	----	----	----

$=$

Encoded data:

			XX	XX	XX	XX	XX
--	--	--	----	----	----	----	----

“Success”



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XX	XX	XX	XX	XX	XX	XX	XX
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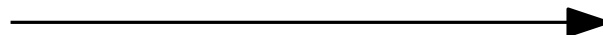
			21	00	7C	02	9E
--	--	--	----	----	----	----	----

$=$

Encoded data:

			06	06	06	06	06
--	--	--	----	----	----	----	----

“Success”



“Error”

Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

$0x9E \oplus 0x06$

\oplus

IV :

			21	00	7C	02	9E
--	--	--	----	----	----	----	----

$=$

Encoded
data:

			06	06	06	06	06
--	--	--	----	----	----	----	----

“Success”



“Error”

Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	01	4F	21	00	7C	02	9E
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	06	06	06	06	06	06
----	----	----	----	----	----	----	----

Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

0x98 \oplus 0x07

IV:

AB	01	4F	21	00	7C	02	9F
----	----	----	----	----	----	----	----

=

Encoded
data:

XX	XX	06	06	06	06	06	06
----	----	----	----	----	----	----	----

Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	01	4F	21	00	7C	02	9F
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	06	06	06	06	06	07
----	----	----	----	----	----	----	----

Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

0x02 \oplus 0x06 \oplus 0x07

IV :

AB	01	4F	21	00	7C	02	9F
----	----	----	----	----	----	----	----

=

Encoded
data:

XX	XX	06	06	06	06	06	07
----	----	----	----	----	----	----	----

Padding-oracle attack

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$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

0x02 \oplus 0x06 \oplus 0x07

IV :

AB	01	4F	21	00	7C	03	9F
----	----	----	----	----	----	----	----

=

Encoded
data:

XX	XX	06	06	06	06	06	07
----	----	----	----	----	----	----	----

Padding-oracle attack

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$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	01	4F	21	00	7C	03	9F
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	06	06	06	06	07	07
----	----	----	----	----	----	----	----

Padding-oracle attack

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$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	01	4E	20	01	7D	03	9F
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	07	07	07	07	07	07
----	----	----	----	----	----	----	----

Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	00	4E	20	01	7D	03	9F
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	07	07	07	07	07	07
----	----	----	----	----	----	----	----

Padding-oracle attack

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$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	01	4E	20	01	7D	03	9F
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	07	07	07	07	07	07
----	----	----	----	----	----	----	----

Padding-oracle attack

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$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	02	4E	20	01	7D	03	9F
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	07	07	07	07	07	07
----	----	----	----	----	----	----	----

Padding-oracle attack

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$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	41	4E	20	01	7D	03	9F
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	XX	07	07	07	07	07	07
----	----	----	----	----	----	----	----

“Success”

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XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	41	4E	20	01	7D	03	9F
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	07	07	07	07	07	07	07
----	----	----	----	----	----	----	----

“Success”

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----	----	----	----	----	----	----	----

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----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	07	07	07	07	07	07	07
----	----	----	----	----	----	----	----

“Success”

$$\begin{aligned} XX \oplus 0x41 &= 0x07 \\ \Rightarrow XX &= 0x41 \oplus 0x07 \end{aligned}$$

Padding-oracle attack

■ Encoded data = $F_k^{-1}(c) \oplus IV$

$F_k^{-1}(c_1)$:

XX	XX	XX	XX	XX	XX	XX	98
----	----	----	----	----	----	----	----

\oplus

IV :

AB	41	4E	20	01	7D	03	9F
----	----	----	----	----	----	----	----

$=$

Encoded data:

XX	07	07	07	07	07	07	07
----	----	----	----	----	----	----	----

$$XX \oplus 0x41 = 0x07$$

$$\Rightarrow XX = 0x41 \oplus 0x07$$

“Success”

$$\Rightarrow \text{plaintext byte} = XX \oplus 0x01 = 0x47$$

Attack complexity

- $\leq L$ tries to learn the # of padding bytes (b)
- $\leq 2^8 = 256$ tries to learn each plaintext byte



CCA-security: a summary

- *Chosen-ciphertext attacks* represent a significant, real-world threat
- Modern encryption schemes are designed to be *CCA-secure*
- **None** of the schemes we have seen so far are *CCA-secure*



Secrecy vs. integrity

- So far we have been concerned with ensuring *secrecy* of communication

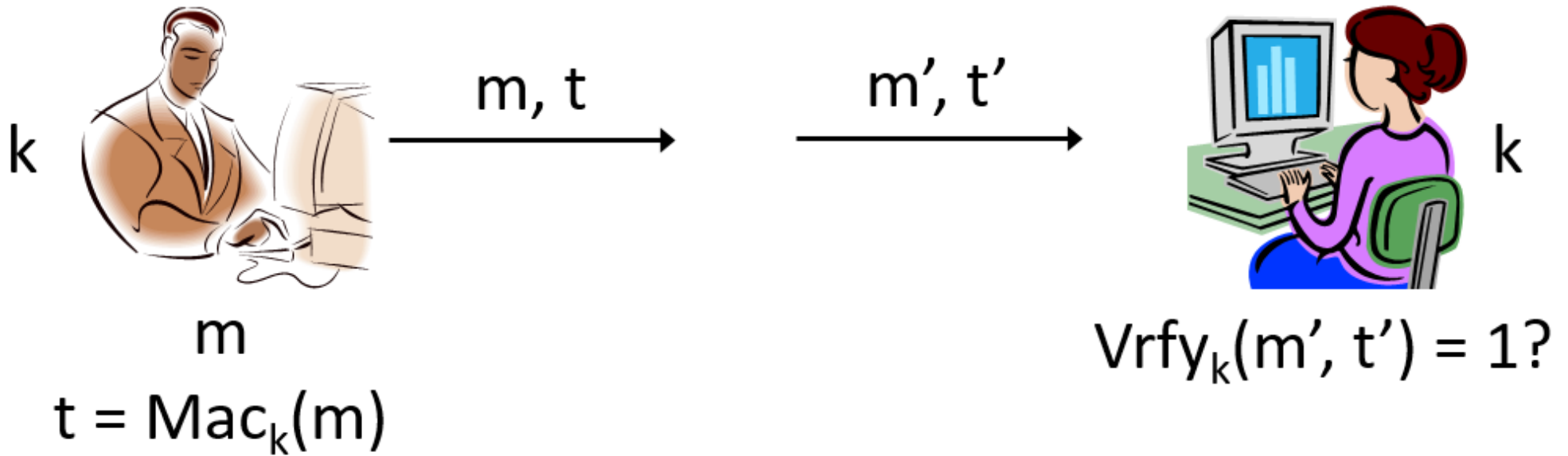


Secrecy vs. integrity

- So far we have been concerned with ensuring *secrecy* of communication
- What about *integrity*?
 - I.e., ensuring that a received message originated from the intended party, and was not modified
 - Even if an attacker **controls** the channel!
 - Standard error-correction techniques **not** enough!
 - The right tool is a *message authentication code*



Secrecy vs. integrity



Secrecy vs. integrity

- *Secrecy* and *integrity* are *orthogonal* concerns
 - Possible to have either one without the other
 - Sometimes you might want one without the other
 - Most often, *both* are needed



Secrecy vs. integrity

- *Secrecy* and *integrity* are *orthogonal* concerns
 - Possible to have either one without the other
 - Sometimes you might want one without the other
 - Most often, **both** are needed
- Encryption does **not** (in general) provide any integrity
 - Integrity is even stronger than *non-malleability*
 - **None** of the schemes we have seen so far provide any integrity



Message authentication code (MAC)

- A *message authentication code* is defined by three PPT algorithms (*Gen*, *Mac*, *Vrfy*):
 - *Gen*: take as input 1^n ; outputs k . (Assume $|k| \geq n$.)
 - *Mac*: take as input key k and message $m \in \{0, 1\}^*$; outputs *tag* t : $t := \text{Mac}_k(m)$
 - *Vrfy*: takes key k , message m , and tag t as input; outputs 1 (“accept”) or 0 (“reject”)



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For all m and all k output by Gen ,

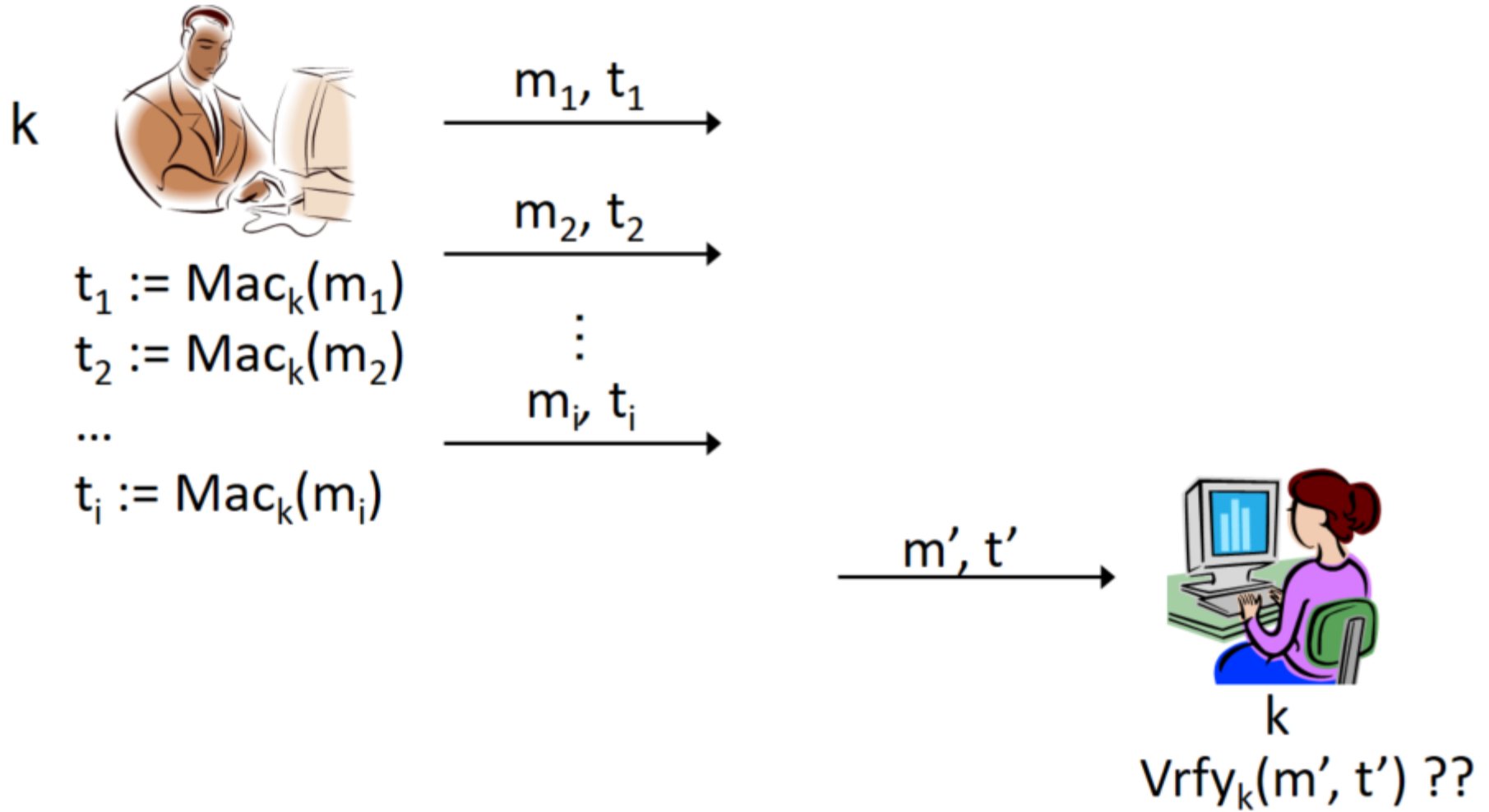
$$Vrfy_k(m, Mac_k(m)) = 1$$


- Threat model
 - “Adaptive chosen-message attack”
 - Assume the attacker can induce the sender to authenticate *messages of the attacker's choice*



- Threat model
 - “Adaptive chosen-message attack”
 - Assume the attacker can induce the sender to authenticate *messages of the attacker's choice*
- Security goal
 - “Existential unforgeability”
 - Attacker should be **unable** to forge a valid tag on **any** message not previously authenticated by the sender

MAC



Formal definition

- Fix A, Π . Define a randomized experiment $\text{Forge}_{A, \Pi}(n)$:
 1. $k \leftarrow \text{Gen}(1^n)$
 2. $A(1^n)$ **interacts** with an **oracle** $\text{Mac}_k(\cdot)$; let M be the set of messages submitted to this oracle
 3. A outputs (m, t)
 4. A *succeeds*, and the experiment evaluates to 1, if $\text{Vrfy}_k(m, t) = 1$ and $m \notin M$



Formal definition

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Definition 6.2 Π is **secure** if for **all PPT** attackers A , there is a **negligible** function ϵ such that

$$\Pr[Forge_{A, \Pi}(n) = 1] \leq \epsilon(n)$$



- Is the definition too strong?
 - We don't want to make any assumptions about what the sender might authenticate
 - We don't want to make any assumptions about what forgeries are “meaningful”



- Is the definition too strong?
 - We don't want to make any assumptions about what the sender might authenticate
 - We don't want to make any assumptions about what forgeries are “meaningful”
- A *MAC* satisfying this definition can be used anywhere integrity is needed



Replay attacks

- Replay attacks are **not** prevented
 - No *stateless* mechanism can prevent them
- Replay attacks are often a significant real-world concern
- Need to protect against replay attacks at a higher level
 - Decision about what to do with a replayed message is **application-dependent**

A fixed-length MAC

- Intuition: we need a keyed function Mac such that:
 - Given $Mac_k(m_1), Mac_k(m_2), \dots$,
 - It is **infeasible** to predict the value $Mac_k(m)$ for any $m \notin \{m_1, m_2, \dots\}$



A fixed-length MAC

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 - Given $Mac_k(m_1), Mac_k(m_2), \dots$,
 - It is **infeasible** to predict the value $Mac_k(m)$ for any $m \notin \{m_1, m_2, \dots\}$
- Let Mac be a PRF!

Construction

- Let F be a length-preserving PRF (aka block cipher)



Construction

- Let F be a length-preserving PRF (aka block cipher)
- Construct the following MAC Π :
 - Gen : choose a uniform key k for F
 - $Mac_k(m)$: output $F_k(m)$
 - $Vrfy_k(m, t)$: output 1 iff $F_k(m) = t$



Construction

- Let F be a length-preserving PRF (aka block cipher)
- Construct the following MAC Π :
 - Gen : choose a uniform key k for F
 - $Mac_k(m)$: output $F_k(m)$
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- **Theorem 6.3** Π is a *secure* MAC



Next Lecture

- proof, authenticated encryption ...

