Problem Set 3

Nicolai H. Brand

1

1.1

Given grammar:

```
A \rightarrow A + B \mid B
B \rightarrow B - Z \mid Z
Z \rightarrow X \mid Y
X \rightarrow X
Y \rightarrow i j
```

Augmented grammar:

```
S \rightarrow A  # rewritten axiom

A \rightarrow A + B

A \rightarrow B

B \rightarrow B - Z

B \rightarrow Z

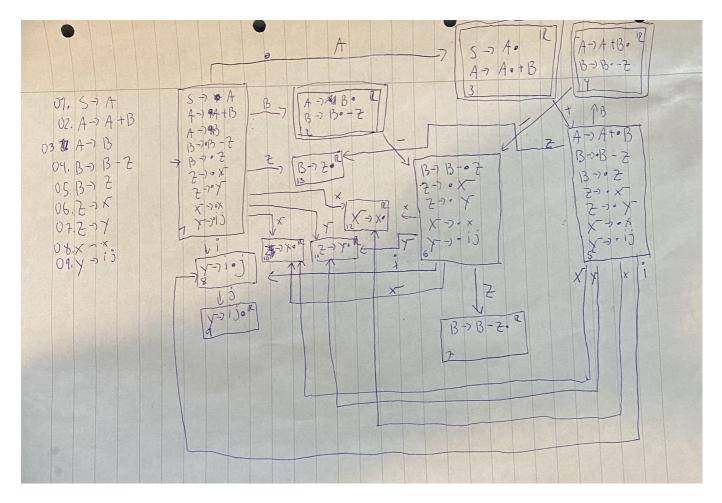
Z \rightarrow X

Z \rightarrow Y

X \rightarrow X

Y \rightarrow i j
```

An R at the right-hand corner of a state signifies that a reduce action can be applied



1.2

The states with a double-outline have shift/reduce conflicts as both actions are possible.

1.3

Production rules with labels:

```
01 \text{ S} \rightarrow A
02 \text{ A} \rightarrow A + B
03 \text{ A} \rightarrow B
04 \text{ B} \rightarrow B - Z
05 \text{ B} \rightarrow Z
06 \text{ Z} \rightarrow X
07 \text{ Z} \rightarrow Y
08 \text{ X} \rightarrow X
09 \text{ Y} \rightarrow i \text{ j}
```

I have used these labels to denote where the reduce actions go to. (I realize this method is not perfect, but I don't have the time to redo it properly).

LR(0) table:

	X	i	j	-	+	\$ Α	В	Z	X	Υ
1	s12	s8				g3	g2	g13	g10	g11
						2/4				

	х	i	j	-	+	\$	Α	В	Z	X	Υ
2	r03	r03	r03	s6 / r03	r03	r03					
3	s5 / a					а					
4	r02	r02	r02	s6 / r02	r02	r02					
5	s12	s8							g13	g10	g11
6	s12	s8							g7	g10	g11
7	r04	r04	r04	r04	r04	r04					
8			s9								
9	r09	r09	r09	r09	r09	r09					
10	r06	r06	r06	r06	r06	r06					
11	r07	r07	r07	r07	r07	r07					
12	r08	r08	r08	r08	r08	r08		_		_	_
13	r05	r05	r05	r05	r05	r05			_		_

Follow sets:

```
follow(S) = { }
follow(A) = { + }
follow(B) = { + - }
follow(Z) = { + - }
follow(X) = { + - }
follow(Y) = { + - }
```

Given the follow sets we can produce the SLR table:

	X	i	j	-	+	\$	Α	В	Z	X	Y
1	s12	s8					g3	g2	g13	g10	g11
2				s6	r03	r03					
3	s5					а					
4				s6 / r02	r02	r02					
5	s12	s8							g13	g10	g11
6	s12	s8							g7	g10	g11
7				r04	r04	r04					
8			s9								
9				r09	r09	r09					

	Х	i	j	-	+	\$	Α	В	Z	Х	Y
10					r06	r06					
11				r07	r07	r07					
12				r08	r08	r08					
13				r05	r05	r05					

Here we see see there is still a conflict. This means the grammar is not SLR parseable.

2

See ps3_skeleton/src/tree.c.