

# DETERMINISTIC FINITE AUTOMATON (DFA) PROJECT

## FINAL REPORT

## Section 1. SUMMARY OF THE DETERMINISTIC FINITE AUTOMATON

### 1.1 DESCRIPTION OF THE DFA

My project implements a DFA simulator in C++.

It consists of:

- A DFA class that loads DFA specifications from files and simulates string acceptance
- Input validation and error handling
- An interactive command-line simulator for testing DFA behavior

### 1.2 WHAT DOES IT DO?

1. Reads a DFA specification from a text file containing:
  - A set of states ( $Q$ )
  - An alphabet of symbols ( $\Sigma$ )
  - An initial state ( $q_0$ )
  - A set of accepting/final states ( $F$ )
  - A transition function ( $\delta$ ) defined as rules
2. Validates the DFA structure to ensure:
  - The initial state exists in the state set
  - All accepting states exist in the state set
  - All transitions reference valid states and symbols
3. Tests string acceptance by:
  - Starting at the initial state
  - Following transitions for each input symbol
  - Accepting the string if it ends in a final state
4. Provides interactive commands:
  - `load <file>`: Load a DFA from a file
  - `readstring <string>`: Test if a string is accepted

- visualize <string>: Display state transitions step by step
- display: Show the DFA formal representation
- exit: Exit the simulator

### 1.3 DATA STRUCTURES USED

The implementation uses the following data structures:

1. `tcp::Set<string> Q`
  - Type: Custom set class
  - Purpose: Stores all states in the DFA
2. `tcp::Set<char> Sigma`
  - Type: Custom set class
  - Purpose: Stores all symbols in the alphabet
3. `string q0`
  - Type: String
  - Purpose: Stores the initial/start state
4. `tcp::Set<string> F`
  - Type: Custom set class
  - Purpose: Stores all accepting/final states
5. `tcp::Set<tcp::Triple> delta`
  - Type: Custom set of Triple objects
  - Purpose: Stores the transition function ( $\delta$ )
  - Triple structure: `first()` returns current state (string), `second()` returns symbol (char), `third()` returns next state (string)

### 1.4 CUSTOM DATA STRUCTURES

The project implements two custom data structures in the `tcp` namespace:

1. `tcp::Set<T>`
  - Type: Template class for a set data structure
  - Purpose: Provides a custom set implementation using a linked list
  - Key Methods:
    - `size()`: Returns the number of elements in the set
    - `contains(const T& obj)`: Checks if an object is in the set
    - `insert(const T& obj)`: Adds an object to the set if not already present
    - `operator[](size_t i)`: Accesses the i-th element in the set

```
- toString(): Returns a string representation of the set
- Implementation: Uses a singly-linked list with Node structs

2. tcp::Triple
- Type: Class to store three related values
- Purpose: Represents DFA transitions with start state, symbol, and end
state
- Structure: Contains three private members (string, char, string)
- Key Methods:
  - first(): Returns the first string (start state)
  - second(): Returns the char (symbol)
  - third(): Returns the second string (end state)
  - toString(): Returns a formatted string representation
- Usage: Used in the delta set to store transition rules
```

## Section 2. CLASS DOCUMENTATION

### 2.1 CLASS: DFA

#### Description:

The DFA class represents a Deterministic Finite Automaton. It inherits from `tcp::Object` to support string output formatting. The class encapsulates the five components of a formal DFA: states, alphabet, initial state, accepting states, and transition function.

#### PUBLIC FIELDS:

None (all members are private)

#### PRIVATE FIELDS:

- `vector<string> Q`: Set of states
- `vector<char> Sigma`: Alphabet of input symbols
- `string q0`: Initial state
- `vector<string> F`: Set of accepting/final states
- `map<pair<string,char>, string> delta`: Transition function

## 2.2 METHOD DOCUMENTATION

METHOD: DFA()

Return Type: (Constructor)

PRECONDITIONS:

- None

PSEUDOCODE:

```
FUNCTION DFA()
    Q.clear()
    Sigma.clear()
    q0 = ""
    F.clear()
    delta.clear()
END FUNCTION
```

DESCRIPTION:

Initializes a new DFA object with empty state set, alphabet, initial state, final states, and transition function. All vectors and maps are cleared to have a clean state.

METHOD: loadFromFile(const string& filename)

Return Type: bool

Parameters: string filename - the path to the DFA specification file

PRECONDITIONS:

- The file must exist and be readable
- The file must contain DFA specification in the correct format:
  - Line 1: Space-separated states
  - Line 2: Symbol characters (no spaces)
  - Line 3: Initial state name
  - Line 4: Space-separated final states
  - Lines 5+: Transitions in format "state symbol nextstate"

PSEUDOCODE:

```
FUNCTION loadFromFile(filename: string) RETURNS boolean
    Open file at filename
    IF file cannot be opened THEN
        Print error message
        RETURN false
    END IF

    Clear all DFA components: Q, Sigma, q0, F, delta

    step = 0
    FOR EACH line in file DO
```

```

Remove leading and trailing whitespace
IF line is empty THEN continue END IF

IF step == 0 THEN      Parse states Q
    Extract space-separated states
    FOR EACH state DO
        Validate: state contains only alphanumeric or underscore
        Add to unique set
    END FOR
    Q = unique states
    step = 1
ELSE IF step == 1 THEN      Extract alphanumeric characters
    Add unique symbols to Sigma
    step = 2
ELSE IF step == 2 THEN      q0 = line
    step = 3
ELSE IF step == 3 THEN      Extract space-separated states
    Add to unique set
    F = unique states
    step = 4 ELSE IF step >= 4 THEN
        Parse: "start symbol end"
        delta.insert(Triple(start, symbol, end))
    END IF
END FOR

Close file
RETURN isValid()
END FUNCTION

```

**DESCRIPTION:**

We load a DFA specification from a file. Parses the five-tuple from the file in the specified format. It then validates state names and removes duplicates then finally calls `isValid()` to verify the complete DFA structure.

**METHOD:** `isValid()` const

**Return Type:** bool

**PRECONDITIONS:**

- All DFA components must be populated
- This is typically called after `loadFromFile()`

**PSEUDOCODE:**

```

FUNCTION isValid() RETURNS boolean
    Check 1: Initial state in Q
    IF q0 not in Q THEN
        Print error: "Invalid DFA: q0 not in Q"
        RETURN false
    END IF

```

```

Check 2: All final states in Q
FOR EACH state f in F DO
    IF f not in Q THEN
        Print error: "Invalid DFA: F contains state not in Q"
        RETURN false
    END IF
END FOR

Check 3: All transitions valid
FOR EACH transition t in delta DO
    start = t.first()
    symbol = t.second()
    end = t.third()
    IF start not in Q THEN
        Print error: "Invalid DFA: transition from state not in Q"
        RETURN false
    END IF
    IF end not in Q THEN
        Print error: "Invalid DFA: transition to state not in Q"
        RETURN false
    END IF
    IF symbol not in Sigma THEN
        Print error: "Invalid DFA: transition uses symbol not in Sigma"
        RETURN false
    END IF
END FOR

RETURN true
END FUNCTION

```

**DESCRIPTION:**

Validates the DFA structure by checking:

1. The initial state  $q_0$  exists in the state set  $Q$
2. All accepting states in  $F$  are members of  $Q$
3. All transitions reference valid states and alphabet symbols

This ensures the DFA follows the formal definition before execution.

METHOD: `displayFormal()` const

Return Type: void

**PRECONDITIONS:**

- The DFA must be loaded and valid

**PSEUDOCODE:**

```

FUNCTION displayFormal()
    Print "Q: "

```

```

FOR EACH state in Q DO
    Print state + " "
END FOR
Print newline

Print " $\Sigma$ : "
FOR EACH symbol in Sigma DO
    Print symbol + " "
END FOR
Print newline

Print "q0: " + q0
Print newline

Print "F: "
FOR EACH state in F DO
    Print state + " "
END FOR
Print newline

Print " $\delta$ : "
Print newline
FOR EACH transition t in delta DO
    Print t.first() + " " + t.second() + " " + t.third()
    Print newline
END FOR
END FUNCTION

```

**DESCRIPTION:**

Displays the formal definition of the DFA in the standard mathematical notation, showing all five components in a readable format.

**METHOD:** runString(const string& input) const

**Return Type:** bool

**Parameters:** string input - the input string to test

**PRECONDITIONS:**

- The DFA must be loaded and valid
- All symbols in input must be in Sigma

**PSEUDOCODE:**

```

FUNCTION runString(input: string) RETURNS boolean
    current = q0
    FOR EACH character c in input DO
        found = false
        FOR EACH transition t in delta DO
            IF t.first() == current AND t.second() == c THEN
                current = t.third()

```

```

        found = true
        BREAK
    END IF
END FOR
IF not found THEN
    RETURN false
    END IF
END FOR

RETURN F.contains(current)
END FUNCTION

```

**DESCRIPTION:**

Simulates the DFA by processing each input character in sequence, following transitions from the delta table. Returns true if the DFA ends in an accepting state, false otherwise.

METHOD: displayComputation(const string& input) const

Return Type: void

Parameters: string input - the input string to display computation for

**PRECONDITIONS:**

- The DFA must be loaded and valid
- All symbols in input should be in Sigma

**PSEUDOCODE:**

```

FUNCTION displayComputation(input: string)
    current = q0
    Print "Initial state: " + current
    Print newline

    FOR i = 0 to length(input)-1 DO
        c = input[i]
        found = false
        FOR EACH transition t in delta DO
            IF t.first() == current AND t.second() == c THEN
                nextstate = t.third()
                Print " $\delta(" + current + ", " + c + ") \rightarrow$ " + nextstate
                Print newline
                current = nextstate
                found = true
                BREAK
            END IF
        END FOR
        IF not found THEN
            Print "No transition from state " + current +
                " on symbol " + c
            Print newline
        RETURN
    
```

```

        END IF
    END FOR

    IF F.contains(current) THEN
        Print "String accepted. Final state: " + current
    ELSE
        Print "String rejected. Final state: " + current
    END IF
    Print newline
END FUNCTION

```

**DESCRIPTION:**

Displays the step by step computation of processing an input string through the DFA. Shows each state transition and whether the final state is accepting or rejecting.

**METHOD:** `toString()` const override

**Return Type:** string

**PRECONDITIONS:**

- The DFA must be loaded

**PSEUDOCODE:**

```

FUNCTION toString() RETURNS string
    output = ""

    output += "DFA Formal Representation:\n"
    output += "Q: "
    FOR EACH state in Q DO
        output += state + " "
    END FOR
    output += "\n"

    output += "Σ: "
    FOR EACH symbol in Sigma DO
        output += symbol + " "
    END FOR
    output += "\n"

    output += "q0: " + q0 + "\n"

    output += "F: "
    FOR EACH state in F DO
        output += state + " "
    END FOR
    output += "\n"

    output += "δ:\n"

```

```

FOR EACH transition t in delta DO
    output += t.first() + " " + t.second() + " " + t.third() + "\n"
END FOR

RETURN output
END FUNCTION

```

**DESCRIPTION:**

It converts the DFA to a string representation and overrides the parent class method then returns the formal DFA representation suitable for printing.

### Section 3. HOW TO RUN THE PROGRAM

#### STEP 1: COMPILE THE PROGRAM

Open a terminal and navigate to the project directory, then run:

```
clang++ -std=c++17 main.cpp DFA.cpp -o main
```

#### Alternative compilers:

```
g++ -std=c++17 main.cpp DFA.cpp -o main
```

#### STEP 2: RUN THE PROGRAM

Execute the compiled program:

```
./main
```

#### STEP 3: INTERACTIVE COMMANDS

The program displays the prompt "> " and waits for commands. Type the following commands:

A. Load a DFA from file:

Command: load <filename>

Example: load test\_dfa\_valid.txt

Output: "DFA loaded successfully from test\_dfa\_valid.txt"

B. Test string acceptance:

Command: readstring <string>

Example: readstring abba

Output: "String accepted!" or "String rejected."

C. Display step-by-step computation:

Command: visualize <string>

Example: visualize abba

Output: Shows each state transition:

Initial state: q0

```

 $\delta(q_0, a) \rightarrow q_1$ 
 $\delta(q_1, b) \rightarrow q_1$ 
 $\delta(q_1, b) \rightarrow q_1$ 
 $\delta(q_1, a) \rightarrow q_2$ 
String accepted. Final state: q2

```

D. Display DFA definition:

Command: display

Output: Shows complete DFA formal representation

E. Exit the program:

Command: exit

## Execution Flow

Command	Execution Steps
LOAD <file>	<ol style="list-style-type: none"> <li>1. Open specified file</li> <li>2. Parse DFA components</li> <li>3. Validate the DFA structure</li> <li>4. Store in memory</li> <li>5. Return to the command prompt</li> </ol>
READSTRING <string>	<ol style="list-style-type: none"> <li>1. Start at initial state <math>q_0</math></li> <li>2. For each input symbol: <ul style="list-style-type: none"> <li>- Look up transition in delta</li> <li>- Move to next state</li> <li>- If no transition state exists, we will reject it.</li> </ul> </li> <li>3. Check if final state is in <math>F</math></li> <li>4. We print string accepted or rejected based on outcome</li> <li>5. Return to command prompt</li> </ol>
DISPLAY	<ol style="list-style-type: none"> <li>1. Print out formal DFA representation (<math>Q, \Sigma, q_0, F, \delta</math>)</li> <li>2. Return to command prompt</li> </ol>
VISUALIZE <string>	<ol style="list-style-type: none"> <li>1. Start at <math>q_0</math></li> <li>2. For each symbol <ul style="list-style-type: none"> <li>- Look up transition in delta</li> <li>- Print the step: <math>\delta(state, symbol) \rightarrow nextstate</math></li> <li>- Move to next state</li> </ul> </li> </ol>

	<ul style="list-style-type: none"> <li>- If no transition exists, prints an error and stops.</li> </ul> <ol style="list-style-type: none"> <li>3. Print the final result (accepted or rejected)</li> <li>4. Returns back to command prompt</li> </ol>
EXIT	<ol style="list-style-type: none"> <li>1. Terminates the program and exits.</li> <li>2. Return control to OS</li> </ol>

## Section 4. TESTING AND VALIDATION

My project includes two test files for validation:

`test_dfa_valid.txt:`

Represents a valid DFA that accepts strings ending with 'a' following a transition through 'b'

`test_dfa_invalid.txt:`

Represents an invalid DFA (final state q2 not in state set Q)  
Tests error handling and validation logic