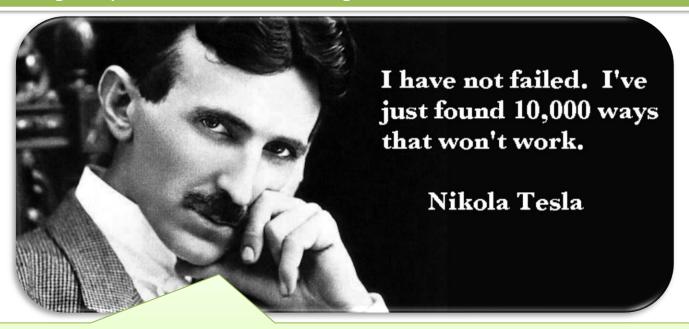


Arguments & Truth Tables

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# **Critical Thinking Quote of the Class**

Nikola Tesla was a Serbian American inventor, electrical engineer, mechanical engineer, and futurist. Most well known for harnessing light, inventing x-rays, radio, and alternating current.



Even when our efforts don't seem to provide results, that doesn't mean we've failed or should give up! Consider them part of the process of <u>finding what does work.</u>



# Arguments! What are they?

- Arguments are one of the ways used to settle issues.
- The process of an argument is actually where 2 or more people are debating (responding to each other) and making arguments on a particular topic.
  - Moving away from just stating claims but actually defending these claims by providing reasons.
- Arguments are actually claims backed by reasons that are supported by some form of evidence.
- Arguments attempt to support a claim by giving reasons for believing it (the *premises*).
- The issue is "Whether or not the claim is acceptable given the reasons."



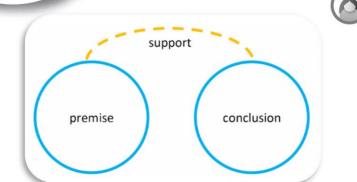
- A claim is a sentence that is used to make a claim capable of being true or false.
- Claims are the basic units of <u>arguments</u>.
- An argument is a set of claims (2 claims)
   where a premise, supports another
   (particular one) of them called the
   conclusion.





- A conclusion is:
  - A claim, and
  - Supported by one or more premises.

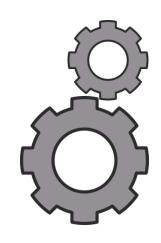
- A <u>premise</u> is:
  - A claim too, and
  - Used as a reason for believing the conclusion.





Each of the following <u>premises</u> are highlighted in <u>blue</u> and conclusion in red.

- 1. My 1:30pm train was cancelled because it was involved in an accident at 1:20pm.
- 2. Jane likes blue so her sister likes blue too.
- 3. I study hard because I want a good job.
- 4. The PlayStation network is down <u>because</u> hackers broke in and stole all the data.



A claim used as a reason for believing the conclusion.

# Quick Thinking Task! Premise/Conclusion

An argument has a premise and a conclusion. The premise supports the conclusion! (sometimes the conclusion can be  $2^{nd!}$ )



### For example:

Jack is taller than Paul, and Paul is taller than Jill.

Therefore, Jack is taller than Jill.

Which is the premise?

Which is the conclusion?

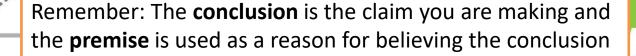




### Do Video Games Make People More Violent?

- A 2011 study by the Center for European Economic Research found that although violent video games might increase aggression they also have a paradoxical effect of reducing crime.
- This is possibly because the time spent playing games reduces time spent engaged in more antisocial actives.

The study states that: violent video games "paradoxically may reduce violence while increasing the aggressiveness of individuals by simply shifting these individuals out of alternative activities where crime is more likely to occur."





## Do Video Games Make People More Violent?



Let's spend 10 minutes to analyse the previous research.

Can you suggest 2 arguments either for, or against?

Premise	Conclusion



- Do Video Games Make People More Violent?
- The catharsis explanation on the impact of violent video game is based on the economic theory of time use
- What arguments did you find in this research paper? List any least two
  of them.



Please enter the code

1234 5678

Submit

The code is found on the screen in front of you



#### **Truth Tables**

## ... Why do we need them?

It is often difficult to determine the **validity** of long and/or complex arguments by just reading them!

### Truth tables provide:

- A visual way to see relationships between claim variables
- Ways to determine validity









- There are two kinds of truth tables
  - Long Truth Table
  - Short Truth Table



- Development of a long truth table normally takes more time...
- A short truth table can be done faster than a long truth table but you need to think critically!



### Example:

Tina is tall	John is tall
T	T
T	F
F	Т
F	F

Meaning	Meaning
Tina is tall	John is tall
Tina is tall	John is not tall (short)
Tina is not tall (short)	John is tall
Tina is not tall (short)	John is not tall (short)

# Logic and Types of Claims

 There are 4 logic operations that are being used in truth functional arguments:

- Negation NOT
- Conjunction AND
  - Disjunction OR
- The Conditional IF,THEN

# Negation (Not) ~

Whatever truth value a claim may have, the negation will result in the other value.

- Example, let p = Tina is tall
  - Then **not** (Tina is tall) = Tina is short
- '~p' represents 'not p'

р	~p (i.e., not p)
T	F
F	Т

p = Tina is tall



- A conjunction is a compound claim made up of two simpler claims
- Example, Tina is tall and John is short
- '●' represents 'and' (sometimes ∧ is used)

р	q	p • q
Т	Т	Т
Т	F	F
F	Т	F
F	F	F

p = Tina is tall

q = John is short

True value is when both claims are True, all other times False



A disjunction is a compound claim made up of two simpler claims

- Example, Tina is tall or John is short
- 'V' represents 'or'

р	q	p V q
Т	Т	Т
Т	F	Т
F	Т	Т
F	F	F

False value is when both claims are False, all other times True



- A conditional is a compound claim made up of two simpler claims
- E.g. If Jack is my son, Jack is younger than me
- '→' represents the conditional operator

р	q	$p \rightarrow q$
Т	Т	Т
Т	F	F
F	Т	Т
F	F	Т

False value is when the first claims is True and the second claims is False, all others True



- 1. **Summarise** the argument
- 2. Calculate the number of rows
- 3. **Draw** the table
- 4. Fill the table
- 5. Identify whether the argument is valid or invalid





# Steps Involved in a Long Truth Table

#### 1. Summarise the argument (cont.)

- Firstly create a single variable code for each, something that relates to the claim/s used... apple = a.
- Use the logical operators we looked at earlier: ~/V / / →
- Michael does NOT like apple = ~a
- Michael likes apple OR banana = a V b
- Michael likes apple AND banana = a b
- IF Michael likes apple, THEN he likes banana =  $a \rightarrow b$

# Steps Involved in a Long Truth Table

#### 2. Calculate the number of rows that table needs:

The number of rows =  $2^n$ 

**n** is the number of **variables** that you have when you summarise the argument.

If there is positive and negative of a variable you should only count it once: **a and ~a** are both count as one variable

$$2^2 = 4$$

$$2^3 = 8$$

$$2^4 = 16$$



3. Draw the table. List all variables as a single form then list premises and the conclusion.

Michael does not like apple =  $^{\sim}a$  (p1)

Michael likes apple OR banana = a V b (p2)

Therefore, Michael likes banana = b (c)

Number of rows:  $2^2 = 4$ 

а	b	~a <sub>p1</sub>	aVb <sub>p2</sub>	b <sub>c</sub>



#### 4. Fill the first column:

First column always gets TRUE for half of the number of rows and FALSE for the other half

Number of rows = 4 (first column gets 2 trues and 2 false) Number of rows = 8 (first column gets 4 trues and 4 false) Number of rows = 16 (first column gets 8 trues and 8 false)

а	b	~a <sub>p1</sub>	aVb <sub>p2</sub>	b <sub>c</sub>
Т				
Т				
F				
F				



#### 4. Fill the next column:

- If column 1 has 2 T and 2 F the next column needs to have 1 T and 1 F.
- If column 1 has 4 T and 4 F the next column needs to have 2 T and 2 F.
- If column 1 has 8 T and 8 F the next column needs to have 4 T and 4 F.

а	b	~a <sub>p1</sub>	aVb <sub>p2</sub>	b <sub>c</sub>
Т	Т			
Т	F			
F	Т			
F	F			



#### 4. Fill the table cells:

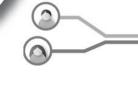
#### **Apply operations:**

Negation (~) when T then ~T = F

Conjunction (●) The only T answer is when both variables are T Disjunction (V) The only F answer is when both variables are F Conditional (→) The only F answer is when the first variable is T and the second variable is F

а	b	~a <sub>p1</sub>	aVb <sub>p2</sub>	b <sub>c</sub>
Т	Т	F	Т	Т
Т	F	F	Т	F
F	Т	Т	Т	Т
F	F	Т	F	F





Exercise: Let's tackle a long truth table for this new argument!

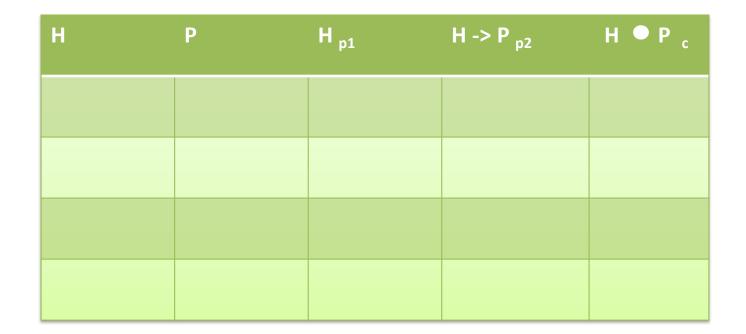
Angela is hungry
If Angela is hungry, she eats pizza
Therefore, Angela is hungry and eats pizza

#### Answer:

Angela is hungry H

If Angela is hungry, she eats pizza H → P

Therefore, Angela is hungry and eats pizza H • P





Answer: Fill the table for Angela's Argument

Н	Р	H <sub>p1</sub>	H -> P <sub>p2</sub>	H⊕P c
Т	Т	Т	Т	Т
Т	F	Т	F	F
F	Т	F	Т	F
F	F	F	Т	F

Valid or invalid argument? Find out next slide!



# Steps Involved in a Long Truth Table

#### 5. Find whether an argument is valid or invalid

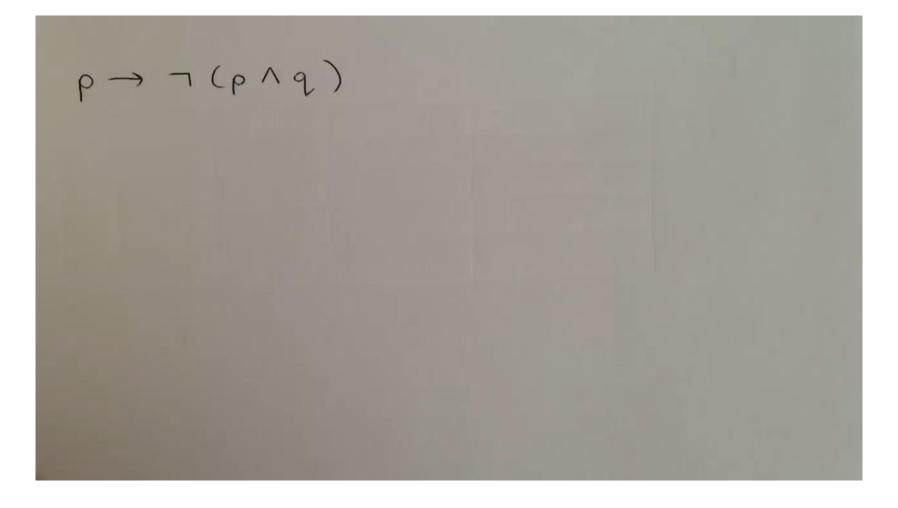
**REMEMBER:** an argument is invalid when it has a false conclusion and all premises true.

If you find the conclusion that is F when all premises are T the argument is invalid; otherwise it is valid.

	н	Р	H <sub>p1</sub>	H -> P <sub>p2</sub>	H⊕P c
	Т	Т	Т	Т	Т
Valid!	Т	F	Т	F	F
	F	Т	F	Т	F
	F	F	F	Т	F

Based on above truth table, is this argument valid or invalid?

# Let us watch another demo







 We will use our example from earlier to conduct the short truth table.

Michael does not like apple = ~a (p1) Michael likes apple OR banana = a V b (p2) Therefore, Michael likes banana = b (c)

а	b	~a pl	aVb <sub>p2</sub>	b c



# 1. Draw a table with only one row (Excluding Header)

In header list single variables first then premises and at the end conclusion(same as long truth table)

а	b	~a pl	aVb <sub>p2</sub>	b c

# Steps to Develop a Short Truth Table

### 2. First assume that this is an invalid argument

**REMEMBER**: an argument is invalid when it has a **false conclusion** and all **premises true** 

а	b	~a <sub>p1</sub>	aVb <sub>p2</sub>	b c
		Т	T	F

### 3. Fill the empty cells by considering second step

а	b	~a <sub>p1</sub>	aVb <sub>p2</sub>	b c
F	F	T	Т	F



4. Check whether your assumption (invalid) is correct or not by finding a conflict in the table.

If you have found the **conflict** it means your assumption is not correct therefore the argument is **Valid**.

а	b	~a pl	aVb <sub>p2</sub>	b c
F	F	Τ	Τ	F

In this case a V b (p2) should be False. Why? Because (F V F = F) all other times its True! Valid!

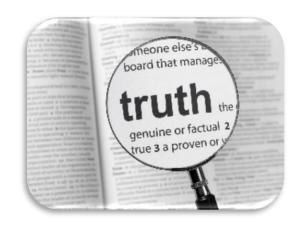
### Let us watch another demo

$$p \rightarrow q q \rightarrow r : p \rightarrow r$$

Valid argument: **true** premises lead to **true** conclusion Invalid argument: **true** premises lead to **false** conclusion



- 1. Draw a table with only 1 row (Consider heading)
- 2. Assume that the argument is invalid (F conclusion and T premises)
- 3. Fill empty cells by considering second step
- 4. Check whether your assumption (invalid) is correct or not by finding a conflict in your table.





### In Conclusion...

- Arguments attempt to support a claim by giving reasons for believing it (the premises).
- An argument normally contains 2 parts.
  - Each part is a claim.
  - One part is called the premise, and;
  - The second part is called the conclusion.
- A conclusion is:
  - A claim, and supported by one or more premises.
- A premise is:
  - A claim too, and used as a reason for believing the conclusion.
- Truth tables are a tool to help us to check whether an argument is valid or not.



