

Complex numbers and templating

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Complex numbers

1. Complex numbers

```
#include <complex>

complex<float> f;
f.re = 1.; f.im = 2.;
complex<double> d(1.,3.);

using std::complex_literals::i;
std::complex<double> c = 1.0 + 1i;

conj(c); exp(c);
```

Complex Newton

Exercise 1

Rewrite your Newton program so that it works for complex numbers:

```
complex<double> z{.5,.5};  
while ( true ) {  
    auto fz = f(z);  
    cout << "f( " << z << " ) = " << fz << '\n';  
    if (std::abs(fz)<1.e-10 ) break;  
    z = z - fz/fprime(z);  
}
```

You may run into the problem that you can not operate immediately between a complex number and an integer. Use `static_cast`.

Templated functions

You can templatize your Newton function and derivative:

```
template<typename T>
T f(T x) { return x*x - 2; };
template<typename T>
T fprime(T x) { return 2 * x; };
```

and then write

```
double x{1.};
while ( true ) {
    auto fx = f<double>(x);
    cout << "f( " << x << " ) = " << fx << '\n';
    if (std::abs(fx)<1.e-10 ) break;
    x = x - fx/fprime<double>(x);
}
```

Exercise 2

Update your Newton program with templates. If you have it working for `double`, try using `complex<double>`. Does it work?

Exercise 3

Use your complex Newton method to compute $\sqrt{2}$. Does it work?

Exercise 4

Can you templatize your Newton code that used lambda expressions? Your function header would now be:

```
template<typename T>
T newton_root
    ( function< T(T) > f,
      function< T(T) > fprime,
      T init) {
```

You would for instance compute $\sqrt{2}$ as:

```
cout << "sqrt -2 = " <<
    newton_root<complex<double>>
        ( [] (complex<double> x) {
            return x*x + static_cast<complex<double>>(2); },
          [] (complex<double> x) {
            return x * static_cast<complex<double>>(2); },
          complex<double>{.1,.1}
        )
    << '\n';
```