Sistemi Operativi I

Corso di Laurea in Informatica 2024-2025



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Recap from Last Lecture

- Synchronization primitives:
 - Locks
 - Semaphores
 - Monitors

Recap from Last Lecture

- Synchronization primitives:
 - Locks
 - Semaphores
 - Monitors
- 2 fundamental synchronization problems:
 - Producers-Consumers
 - Readers-Writers

Our Journey

- What is deadlock?
- Conditions for deadlock to happen
- Deadlock detection
- Deadlock prevention
- Deadlock avoidance

Our Journey

- What is deadlock?
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"When two trains approach each other at a crossing, both shall come to a full stop and neither shall start up again until the other has gone."

Kansas legislation early 1900's

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

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```
Thread A

printer.wait();
disk.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

```
Thread B

disk.wait();
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

A starts first

printer.wait();

disk.wait();

// copy from disk to printer

printer.signal();

disk.signal();
```

```
Thread B

disk.wait();
printer.wait();

// copy from disk to printer
printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.wait(); Acquires printer and context switch
disk.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

```
Thread B

disk.wait();
printer.wait();

// copy from disk to printer
printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.wait();
disk.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

```
Thread B

B takes over

disk.wait();
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

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Thread A

printer.wait();
disk.wait();

// copy from disk to printer

printer.signal();
disk.signal();
```

```
Thread B

disk.wait(); Acquires disk and printer.wait(); context switch

// copy from disk to printer

printer.signal(); disk.signal();
```

Intuitively, a condition where two or more threads are waiting for an event that can only be generated by the very same threads

```
Thread A

printer.wait(); A executes again and blocks disk.wait();

// copy from disk to printer

printer.signal(); disk.signal();
```

```
Thread B

disk.wait();
printer.wait();

// copy from disk to printer

printer.signal();
disk.signal();
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```

A waits B to release the disk

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// copy from disk to printer

printer.signal();
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Thread B

disk.wait();
printer.wait();

// copy from disk to printer
printer.signal();
disk.signal();
```

B waits A to release the printer

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- Deadlock detection: finds instances of deadlocks and tries to recover
- Deadlock prevention (offline): imposes restrictions/rules on how to write deadlock-free programs
- Deadlock avoidance (online): runtime support checks resource requests made by threads to avoid deadlocks

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- Related terms but each one refers to a specific situation
- Starvation occurs when a thread waits indefinitely for some resource but other threads are actually making progress using that resource
- The main difference with deadlock is that the system is not completely stuck!

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 neither another thread nor the OS can force it to release the resource
 - Circular Wait \rightarrow a set of waiting threads t_1 , ..., t_n where t_i is waiting on $t_{(i+1)\%n}$

Our Journey

- What is deadlock?
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• We define a directed graph G=(V, E) where:

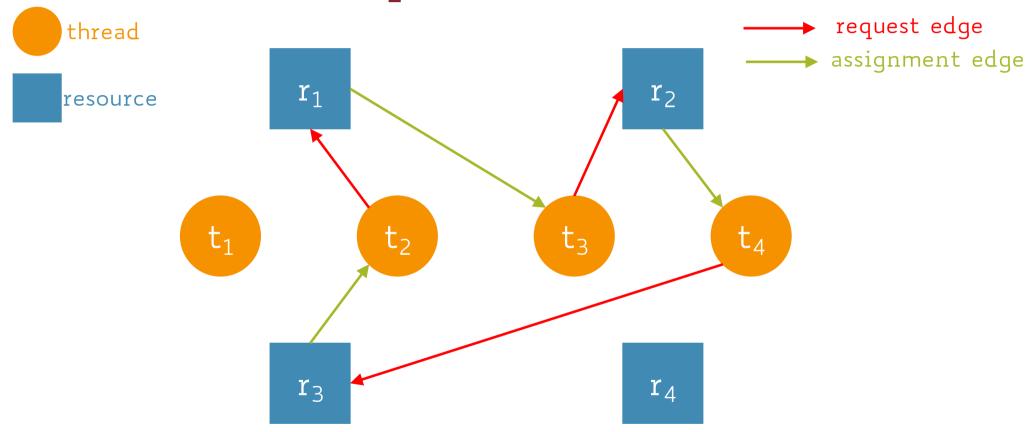
- We define a directed graph G=(V, E) where:
 - V is the set of vertices representing both resources $\{r_1, ..., r_m\}$ and threads $\{t_1, ..., t_n\}$

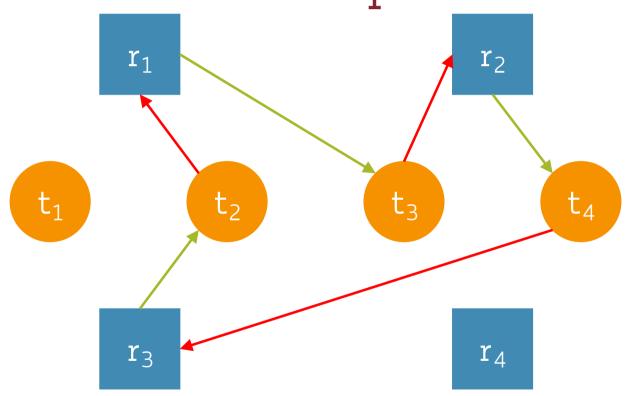
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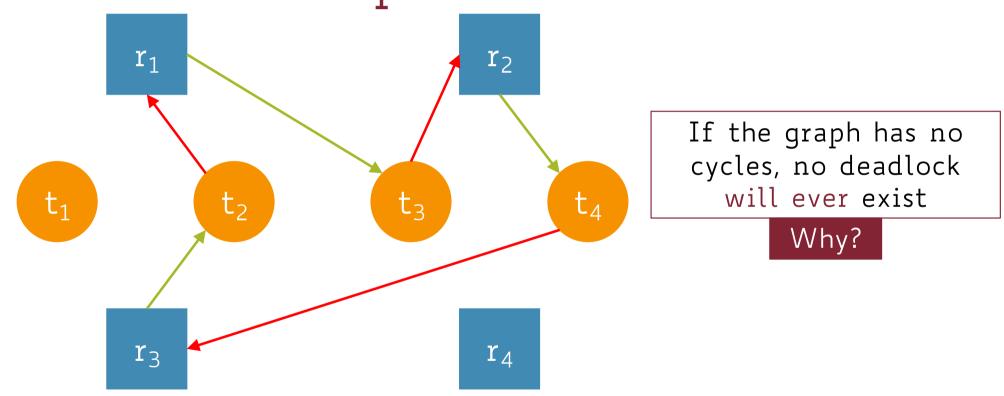
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 - Request Edge \rightarrow a directed edge (t_i, r_j) indicates that t_i has requested r_i , but not yet acquired
 - Assignment Edge \rightarrow a directed edge (r_j, t_i) indicates that the OS has allocated r_i to t_i





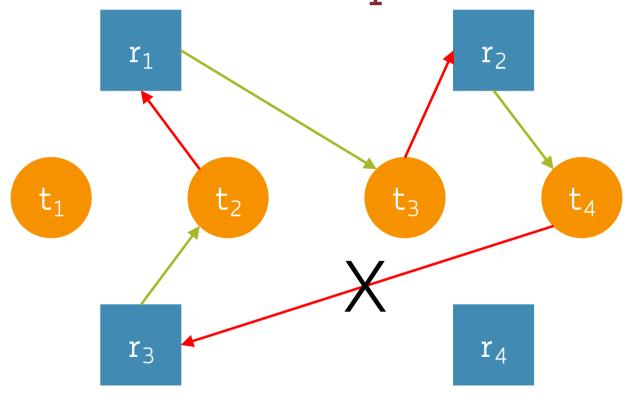
If the graph has no cycles, no deadlock will ever exist



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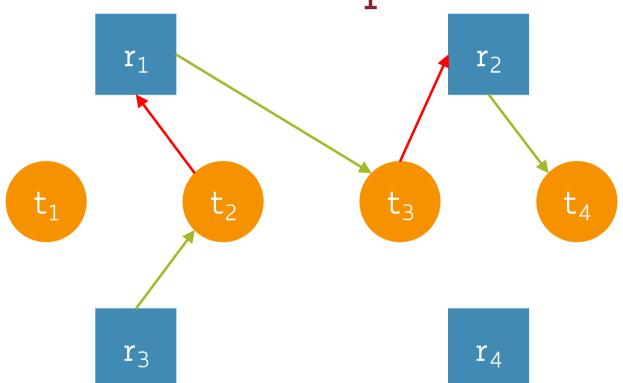
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Allocation Graph



Suppose we remove the edge (t₄, r₃) so as to remove the cycle

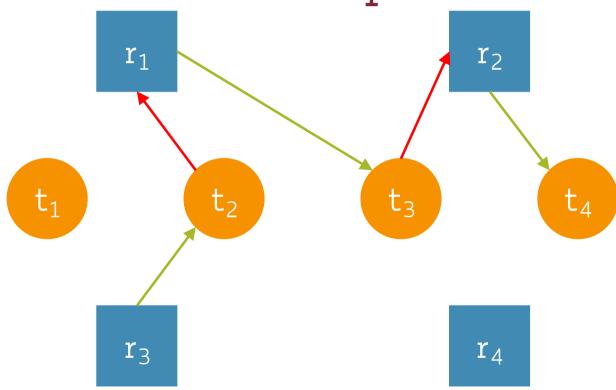
Allocation Graph



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Allocation Graph

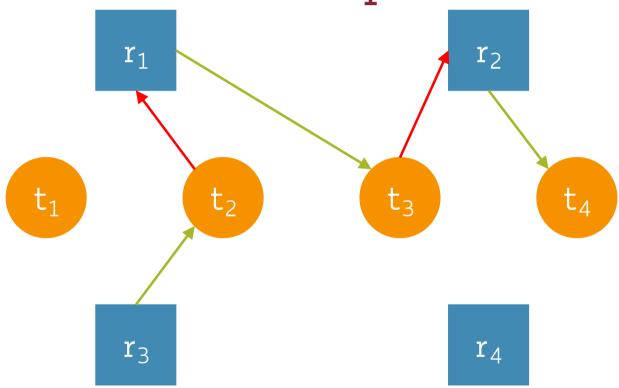


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Allocation Graph

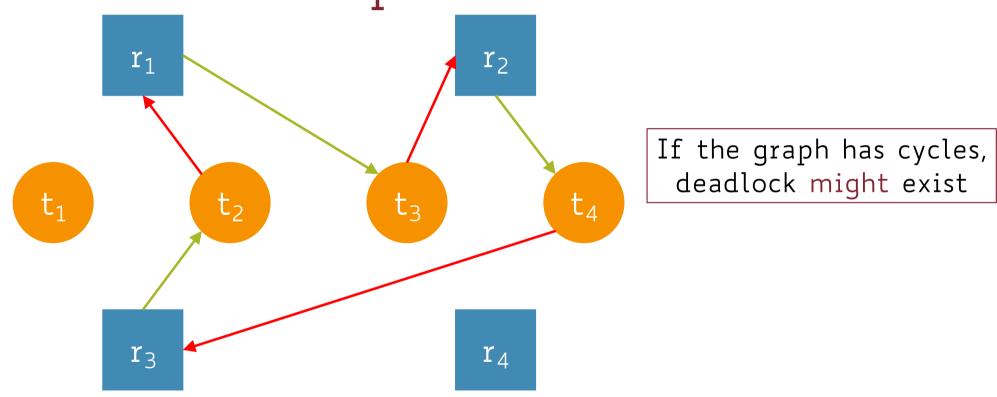


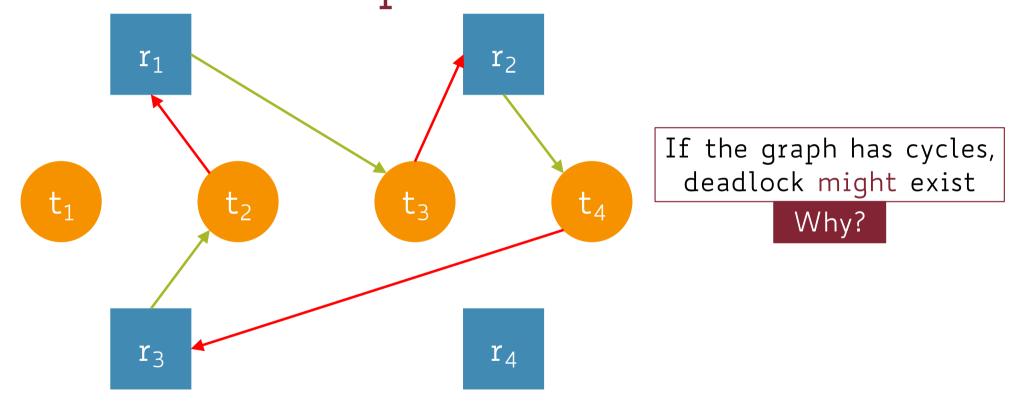
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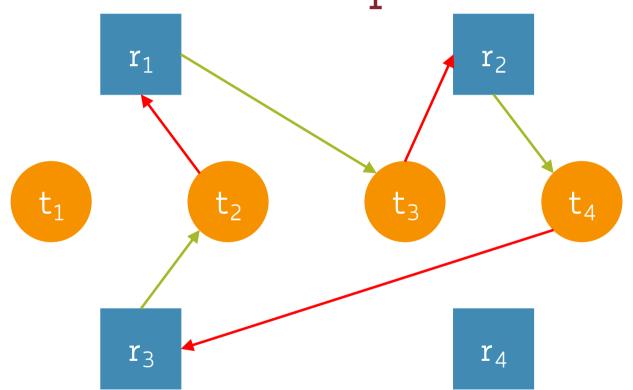
No deadlock can occur as t₄ is not waiting on anything...

Therefore, t₄ can run and eventually will release r₂, which wakes up t₃

And so on and so forth...

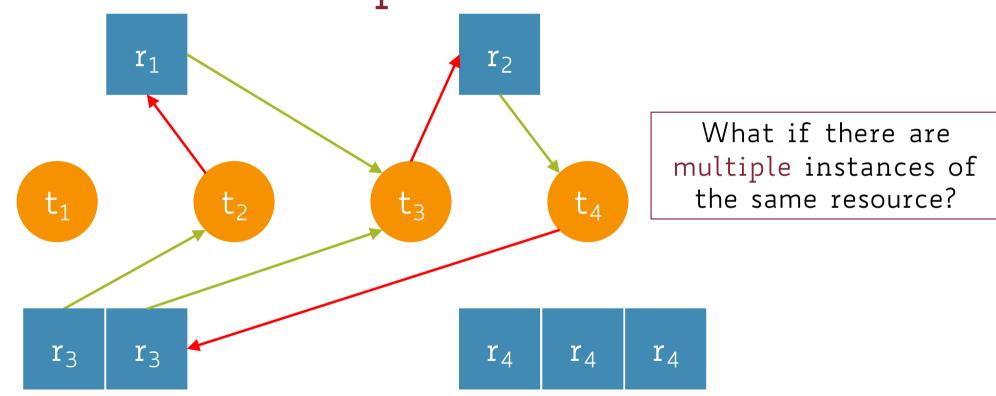


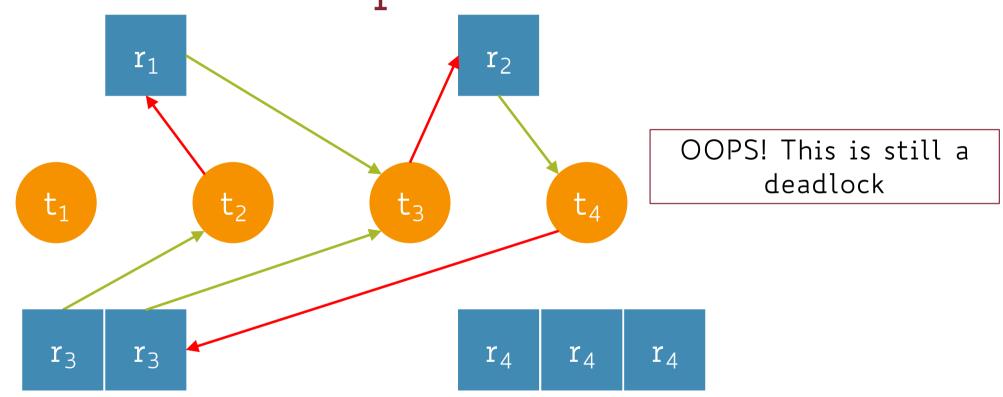


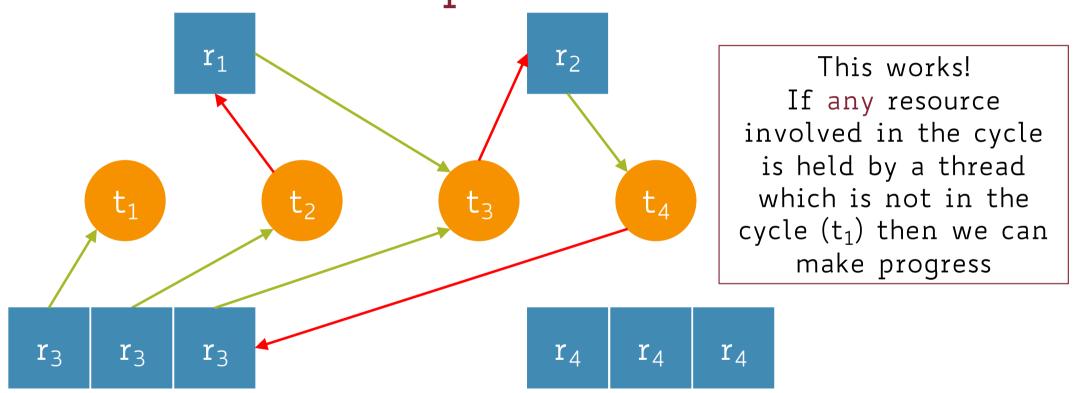


If the graph has cycles, deadlock might exist

We are assuming the multiplicity of each resource is 1 (i.e., one r_1 , one r_2 , etc.)







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- We would like to be more precise than that...

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- Known algorithms based on depth-first search (DFS) take O(|V|+|E|) time
- $O(|V|+|E|) \sim O(|V|^2)$ as $|E| = O(|V|^2)$ for dense graphs, and |V| = #threads + #resources

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 - Before granting a resource \rightarrow each granted request will take $O(|V|^2)$
 - When a request cannot be fulfilled \rightarrow each failed request will take $O(|V|^2)$
 - On a regular schedule or when the CPU is under-utilized

Our Journey

- What is deadlock?
- Conditions for deadlock to happen
- Deadlock detection
- Deadlock prevention
- Deadlock avoidance

- Ensure that at least one of the 4 necessary conditions doesn't hold
 - Mutual Exclusion → make all resources sharable
 - Not all can be shared
 - E.g., disks, printers, etc.

- Ensure that at least one of the 4 necessary conditions doesn't hold
 - Hold and Wait → a thread cannot hold one resource when it requests another
 - Enforce requests to be made all at once
 - Hard to predict all the resources a thread will need

- Ensure that at least one of the 4 necessary conditions doesn't hold
 - No Preemption → if a thread requests a resource that cannot be allocated to it, the OS preempts (releases) all the resources that the thread is already holding
 - Not all resources can be easily preempted (e.g., printers)

- Ensure that at least one of the 4 necessary conditions doesn't hold
 - Circular Wait → impose an ordering (i.e., numbering) on resources and enforce to request them in such order
 - Hard to establish such an order

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Deadlock Avoidance: Resource Reservation

Each thread provides information about the maximum number of resources it might need during execution

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```
m_i = maximum number of resources that thread i might request c_i = current number of resources that thread i is holding
```

$$C = \sum_{i=1}^{n} c_i = total$$
 number of resources currently allocated

R = maximum number of resources overall available

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 $C = \sum_{i=1}^{n} c_i = total$ number of resources currently allocated

R = maximum number of resources overall available

Any thread sequence is safe if for each thread it holds that:

$$\underbrace{m_i - c_i}_{\text{resources } t_i \text{ might still request}} \leq \underbrace{R - C}_{\text{resources currently available}} + \underbrace{\sum_{j=1}^{i-1} c_j}_{\text{resources currently allocated up to } t_i, j < i}$$

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- This policy ensures no circular-wait condition exists

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t_1	4	3	1
t ₂	8	4	4
t ₃	12	4	8

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Is the current state safe?

Thread	m_i	c_{i}	m_i – c_i
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t ₃	12	4	8

The current state is safe: there exists a sequence of threads (t_1, t_2, t_3) where each one gets the maximum number of resources without waiting

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t₁ can complete using the current allocation and the 1 drive left

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t₁ can complete using the current allocation and the 1 drive left

t₂ can use the current allocation, plus t₁'s resources and 1 drive left (4 drives)

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t₂ can use the current allocation, plus t₁'s resources and 1 drive left (4 drives)

 t_3 can use the current allocation, plus t_1 's & t_2 's resources and 1 drive left (8 drives)

Thread	m_i	c_{i}	m_i – c_i
t ₁	4	3	1
t ₂	8	4	4
t ₃	12	5	7

Suppose t_3 requests one more drive, then now there are no more available drives

Thread	m_i	c_{i}	m_i – c_i
t ₁	4	3	1
t ₂	8	4	4
t ₃	12	5	7

Suppose t₃ requests one more drive, then now there are no more available drives

Theoretically, everything might still work (e.g., t₁ may never request another drive)

Thread	m_i	c_{i}	m_i – c_i
t ₁	4	3	1
t ₂	8	4	4
t ₃	12	5	7

Suppose t₃ requests one more drive, then now there are no more available drives

Theoretically, everything might still work (e.g., t₁ may never request another drive)

However, t₃ must wait because allocating that extra drive would lead to an unsafe state, which in turn might lead to deadlock

• An extension of the original resource allocation graph

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- Edges can now be of 3 types:
 - Request Edge → a directed edge (t_i, r_j) indicates that t_i has requested r_j, but not yet acquired
 - Claim (dotted) Edge \rightarrow a directed edge (t_i, r_j) indicates that t_i might request r_i in the future
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 - Assignment Edge \rightarrow a directed edge $(r_j, \, t_i)$ indicates that the OS has allocated r_j to t_i
- Satisfying a request means converting a claim into an assignment edge

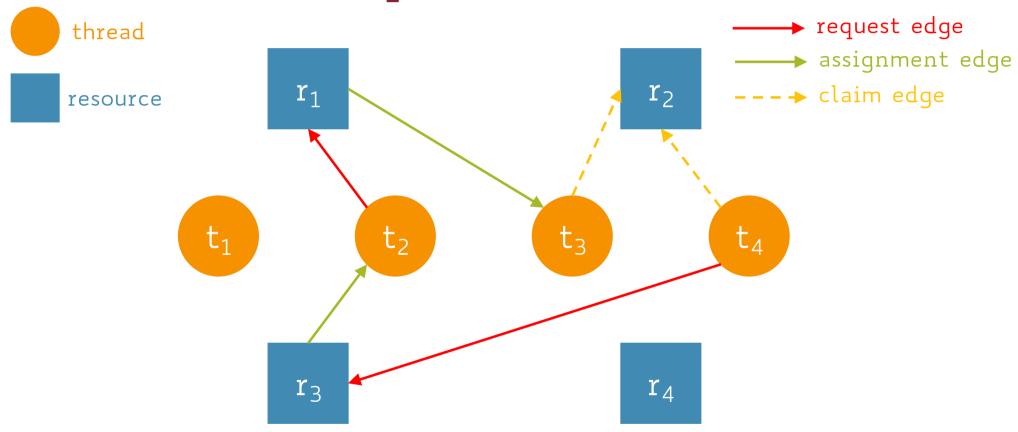
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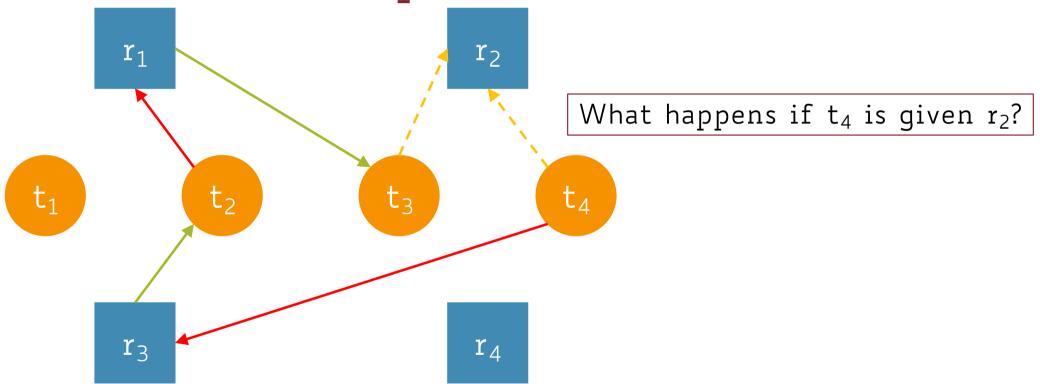
• A cycle in this extended RAG indicates an unsafe state

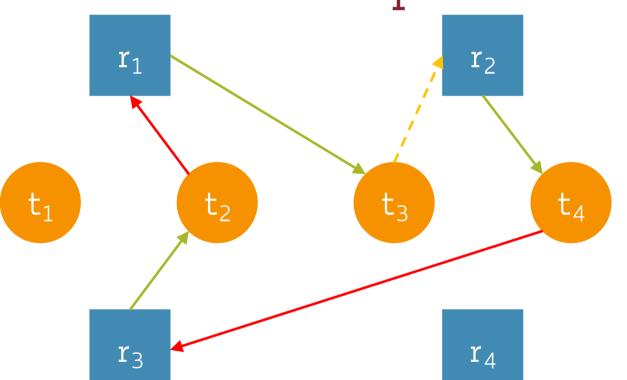
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- A cycle in this extended RAG indicates an unsafe state
- If the allocation results in an unsafe state, this will be denied even if the resource is actually available
- In other words, the claim edge is converted into a request edge and the thread will wait
- NOTE: This solution does not work when there are multiple instances of the same resource

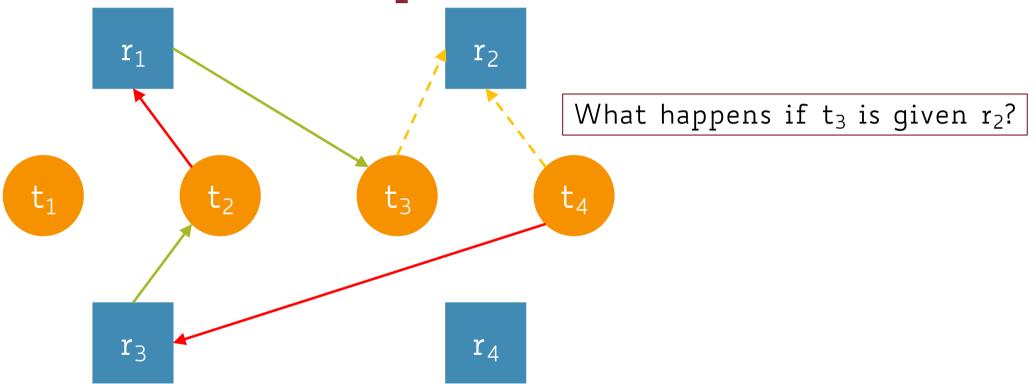


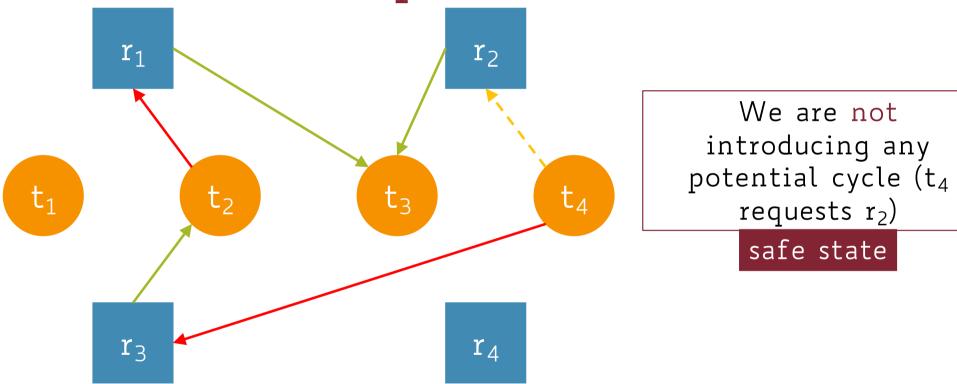


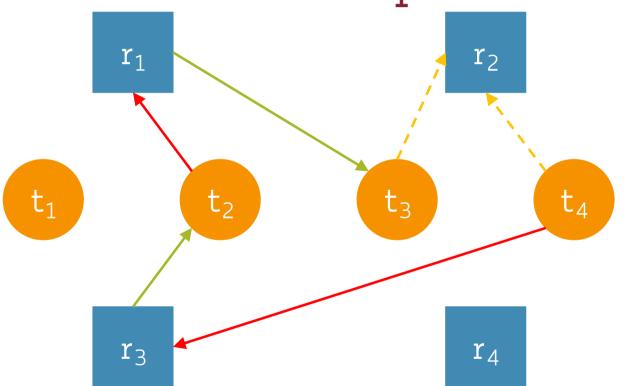


We are introducing a potential cycle (t₃ requests r₂), which in turn might cause deadlock

unsafe state







Start from a safe state

Invariant

Accept a request iff we move from a safe state to another

Banker's Algorithm

- Handles multiple instances of the same resource
- Forces threads to provide information on what resource they might need, in advance
- The resources requested must not exceed the total available in the system
- The algorithm allocates resources to a requesting thread if the allocation leaves the system in a safe state, otherwise the thread waits

Banker's Algorithm: Data Structures

- n = number of threads; m = number of resource types
- available[1..m]: m-dimensional vector
 - available[j] = k means there are k resources of type j available
- max[1..n, 1..m]: n x m matrix
 - max[i, j] = k means thread i may require at most k resources of type j
- allocation[1..n, 1..m]: n x m matrix
 - allocation[i, j] = k means thread i has allocated k resources of type j
- need[1..n, 1..m]: n x m matrix
 - need[i, j] = max[i, j] allocation[i, j] = k means thread i may need k more resources of type j to complete its task

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Banker's Algorithm: Idea

- The algorithm is divided in 2 tasks:
 - isSafeState → given the current status of allocation of resources, tests if this is a safe state
 - resourceRequest → given a thread and its resource request decides if such a request can be satisfied

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 - resourceRequest → given a thread and its resource request decides if such a request can be satisfied
- A request can be satisfied iff this leads to a safe state!
- In other words, the second tasks uses the output of the first one in order to make a decision

Banker's Algorithm: isSafeState

1. Let work and finish be vectors of length m and n, respectively

Initialize: work = available; finish[i] = false; for all i

2. Find an i such that:

finish[i] = false && need[i] ≤ work
If no such i exists, go to step 4.

3. Assume thread i executes:

```
work = work + allocation[i]; finish[i] = true; go to step 2.
```

4. If finish[i] == true for all i, the system is in a safe state

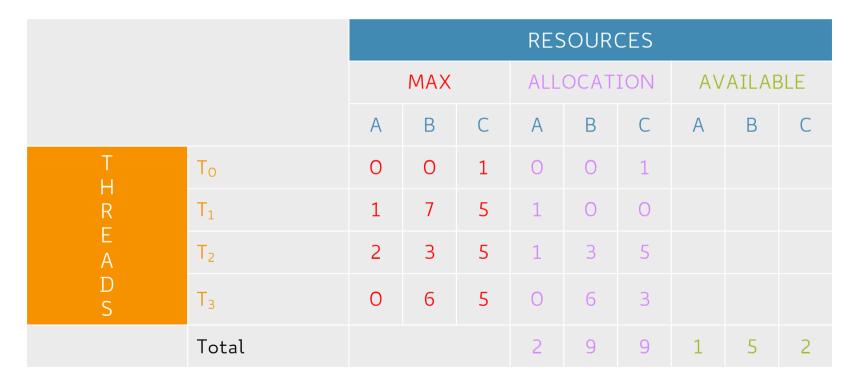
Banker's Algorithm: requestResource

Input: i (thread) and request an m-dimensional vector of requests

- 1. If request > need[i] raise an error as thread i is attempting to request more resources that it claimed, otherwise go to step 2.
- 2. If request > available thread i must wait since resources are not available, otherwise go to step 3.
- 3. Even if resources are available, test if this allocation will lead to a safe state by simulating it available -= request; allocation[i] += request; need[i] -= request; isSafeState() ? OK : rollback() and wait()

Banker's Algorithm: Example

A snapshot of the current state of the system



Q1: How many resources of type A, B, and C are there overall?

					RES	SOUR	CES			
			MAX		ALL	OCAT	ION	AV	AILAE	BLE
		А	В	С	Α	В	С	Α	В	С
T	T ₀	0	0	1	0	0	1			
R	T ₁	1	7	5	1	0	0			
E A	T ₂	2	3	5	1	3	5			
D S	T ₃	0	6	5	0	6	3			
	Total				2	9	9	1	5	2

Q1: How many resources of type A, B, and C are there overall?

					RES	SOUR	CES			
			MAX		ALL	OCAT	ION	AV	AILAE	BLE
		А	В	С	Α	В	С	Α	В	С
T H	T ₀	0	0	1	0	0	1			
R	T ₁	1	7	5	1	0	0			
E A	T ₂	2	3	5	1	3	5			
D S	T ₃	0	6	5	0	6	3			
	Total				2	9	9	1	5	2

Q2: What is the content of the NEED matrix?

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		А	В	С	А	В	С	Α	В	С	А	В	С
T H	To	0	0	1	0	0	1						
R	T_1	1	7	5	1	0	0						
E A	T ₂	2	3	5	1	3	5						
D S	T ₃	0	6	5	0	6	3						
	Total				2	9	9	1	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	'AILAE	BLE		NEED	
		А	В	С	Α	В	С	Α	В	С	А	В	С
T H	To	0	0	1	0	0	1						
R	T ₁	1	7	5	1	0	0						
E A	T ₂	2	3	5	1	3	5						
D S	T ₃	0	6	5	0	6	3						
	Total				2	9	9	1	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		Α	В	С	А	В	С	А	В	С	А	В	С
T H	T ₀	0	0	1	0	0	1				O − O = O		
R	T ₁	1	7	5	1	0	0						
E A	T ₂	2	3	5	1	3	5						
D S	T ₃	0	6	5	0	6	3						
	Total				2	9	9	1	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	3LE		NEED	
		Α	В	С	Α	В	С	Α	В	С	А	В	С
T H	T ₀	0	0	1	0	0	1				0	0-0 =	
R	T ₁	1	7	5	1	0	0						
E A	T ₂	2	3	5	1	3	5						
D S	T ₃	0	6	5	0	6	3						
	Total				2	9	9	1	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		А	В	С	Α	В	С	Α	В	С	А	В	С
T H	T ₀	0	0	1	0	0	1				0	0	1-1 = O
R	T ₁	1	7	5	1	0	0						
E A	T ₂	2	3	5	1	3	5						
D S	T ₃	О	6	5	0	6	3						
	Total				2	9	9	1	5	2			

Q2: What is the content of the NEED matrix?

NEED[i, j] = MAX[i, j] - ALLOCATION[i, j]

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		Α	В	С	Α	В	С	Α	В	С	А	В	С
T H	To	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Q3: Is the system in a safe state? Why?

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		А	В	С	А	В	С	Α	В	С	А	В	С
T H	To	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Let's start with T₀

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	'AILAE	BLE		NEED	
		Α	В	С	Α	В	С	Α	В	С	А	В	С
T H	To	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

Eventually, To finishes and releases all its resources

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	AILA	BLE		NEED	
		Α	В	С	А	В	С	Α	В	С	А	В	С
T H	To	0	0	1	0	0	1				0	0	0
R	T_1	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

 T_1 can't execute as it still might NEED (0, 7, 5) and AVAILABLE = (1, 5, 3)

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		А	В	С	Α	В	С	Α	В	С	А	В	С
T H	To	0	0	1	-	-	-				-	-	_
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	8	1	5	3			

 T_2 can execute as it still might NEED (1, 0, 0) and AVAILABLE = (1, 5, 3)

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		Α	В	С	Α	В	С	А	В	С	А	В	С
T H	T ₀	0	0	1	-	-	-				-	-	_
R	T ₁	1	7	5	1	0	0				0	7	5
E A D S	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	8	1	5	3			

 T_2 can execute as it still might NEED (1, 0, 0) and AVAILABLE = (1, 5, 3)



T₂ eventually finishes and releases all its resources



T₃ can execute as it still might NEED (O, O, 2) and AVAILABLE = (2, 8, 8)

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		А	В	С	А	В	С	А	В	С	А	В	С
T H	To	0	0	1	-	-	-				_	-	_
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	-	_	_				-	-	-
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				1	6	3	2	8	8			

T₃ can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 3, 6)



T₃ eventually finishes and releases all its resources



 T_1 can now execute since NEED (0, 7, 5) and AVAILABLE = (2, 14, 11)

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	'AILAE	BLE		NEED	
		Α	В	С	А	В	С	Α	В	С	А	В	С
T H	T ₀	0	0	1	-	-	-				-	-	-
R	T_1	1	7	5	1	7	5				0	0	0
E A	T ₂	2	3	5	-	-	-				-	-	-
D S	T ₃	0	6	5	-	_	-				-	-	-
	Total				1	7	5	2	7	6			

We have found a sequence of execution T_0 , T_2 , T_3 , T_1 which leads to safe state!

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		Α	В	С	Α	В	С	Α	В	С	А	В	С
T H	T ₀	0	0	1	-	_	-				_	-	-
R	T ₁	1	7	5	-	_	-				-	-	_
E A	T ₂	2	3	5	-	_	-				-	-	-
D S	T ₃	0	6	5	-	_	_				-	-	-
	Total				-	-	-	3	14	11			

Q4: If T_1 issues a REQUEST (0, 5, 2), can this be granted immediately?

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	3LE		NEED	
		А				В	С	Α	В	С	А	В	С
T H	To	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

We have to ask ourselves: 1. if the request can be satisfied;

2. if it will lead to a safe state

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		А				В	С	Α	В	С	А	В	С
T H	T ₀	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

To answer 1. check if: a. REQUEST <= NEED and b. REQUEST <= AVAILABLE

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	3LE		NEED	
		А				В	С	Α	В	С	А	В	С
T H	To	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

1.a. REQUEST <= NEED?

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	3LE		NEED	
		А				В	С	Α	В	С	А	В	С
T H	To	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

1.a. REQUEST <= NEED? YES! (0, 5, 2) <= (0, 7, 5)

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	'AILAE	BLE		NEED	
		Α	В	С	А	В	С	А	В	С	А	В	С
T H	T ₀	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

1.b. REQUEST <= AVAILABLE?

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		А	В	С	Α	В	С	А	В	С	А	В	С
T H	T ₀	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

1.b. REQUEST <= AVAILABLE? YES! (0, 5, 2) <= (1, 5, 2)

					RES	OUR	CES						
			MAX		ALL	OCAT	ION	AV	AILAE	BLE		NEED	
		А	В	С	Α	В	С	А	В	С	А	В	С
T H	T ₀	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

To answer 2. we simulate the request is granted and see if we are still in a safe state

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AV	'AILAE	BLE		NEED	
		А	В	С	А	В	С	А	В	С	А	В	С
T H	To	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	0	0				0	7	5
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	9	9	1	5	2			

To answer 2. we simulate the request is granted and see if we are still in a safe state

					RES	SOUR	CES							
			MAX		ALL	ALLOCATION			AVAILABLE			NEED		
		А	В	С	Α	В	С	Α	В	С	А	В	С	
T H	T ₀	0	0	1	0	0	1				0	0	0	
R	T ₁	1	7	5	1	5	2				0	2	3	
E A	T ₂	2	3	5	1	3	5				1	0	0	
D S	T ₃	0	6	5	0	6	3				0	0	2	
	Total				2	14	11	1	0	0				

Let's start with T₀

					RES	SOUR	CES						
			MAX		ALL	OCAT	ION	AVAILABLE			NEED		
		Α	В	С	А	В	С	Α	В	С	А	В	С
T H	T ₀	0	0	1	0	0	1				0	0	0
R	T ₁	1	7	5	1	5	2				0	2	3
E A	T ₂	2	3	5	1	3	5				1	0	0
D S	T ₃	0	6	5	0	6	3				0	0	2
	Total				2	14	11	1	0	0			

Eventually, To finishes and releases all its resources

			MAX		ALL	ALLOCATION			AVAILABLE			NEED		
		Α	В	С	А	В	С	А	В	С	А	В	С	
T H	T ₀	0	0	1	-	-	-				-	-	-	
R	T ₁	1	7	5	1	5	2				0	2	3	
E A	T ₂	2	3	5	1	3	5				1	0	0	
D S	T ₃	0	6	5	0	6	3				0	0	2	
	Total				2	14	10	1	0	1				

 T_1 can't execute as it still might NEED (0, 2, 3) and AVAILABLE = (1, 0, 1)

					RES	OUR	CES							
			MAX		ALL	ALLOCATION			AVAILABLE			NEED		
		А	В	С	Α	В	С	Α	В	С	А	В	С	
T H	T ₀	0	0	1	-	-	-				-	-	-	
R	T_1	1	7	5	1	5	2				0	2	3	
E A	T ₂	2	3	5	1	3	5				1	0	0	
D S	T ₃	0	6	5	0	6	3				0	0	2	
	Total				2	14	10	1	0	1				

 T_2 can execute as it still might NEED (1, 0, 0) and AVAILABLE = (1, 0, 1)

			MAX		ALL	ALLOCATION			AVAILABLE			NEED		
		А	В	С	Α	В	С	Α	В	С	А	В	С	
T H	T ₀	0	0	1	-	-	-				-	-	-	
R	T ₁	1	7	5	1	5	2				0	2	3	
E A	T ₂	2	3	5	1	3	5				1	0	0	
D S	T ₃	0	6	5	0	6	3				0	0	2	
	Total				2	14	10	1	0	1				

T₂ can execute as it still might NEED (1, 0, 0) and AVAILABLE = (1, 0, 1)

			MAX		ALL	ALLOCATION			AVAILABLE			NEED		
		А	В	С	Α	В	С	Α	В	С	А	В	С	
T H	T ₀	0	0	1	-	_	-				-	-	-	
R	T ₁	1	7	5	1	5	2				0	2	3	
E A	T ₂	2	3	5	2	3	5				0	0	0	
D S	T ₃	0	6	5	0	6	3				0	0	2	
	Total				3	14	10	0	0	1				

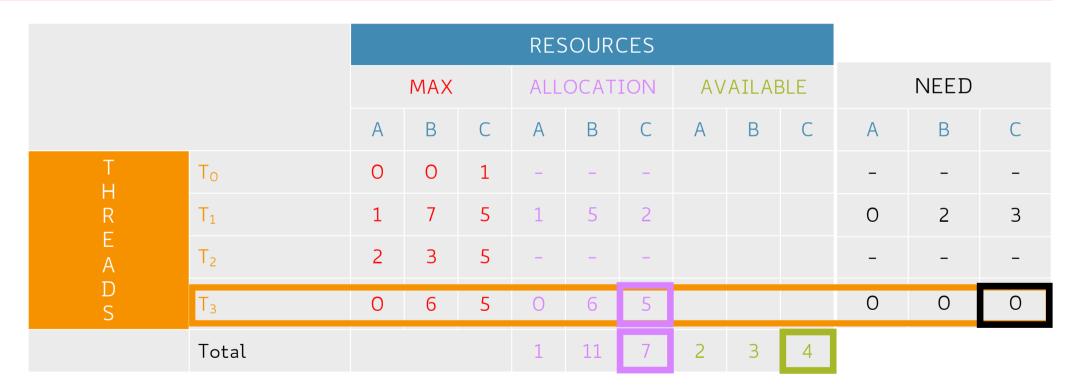
T₂ eventually finishes and releases all its resources



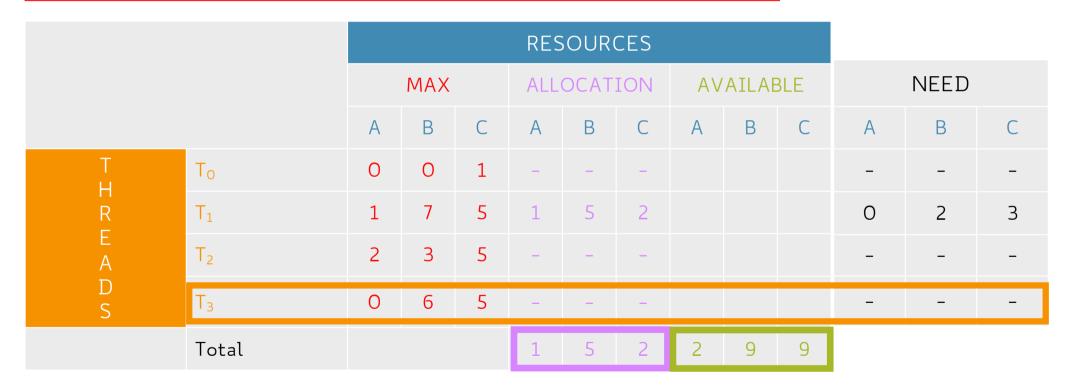
T₃ can execute as it still might NEED (O, O, 2) and AVAILABLE = (2, 3, 6)

			MAX		ALL	ALLOCATION			AVAILABLE			NEED		
		А	В	С	Α	В	С	А	В	С	А	В	С	
T H	To	0	0	1	-	-	-				-	-	-	
R	T ₁	1	7	5	1	5	2				0	2	3	
E A	T ₂	2	3	5	-	-	-				-	-	-	
D S	T ₃	0	6	5	0	6	3				0	0	2	
	Total				1	11	5	2	3	6				

T₃ can execute as it still might NEED (0, 0, 2) and AVAILABLE = (2, 3, 6)



T₃ eventually finishes and releases all its resources



 T_1 can now execute since NEED (0, 2, 3) and AVAILABLE = (2, 9, 9)

					RES	OUR	CES							
			MAX		ALL	ALLOCATION			AVAILABLE			NEED		
		А	В	С	Α	В	С	Α	В	С	А	В	С	
T H	To	0	0	1	-	-	-				-	-	-	
R	T_1	1	7	5	1	7	5				0	0	0	
E A	T ₂	2	3	5	_	-	-				_	-	-	
D S	T ₃	0	6	5	_	_	-				-	-	-	
	Total				1	7	5	2	7	6				

We have found a sequence of execution T_0 , T_2 , T_3 , T_1 which leads to safe state!

					RES	OUR	CES							
			MAX		ALL	ALLOCATION			AVAILABLE			NEED		
		А	В	С	Α	В	С	Α	В	С	А	В	С	
T H	To	0	0	1	_	_	-				_	-	-	
R	T ₁	1	7	5	-	-	-				-	-	-	
E A	T ₂	2	3	5	-	_	-				-	-	-	
D S	T ₃	0	6	5	-	_	-				-	-	-	
	Total				-	-	-	3	14	11				

 Deadlock → a situation in which a set of threads/processes cannot proceed because each one requires resources held by another

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- Detection and Recovery → recognize deadlock after it has occurred and break it

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- Detection and Recovery → recognize deadlock after it has occurred and break it
- Prevention → design resource allocation strategies which guarantee at least one of the 4 necessary deadlock conditions never holds

- Deadlock → a situation in which a set of threads/processes cannot proceed because each one requires resources held by another
- Detection and Recovery → recognize deadlock after it has occurred and break it
- Prevention → design resource allocation strategies which guarantee at least one of the 4 necessary deadlock conditions never holds
- Avoidance → runtime checks to avoid deadlock online

In practice, most OSs don't do anything and leave it all to applications

