

Contents

1 Foundations	1
1.1 PyMath	1
1.2 Java Integer	1
1.3 Java String	1
1.4 Java String builder	2
1.5 Java Math	2
2 Mathematics & Number Theory	2
2.1 Number Theory	2
2.2 Combinatorics	3
2.3 Geometry	3
3 Data Structure	3
3.1 MST	3
3.2 SegmentTree	3
3.3 HLD	4
3.4 PST	4
3.5 Trie	5
3.6 BIT 單修區查	5
3.7 BIT 區修單查	5
3.8 BIT 區修區查	5
4 Graph	5
4.1 cut vertex AND bridges	5
4.2 SCC - Tarjan	5
4.3 BCC - Tarjan	6
4.4 Convex	6
4.5 Max Flow	6
4.6 min cut max flow	7
5 String	7
5.1 KMP	7
5.2 ACAM	7
6 Techniques	8
6.1 二分搜	8
6.2 傷增 LCA	8
6.3 SG	8
7 DP	8
7.1 輪廓線 DP	8
7.2 數位 DP	8
7.3 樹 DP	8

1 Foundations

1.1 PyMath

```

1 import math
2
3     math.ceil(x) #上高斯
4     math.floor(x) #下高斯
5     math.factorial(x) #階乘
6     math.fabs(x) #絕對值
7     math.fsum(arr) #求和
8     math.gcd(x, y)
9     math.exp(x) # e^x
10    math.log(x, base)
11    math.log2(x)
12    math.log10(x)
13    math.sqrt(x)
14    math.pow(x, y, mod)
15    math.sin(x) # cos, tan, asin, acos, atan,
16      atan2, sinh ...
17    math.hypot(x, y) #歐幾里德範數
18    math.degrees(x) #x從弧度轉角度
19    math.radians(x) #x從角度轉弧度
20    math.gamma(x) #x的gamma函數
21    math.pi #const
22    math.e #const
23    math.inf

```

1.2 Java Integer

```

1 // 常量
2 MAX_VALUE, MIN_VALUE, BYTES, SIZE, TYPE
3
4 // 轉換/解析
5 static int parseInt(String s)
6 static int parseInt(String s, int radix)
7 static int parseUnsignedInt(String s)
8 static int parseUnsignedInt(String s, int
9   radix)
10 static Integer valueOf(int i)
11 static Integer valueOf(String s)
12 static Integer valueOf(String s, int radix)
13 static String toString(int i)
14 static String toString(int i, int radix)
15 static String toUnsignedString(int i)
16 static String toUnsignedString(int i, int
17   radix)
18 static long toUnsignedLong(int x)
19 static Integer decode(String nm)
20   // 支援 0x/0/# 前綴
21 static Integer getInteger(String nm[, int
22   val]) // 從系統屬性讀取整數
23
24 // 比較/雜湊/聚合
25 static int compare(int x, int y)
26 static int compareUnsigned(int x, int y)
27 static int hashCode(int value)
28 static int min(int a, int b)
29 static int max(int a, int b)
30 static int sum(int a, int b)
31
32 // 位元操作
33 static int bitCount(int i) // 設定位數
34 static int highestOneBit(int i)
35 static int lowestOneBit(int i)
36 static int numberOfLeadingZeros(int i)
37 static int numberOfTrailingZeros(int i)
38 static int rotateLeft(int i, int distance)
39 static int rotateRight(int i, int distance)
40 static int reverse(int i)
41 static int reverseBytes(int i)
42
43 // 無號運算
44 static int divideUnsigned(int dividend, int
45   divisor)

```

```

41 static int remainderUnsigned(int dividend,
42   int divisor)

```

1.3 Java String

```

1 // 查詢
2 int length()
3 boolean isEmpty()
4 boolean isBlank() // (since 11)
5 char charAt(int index)
6 int codePointAt(int index)
7 int codePointBefore(int index)
8 int codePointCount(int beginIndex, int
9   endIndex)
10 boolean contains(CharSequence s)
11 boolean startsWith(String prefix[, int
12   toffset])
13 boolean endsWith(String suffix)
14 int indexOf(String str[, int fromIndex])
15 int lastIndexOf(String str[, int
16   fromIndex])
17 // 取子字串/子序列
18 String substring(int beginIndex)
19 String substring(int beginIndex, int
20   endIndex)
21 CharSequence subSequence(int beginIndex, int
22   endIndex)
23
24 // 比較/等價
25 boolean equals(Object obj)
26 boolean equalsIgnoreCase(String
27   anotherString)
28 int compareTo(String anotherString)
29 int compareToIgnoreCase(String str)
30 boolean matches(String regex)
31 boolean regionMatches(int toffset, String
32   other, int offset, int len)
33 boolean regionMatches(boolean ignoreCase,
34   int toffset, String other, int offset,
35   int len)
36
37 // 建構/轉換/連接
38 String concat(String str)
39 String replace(char oldChar, char newChar)
40 String replace(CharSequence target,
41   CharSequence replacement)
42 String replaceAll(String regex, String
43   replacement)
44 String replaceFirst(String regex, String
45   replacement)
46 String[] split(String regex[, int limit])
47 String toLowerCase()
48 String toUpperCase()
49 String trim()
50 String strip() // (since 11)
51 String stripLeading() // (since 11)
52 String stripTrailing() // (since 11)
53 String repeat(int count) // (since 11)
54 IntStream chars()
55 Stream<String> lines() // (since 11)
56 String intern()
57
58 // 靜態工具
59 static String format(String format,
60   Object... args)
61 static String join(CharSequence delimiter,
62   CharSequence... elements)
63 static String join(CharSequence delimiter,
64   Iterable<? extends CharSequence>
65   elements)
66 static String
67   valueOf(primitive/char[]/Object)
68 static String copyValueOf(char[] data[, int
69   offset, int count])

```

1.4 Java String builder

```

1 // 長度/容量
2 int length()
3 int capacity()
4 void ensureCapacity(int minimumCapacity)
5 void trimToSize()
6 void setLength(int newLength)
7
8 // 存取/修改
9 char      charAt(int index)
10 void     setCharAt(int index, char ch)
11 StringBuilder append(... 各種型別 ...)
12 StringBuilder insert(int offset, ... 各種型別
    ...)
13 StringBuilder delete(int start, int end)
14 StringBuilder deleteCharAt(int index)
15 StringBuilder replace(int start, int end,
    String str)
16 StringBuilder reverse()
17
18 // 子字串/查找
19 String      substring(int start)
20 String      substring(int start, int end)
21 CharSequence subSequence(int start, int end)
22 int         indexOf(String str[], int
    fromIndex])
23 int         lastIndexOf(String str[], int
    fromIndex])
24
25 // 轉換
26 String toString()

```

1.5 Java Math

```

1 // 常量
2 static final double E, PI
3
4 // 絶對值/比較
5 static int/long/float,double abs(x)
6 static T max(a, b)
7 static T min(a, b)
8
9 // 取整/四捨五入
10 static double floor(double a)
11 static double ceil(double a)
12 static double rint(double a)          // 最接近整數(偶數優先)
13 static long round(double a) / int
    round(float a)
14 static int   floorDiv(int x, int y)
15 static int   floorMod(int x, int y)
16
17 // 溢位保護(exact 系列, Java 8+)
18 static int/long addExact(a, b)
19 static int/long subtractExact(a, b)
20 static int/long multiplyExact(a, b)
21 static int/long incrementExact(a)
22 static int/long decrementExact(a)
23 static int   toIntExact(long value)
24 static int/long negateExact(a)
25
26 // 指對數/冪根
27 static double pow(double a, double b)
28 static double sqrt(double a)
29 static double cbrt(double a)
30 static double exp(double a)
31 static double expm1(double x)
32 static double log(double a)
33 static double log10(double a)
34 static double log1p(double x)
35
36 // 三角/雙曲
37 static double sin/cos/tan(double a)
38 static double asin/acos/atan(double a)
39 static double atan2(double y, double x)

```

```

40 static double sinh/cosh/tanh(double a)
41
42 // 其他實用
43 static double hypot(double x, double y)
44 static double toDegrees(double angrad)
45 static double toRadians(double angdeg)
46 static double copySign(double magnitude,
    double sign)
47 static double nextUp/nextDown(double a)
48 static double nextAfter(double start, double
    direction)
49 static double ulp(double d)
50 static double random()
51 static double scalb(double d, int
    scaleFactor)
52 static double fma(double a, double b, double
    c) // (since 8)
53 static long multiplyHigh(long x, long y)
    // (since 9)
54 static long multiplyFull(int x, int y)
    // (since 9, 回傳 long)

```

Congruence ($a \equiv b \pmod{m}$) Essentials

- $a \equiv b \pmod{m} \iff m | (a - b)$, 同餘類以差整除判斷。
- $a \equiv b \pmod{m} \Rightarrow f(a) \equiv f(b) \pmod{m}$ 對所有以整數係數的多項式 f 成立。
- 若 $a \equiv b \pmod{m}$ 且 $c \equiv d \pmod{m}$, 則 $a \pm c \equiv b \pm d \pmod{m}$, $ac \equiv bd \pmod{m}$, $a^n \equiv b^n \pmod{m}$ 。
- 若 $\gcd(k, m) = 1$ 且 $ka \equiv kb \pmod{m}$, 可約去 k : $a \equiv b \pmod{m}$ 。
- 若 $a \equiv b \pmod{m}$, 則 $a \equiv b \pmod{d}$ 對任何 d 整除 m 亦成立。
- 若 $d | a, b, m$, 則 $\frac{a}{d} \equiv \frac{b}{d} \pmod{\frac{m}{d}}$

Bézout's Identity

若 $a, b \in \mathbb{Z}$, $\exists x, y \in \mathbb{Z}$ 使得 $ax + by = \gcd(a, b)$.

任何方程 $ax + by = c$ 有整數解當且僅當 $\gcd(a, b) | c$ 。擴展歐幾里得演算法可同時求得 \gcd 與一組 (x, y) , 常用於計算模逆與結合 China Remainder。

Extended Euclidean algorithm 給定 a, b, c , 求 $ax + by = c$ 的解

```

1 ll extgcd(ll a, ll b, ll c, ll &x, ll
    &y){
2     if(b == 0){
3         x = c/a ;
4         y = 0 ;
5         return a ;
6     }
7     ll d = extgcd(b, a%b, c, x, y), tmp =
        x ;
8     x = y ;
9     y = tmp - (a/b)*y ;
10    return d ;
11}

```

根據貝祖定理, 只有當 $d | c$ 時, $ax + by = c$ 才有整數解
對於 $ax + by = c$ 假設有整數解, 且 $\gcd(a, b) = 1$
使用 extgcd 求出 (a_0, b_0) 的特解後, 根據逆模元可得出通解:
 $a = a_0 + \frac{b}{d}t$, $b = b_0 - \frac{a}{d}t$ 其中 t 可以為任意整數

2 Mathematics & Number Theory

2.1 Number Theory

Fermat's Little Theorem:

$$a^{p-1} \equiv 1 \pmod{p} \quad (\gcd(a, p) = 1, p \text{ prime})$$

Euler's Theorem:

$$a^{\varphi(n)} \equiv 1 \pmod{n} \quad (\gcd(a, n) = 1)$$

Modular Inverse:

$$a^{-1} \equiv a^{p-2} \pmod{p} \quad (\gcd(a, p) = 1, p \text{ prime})$$

Euler Totient:

$$\varphi(n) = n \prod_{p|n} \left(1 - \frac{1}{p}\right)$$

Fast Modular Exponentiation

```

long long mod_pow(long long a, long long b,
    long long mod) {
    long long res = 1 % mod;
    while (b > 0) {
        if (b & 1) res = res * a % mod;
        a = a * a % mod;
        b >>= 1;
    }
    return res;
}

```

Counting Coprimes Below n

$$\forall n > 0, \sum_{d|n} \varphi(d) = n, \quad \sum_{d|n} \mu(d) \left\lfloor \frac{n}{d} \right\rfloor = 1,$$

其中 μ 為莫比烏斯函數; 常用於反演及計算互質對數量。

Modulo Arithmetic Quick Facts

$$(a \pm b) \pmod{m} = ((a \pmod{m}) \pm (b \pmod{m})) \pmod{m},$$

$$(ab) \pmod{m} = ((a \pmod{m})(b \pmod{m})) \pmod{m},$$

$$(a^k) \pmod{m} = ((a \pmod{m})^k) \pmod{m},$$

$$(-a) \pmod{m} = (m - (a \pmod{m})) \pmod{m}.$$

若 $\gcd(a, m) = 1$, 可計算乘法逆元 a^{-1} 並套用 $(a/b) \pmod{m} \equiv a \cdot b^{-1} \pmod{m}$ 。

Modular Inverse Basics 對於 $\gcd(a, m) = 1$, 存在唯一 $a^{-1} \in [0, m)$ 使得 $a \cdot a^{-1} \equiv 1 \pmod{m}$ 。

- 用途: 實作模除法、解線性同餘、組合數除法、CRT 等。
- 求法: 擴展歐幾里得適用任意模數; 若 m 為質數可用 $a^{m-2} \pmod{m}$ 。
- 存在條件: 僅當 $\gcd(a, m) = 1$; 不互質時可除以 $d = \gcd(a, m)$ 後再檢查。

Chinese Remainder Theorem

設同餘系統

$$x \equiv a_i \pmod{m_i} \quad (i = 1, \dots, k),$$

其中 m_i 兩兩互質, 令 $M = \prod_{i=1}^k m_i$, $M_i = M/m_i$, 再取 $t_i \equiv M_i^{-1} \pmod{m_i}$ 。則唯一解(模 M)為

$$x \equiv \sum_{i=1}^k a_i M_i t_i \pmod{M}.$$

兩式合併 (允許非互質)

```

1 // solve x a1 (mod m1), x a2 (mod m2)
2 // return {x0, lcm}; if no solution, lcm = -1
3 pair<ll, ll> crt(ll a1, ll m1,
    ll a2, ll m2) {
4     ll g = std::gcd(m1, m2);
5     if ((a2 - a1) % g != 0) return {0, -1};
        // no solution
6
7     ll lcm = m1 / g * m2;
8     ll m1_reduced = m1 / g;
9     ll m2_reduced = m2 / g;
10
11    diff = (a2 - a1) / g % m2_reduced;
12    if (diff < 0) diff += m2_reduced;
13
14    inv = mod_pow(m1_reduced, m2_reduced
        - 1, m2_reduced);
15    step = diff * inv % m2_reduced;
16    ll x0 = (a1 + step * m1) % lcm;
17    if (x0 < 0) x0 += lcm;
18
19    return {x0, lcm};
20}

```

遞增地將每個同餘式與當前解做合併即可取得最終答案，也能偵測無解情況。給定 a, b, c ，求 $ax + by = c$ 的解

```

1  ll extgcd(ll a, ll b, ll c, ll &x, ll
2      &y){
3      if(b == 0){
4          x = c/a ;
5          y = 0 ;
6          return a ;
7      }
8      ll d = extgcd(b, a%b, c, x, y), tmp =
9          x ;
10     x = y ;
11     y = tmp - (a/b)*y ;
12     return d ;
13 }
```

2.2 Combinatorics

Binomial Coefficient Identities

$$\begin{aligned} \binom{n}{k} &= \frac{n!}{k!(n-k)!}, \\ \binom{n}{k} &= \binom{n-1}{k} + \binom{n-1}{k-1}, \\ \sum_{k=0}^n \binom{n}{k} &= 2^n, \quad \sum_{k=0}^n k \binom{n}{k} = n2^{n-1}. \end{aligned}$$

Stars and Bars 非負整數解數量：

$$x_1 + x_2 + \dots + x_k = n \Rightarrow \binom{n+k-1}{k-1}.$$

若各變數至少為 1，將 $x_i = y_i + 1$ 轉為非負情況即可。

Inclusion-Exclusion Principle 對集合 A_1, \dots, A_k ：

$$\left| \bigcup_{i=1}^k A_i \right| = \sum_{i=1}^k |A_i| - \sum_{1 \leq i < j \leq k} |A_i \cap A_j| - \dots + (-1)^{k-1} |A_1 \cap \dots \cap A_k|.$$

計算滿足限制的排列或整數解時廣泛使用。

Catalan Numbers 基本定義：

$$C_n = \frac{1}{n+1} \binom{2n}{n}, \quad C_{n+1} = \frac{4n+2}{n+2} C_n.$$

$$C = 1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, \dots$$

常見應用包含合法括號、凸多邊形三角剖分、二元樹結構計數等。

2.3 Geometry

對於 V 個點， E 條邊， F 個面， C 個連通分量

$$V + F = E + 2$$

$$V + F = E + C + 1$$

點座標均是整數或是正方形格子點的簡單多邊形，其面積 A 和內部點數量 i ，邊上格點數量 b 的關係為

$$A = i + \frac{b}{2} - 1$$

3 Data Structure

3.1 MST

```

1  struct Edge{
2      int u, v, w ;
3      // 這是最大生成樹，最小生成樹要改成 w < o.w
4      bool operator>(const Edge &o) const
5          {return w > o.w ;}
6  };
7  int par[N] ;
8  int sz[N] ;
9  int sum ;
10
11 vector<Edge> edge ;
12
13 void init(){
14     edge.clear() ;
15     for ( int i=0 ; i<N ; i++ ){
16         par[i] = i ;
17         sz[i] = 1 ;
18     }
19     sum = 0 ;
20 }
21
22 int find(int x){
23     if(x == par[x]) return x ;
24     return par[x] = find(par[x]) ;
25 }
26
27 int merge(int x, int y){
28     x = find(x) ;
29     y = find(y) ;
30
31     if(x == y) return 0 ;
32     if(sz[x] > sz[y]) swap(x, y) ;
33     par[x] = y ;
34     sz[y] += sz[x] ;
35
36     return 1 ;
37 }
38
39 void MST(){
40     int cnt = 0 ;
41     for ( int i=0 ; i<edge.size() && cnt < n-1
42             ; i++ ){
43         auto [u, v, w] = edge[i] ;
44         if(merge(u, v)){
45             cnt++ ;
46             sum -= w ;
47         }
48     }
49
50     int main(){
51         for ( int i=0 ; i<m ; i++ ){
52             scanf("%d%d%d", &u, &v, &w) ;
53             edge.push_back({u, v, w}) ;
54             sum += w ;
55         }
56
57         sort(edge.begin(), edge.end(),
58              greater<Edge>()) ;
59         MST() ;
60     }
61
62     if(l <= L && R <= r){
63         AddTag(id, tag) ;
64         return ;
65     }
66
67     push(id) ;
68     int M = (L + R) >> 1 ;
69     build(L, M, lc) ;
70     build(M+1, R, rc) ;
71
72     pull(id) ;
73     seg[id].sz = seg[lc].sz + seg[rc].sz ;
74 }
75
76 void modify(int l, int r, LazyTag &tag,
77             int L=1, int R=n, int id=1){
78     if(l <= L && R <= r){
79         AddTag(id, tag) ;
80         return ;
81     }
82
83     push(id) ;
84     int M = (L + R) >> 1 ;
85     if(r <= M) modify(l, r, tag, L, M,
86                         lc) ;
87     else if(l > M) modify(l, r, tag, M+1,
88                           R, rc) ;
89     else{
90         modify(l, r, tag, L, M, lc) ;
91         modify(l, r, tag, M+1, R, rc) ;
92     }
93
94     pull(id) ;
95 }
96
97 int query(int l, int r, int L=1, int R=n,
98           int id=1){
99 }
```

3.2 SegmentTree

```

1 #define lc (id << 1)
2 #define rc ((id << 1) | 1)
3
4 struct LazyTag{
5     // type 0 : increase val
6     // type 1 : set to val
7     // type 1 can overwrite type 0
8 }
```

```

78     if(l <= L && R <= r) return
79         seg[id].sum ;
80
81     push(id) ;
82     int M = (L + R) >> 1 ;
83     if(r <= M) return query(l, r, L, M,
84                               lc) ;
85     else if(l > M) return query(l, r,
86                                  M+1, R, rc) ;
87     else return query(l, r, L, M, lc) +
88             query(l, r, M+1, R, rc) ;
89
90 }tree ;

```

3.3 HLD

```

56 private:
57     void pull(int id){
58         // normal pull
59     }
60
61     void AddTag(int id, int tag){
62         // normal AddTag
63     }
64
65     void push(int id){
66         // normal push
67     }
68
69     void modify(int l, int r, int tag, int
70                 L=1, int R=n, int id=1){
71         // normal modify
72     }
73
74     ColorSeg query(int l, int r, int L=1, in
75                     R=n, int id=1){
76         // normal query
77     }
78 public:
79     void build(int L=1, int R=n, int id=1){
80         // normal build
81     }
82
83     // update val from u to v (simple path)
84     void update(int u, int v, int val){
85         while(top[u] != top[v]){
86             if(dep[top[u]] < dep[top[v]]) swap(u,
87                                         v) ;
88             modify(dfn[top[u]], dfn[u], val) ;
89             u = fa[top[u]] ;
90         }
91
92         if(dep[u] < dep[v]) swap(u, v) ;
93         modify(dfn[v], dfn[u], val) ;
94     }
95
96     // get sum from u to v (simple path)
97     int get(int u, int v){
98         pair<int, ColorSeg> U, V ;
99         ColorSeg M ;
100        U = {u, {0, 0, 0}} ;
101        V = {v, {0, 0, 0}} ;
102
103        while(top[U.first] != top[V.first]){
104            if(dep[top[U.first]] <
105                dep[top[V.first]]) swap(U, V) ;
106            U.second = query(dfn[top[U.first]],
107                             dfn[U.first]) + U.second ;
108            U.first = fa[top[U.first]] ;
109        }
110
111        if(dep[U.first] < dep[V.first]) swap(U,
112                                         V) ;
113
114        M = query(dfn[V.first], dfn[U.first])
115
116        return (U.second.tot + V.second.tot +
117                  M.tot) - (U.second.left == M.right
118                  - (V.second.left == M.left) ;
119    }
120 }tree ;
121
122 void init(){
123     memset(son, -1, sizeof(son)) ;
124 }

```

3.4 PST

```

6  class PersistentSegmentTree{
7  private:
8    int n ;
9    int cnt ;
10   vector<int> version ;
11
12  int build(int L, int R){
13    int cur_cnt = cnt++ ;
14    if(L == R){
15      seg[cur_cnt] = {0, 0, 0} ;
16      return cur_cnt ;
17    }
18
19    int M = (L + R) >> 1 ;
20    int lc = build(L, M) ;
21    int rc = build(M+1, R) ;
22
23    seg[cur_cnt] = {0, lc, rc} ;
24    return cur_cnt ;
25  }
26 public:
27 PersistentSegmentTree(int _n){
28   n = _n ;
29   cnt = 0 ;
30
31   int root = build(1, n) ;
32   version.push_back(root) ;
33 }
34
35 void update(int ver, int idx){
36   auto upd = [&](auto &self, const int
37                 cur, int L, int R){
38     int cur_cnt = cnt++ ;
39
40     if(L == R){
41       seg[cur_cnt] = {seg[cur].sum + 1, 0,
42                      0} ;
43       return cur_cnt ;
44     }
45
46     int M = (L + R) >> 1 ;
47     int lc = seg[cur].left ;
48     int rc = seg[cur].right ;
49
50     if(idx <= M) lc = self(self,
51                               seg[lc].left, L, M) ;
52     else rc = self(self, seg[rc].right,
53                    M+1, R) ;
54
55     seg[cur_cnt] = {seg[lc].sum +
56                     seg[rc].sum, lc, rc} ;
57
58     return cur_cnt ;
59   };
60
61   int root = upd(upd, version[ver], 1, n) ;
62   version.push_back(root) ;
63 }
64
65 int query(int verL, int verR, int k){
66   auto qry = [&](auto &self, const int
67                 cur_old, const int cur_new, int L,
68                 int R){
69     if(L == R) return L ;
70
71     int old_l = seg[cur_old].left, old_r =
72                seg[cur_old].right ;
73     int new_l = seg[cur_new].left, new_r =
74                seg[cur_new].right ;
75
76     int dl = seg[new_l].sum -
77              seg[old_l].sum ;
78     int dr = seg[new_r].sum -
79              seg[old_r].sum ;
80
81     int M = (L + R) >> 1 ;
82
83     if(k <= M) return self(self,
84                               seg[dl].left, L, M) ;
85     else return self(self, seg[dr].right,
86                      M+1, R) ;
87   };
88
89   int res = qry(qry, version[verL], 1, n, verR) ;
90
91   return res ;
92 }
```

```

72     if(dl >= k) return self(self, old_l,
73         new_l, L, M) ;
74     k -= dl ;
75     return self(self, old_r, new_r, M+1,
76         R) ;
77 }
78 int idx = qry(qry, version[verL-1],
79     version[verR], 1, n) ;
80 };
```

3.5 Trie

```

1 class TrieNode{
2 public:
3     set<int> end ;
4     TrieNode *next[26] ;
5
6     TrieNode(){
7         for ( int i=0 ; i<26 ; i++ ) next[i]
8             = nullptr ;
9     }
10
11 class Trie{
12 private:
13     int cnt ;
14     TrieNode *root ;
15 public:
16     Trie() : cnt(0) {
17         root = new TrieNode() ;
18     }
19
20     void insert(string &str, int n){
21         TrieNode* node = root ;
22         for ( auto s : str ){
23             int path = s - 'a' ;
24
25             if(node->next[path] == nullptr)
26                 node->next[path] = new
27                     TrieNode() ;
28             node = node->next[path] ;
29         }
30         node->end.insert(n) ;
31     }
32
33     void search(string &str){
34         TrieNode* node = root ;
35         for ( auto s : str ){
36             int path = s - 'a' ;
37             if(node->next[path] == nullptr)
38                 return ;
39             node = node->next[path] ;
40         }
41
42         int flg = 0 ;
43         for ( auto n : node->end ) {
44             if(flg) cout << " " ;
45             else flg = 1 ;
46             cout << n ;
47         }
48
49     void clear(TrieNode* node) {
50         if (!node) return ;
51         for (int i = 0; i < 26; i++) {
52             if (node->next[i]) {
53                 clear(node->next[i]) ;
54             }
55             delete node ;
56         }
57     ~Trie(){}
58 }
```

3.6 BIT 單修區查

```

1 // 單點修改 區間查詢
2 #define lowbit(x) (x & -x)
3
4 int BIT[MAX_SIZE] ;
5 int n ;
6
7 void modify(int idx, int val){
8     for ( ; idx <= n ; idx += lowbit(idx) ){
9         BIT[idx] += val ;
10    }
11 }
12
13 // ans: query(R) - query(L-1)
14 int query(int idx){
15     int sum = 0 ;
16     for ( ; idx ; idx -= lowbit(idx) ){
17         sum += BIT[idx] ;
18     }
19 }
20
21 void init(){
22     memset(BIT, 0, sizeof(BIT)) ;
23 }
```

3.7 BIT 區修單查

```

1 // 區間修改， 單點查詢
2 #define lowbit(x) (x & -x)
3
4 int BIT[MAX_SIZE] ;
5 int n ;
6
7 void modify(int idx, int val){
8     for ( ; idx <= n ; idx += lowbit(idx) ){
9         BIT[idx] += val ;
10    }
11 }
12
13 // ans: query(i)
14 int query(int idx){
15     int sum = 0 ;
16     for ( ; idx ; idx -= lowbit(idx) ){
17         sum += BIT[idx] ;
18     }
19
20     return sum ;
21 }
22
23 void init(){
24     memset(BIT, 0, sizeof(BIT)) ;
25 }
26
27 void build(){
28     arr[0] = 0 ;
29     for ( int i=1 ; i<=n ; i++ ) modify(i,
30             arr[i] - arr[i-1]) ;
31 }
32
33 // usage
34 // add val
35 modify(L, x) ;
36 modify(R+1, -x) ;
```

3.8 BIT 區修區查

```

1 // 區間修改 區間查詢
2 #define lowbit(x) x & -x
3
4 ll BIT1[MAXN], BIT2[MAXN] ;
5
6 void update(int idx, ll val){
7     for ( int i=idx ; i<=n ; i+=lowbit(i) ){
8         BIT1[i] += val ;
9         BIT2[i] += idx * val ;
10    }
11 }
12
13 // range query: query(R) - query(X - 1)
14 ll query(int idx){
15     ll sum1 = 0, sum2 = 0 ;
16     for ( int i=idx ; i ; i-=lowbit(i) ){
17         sum1 += BIT1[i] ;
18         sum2 += BIT2[i] ;
19     }
20
21     return (idx + 1) * sum1 - sum2 ;
22 }
23
24 void build(){
25     for ( int i=1 ; i<=n ; i++ ){
26         update(i, arr[i] - arr[i-1]) ;
27     }
28 }
29
30 void usage(){
31     update(L, x) ;
32     update(R+1, -x) ;
33 }
34
35 void init(){
36     memset(BIT1, 0, sizeof(BIT1)) ;
37     memset(BIT2, 0, sizeof(BIT2)) ;
38 }
```

4 Graph

4.1 cut vertex AND bridges

```

1 int dfn[Maxn] = {-1}, low[Maxn] = {-1},
2     dfscnt ;
3
4 void dfs(int u, int fa){
5     dfn[u] = low[u] = ++dfscnt ;
6     int child = 0 ;
7
8     for ( auto v : g[u] ) if(v != fa){
9         if(dfn[v] == -1){
10             child++ ;
11             dfs(v, u) ;
12             low[u] = min(low[u], low[v]) ;
13
14             if(low[v] >= dfn[u]){
15                 // this edge is a bridge
16             }
17
18             if(u != fa && low[v] >= dfn[u]){
19                 // this node v is a articulation point
20             }
21         }
22     }
23
24     if(u == fa && child > 1){
25         // this node u is a articulation point
26     }
27 }
```

4.2 SCC - Tarjan

4.3 BCC - Tarjan

```

1 struct Edge{
2     int v, next ;
3 }e[Maxm << 1] ;
4 int head[Maxm], tot = 1 ;
5
6 void add(int u, int v){
7     e[++tot] = {v, head[u]} ;
8     head[u] = tot ;
9     e[++tot] = {u, head[v]} ;
10    head[v] = tot ;
11 }
12
13 bitset<Maxm << 1> bz ;
14 vector<vector<int>> bcc ;

```

4.4 Convex

```
1 struct Coordinate{
2     long long x, y ;
3
4     friend bool operator<(const Coordinate&
5         const Coordinate& b){
6         if(a.x == b.x) return a.y < b.y ;
7         return a.x < b.x ;
8     }
9
10    friend bool operator==(const Coordinate&
11        const Coordinate& b){
12        return a.x == b.x && a.y == b.y ;
13    }
14    vector<Coordinate> nodes ;
15
16    long long cross(const Coordinate& o, const
17        Coordinate& a, const Coordinate& b){
```

4.5 Max Flow

```
1 struct Edge{
2     int v, cap, next ;
3 };
4
5 class MaxFlow{
6 private:
7     int N, S, T ;
8     vector<Edge> e ;
9     vector<int> head, cur, dep ;
10
11    bool bfs(){
12        queue<int> q ;
13        for ( int i=0 ; i<=N ; i++ ){
14            cur[i] = head[i] ;
15            dep[i] = -1 ;
16        }
17
18        q.push(S) ;
19        dep[S] = 0 ;
20
21        while(!q.empty()){
22            int u = q.front() ; q.pop() ;
23
24            for ( int i=head[u] ; i!=-1 ;
25                  i=e[i].next ){
26                int v = e[i].v ;
27                if(dep[v] == -1 && e[i].cap > 0){
28                    dep[v] = dep[u] + 1 ;
29                    if(v == T) return 1 ;
30                    q.push(v) ;
31                }
32            }
33        }
34    }
35
36    int dfs(int u, int t, int f){
37        if(u == t) return f ;
38        for ( int i=head[u] ; i!= -1 ;
39              i=e[i].next ){
40            int v = e[i].v ;
41            if(dep[v] == dep[u]+1 && e[i].cap > 0){
42                int d = dfs(v, t, min(f, e[i].cap)) ;
43                if(d > 0){
44                    e[i].cap -= d ;
45                    e[i^1].cap += d ;
46                    return d ;
47                }
48            }
49        }
50        return 0 ;
51    }
52
53    int maxFlow(){
54        int s = S, t = T ;
55        int f = 0 ;
56
57        while(1){
58            if(bfs() == 0) break ;
59            f += dfs(s, t, INT_MAX) ;
60        }
61
62        return f ;
63    }
64}
```

```

30     }
31 }
32 }
33 return 0 ;
34 }
35 }
36
37 int dfs(int u, int flow){
38   if(u == T) return flow ;
39   int d, rest = 0 ;
40
41   for ( int &i=cur[u] ; i!=-1 ;
42     i=e[i].next ){
43     int v = e[i].v ;
44     if(dep[v] == dep[u] + 1 && e[i].cap >
45       0){
46       d = dfs(v, min(flow - rest,
47                 e[i].cap)) ;
48
49       if(d > 0){
50         e[i].cap -= d ;
51         e[i^1].cap += d ;
52         rest += d ;
53
54         if(rest == flow) break ;
55       }
56
57     if(rest != flow) dep[u] = -1 ;
58   return rest ;
59 }
60
61 public:
62 MaxFlow(int n, int s, int t){
63   N = n ; S = s ; T = t ;
64   e.reserve(n*n) ;
65   head.assign(n+1, -1) ;
66   cur.resize(n+1) ;
67   dep.resize(n+1) ;
68 }
69
70 void AddEdge(int u, int v, int cap){
71   e.push_back({v, cap, head[u]}) ;
72   head[u] = e.size() - 1 ;
73   e.push_back({u, 0, head[v]}) ;
74   head[v] = e.size() - 1 ;
75 }
76
77 int run(){
78   int ans = 0 ;
79   while(bfs()){
80     ans += dfs(S, 0x3f3f3f3f) ;
81   }
82   return ans ;
83 }
```

4.6 min cut max flow

```

1 struct Edge{
2   int v, cap, cost , next ;
3 };
4
5 using pii = pair<int, int> ;
6 class MCMF{
7   private:
8   int N, s, t, tot ;
9   vector<Edge> e ;
10  vector<int> head ;
11
12  public:
13  MCMF(int n, int _s, int _t){
14    N = n ;
15    s = _s ;
16    t = _t ;
17    e.resize(n*n + 5) ;
18    head.assign(n+5, -1) ;
19    tot = -1 ;
20  }
21
22  int dfs(int u, int flow){
23   if(u == T) return flow ;
24   int d, rest = 0 ;
25
26   for ( int &i=cur[u] ; i!=-1 ;
27     i=e[i].next ){
28     int v = e[i].v ;
29     if(dep[v] == dep[u] + 1 && e[i].cap >
30       0){
31       d = dfs(v, min(flow - rest,
32                 e[i].cap)) ;
33
34       if(d > 0){
35         e[i].cap -= d ;
36         e[i^1].cap += d ;
37         rest += d ;
38
39         if(rest == flow) break ;
40       }
41
42     if(rest != flow) dep[u] = -1 ;
43   return rest ;
44 }
45
46 public:
47 MaxFlow(int n, int s, int t){
48   N = n ; S = s ; T = t ;
49   e.reserve(n*n) ;
50   head.assign(n+1, -1) ;
51   cur.resize(n+1) ;
52   dep.resize(n+1) ;
53 }
54
55 void AddEdge(int u, int v, int cap){
56   e.push_back({v, cap, head[u]}) ;
57   head[u] = e.size() - 1 ;
58   e.push_back({u, 0, head[v]}) ;
59   head[v] = e.size() - 1 ;
60 }
61
62 int run(){
63   int ans = 0 ;
64   while(bfs()){
65     ans += dfs(S, 0x3f3f3f3f) ;
66   }
67   return ans ;
68 }
```

```

19   }
20 }
21 void AddEdge(int u, int v, int cap, int
22   cost){
23   e[++tot] = {v, cap, cost, head[u]} ;
24   head[u] = tot ;
25   e[++tot] = {u, 0, -cost, head[v]} ;
26   head[v] = tot ;
27 }
28
29 int run(){
30   vector<int> dis(N+1), pot(N+1, 0),
31   preE(N+1) ;
32   int flow = 0, cost = 0 ;
33
34   auto dijkstra = [&](){
35     fill(dis.begin(), dis.end(), INF) ;
36     priority_queues<pii, vector<pii>,
37       greater<pii>> pq ;
38     dis[s] = 0 ;
39     pq.push({0, s}) ;
40
41     while(!pq.empty()){
42       auto [d, u] = pq.top() ; pq.pop() ;
43       if(d > dis[u]) continue ;
44       for ( int i=head[u] ; i!=-1 ;
45         i=e[i].next ){
46         int v = e[i].v, cap = e[i].cap, w =
47           e[i].cost ;
48         if(cap && dis[v] > d + w + pot[u] -
49           pot[v]){
50           dis[v] = d + w + pot[u] - pot[v] ;
51           preE[v] = i ;
52           pq.push({dis[v], v}) ;
53         }
54       }
55
56       return dis[t] != INF ;
57     };
58
59   while(dijkstra()){
60     for ( int v=1 ; v<=N ; v++ ) if(dis[v]
61       < INF){
62       pot[v] += dis[v] ;
63     }
64
65     int aug = INT_MAX ;
66     for ( int v=t ; v!=s ;
67       v=e[preE[v]^1].v ){
68       aug = min(aug, e[preE[v]].cap) ;
69     }
70
71     for ( int v=t ; v!=s ;
72       v=e[preE[v]^1].v ){
73       e[preE[v]].cap -= aug ;
74       e[preE[v]^1].cap += aug ;
75       cost += aug * e[preE[v]].cost ;
76     }
77   }
78
79   return cost ;
80 }
81
82
83 while(cur < str.size()){
84   if(str[cur - 1 ] == str[check])
85     Next[cur++] = ++check ;
86   else if(check > 0) check =
87     Next[check] ;
88   else Next[cur++] = 0 ;
89 }
90
91 int main(){
92   ios::sync_with_stdio(false) ;
93   cin.tie(nullptr) ;
94   cout.tie(nullptr) ;
95
96   string s1, s2 ;
97   while(cin >> s1){
98     s2 = s1 ;
99     reverse(s2.begin(), s2.end()) ;
100    kmp(s2) ;
101
102    int x=0, y=0 ;
103    while(x < s1.size() && y < s2.size()){
104      if(s1[x] == s2[y]){
105        x++ ;
106        y++ ;
107      }
108      else if(y > 0) y = Next[y] ;
109      else x++ ;
110    }
111
112    cout << s1 << s2.substr(y) << endl ;
113  }
114
115  return 0 ;
116 }
```

5.2 ACAM

```

1 class ACAutomaton{
2   private:
3   vector<int> fail, end, order ;
4   vector<vector<int>> tree ;
5
6   int base, alpha ;
7
8   int new_node(){
9     tree.emplace_back(alpha, 0) ;
10    fail.push_back(0) ;
11
12    return tree.size() - 1 ;
13  }
14
15 public:
16  ACAutomaton(int _base='a', int _alpha=26)
17    : base(_base), alpha(_alpha) {
18      clear() ;
19    }
20
21  void clear(){
22    fail.assign(1, 0) ;
23    order.clear() ;
24    end.clear() ;
25    tree.assign(1, vector<intvoid add_pattern(const string &pattern){
29    int u = 0 ;
30    for ( auto ch : pattern ){
31      int v = ch - base ;
32
33      if(tree[u][v] == 0) tree[u][v] =
34        new_node() ;
35      u = tree[u][v] ;
36
37      end.push_back(u) ;
38    }
39  }
```

5 String

5.1 KMP

```

1 int Next[N] ;
2 void kmp(string &str){
3   Next[0] = -1 ;
4   if(str.size() <= 1) return ;
5   Next[1] = 0 ;
6
7   int cur = 2, check = 0 ;
```

```

void build(){
    queue<int> q ;
    order.clear() ;
    order.push_back(0) ;

    for ( int i=0 ; i<alpha ; i++ )
        if(tree[0][i] > 0){
            q.push(tree[0][i]) ;
        }
}

while(!q.empty()){
    int u = q.front() ; q.pop() ;
    order.push_back(u) ;

    for ( int i=0 ; i<alpha ; i++ ){
        if(tree[u][i] == 0) tree[u][i] =
            tree[fail[u]][i] ;
        else{
            fail[tree[u][i]] = tree[fail[u]][i]
            ;
            q.push(tree[u][i]) ;
        }
    }
}
}

vector<int> count_per_pattern(const string
    &text) const {
int u = 0 ;
vector<int> vis(tree.size(), 0) ;

for ( char ch : text ){
    u = tree[u][ch - base] ;
    vis[u]++;
}

for ( int i=order.size()-1 ; i>=1 ; i-- ){
    int x = order[i] ;
    vis[fail[x]] += vis[x] ;
}

vector<int> ans(end.size(), 0) ;
for ( int id=0 ; id<end.size() ; id++ ){
    ans[id] = vis[end[id]] ;
}

return ans ;
}

```

6 Techniques

6.1 二分搜

```

// xxxxxxxx 找最小解
bool binary_search(){
    while(l < r){
        int m = (l + r) >> 1 ;
        if(check(m)) r = m ;
        else l = m + 1 ;
    }

    return l ;
}

// oooooxxx 找最大解
bool binary_search(){
    while(l < r){
        int m = (l + r) >> 1 ;
        if(check(m)) l = m ;
        else r = m - 1 ;
    }

    return l ;
}

int u, v ;
scanf("%d%d", &u, &v) ;
e[u].push_back(v) ;
e[v].push_back(u) ;
}

dfs(root, root, 0) ;

while(q--){
    int u, v ;
    scanf("%d%d", &u, &v) ;
    printf("%d\n", lca(u, v)) ;
}

return 0 ;
}

```

6.3 SO

6.2 倍增 LCA

```
1 #include <bits/stdc++.h>
2
3 using namespace std ;
4
5 const int Maxn = 500005 ;
6
7 vector<int> e[Maxn] ;
8 int depth[Maxn] ;
9 int up[Maxn][40] ;
10 int MaxLog ;
11
12 void dfs(int u, int from, int d){
13     up[u][0] = from ;
14     depth[u] = d ;
15
16     for ( int i=1 ; i<=MaxLog ; i++ ){
17         up[u][i] = up[up[u][i - 1]][i - 1] ;
18     }
19
20     for ( auto v : e[u] ){
21         if(v == from) continue ;
22         dfs(v, u, d + 1) ;
23     }
24 }
25
26 int lca(int u, int v){
27     if(depth[u] < depth[v]) swap(u, v) ;
28
29     for ( int i=MaxLog ; i>=0 ; i-- )
30         if(depth[u] - (1 << i) >= depth[v])
31             u = up[u][i] ;
32
33     if(u == v) return u ;
34
35     for ( int i=MaxLog ; i>=0 ; i-- )
36         if(up[u][i] != up[v][i]){
37             u = up[u][i] ;
38             v = up[v][i] ;
39         }
40
41     return up[u][0] ;
42 }
```

```

1 long long SG(long long k){
2
3     if(k % 2 == 0){
4         return k / 2;
5     }
6     else{
7         return SG(k / 2);
8     }
9 }
10 }
11
12 int main(){
13     int cas, n;
14
15     scanf("%d", &cas);
16     while(cas--){
17         scanf("%d", &n);
18
19         long long s, v = 0;
20
21         for(int i = 0; i < n; i++){
22             scanf("%lld", &s);
23             v ^= SG(s); //XOR
24         }
25
26         if(v) printf("YES\n");
27         else printf("NO\n");
28     }
29 }
30
31 int SG[30] ;
32 int vis[Maxn], stone[Maxn] ;
33
34 void build(){
35     SG[0] = 0 ;
36     memset(vis, 0, sizeof(vis)) ;
37
38     for ( int i=1 ; i<30 ; i++ ){
39         int cur = 0 ;
40         for ( int j=0 ; j<i ; j++ ) for ( int
41             k=0 ; k<=j ; k++ ){
42             vis[SG[j] ^ SG[k]] = i ;
43         }
44         while(vis[cur] == i) cur++ ;
45         SG[i] = cur ;
46     }
47 }
48
49 int main(){
50     build() ;
51
52     int T = 0 ;
53     while(~scanf("%d", &n) && n){
54         int ans = 0 ;
55
56         for ( int i=1 ; i<=n ; i++ ) scanf("%d",
57             &stone[i]) ;
58
59         for ( int i=1 ; i<=n ; i++ ) if(stone[i]
60             & 1){
61             ans ^= SG[n-i] ;
62         }
63     }
64 }
```

7 DR

7.1 輪廓線 DP

```
1 #include <bits/stdc++.h>
2
3 using namespace std ;
4 using ll = long long ;
5
6 ll dp[2][(1 << 10) + 5] ;
7 int n, m ;
```

```

8 int cur ;
9
10 void update(int s1, int s2){
11     if(s2 & (1 << m)){
12         dp[cur][s2 ^ (1 << m)] += dp[cur ^ 1][s1] ;
13     }
14 }
15
16 int main(){
17     while(~scanf(" %d%d", &n, &m)){
18         if(m > n) swap(n, m) ;
19         memset(dp, 0, sizeof(dp)) ;
20         cur = 0 ;
21         dp[cur][(1 << m) - 1] = 1 ;
22         for ( int i=0 ; i<n ; i++ ) for ( int
23             j=0 ; j<m ; j++ ){
24             cur ^= 1 ;
25             memset(dp[cur], 0, sizeof(dp[cur])) ;
26
27             for ( int k=0 ; k<(1 << m) ; k++ ){
28                 update(k, k << 1) ; // not put
29                 if(i && !(k & (1 << (m - 1)))) {
30                     update(k, (k << 1) | (1 << m) |
31                     1) ; // put up
32                     if(j && !(k & 1)) update(k, (k << 1)
33                     | 3) ; // put left
34                 }
35             }
36             printf("%lld\n", dp[cur][(1 << m) - 1]) ;
37         }
38         return 0 ;
39     }
}

```

7.2 數位 DP

```

1 #include <bits/stdc++.h>
2
3 using namespace std ;
4
5 int K ;
6 int dp[20][105][105][2] ;
7 vector<int> dig ;
8
9 int solve(int pos, int sum, int dsum, bool
10    lim){
11    if(pos == -1){
12        if(sum == 0 && dsum == 0) return 1 ;
13        return 0 ;
14    }
15
16    int &d = dp[pos][sum][dsum][lim] ;
17    if(d != -1) return d ;
18
19    int up = lim ? dig[pos] : 9 ;
20    int res = 0 ;
21    for ( int i=0 ; i<=up ; i++ ){
22        res += solve(pos-1, (sum * 10 + i) %
23            K, (dsum + i) % K, lim && i==up)
24            ;
25    }
26
27    return d = res ;
28 }
29
30 int count(int n){
31     memset(dp, -1, sizeof(dp)) ;
32     dig.clear() ;
33
34     while(n > 0){
35         dig.push_back(n % 10) ;
36         n /= 10 ;
37     }
38
39     return solve(dig.size() - 1, 0, 0, 1) ;
40 }

```

```

39 int main(){
40     int T ;
41     scanf("%d", &T) ;
42
43     int a, b ;
44     while(T--){
45         scanf("%d%d%d", &a, &b, &K) ;
46         if(K > 90) printf("0\n") ;
47         else printf("%d\n", count(b) -
48             count(a-1)) ;
49     }
50 }
51

```

```

54
55     int q, e ;
56     scanf("%d", &q) ;
57
58     while(q--){
59         scanf("%d", &e) ;
60
61         for ( int i=n ; i>=1 ; i-- )
62             if(dp[0][i][0] <= e){
63                 printf("%d\n", i) ;
64                 break ;
65             }
66     }
67
68     return 0 ;
69 }

```

7.3 樹 DP

```

1 #include <bits/stdc++.h>
2
3 #define N 505
4 #define INF 0x3f3f3f3f
5
6 using namespace std ;
7
8 struct Edge{
9     int v, w ;
10}
11
12 vector<Edge> edge[N] ;
13 int n ;
14 int cnt[N] ;
15 int dp[N][N][2] ;
16
17 void init(){
18     for ( int i=0 ; i<N ; i++ )
19         edge[i].clear() ;
20     memset(cnt, 0, sizeof(cnt)) ;
21     memset(dp, INF, sizeof(dp)) ;
22 }
23
24 void DFS(int u){
25     cnt[u] = 1 ;
26     for ( auto [v, w] : edge[u] ){
27         DFS(v) ;
28         cnt[u] += cnt[v] ;
29     }
30
31     dp[u][1][0] = dp[u][1][1] = 0 ;
32
33     for ( auto [v, w] : edge[u] ){
34         for ( int i=cnt[u] ; i>1 ; i-- ) for (
35             int j=1 ; j<i && j<=cnt[v] ; j++ ){
36             dp[u][i][1] = min(dp[u][i][1],
37                 dp[u][i-j][1] + dp[v][j][1] + 2 *
38                 w) ;
39             dp[u][i][0] = min(dp[u][i][0],
40                 dp[u][i-j][1] + dp[v][j][0] + w) ;
41             dp[u][i][0] = min(dp[u][i][0],
42                 dp[u][i-j][0] + dp[v][j][1] + 2 *
43                 w) ;
44         }
45     }
46 }
47
48 int main(){
49     int t = 0 ;
50
51     while(~scanf(" %d", &n) && n){
52         init() ;
53         for ( int i=0 ; i<n-1 ; i++ ){
54             int u, v, w ;
55             scanf("%d%d%d", &v, &u, &w) ;
56             edge[u].push_back({v, w}) ;
57         }
58
59         DFS(0) ;
60         printf("Case %d:\n", ++t) ;
61     }
62 }

```