## **Neighbor RSA**

main part:

```
1    e = 65537
2    p = random_prime(1<<2048)
3    q = random_prime(1<<512)
4    r = random_prime(1<<512)
5    n1 = p * q
6    n2 = next_prime(p) * r
7    assert m1 < n1 and m2 < n2</pre>
```

Since that we notice that the special generation of p, q, we find that this is an agcd problem since that agcd is like xi = p\*qi+r for 1 <= i <= t, where ri is small. Given some xi, solve for common divisor p. Using what I have written in my repo on github /cryptography/agcd can solve it with rho=512 since r is 512 bits.

## **Sexy RSA**

main part:

```
def getSexyPrime(n=512):
    # Sexy prime: https://en.wikipedia.org/wiki/Sexy_prime
    while True:
    p = getPrime(n)
    if isPrime(p+6):
        return p, p+6
```

Notice this function, we can find that p,q are really near. So just use fermat method to factorize n.

## **Proth RSA**

In this challenge, we have:

and we also know this:

```
1 | s = (k1 * k2) % n
```

hmmm looks like we have only 2 unknown vars: k1, k2. So we need try to solve them over zmod(n). What came my mind is using groebner basis since this is really fast and helpful when we are trying to solve complex equations over polynomial ring. So I just use k1, k2 to represent p, q and then construct:

$$p*q-n$$
$$k1*k2-s$$

And then solve for gb. But unfortunately it just gives me something like  $k_2^2+ak_2+b$ . But don't worry, just use <code>small\_roots</code> to solve for k2 . After solving for k2 , just recover q .

## **Leaky RSA**

In this challenge, we are given the bit of p and q, also gives us s = ((p\*\*3 - 20211219\*q) \* inverse(p\*p+q\*q,n)) % n. Seeing this, I know that this is a challenge to let us using coppersmith method to recover <math>p,q. In this way, we have to clear s.

$$s = (p^3 - aq)(p^2 + q^2)^{-1} \mod n$$
  
 $=> (p^2 + q^2)s = (p^3 - aq) \mod n$   
 $=> p^3 - aq - p^2s - q^2s = 0 \mod n$   
 $=> -aq - q^2s = 0 \mod p^2$   
 $=> aq + q^2s = 0 \mod p^2$   
 $a + qs = 0 \mod p^2$ 

So in this way, we construct a polynomial and use  $small_roots$  to solve for q. After getting q, we can just encrypt over  $zmod(q^2)$  with out solving for p. Little trick make us to be faster than solving for p lol (but only when the message has no padding)