

# Homework #4

**Due** May 31 by 11:59pm      **Points** 20      **Submitting** a file upload  
**Available** May 17 at 12am - Jun 2 at 11:59pm

This assignment was locked Jun 2 at 11:59pm.

1. (7 points) Decide if each of the following sentences is valid, unsatisfiable, or neither. Verify your decision using truth tables or the equivalence rules. (I used - for negation, V for or, and ^ for and).

- a. Smoke  $\Rightarrow$  Smoke
- b. Smoke  $\Rightarrow$  Fire
- c. (Smoke  $\Rightarrow$  Fire)  $\Rightarrow$  (- Smoke  $\Rightarrow$  - Fire)
- d. Smoke V Fire V - Fire
- e. ((Smoke ^ Heat)  $\Rightarrow$  Fire)  $\Leftrightarrow$  ((Smoke  $\Rightarrow$  Fire) V (Heat  $\Rightarrow$  Fire))
- f. (Smoke  $\Rightarrow$  Fire)  $\Rightarrow$  ((Smoke ^ Heat)  $\Rightarrow$  Fire)
- g. Big V Dumb V (Big  $\Rightarrow$  Dumb)

2. (7 points) Given the following, can you prove that the Unicorn is mythical? How about magical? Horned?

``If the unicorn is mythical, then it is immortal; but if it is not mythical, then it is a mortal mammal. If the unicorn is either immortal or a mammal, then it is horned. The unicorn is magical if it is horned."`

3. (6 points) Consider the following sentence

$[(\text{Food} \Rightarrow \text{Party}) \vee (\text{Drinks} \Rightarrow \text{Party})] \Rightarrow [(\text{Food} \wedge \text{Drinks}) \Rightarrow \text{Party}]$

- a. Determine, using enumeration, whether this sentence is valid, satisfiable but not valid, or unsatisfiable.
- b. Convert the left hand side and the right hand sides of the main implication into CNF, showing each step, and explain how the results confirm your answer to (a).
- c. Prove your answer to (a) using resolution.