

1. In recent lectures we spoke about computing *vertex* normals by taking the “average” of the normals of all polygons incident to the vertex. We then suggested two refinements of this by applying a weighting to each normal so that some would be more important than others. Then if a vertex  $v$  had incident polygons  $p_1, \dots, p_n$  with normals  $\mathbf{N}_1 = \mathbf{n}_1/|\mathbf{n}_1|, \dots, \mathbf{N}_n = \mathbf{n}_n/|\mathbf{n}_n|$ , respectively, we would replace the vertex normal calculations

$$\mathbf{n}_v = \frac{1}{n} \sum_{i=1}^n \mathbf{N}_i$$

and (after normalizing)

$$\mathbf{N}_v = \frac{\mathbf{n}_v}{|\mathbf{n}_v|} = \frac{1}{n} \sum_{i=1}^n \mathbf{N}_i \times \frac{n}{|\sum_{i=1}^n \mathbf{N}_i|}$$

with

$$\mathbf{n}_v = \sum_{i=1}^n w_i \mathbf{N}_i$$

where  $w_i$  is a weighting term. The two weights we mentioned were:

- $w_i$  is the area of  $p_i$
- $w_i$  is the angle of the two sides of  $p_i$  at  $v_i$

Show how to compute these two weighting functions.