

All APS Formula:

• Class Limit:

IF Upper Class and Lower Class of consecutive classes are different

i.e $6 \rightarrow 8$

$9 \rightarrow 11$

• Class Boundaries:

IF Upper Class and Lower Class are same of consecutive classes

i.e $6 \rightarrow 8$

$8 \rightarrow 10$

• Class Marks

Add Upper Class and Lower Class of Class Boundary

Divide it by 2

i.e $6 - 8$

7

$8 - 10$

9

• Class Interval height

Difference btw upper Class and Lower Class of Class Boundary

i.e

$6 - 8$

$\Rightarrow 2$

$8 - 10$

$\Rightarrow 2$

Uniform Data

Class Interval for all classes are same

i.e. $6-8 \rightarrow 2$

$8-10 \rightarrow 2$

Uniform Data

Non or Un-Uniform Data

- Class Interval of classes are not same

$6-8 \Rightarrow 2$

$8-11 \Rightarrow 3$

$11-12 \Rightarrow 1$


- So we need Proportional height = F/h ($\frac{\text{Frequency}}{\text{Class Interval}}$)

~~Chart Diagram~~ + Pie Diagram: \Rightarrow 

$\rightarrow \text{Angle} = \frac{\text{Component Part}}{\text{Whole Quantity}} \times 360^\circ$

\rightarrow Each Component is represent by Unique Key



Histogram \Rightarrow 

If Data is Uniform

We need


- Class Boundaries
- Frequency

If Un-Uniform We need

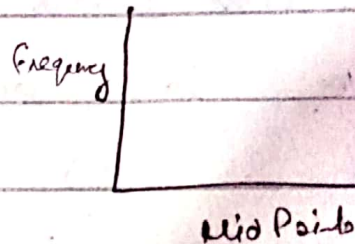
- Class Boundaries
- Frequency $\rightarrow F$
- Class Interval $\rightarrow h$
- Proportional Height $\rightarrow F/h$

Note :

In Histogram, if data is non-uniform we need to Graph w.r.t their (height & class interval)

Frequency Polygons: \Rightarrow 

- Frequency
- Mid Points



Measure of Central Tendency

1) Arithmetic Mean: \bar{x}

$$\bar{x} = \frac{\sum x}{n}$$

$$\bar{x} = \frac{\sum fx}{\sum f}$$

2) Scale, Change of origin, Coding

$$u = \frac{x - a}{h}$$

$$\bar{x} = a + \frac{\sum u}{\sum n} \times h$$

$$\bar{x} = a + \frac{\sum fu}{\sum f} \times h$$

- We use when Data Uncle is too large so we convert it into Small Subgroups which is easy to compute and have no effect on Mean

3) Geometric Mean:

$$G = \text{antilog} \left[\frac{1}{n} \times \sum \log x \right]$$

$$G = \text{antilog} \left[\frac{1}{\sum f} \times \sum f \log x \right]$$

4) Harmonic Mean:

$$H = \frac{\sum f}{\sum f \left(\frac{1}{x} \right)}$$

$$H = \frac{n}{\sum \frac{1}{x}}$$

Median:

- Value that divides your data in two equal parts

① Not Necessary, the value is in Data

② Necessary, the value is in Range

i.e. 2, 3, 5, 7, 9

5 is median

2, 3, 7, 9

5 is median

$$\text{median} = l + \frac{h}{f} \left(\frac{n}{2} - C \right) \Rightarrow C, \text{ C.F of above class}$$

$$\text{median Class} = \frac{n}{2} \Rightarrow \text{look in C.F}$$

Mode:

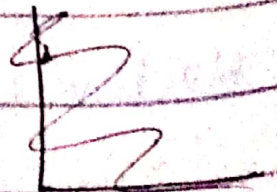
- Most Frequent Value \ Popular Value
- Data having One Mode \rightarrow Uni-Modal Data
- Data having Two Mode \rightarrow Bi-Modal Data

$$\text{Mode} = l + \frac{f_m - f_1}{(f_m - f_1) + (f_m - f_2)} \times h$$

- Mode Class \rightarrow Highest Frequency occurred class

Impeical Relation blw Mean Median Mode

$$\text{Mode} = 3 \text{ Median} - 2 \text{ Mean}$$

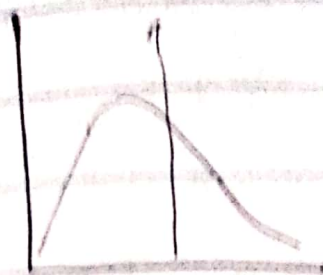


- 3 Possibility

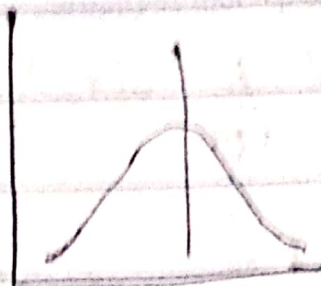
$$\text{mean} > \text{median} > \text{mode} \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{Skewed}$$

$$\text{mean} < \text{median} < \text{mode}$$

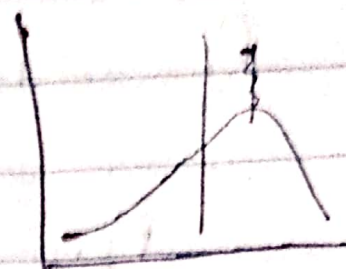
$$\text{mean} = \text{median} = \text{mode} - \text{Symetric}$$



-ve Skewed



Symmetric



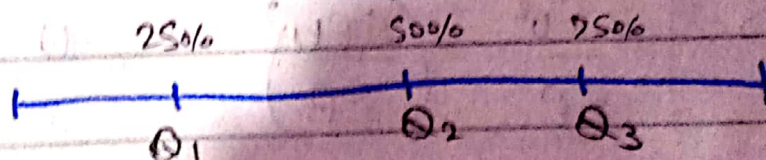
+ve Skewed

Quantiles $\rightarrow 4$

Q_1, Q_2, Q_3

$Q_2 = \text{Median}$

$$Q_i = L + \frac{h}{f} \left(\frac{i}{4} - c \right)$$

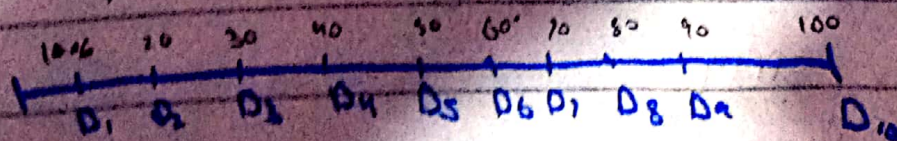


Deciles $\rightarrow 10$

D_1, D_2, \dots, D_{10}

$D_5 = \text{Median}$

$$D_i = L + \frac{h}{f} \left(\frac{i}{10} - c \right)$$



Percentiles: — 100

$$P_i = l + \frac{h}{f} \left(\frac{i}{100} - c \right)$$

$$P_1, \dots, P_{100}$$

Variance & Standard Deviation

$$\bullet U = S^2$$

→ Absolute Dispersion

$$\bullet S = \sqrt{\frac{\sum fx^2}{\sum f} - \left(\frac{\sum fx}{\sum f} \right)^2}$$

$$\bullet S = \sqrt{\frac{\sum fu^2}{\sum f} - \left(\frac{\sum fu}{\sum f} \right)^2}$$

$$U = \frac{x - a}{h}$$

⇒ • Data Spread kila Variance yeah Babla

• More - Min Tells Total Spread of Data

Variance & Standard Deviation \rightarrow Relative Dispersion

To compare two Data Sets of Different Types

$$C.V = \frac{S}{\bar{x}} \times 100$$

- Coefficient of Variance less means reliable

Moments About Mean

$$M_i = \frac{\sum (x - \bar{x})^i}{n} \quad i = 1, 2, 3, 4$$

$$M_i = \frac{\sum f(x - \bar{x})^i}{\sum f}$$

- Moments help us to understand the shape

$$M_2 = \text{Variance} = V$$

$$V = S^2$$

$$S = \sqrt{V}$$

$$B_1 = b_1$$

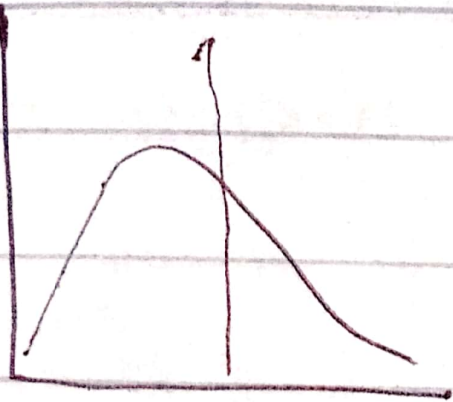
For Large \downarrow For Small

$$B_1 = \frac{M_3}{S^3}$$

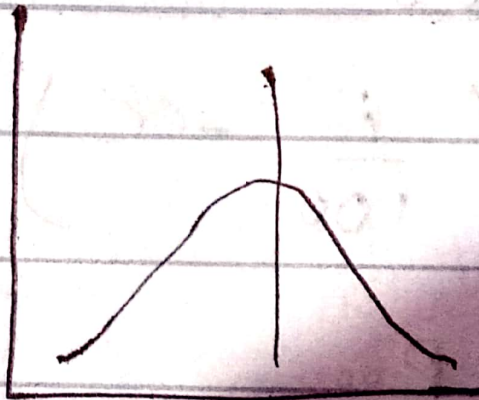
if $B_1 < 0 \rightarrow$ -ve skewed

$B_1 = 0 \rightarrow$ symmetric

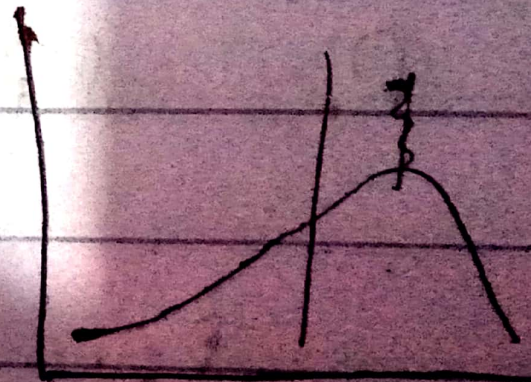
$B_1 > 0 \rightarrow$ +ve skewed



-ve Skewed



Symetric



+ve Skewed

Kurtosis

B_2, b_2

$$b_2 = \frac{m_4}{m_2^2}$$

- If b_2 is near to 3 data-distribution is Normal otherwise Distribution of Different kind.