Sistemi Operativi I

Corso di Laurea in Informatica 2023-2024



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Paging + Segmentation

- Paging (OS' view of memory)
 - Divide memory into fixed-size pages and map them to physical frames
- Segmentation (compiler's view of memory)
 - Divide process into logical segments (e.g., code, data, stack, heap)
- Combine paging with segmentation
 - Segmented Paging

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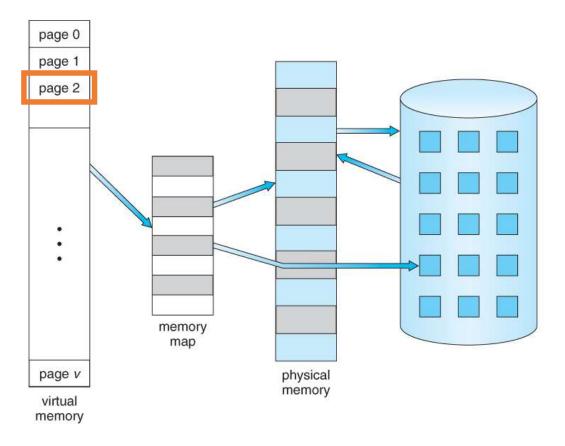
Virtual Memory uses backing storage (i.e., disk) to store unused pages and give the illusion of infinite virtual address space

• The ability to load only the portions of processes that are actually needed (and only when needed) from disk has several benefits:

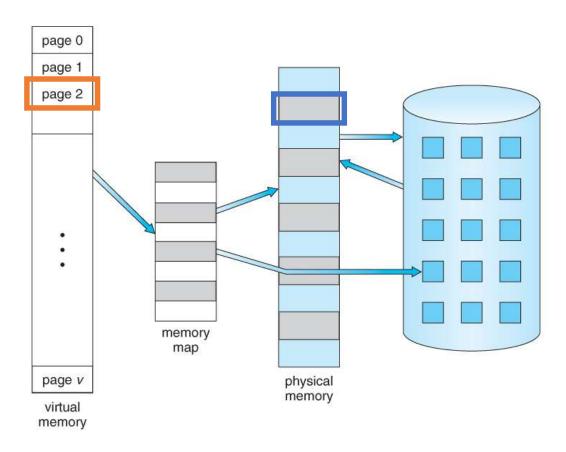
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 - Less I/O is needed for swapping processes in and out of memory, speeding things up

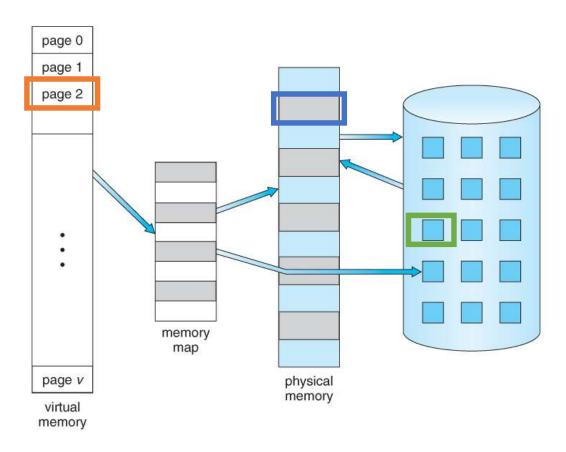


At any given time, each page can be:



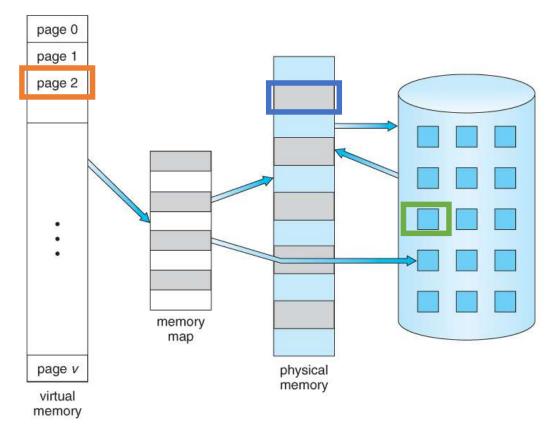
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in memory (physical frame)



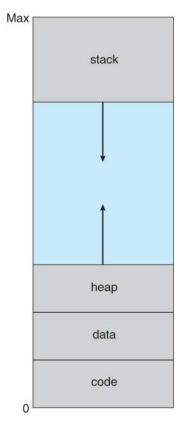
At any given time, each page can be: in memory (physical frame) on backing store (disk)

virtual memory can be much larger than physical memory



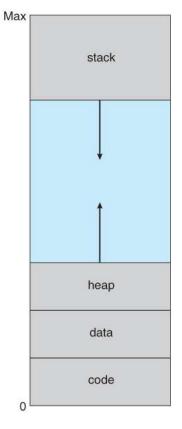
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The Sparseness of Virtual Address Space



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- Once the page is loaded from disk to memory, the OS updates the corresponding entry of the page table along with the valid bit

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- Therefore, memory accesses must reference pages that are in memory with high probability

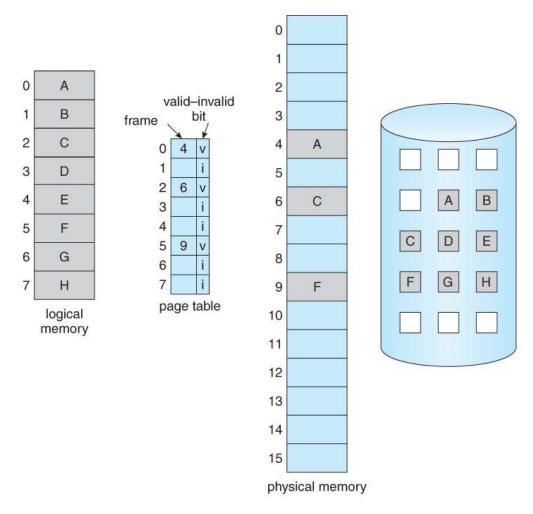
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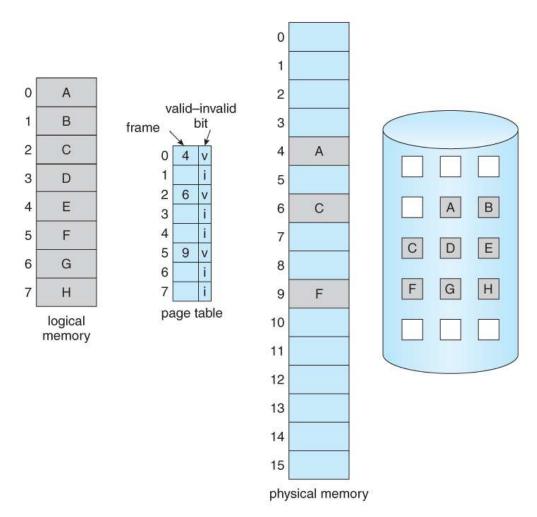
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- We call this area as the working set of the process
- Since the working set is fairly small compared to the whole virtual address space, it will likely fit in memory

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- But in a reasonably small time frame, the working set stays "the same"

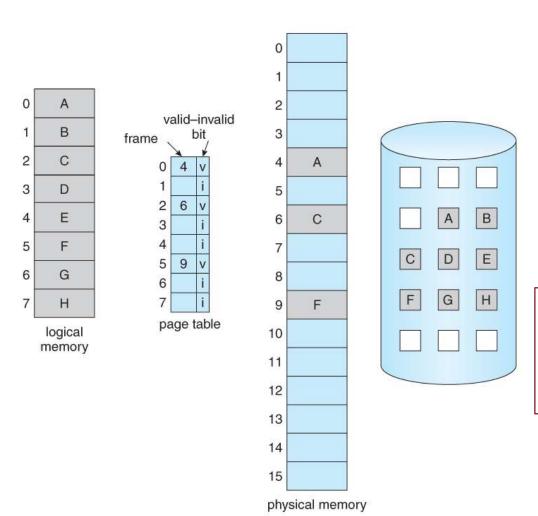


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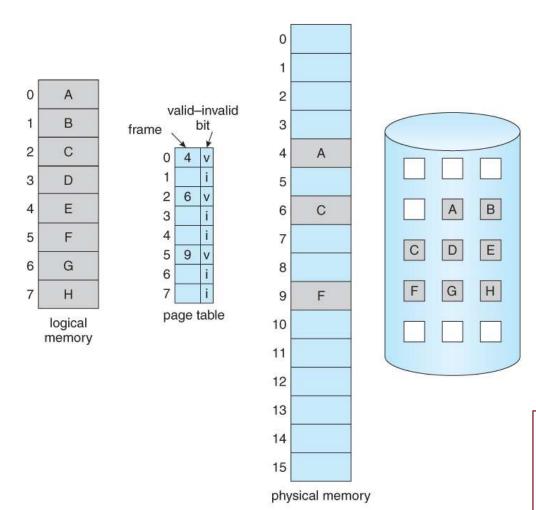
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If the bit is set to 1 it means the page entry is valid (i.e., the requested page is in memory)

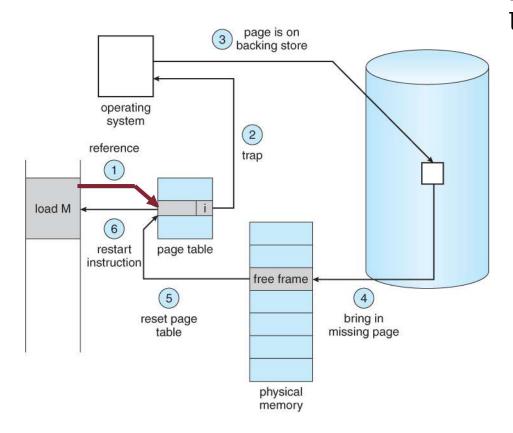


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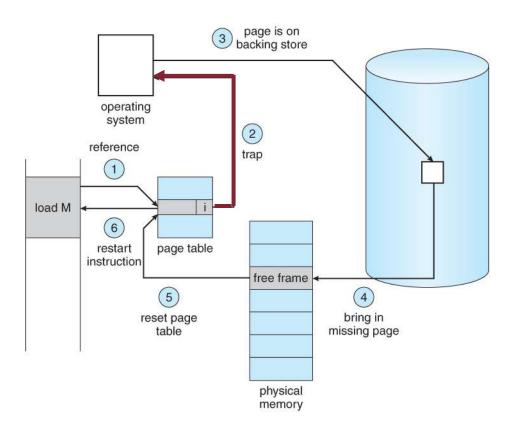
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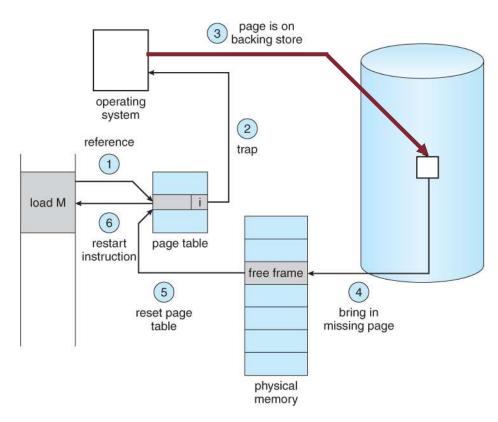
Otherwise, a page fault trap occurs, and the page has to be loaded (i.e., fetched) from disk



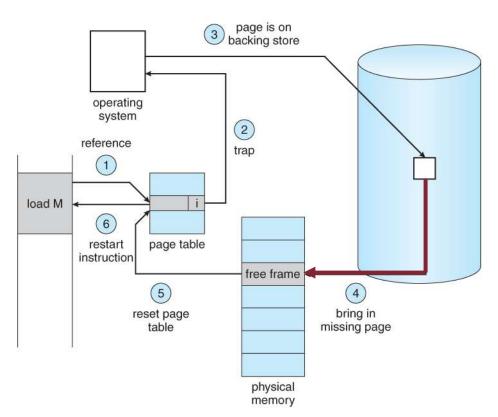
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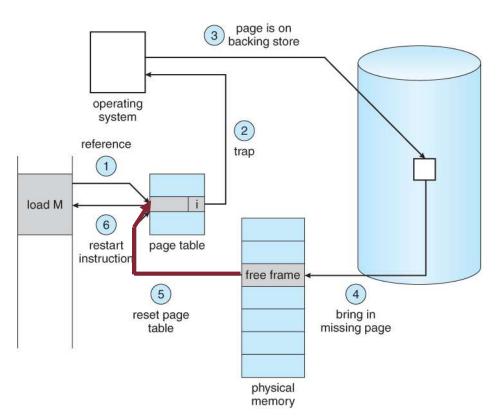


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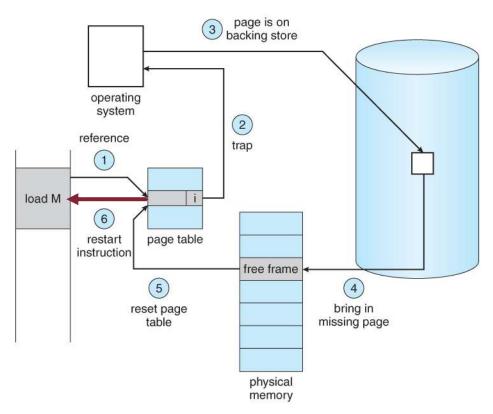
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- 6. The current process gets interrupted and the instruction that caused the page fault must be restarted from the beginning

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- TLB hit means the requested page entry is in the cache and the referenced frame is also in memory

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- If the requested page is not in the cache (TLB miss) and it is not even in memory (i.e., it is sitting on disk):
 - The OS picks a TLB entry to replace and fills it with the new entry as follows
 - invalidates the TLB entry
 - performs page fault trap operations
 - updates the TLB entry
 - restarts the faulting instruction

Page Fault Handling: Faulty Address

 How does the OS figure out which page generated the fault?

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- How does the OS figure out which page generated the fault?
- Architecture-dependent:
 - x86: hardware saves the virtual address that caused the fault (CR2 register)
 - On some platforms, OS gets only address of faulting instruction, must simulate the instruction and try every address to find the one that generated the fault

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- To restart (from scratch) a faulty instruction the OS needs hardware support for saving:
 - The faulting instruction
 - The CPU state

• idempotent vs. non-idempotent instructions

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- idempotent vs. non-idempotent instructions
- non-idempotent → much more difficult to restart
 - MOV [%R1], +(%R2) \rightarrow increment the value of R2 and store it to memory address in R1
 - What if memory address [%R1] causes the page fault?
 - Cannot naively redo the instruction from scratch, otherwise
 R2 gets incremented twice

- Even harder when using instructions that are not easily undoable
 - E.g., instructions that are used to move a block of memory at once
 - The block may span multiple pages: some of them can be in memory while some others not
 - Pages that are in memory can be changed meanwhile a page fault occurs

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How to unwind those complicated side-effects?

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Ensure all the addresses within the block to be moved are in memory before executing the instruction

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- Luckily, processes usually exhibit so-called locality of reference
 - temporal → if a process accesses an item in memory, it will tend to reference the same item again soon
- spatial → if a process accesses an item in memory, it will 12/12/23 tend to reference a close item again soon

 t_{MA} = physical memory access time t_{FAULT} = time to handle a page fault $p \in [0, 1]$ = probability of page fault t_{ACCESS} = effective time for each memory reference

$$t_{ACCESS} = (1 - p) * t_{MA} + p * t_{FAULT}$$

Let's assume: $t_{MA} = 100$ nsec and $t_{FAULT} = 20$ msec = 20,000,000 nsec

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This heavily depends on p!

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The access time increases from just 100 nsec up to ~20.1 microsec

200 times slowdown factor

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$$1.1 * 100 = 100 - 100p + 20,000,000p = 19,999,900p = 110 - 100 =$$

To achieve that goal, we can tolerate at most 1 page fault every about 2 million accesses!

$$p = \frac{10}{19,999,900} = \frac{1}{1,999,990} \approx 0,0000005 = 5 * 10^{-7}$$

More generally, given t_{MA} , t_{FAULT} , and a threshold $\epsilon > 0$ if we want to find p s.t.:

$$t_{ACCESS} = (1 + \epsilon) * t_{MA}$$

We substitute t_{ACCESS} and solve for p the resulting equation:

$$(1-p) * t_{MA} + p * t_{FAULT} = (1+\epsilon) * t_{MA} = t_{MA} - p * t_{MA} + p * t_{FAULT} = t_{MA} + \epsilon * t_{MA}$$

 $p(t_{FAULT} - t_{MA}) = \epsilon * t_{MA} = t_{MA}$

$$p = \frac{\epsilon * t_{MA}}{t_{FAULT} - t_{MA}}$$

Virtual Memory: Considerations

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- So far, we have described how the OS (with the support of HW) manages page faults
- Still, the OS has to answer 2 fundamental questions:
 - When to load process' pages into main memory (page fetching)
 - Which page to remove from memory if this gets filled (page replacement)

Page Fetching Goals

- The overall goal is still to make physical memory look larger than it is
- Exploiting the locality reference of programs
- Keep in memory only those pages that is being used
- Keep on disk those pages that are unused
- Ideally, producing a memory system with the performance of main memory and the cost/capacity of disk!

Page Fetching Strategies

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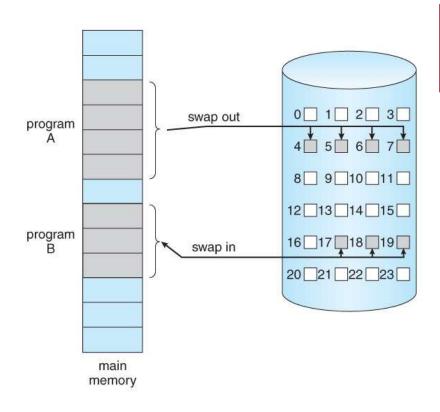
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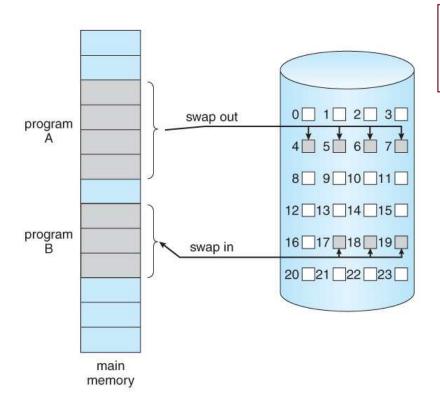
Most modern OSs use demand fetching

(Pure) Demand Paging

- When a process starts up, **none** of its pages are loaded
- Rather, a page is swapped in only when the process references it (upon a page fault)
- This is termed a lazy swapper or pager
- Opposite of loading all the pages at process startup!



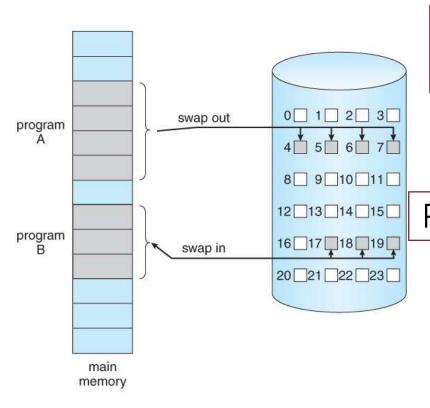
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Trying to avoid page faults

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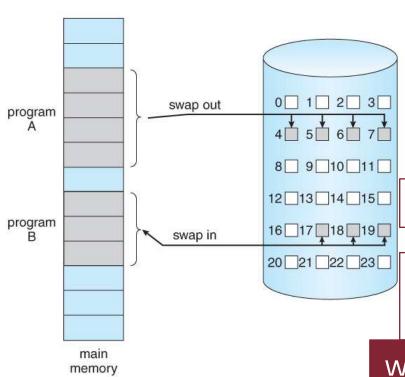


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Possible approach: upon page fault, load many pages instead of only the faulty one

works if program accesses memory sequentially

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- On Mac, instead, swap space is part of the file system (swapfiles)

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- Depending on which kind of page is removed, different optimizations may apply upon page swapout

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- Code page (read-only):
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- Data page:
 - Data content does actually change!
 - Save it to a separate paging file, so that no changes are lost when it will be loaded in the future
 - Need to use the dedicated swap space

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- If physical memory has still free frames, the page can be safely loaded into one of those
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- Several algorithms to select the page to evict from memory

• Random: pick any page at random (works surprisingly well!)

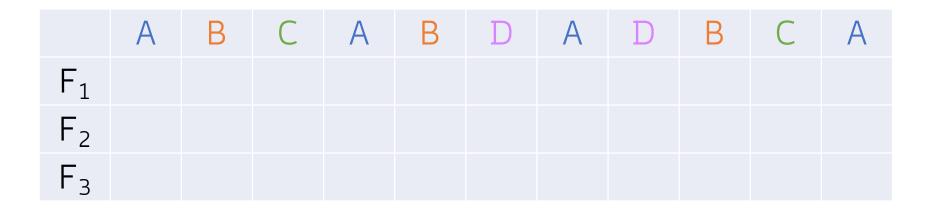
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- LRU (Least Recently Used): approximation of MIN, remove the page that has not been used in the longest time
 - Assumes the past is a good predictor of the future (not always true!)

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

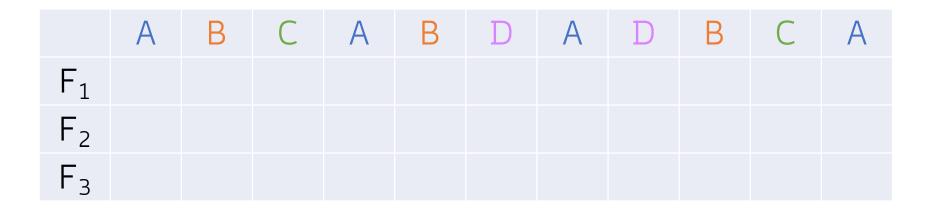
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How many page faults (denoted by *)?

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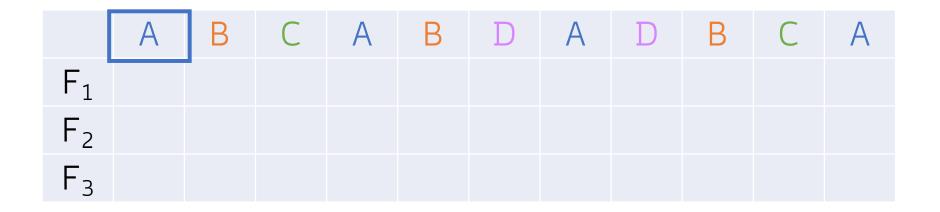
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Initially, no frame is loaded in memory at all (pure demand paging)

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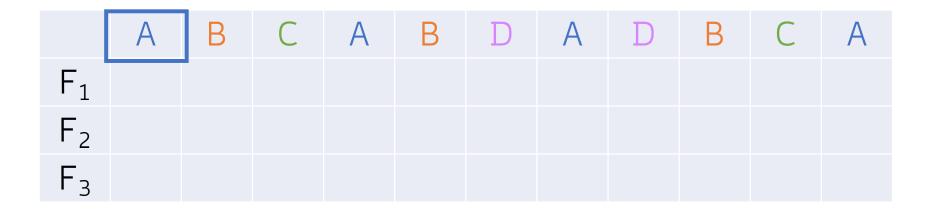
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Virtual address within page A is referenced

3 physical frames: F_1 , F_2 , $F_3 \mid 4$ virtual pages: A, B, C, D

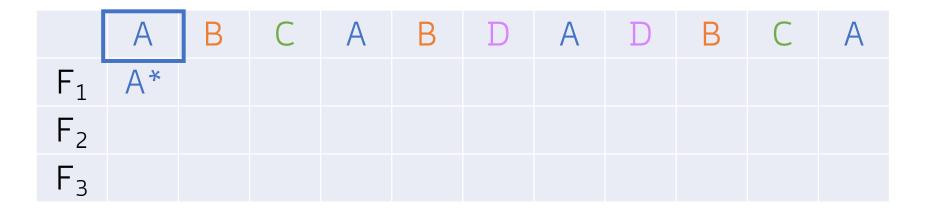
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Virtual address within page A is referenced page fault

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



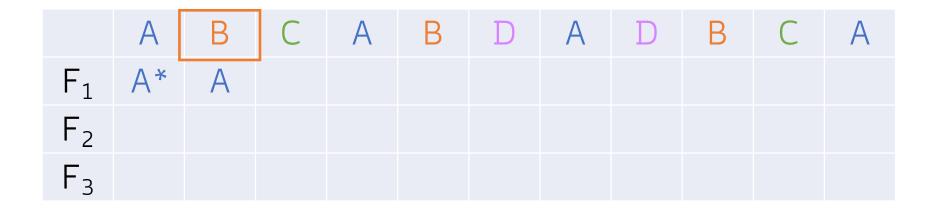
Virtual address within page A is referenced

page fault

A loaded

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

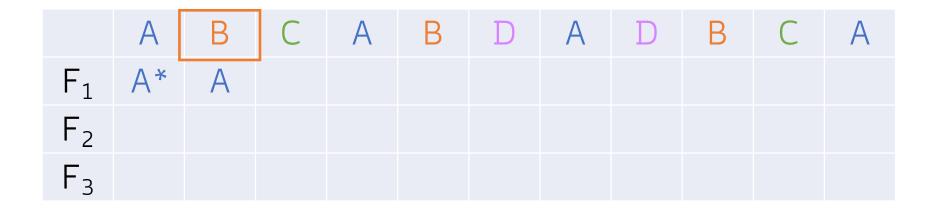


Virtual address within page B is referenced

FIFO = A

3 physical frames: F₁, F₂, F₃ 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



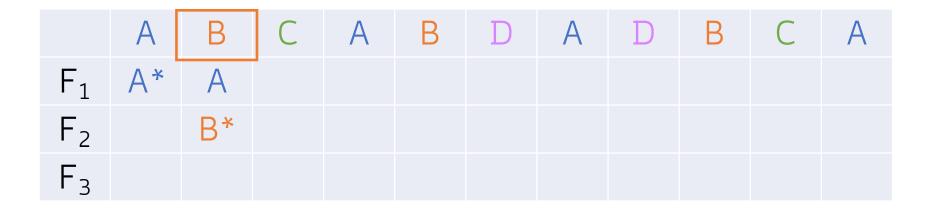
Virtual address within page B is referenced

page fault

FIFO = A

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



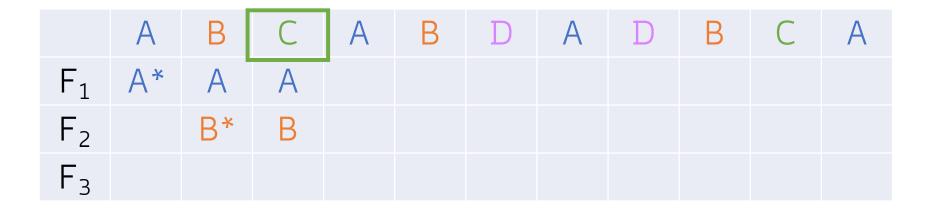
Virtual address within page B is referenced

page fault B loaded

FIFO = A → B

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

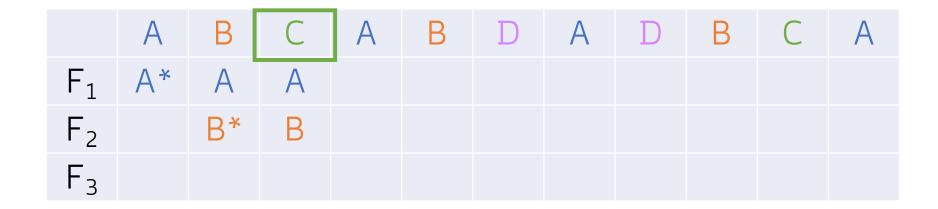


Virtual address within page C is referenced

 $FIFO = A \rightarrow B$

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



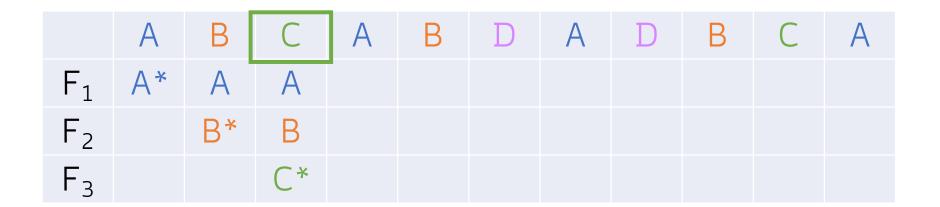
Virtual address within page C is referenced

page fault

 $FIFO = A \rightarrow B$

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

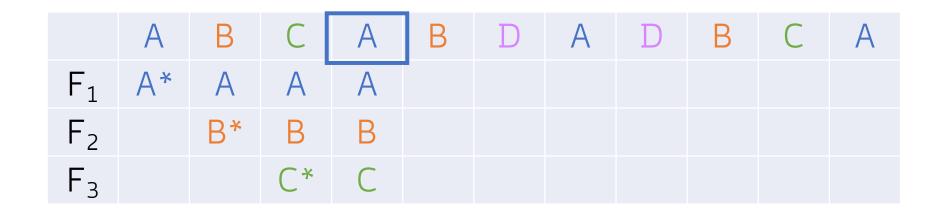


Virtual address within page C is referenced page fault

page fault C loaded

3 physical frames: F_1 , F_2 , $F_3 \mid 4$ virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



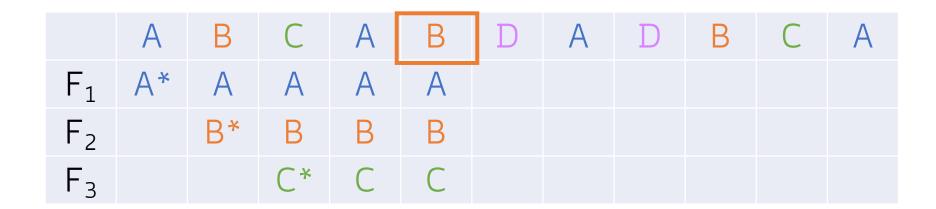
Virtual address within page A is referenced

$$\mathsf{FIFO} = \mathsf{A} \to \mathsf{B} \to \mathsf{C}$$

A is already loaded

3 physical frames: F_1 , F_2 , $F_3 \mid 4$ virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



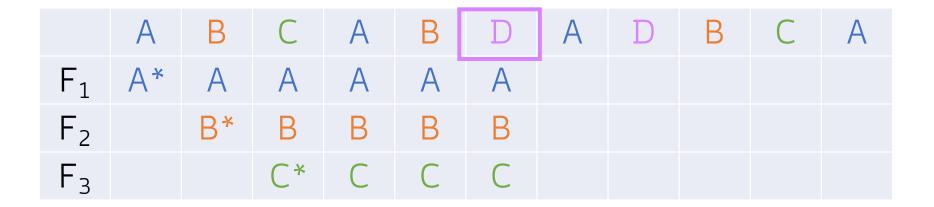
Virtual address within page B is referenced

$$FIFO = A \rightarrow B \rightarrow C$$

B is already loaded

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

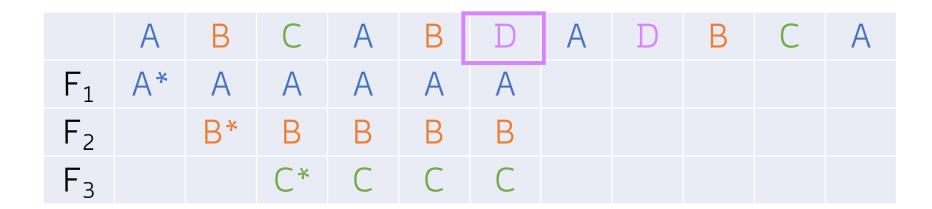


Virtual address within page D is referenced

 $\mathsf{FIFO} = \mathsf{A} \to \mathsf{B} \to \mathsf{C}$

3 physical frames: F_1 , F_2 , $F_3 \mid 4$ virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

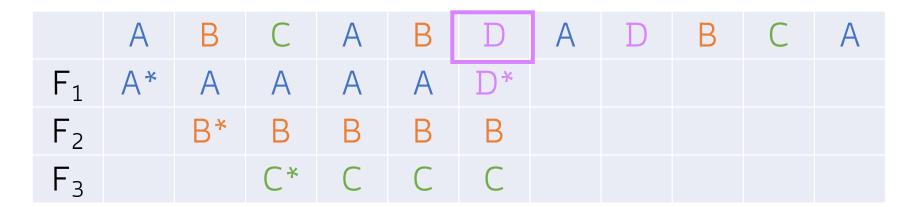


Virtual address within page D is referenced page fault

 $FIFO = A \rightarrow B \rightarrow C$

3 physical frames: F₁, F₂, F₃ 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



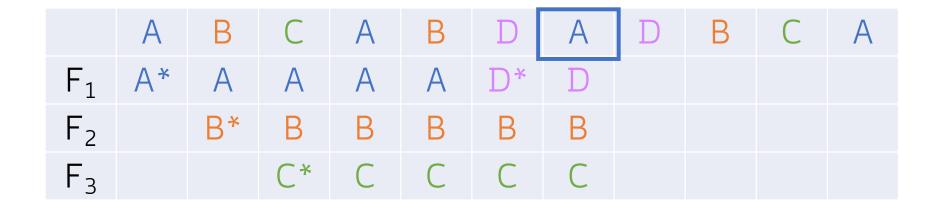
Virtual address within page D is referenced page fault

page fault

A replaced D loaded

3 physical frames: F₁, F₂, F₃ 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

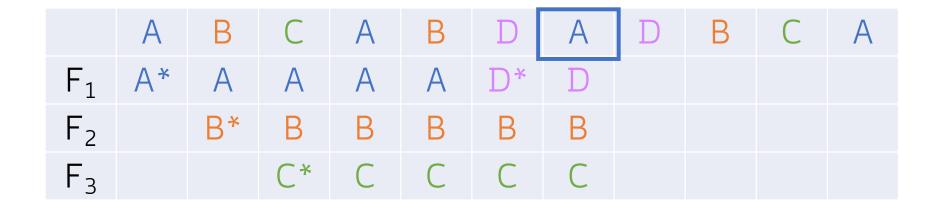


Virtual address within page A is referenced

$$\mathsf{FIFO} = \mathsf{B} \to \mathsf{C} \to \mathsf{D}$$

3 physical frames: F_1 , F_2 , $F_3 \mid 4$ virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

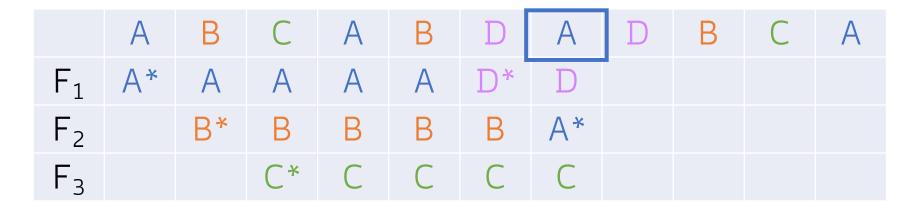


Virtual address within page A is referenced page fault

 $FIFO = B \rightarrow C \rightarrow D$

3 physical frames: F_1 , F_2 , $F_3 \mid 4$ virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

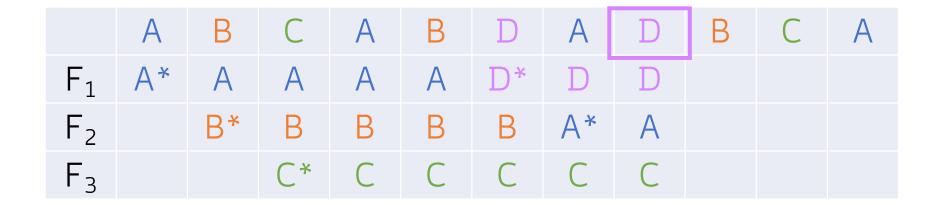


Virtual address within page A is referenced page fault

B replaced A loaded

3 physical frames: F_1 , F_2 , $F_3 \mid 4$ virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



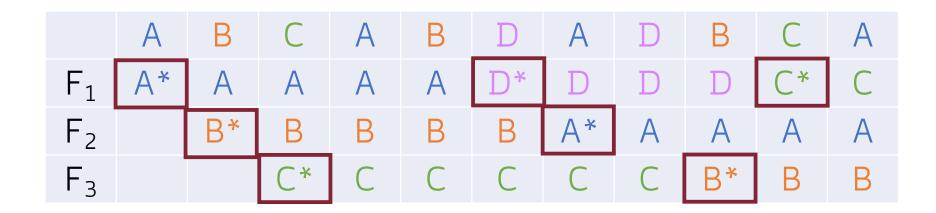
Virtual address within page D is referenced

$$\mathsf{FIFO} = \mathsf{C} \to \mathsf{D} \to \mathsf{A}$$

is already loaded

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

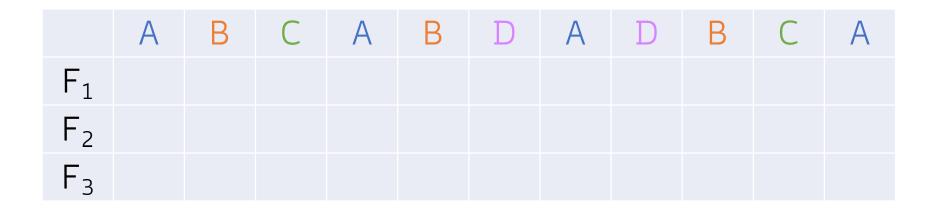
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Eventually, we get a total of 7 page faults

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

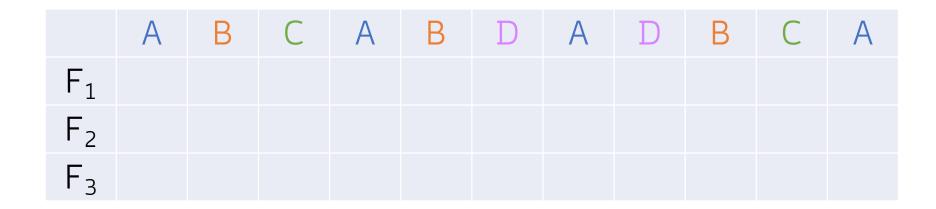
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



How many page faults (denoted by *)?

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

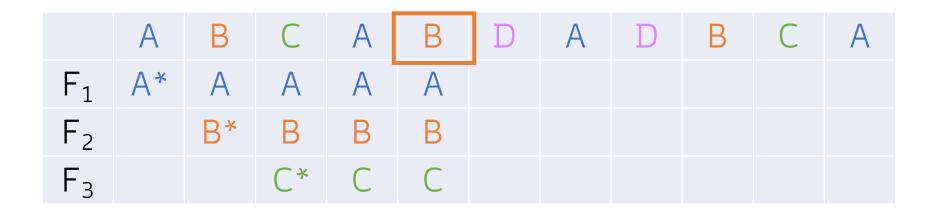
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Initially, no frame is loaded in memory at all (pure demand paging)

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

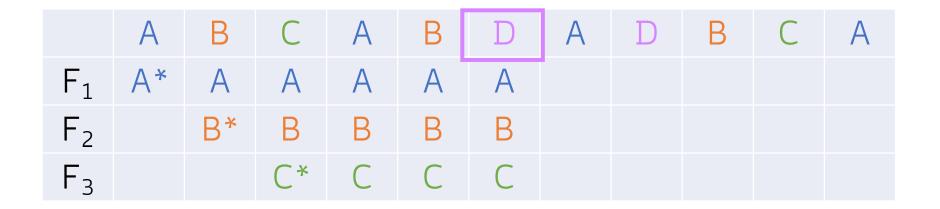
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Up to this point, the same as FIFO

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

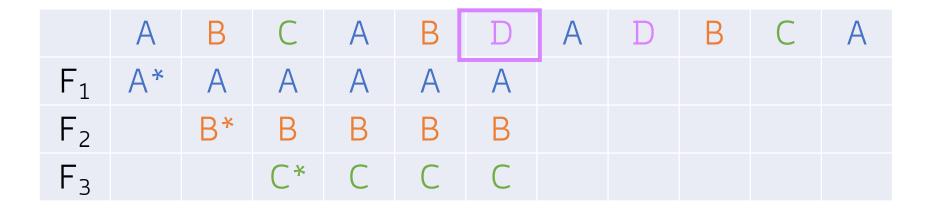
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Virtual address within page D is referenced

```
3 physical frames: F_1, F_2, F_3 \mid | 4 virtual pages: A, B, C, D
```

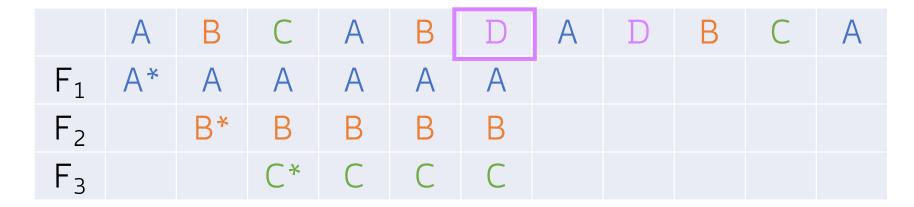
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Virtual address within page D is referenced page fault

3 physical frames: F_1 , F_2 , $F_3 \mid | 4$ virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

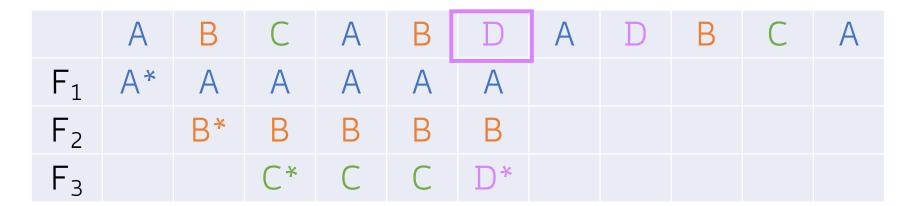


Virtual address within page D is referenced page fault

What's the page that will be requested the furthest away?

3 physical frames: F_1 , F_2 , $F_3 \mid 4$ virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



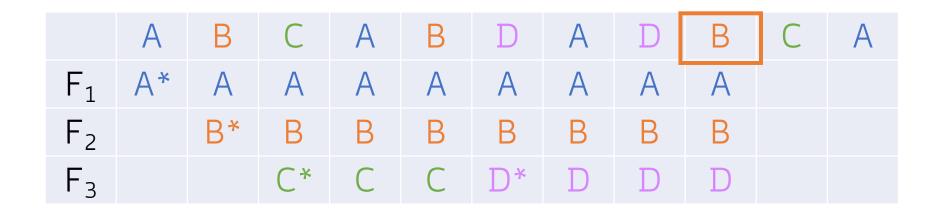
Virtual address within page D is referenced page fault

C replaced D loaded

C is the page that will be requested the furthest away

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

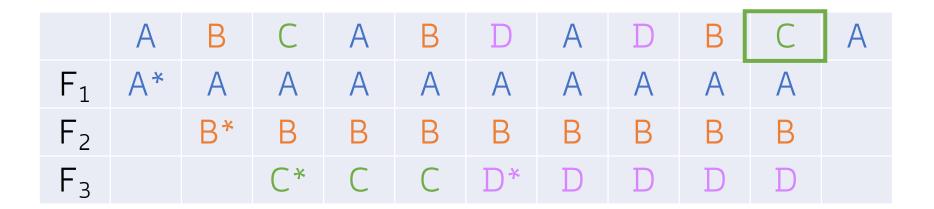
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Up to this point, no more page faults

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

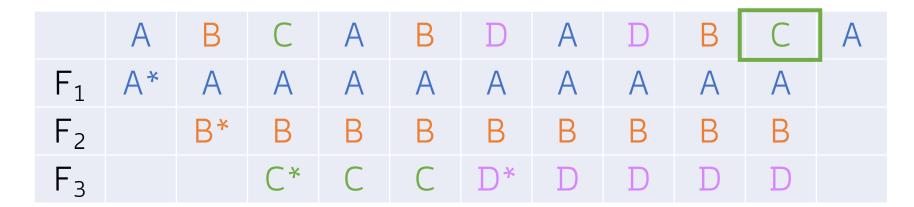
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Virtual address within page C is referenced

3 physical frames: F_1 , F_2 , $F_3 \mid 4$ virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



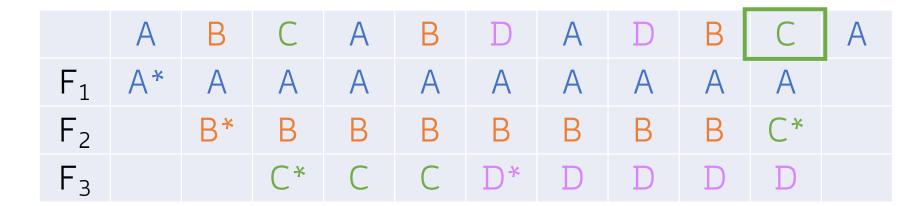
Virtual address within page C is referenced

page fault

What's the page that will be requested the furthest away?

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Virtual address within page C is referenced

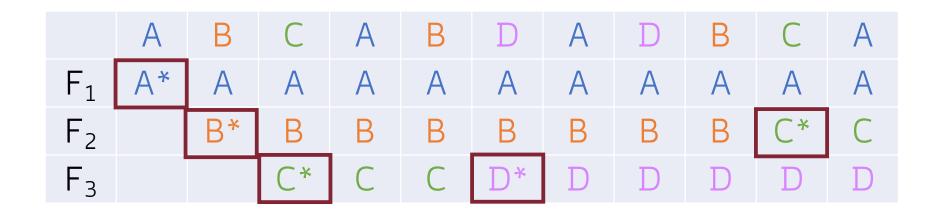
page fault

B replaced C loaded

B or D will be requested the furthest away (surely not A): pick one (e.g., B)

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

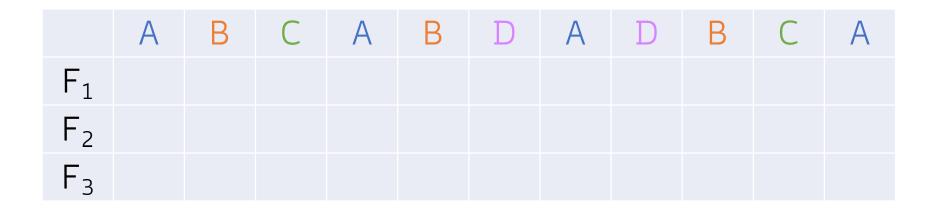
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Eventually, we get a total of 5 page faults

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

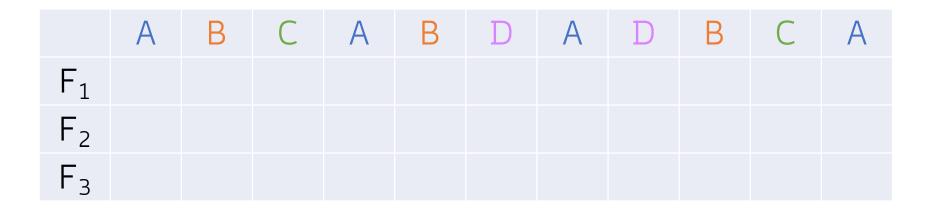
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



How many page faults (denoted by *)?

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

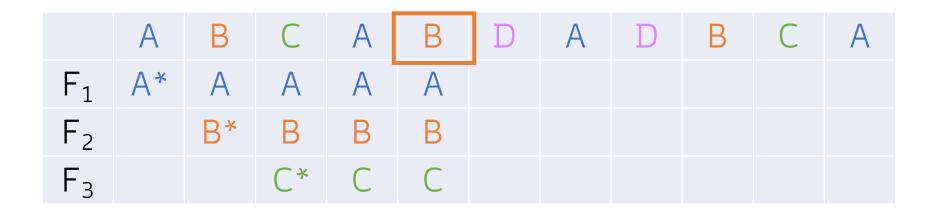
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Initially, no frame is loaded in memory at all (pure demand paging)

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

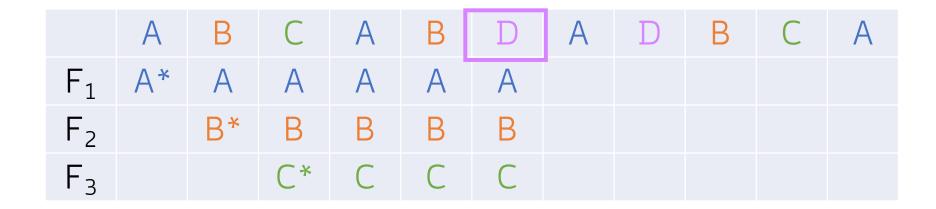
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Up to this point, the same as FIFO

```
3 physical frames: F_1, F_2, F_3 \mid | 4 virtual pages: A, B, C, D
```

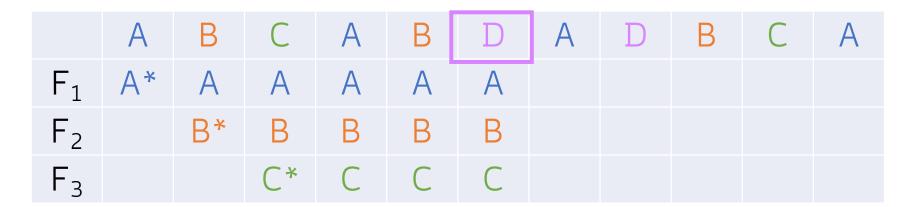
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Virtual address within page D is referenced page fault

```
3 physical frames: F_1, F_2, F_3 \mid 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

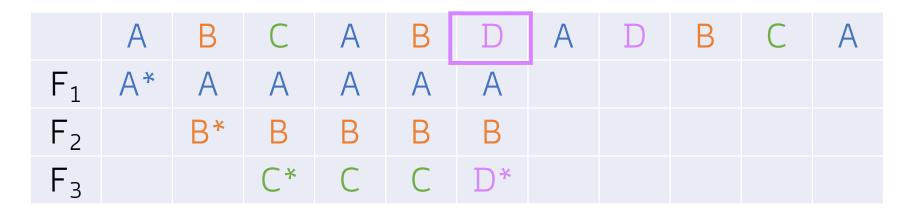


Virtual address within page D is referenced page fault

We can't look forward anymore!

```
3 physical frames: F_1, F_2, F_3 \mid 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



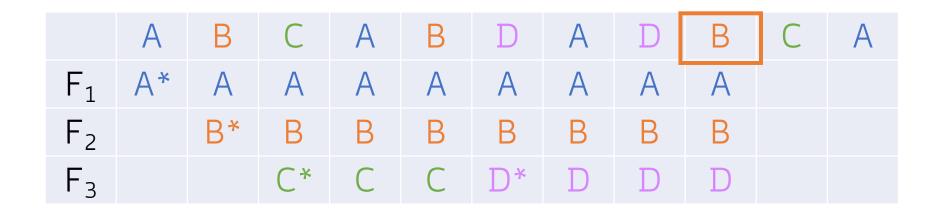
Virtual address within page D is referenced page fault

C replaced D loaded

C is the page that has not been used for the longest time in the past

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

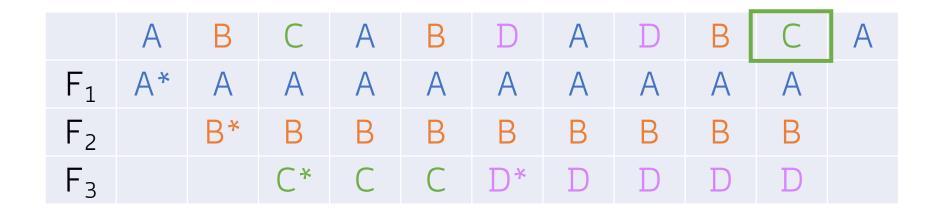


Up to this point, no more page faults

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```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Virtual address within page C is referenced

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

```
      A
      B
      C
      A
      B
      D
      A
      D
      B
      C
      A

      F1
      A*
      A
      A
      A
      A
      A
      A
      A
      A
      A
      A
      A
      A
      A
      A
      A
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      D</td
```

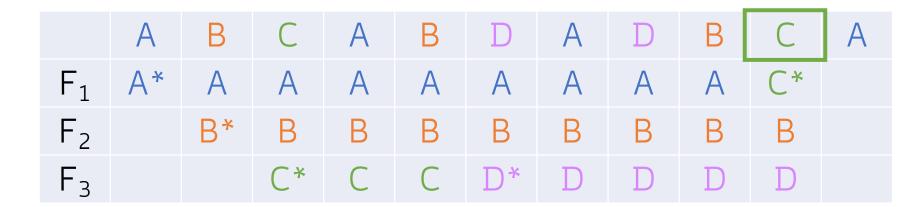
Virtual address within page C is referenced

page fault

We can't look forward anymore!

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Virtual address within page C is referenced

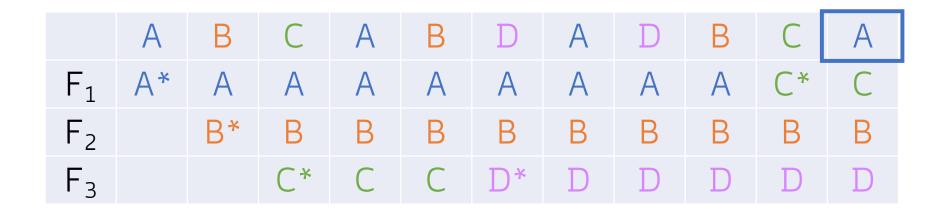
page fault

A replaced C loaded

A is the page that has not been used for the longest time in the past

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Virtual address within page A is referenced

```
3 physical frames: F_1, F_2, F_3 4 vir
```

4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A

```
      A
      B
      C
      A
      B
      D
      A
      D
      B
      C
      A

      F1
      A*
      A
      A
      A
      A
      A
      A
      A
      C*
      C

      F2
      B*
      B
      B
      B
      B
      B
      B
      B
      B
      B

      F3
      C*
      C
      C
      D*
      D
      D
      D
      D
```

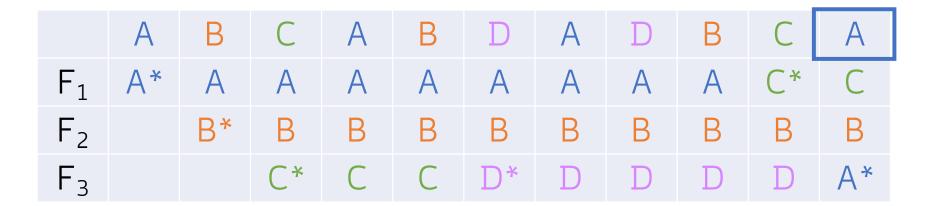
Virtual address within page A is referenced

page fault

We can't look forward anymore!

3 physical frames: F_1 , F_2 , F_3 4 virtual pages: A, B, C, D

Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Virtual address within page A is referenced

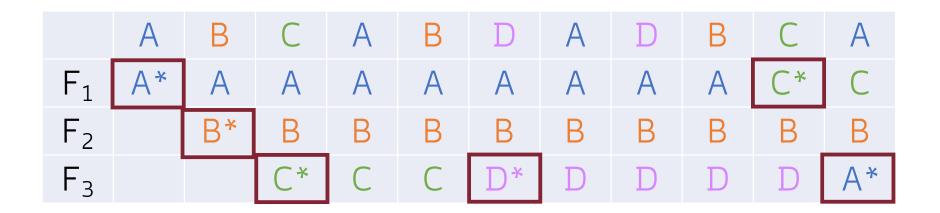
page fault

D replaced A loaded

D is the page that has not been used for the longest time in the past

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

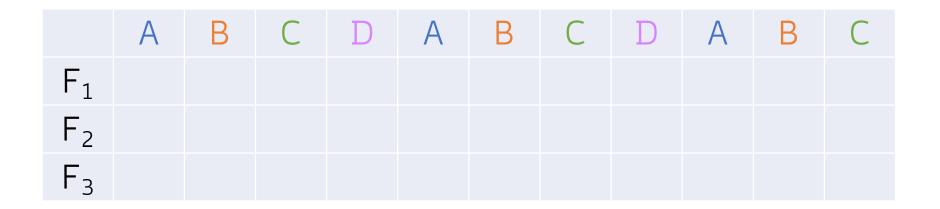
Reference sequence of pages: A, B, C, A, B, D, A, D, B, C, A



Eventually, we get a total of 6 page faults

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C



How many page faults (denoted by *)?

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

	A	В	C	D	Α	В	C	D	A	В	C
F_1	A*	A	A								
F_2		B*	В								
F_3			C*								

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```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

	A	В	C	D	Α	В	C	D	A	В	C
F_1	A *	A	Α	D*							
F_2		B*	В	В							
F_3			C*	C							

```
3 physical frames: F_1, F_2, F_3 \mid | 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

```
A B C D A B
F<sub>1</sub> A* A A D* D
F<sub>2</sub> B* B B A*
F_3
```

```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

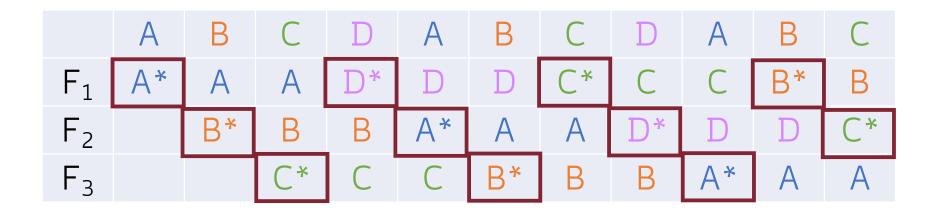
```
3 physical frames: F_1, F_2, F_3 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C

```
A B C D A B C D
F<sub>1</sub> A* A A D* D D C*
F<sub>2</sub> B* B A* A A
F_3
```

```
3 physical frames: F_1, F_2, F_3 \mid 4 virtual pages: A, B, C, D
```

Reference sequence of pages: A, B, C, D, A, B, C, D, A, B, C



Eventually, we get a total of 11 page faults

Page Replacement: What If We Add Memory?

- Does adding memory always reduce the number of page faults?
- Intuitively, it would seem so...
- The answer, in fact, depends on the page replacement algorithm
- Let's see this with an example, using FIFO page replacement

FIFO Page Replacement: Example

```
5 virtual pages: A, B, C, D, E

3 physical frames: F<sub>1</sub>, F<sub>2</sub>, F<sub>3</sub>

4 physical frames: F<sub>1</sub>, F<sub>2</sub>, F<sub>3</sub>, F<sub>4</sub>

Scenario 1
```

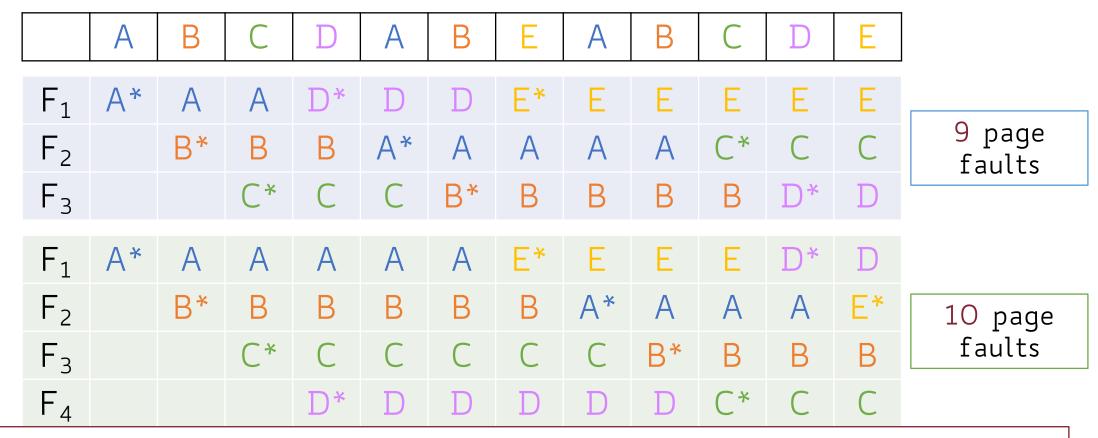
Reference sequence of pages: A, B, C, D, A, B, E, A, B, C, D, E

FIFO Page Replacement: Example

	A	В	U	D	Α	В	Ε	A	В	U	D	Ε
F_1	A *	Α	Α	D*	D	D	E*	Ε	Ε	Ε	Ε	Ε
F_2		B*	В	В	A*	Α	Α	Α	Α	C*	C	C
F_3			C*	C	C	B*	В	В	В	В	D*	D
F_1	A *	Α	Α	Α	Α	Α	E*	Ε	Ε	Ε	D*	D
F_2		B*	В	В	В	В	В	A*	Α	Α	Α	E*
F_3			C*	C	C	C	C	C	B*	В	В	В
F_4				D*	D	D	D	D	D	C*	C	C

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FIFO Page Replacement: Example



Belady's Anomaly

Adding page frames may cause more page faults with some algorithms

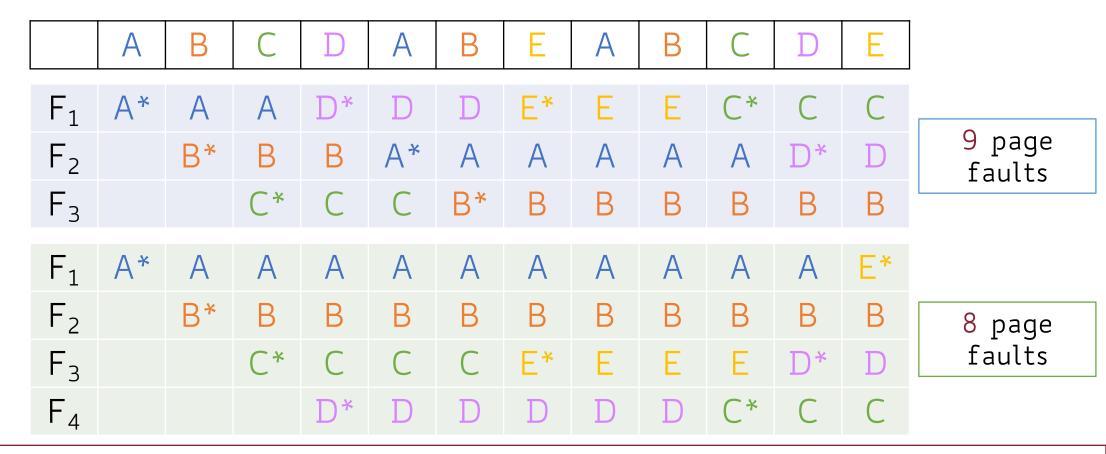
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LRU Page Replacement: Example



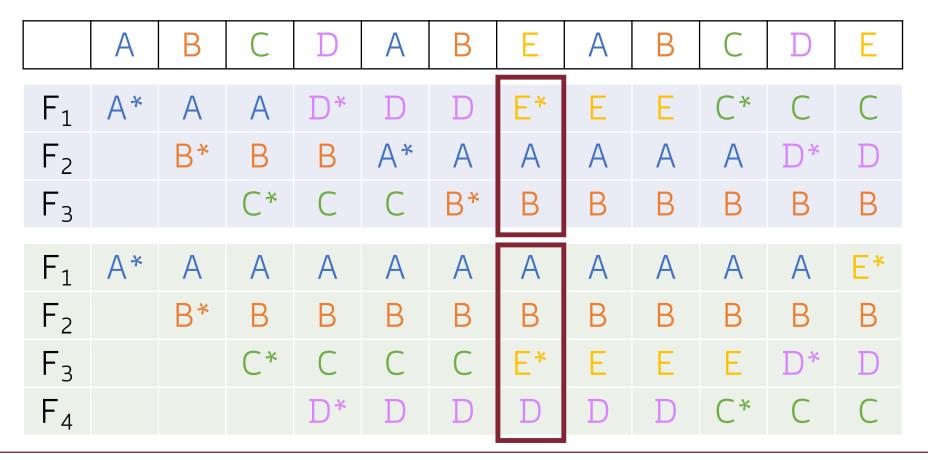
With LRU, adding page frames always decreases the number of page faults

LRU Page Replacement: Example



With LRU, adding page frames always decreases the number of page faults

LRU Page Replacement: Example



At each point in time 4-frame memory contains a subset of 3-frame

Page Replacement: Summary

- FIFO is easy to implement but may lead to too many page faults
- May suffer from Belady's Anomaly

Page Replacement: Summary

 MIN is the optimal choice but cannot be used in practice since future memory references are never known in advance

Page Replacement: Summary

- LRU is a fair approximation of MIN assuming the past is a good predictor of the future
 - Exploits the locality reference (small working set that fits in memory)
 - Works poorly when the locality reference doesn't hold (large working set)