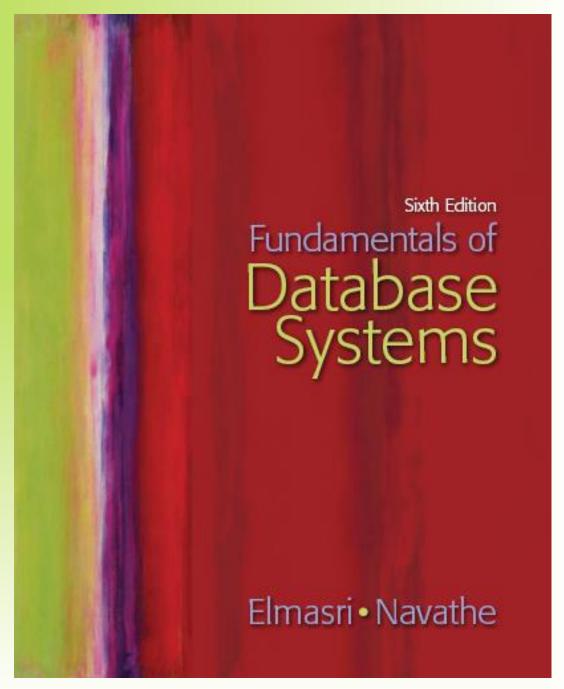
Chapter 3

The Relational Data Model and SQL



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## Chapter 3

# The Relational Data Model and Relational Database Constraints





### Chapter 3 Outline

- Relational Model Concepts
- Relational Model Constraints and Relational Database Schemas
- Update Operations and Dealing with Constraint Violations



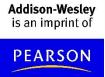
### Relational Model Concepts

- The relational Model of Data is based on the concept of a Relation
  - Has a formal mathematical foundation provided by set theory and first order predicate logic
- We review the essentials of the formal relational model in this chapter
- In practice, there is a standard model based on SQL (Structured Query Language) – described in Chapters 4 and 5
- Note: There are several important differences between the formal model and the practical model, as we shall see



### Relational Model Origins

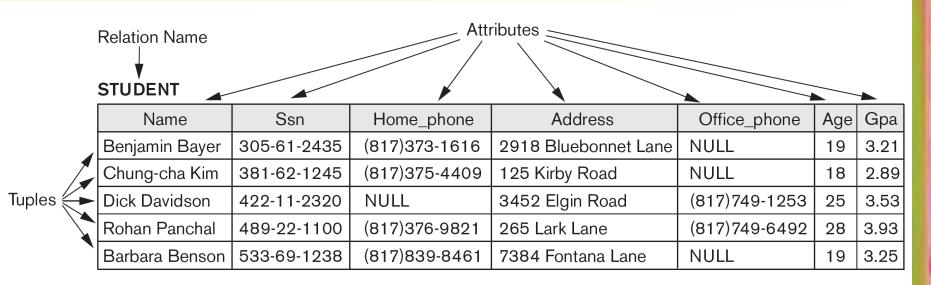
- The model was first proposed by Dr. E.F. Codd of IBM Research in 1970 in the following paper:
  - "A Relational Model for Large Shared Data Banks,"
    Communications of the ACM, June 1970
- The above paper caused a major revolution in the field of database management
- Dr. Codd earned the coveted ACM Turing Award in 1981



### **Informal Definitions**

- Informally, a relation looks like a table of values or a flat file of records (see Figure 3.1 on next slide).
- A relation contains a set of rows.
- The data elements in each row represent certain facts that correspond to a real-world entity or relationship
  - In the formal model, rows are called tuples
- Each column has a column header that gives an indication of the meaning of the data items in that column
  - In the formal model, the column header is called an attribute name (or just attribute)





**Figure 3.1** The attributes and tuples of a relation STUDENT.



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### **Informal Definitions**

- Key of a Relation:
  - Each row (tuple) in the table is uniquely identified by the value of a particular attribute (or several attributes together)
    - Called the key of the relation
  - In the STUDENT relation, SSN is the key
  - If no attributes posses this uniqueness property, a new attribute can be added to the relation to assign unique row-id values (e.g. unique sequential numbers) to identify the rows in a relation
    - Called artificial key or surrogate key



### Formal Definitions — Relation Schema

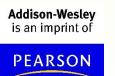
- Relation Schema (or description) of a Relation:
  - Denoted by R(A1, A2, ..., An)
  - R is the name of the relation
  - The attributes of the relation are A1, A2, ..., An
  - n is the cardinality of the relation
- Example:
  - CUSTOMER (Cust-id, Cust-name, Address, Phone#)
    - CUSTOMER is the relation name
    - The CUSTOMER relation schema (or just relation) has four attributes: Cust-id, Cust-name, Address, Phone#
- Each attribute has a domain or a set of valid values.



Addison-Wesley For example, the domain of Cust-id can be 6 digit numbers.

### Formal Definitions - Tuple

- A tuple is an ordered set of values (enclosed in angled brackets '< ... >')
- Each value is derived from an appropriate domain.
- A row in the CUSTOMER relation is a 4-tuple and would consist of four values, for example:
  - <632895, "John Smith", "101 Main St. Atlanta, GA 30332", "(404) 894-2000">
  - Called a 4-tuple because it has 4 values
  - In general, a particular relation will have n-tuples, where n is the number of attributes for the relation
- A relation is a set of such tuples (rows)



### Formal Definitions - Domain

- A domain of values can have a logical definition:
  - Example: "USA\_phone\_numbers" are the set of 10 digit phone numbers valid in the U.S.
- A domain also has a data-type or a format defined for it.
  - The USA\_phone\_numbers may have a format: (ddd)ddd-dddd where each d is a decimal digit.
  - Dates have various formats such as year, month, date formatted as yyyy-mm-dd, or as dd:mm:yyyy etc.
- The attribute name designates the role played by a domain in a relation:
  - Used to interpret the meaning of the data elements corresponding to that attribute
  - Example: The domain Date may be used to define two attributes "Invoice-date" and "Payment-date" with different meanings (roles)



# Formal Definitions – State of a Relation

- Formally, a relation state r(R) is a subset of the Cartesian product of the domains of its attributes
  - each domain contains the set of all possible values the attribute can take.
  - The Cartesian product contains all possible tuples from the attribute domains
  - The relations state r(R) is the subset of tuples that represent valid information in the mini-world at a particular time



### Formal Definitions - Summary

- Formally (see Figure 3.1),
  - Given relation schema R(A1, A2, ......, An)
  - Relation state r(R) ⊂ dom(A1) X dom(A2) X ....X dom(An)
- R(A1, A2, ..., An) is the schema of the relation
- R is the name of the relation
- A1, A2, ..., An are the attributes of the relation
- r(R): is a specific state (or "instance" or "population") of relation R – this is a set of tuples (rows) in the relation at a particular moment in time
  - $r(R) = \{t1, t2, ..., tn\}$  where each ti is an n-tuple
- $ti = \langle v1, v2, ..., vn \rangle$  where each vj element-of dom(Aj)



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### Formal Definitions - Example

- Let R(A1, A2) be a relation schema:
  - Let dom(A1) = {0,1}
  - Let dom(A2) = {a,b,c}
- Then: The Cartesian product dom(A1) X dom(A2) contains all possible tuples from these domains:

- The relation state r(R) ⊂ dom(A1) X dom(A2)
- For example: One possible state r(R) could be {<0,a>,
  <0,b>,<1,c>}
  - This state has three 2-tuples: <0,a> , <0,b> , <1,c>



### Relation Definitions Summary

	Informal Terms	Formal Terms
	Table	Relation
	Column Header	Attribute
	All possible Column Values or Data Type	Domain
	Row	Tuple
	Table Definition	Schema of a Relation
Addison-V	Populated Table	State of the Relation



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### **Characteristics Of a Relation**

- Ordering of tuples in a relation r(R):
  - The tuples are not considered to be ordered, because a relation is a set of tuples (elements of a set are unordered) – see Figure 3.2
- Ordering of attributes in a relation schema R (and of values within each tuple):
  - We will consider the attributes in R(A1, A2, ..., An) and the values in each t=<v1, v2, ..., vn> to be ordered. It is an ordered list of n values.
  - However, a more general definition of relation (which we will not use) does not require attribute ordering
  - In this case, a tuple t = { <ai, vi>, ..., <aj, vj> } is an unordered set of n <attribute, value> pairs one pair for each of the relation attributes (see Figure 3.3)

This is needed in query optimization (see Chapter 19)



Figure 3.2

The relation STUDENT from Figure 3.1 with a different order of tuples.

#### **STUDENT**

Name	Ssn	Home_phone	Address	Office_phone	Age	Gpa
Dick Davidson	422-11-2320	NULL	3452 Elgin Road	(817)749-1253	25	3.53
Barbara Benson	533-69-1238	(817)839-8461	7384 Fontana Lane	NULL	19	3.25
Rohan Panchal	489-22-1100	(817)376-9821	265 Lark Lane	(817)749-6492	28	3.93
Chung-cha Kim	381-62-1245	(817)375-4409	125 Kirby Road	NULL	18	2.89
Benjamin Bayer	305-61-2435	(817)373-1616	2918 Bluebonnet Lane	NULL	19	3.21

#### Figure 3.1

Name	Ssn	Home_phone	Address	Office_phone	Age	Gpa
Benjamin Bayer	305-61-2435	(817)373-1616	2918 Bluebonnet Lane	NULL	19	3.21
Chung-cha Kim	381-62-1245	(817)375-4409	125 Kirby Road	NULL	18	2.89
Dick Davidson	422-11-2320	NULL	3452 Elgin Road	(817)749-1253	25	3.53
Rohan Panchal	489-22-1100	(817)376-9821	265 Lark Lane	(817)749-6492	28	3.93
Barbara Benson	533-69-1238	(817)839-8461	7384 Fontana Lane	NULL	19	3.25





#### Figure 3.3

Two identical tuples when the order of attributes and values is not part of relation definition.

t = < (Name, Dick Davidson),(Ssn, 422-11-2320),(Home\_phone, NULL),(Address, 3452 Elgin Road), (Office\_phone, (817)749-1253),(Age, 25),(Gpa, 3.53)>

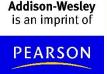
t = < (Address, 3452 Elgin Road),(Name, Dick Davidson),(Ssn, 422-11-2320),(Age, 25), (Office\_phone, (817)749-1253),(Gpa, 3.53),(Home\_phone, NULL)>



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### Characteristics Of Relations (cont.)

- Values in a tuple:
  - All values are considered atomic (indivisible).
    Composite and multivalued attributes not allowed
  - Each value must be from the domain of the attribute for that column
    - If tuple t = <v1, v2, ..., vn> is a tuple (row) in the relation state r
      of R(A1, A2, ..., An)
    - Then each vi must be a value from dom(Ai)
  - A special **null** value is used to represent values that are *unknown*, exist but not available or inapplicable or undefined to certain tuples.



### Characteristics Of Relations (cont.)

#### Notation:

- We refer to component values of a tuple t by:
  - t[Ai] or t.Ai
  - This is the value vi of attribute Ai for tuple t
- Similarly, t[Au, Av, ..., Aw] refers to the subtuple of t containing the values of attributes Au, Av, ..., Aw, respectively in t



### Relational Integrity Constraints

- Constraints are conditions that must hold on all valid relation states.
- Constraints are derived from the mini-world semantics
- There are three main types of built-in constraints in the relational model (Explicit Constraints):
  - Key constraints
  - Entity integrity constraints
  - Referential integrity constraints
- Another implicit constraint is the domain constraint
  - Every value in a tuple must be from the domain of its attribute (or it could be null, if allowed for that attribute)



### **Key Constraints**

- Superkey SK of R:
  - Is a set of attributes SK of R with the following condition:
    - No two tuples in any valid relation state r(R) will have the same value for SK
    - That is, for any distinct tuples t1 and t2 in r(R), t1.SK ≠ t2.SK
    - This condition must hold in any valid state r(R)

						_
Name	Ssn	Home_phone	Address	Office_phone	Age	Gpa
Benjamin Bayer	305-61-2435	(817)373-1616	2918 Bluebonnet Lane	NULL	19	3.21
Chung-cha Kim	381-62-1245	(817)375-4409	125 Kirby Road	NULL	18	2.89
Dick Davidson	422-11-2320	NULL	3452 Elgin Road	(817)749-1253	25	3.53
Rohan Panchal	489-22-1100	(817)376-9821	265 Lark Lane	(817)749-6492	28	3.93
Barbara Benson	533-69-1238	(817)839-8461	7384 Fontana Lane	NULL	19	3.25





### **Key Constraints**

#### • **Key** K of R:

- Is a "minimal" superkey
- Formally, a key K is a superkey such that removal of any attribute from K results in a set of attributes that is not a superkey (or key) any more (does not possess the superkey uniqueness property)
- Hence, a superkey with one attribute is always a key

Name	Ssn	Home_phone	Address	Office_phone	Age	Gpa
Benjamin Bayer	305-61-2435	(817)373-1616	2918 Bluebonnet Lane	NULL	19	3.21
Chung-cha Kim	381-62-1245	(817)375-4409	125 Kirby Road	NULL	18	2.89
Dick Davidson	422-11-2320	NULL	3452 Elgin Road	(817)749-1253	25	3.53
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Barbara Benson	533-69-1238	(817)839-8461	7384 Fontana Lane	NULL	19	3.25



### Key Constraints (cont.)

- Example: Consider the CAR relation schema:
  - CAR(State, Reg#, SerialNo, Make, Model, Year)
  - CAR has two keys (determined from the mini-world constraints):
    - Key1 = {State, Reg#}
    - Key2 = {SerialNo}
  - Both are also superkeys of CAR
  - However, {SerialNo, Make} is a superkey but not a key.
- In general:
  - Any key is a superkey (but not vice versa)
  - Any set of attributes that *includes a key* is a *superkey*
  - A minimal superkey is also a key



### Key Constraints (cont.)

- If a relation has several keys, they are called candidate keys; one is chosen to be the primary key; the others are called unique (or secondary) keys
  - The primary key attributes are underlined.
- Example: Consider the CAR relation schema:
  - CAR(State, Reg#, SerialNo, Make, Model, Year)
  - We choose License\_number (which contains (State, Reg#) together) as the primary key see Figure 3.4
- The primary key value is used to uniquely identify each tuple in a relation
  - Provides the tuple identity
  - Also used to reference the tuple from other tuples
- General rule: Choose the smallest-sized candidate key (in bytes) as primary key
- Not always applicable choice is sometimes subjective (as
  Addison-Wesley in Figure 3.4 see next slide)



#### CAR

#### License number Engine\_serial\_number Make Model Year Texas ABC-739 A69352 Ford Mustang 02 Florida TVP-347 B43696 Oldsmobile Cutlass 05 New York MPO-22 X83554 Oldsmobile Delta 01 California 432-TFY C43742 Mercedes 190-D 99 Camry California RSK-629 Y82935 Toyota 04 Texas RSK-629 U028365 XJS 04 Jaguar

#### Figure 3.4

The CAR relation, with two candidate keys: License\_number and Engine\_serial\_number.

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### Relational Database Schema

#### Relational Database Schema:

- A set S of relation schemas that belong to the same database.
- S is the name of the whole database schema
- $-S = \{R1, R2, ..., Rn\}$
- R1, R2, ..., Rn are the names of the individual relation schemas within the database S
- Figure 3.5 shows a COMPANY database schema with 6 relation schemas



#### **EMPLOYEE**

Fname Minit Lname <u>Ssn</u> Bdate Address Sex Salary Super\_ssn Dno

#### **DEPARTMENT**

Dname Dnumber Mgr\_ssn Mgr\_start\_date

#### **DEPT\_LOCATIONS**

<u>Dnumber</u> <u>Dlocation</u>

#### **PROJECT**

Pname Pnumber Plocation Dnum

#### WORKS\_ON

Essn Pno Hours

#### **DEPENDENT**

Essn Dependent\_name Sex Bdate Relationship

#### Figure 3.5

Schema diagram for the COMPANY relational database schema.

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### Relational Database State

- Next two slides show an example of a COMPANY database state (Figure 3.6)
  - Each relation has a set of tuples
    - The tuples in each table satisfy key and other constraints
    - If all constraints are satisfied by a database state, it is called a valid state
  - The database state changes to another state whenever the tuples in any relation are changed via insertions, deletions, or updates



#### Figure 3.6

One possible database state for the COMPANY relational database schema.

#### **EMPLOYEE**

Fname	Minit	Lname	Ssn	Bdate	Address	Sex	Salary	Super_ssn	Dno
John	В	Smith	123456789	1965-01-09	731 Fondren, Houston, TX	М	30000	333445555	5
Franklin	Т	Wong	333445555	1955-12-08	638 Voss, Houston, TX	М	40000	888665555	5
Alicia	J	Zelaya	999887777	1968-01-19	3321 Castle, Spring, TX	F	25000	987654321	4
Jennifer	S	Wallace	987654321	1941-06-20	291 Berry, Bellaire, TX	F	43000	888665555	4
Ramesh	K	Narayan	666884444	1962-09-15	975 Fire Oak, Humble, TX	М	38000	333445555	5
Joyce	Α	English	453453453	1972-07-31	5631 Rice, Houston, TX	F	25000	333445555	5
Ahmad	V	Jabbar	987987987	1969-03-29	980 Dallas, Houston, TX	М	25000	987654321	4
James	Е	Borg	888665555	1937-11-10	450 Stone, Houston, TX	М	55000	NULL	1

#### **DEPARTMENT**

Dname	<u>Dnumber</u>	Mgr_ssn	Mgr_start_date
Research	5	333445555	1988-05-22
Administration	4	987654321	1995-01-01
Headquarters	1	888665555	1981-06-19

#### **DEPT\_LOCATIONS**

Dnumber	Dlocation
1	Houston
4	Stafford
5	Bellaire
5	Sugarland
5	Houston



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#### WORKS\_ON

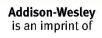
Essn	<u>Pno</u>	Hours
123456789	1	32.5
123456789	2	7.5
666884444	3	40.0
453453453	1	20.0
453453453	2	20.0
333445555	2	10.0
333445555	3	10.0
333445555	10	10.0
333445555	20	10.0
999887777	30	30.0
999887777	10	10.0
987987987	10	35.0
987987987	30	5.0
987654321	30	20.0
987654321	20	15.0
888665555	20	NULL

#### **PROJECT**

Pname	Pnumber	Plocation	Dnum
ProductX	1	Bellaire	5
ProductY	2	Sugarland	5
ProductZ	3	Houston	5
Computerization	10	Stafford	4
Reorganization	20	Houston	1
Newbenefits	30	Stafford	4

#### **DEPENDENT**

Essn	Dependent_name	Sex	Bdate	Relationship
333445555	Alice	F	1986-04-05	Daughter
333445555	Theodore	М	1983-10-25	Son
333445555	Joy	F	1958-05-03	Spouse
987654321	Abner	М	1942-02-28	Spouse
123456789	Michael	М	1988-01-04	Son
123456789	Alice	F	1988-12-30	Daughter
123456789	Elizabeth	F	1967-05-05	Spouse

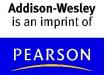




### **Entity Integrity Constraint**

#### Entity Integrity:

- The primary key attributes PK of each relation schema
  R in S cannot have null values in any tuple of r(R).
  - This is because primary key values are used to identify the individual tuples.
  - t.PK ≠ null for any tuple t in r(R)
  - If PK has several attributes, null is not allowed in any of these attributes
- Note: Other attributes of R may be also be constrained to disallow null values (called NOT NULL constraint), even though they are not members of the primary key.



### Referential Integrity Constraint

- A constraint involving two relations
  - The previous constraints (key, entity integrity) involve a single relation.
- Used to specify a relationship among tuples in two relations:
  - The referencing relation and the referenced relation.

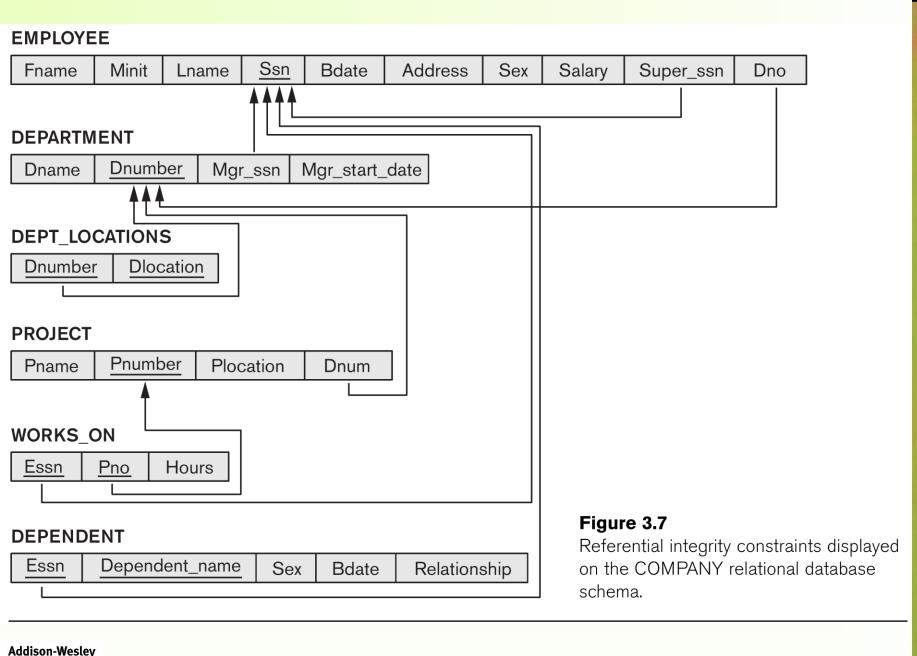


### Referential Integrity (cont.)

- Tuples in the referencing relation R1 have attributes FK (called foreign key attributes) that reference the primary key attributes PK of the referenced relation R2.
  - A tuple t1 in R1 is said to reference a tuple t2 in R2 if t1.FK = t2.PK
  - FK and PK have to be from same domain
- Referential integrity can be displayed as a directed arc from R1.FK to R2.PK – see









# Referential Integrity (or foreign key) Constraint (cont.)

- Statement of the constraint
  - For a particular database state, the value of the foreign key attribute (or attributes) FK in each tuple of the referencing relation R1 can be either:
    - (1) An existing primary key (PK) value of a tuple in the referenced relation R2, or
    - (2) a **null**.
- In case (2), the FK in R1 should **not** be a part of its own primary key, and cannot have the NOT NULL constraint.



### Other Types of Constraints

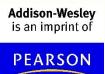
- Semantic Integrity Constraints:
  - cannot be expressed by the built-in model constraints
  - Example: "the max. no. of hours per employee for all projects he or she works on is 56 hrs per week"
- A constraint specification language can be used to express these
- SQL has TRIGGERS and ASSERTIONS to express some of these constraints (see Section





### Relational Update Operations

- Each relation will have many tuples in its current relation state
- The relational database state is a union of all the individual relation states at a particular time
- Whenever the database is changed, a new state arises
- Basic operations for changing the database:
  - INSERT new tuples in a relation
  - DELETE existing tuples from a relation
  - UPDATE attribute values of existing tuples



### Operations to Modify Relations

- Three basic operations:
  - INSERT
  - DELETE
  - UPDATE
- Integrity constraints should not be violated by the update operations.
- Several update operations may have to be grouped together into a transaction.
- Updates may propagate to cause other updates automatically. This may be necessary to maintain

Addison-Wesley integrity constraints.



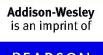
### **Update Operations (cont.)**

- In case of integrity violation, several actions can be taken:
  - Cancel the operation that causes the violation (RESTRICT or REJECT option)
  - Perform the operation but inform the user of the violation
  - Trigger additional updates so the violation is corrected (CASCADE option, SET NULL option)
- Execute a user-specified error-correction
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### **INSERT** operation

- INSERT one or more new tuples into a relation
- INSERT may violate any of the constraints:
  - Domain constraint:
    - if one of the attribute values provided for a new tuple is not of the specified attribute domain
  - Key constraint:
    - if the value of a key attribute in a new tuple already exists in another tuple in the relation
  - Referential integrity:
    - if a foreign key value in a new tuple references a primary key value that does not exist in the referenced relation
  - Entity integrity:
    - if the primary key value is null in a new tuple



### **DELETE** operation

- DELETE one or more existing tuples from a relation
- DELETE may violate only referential integrity:
  - If the primary key value of the tuple being deleted is referenced from other tuples in the database
    - Can be remedied by several actions: RESTRICT, CASCADE, SET NULL (see Chapter 4 for more details)
      - RESTRICT option: reject the deletion
      - CASCADE option: propagate the deletion by automatically deleting the referencing tuples
      - SET NULL option: set the foreign keys of the referencing tuples to NULL (the foreign keys cannot have NOT NULL constraint)
  - One of the above options must be specified during database design for each referential integrity (foreign key) constraint



### **UPDATE** operation

- UPDATE modifies the values of attributes in one or more existing tuples in a relation
- UPDATE may violate domain constraint and NOT NULL constraint on an attribute being modified
- Other constraints may also be violated:
  - Updating the primary key (PK):
    - Similar to a DELETE followed by an INSERT
    - Need to specify similar options to DELETE
    - The CASCADE option propagates the new value of PK to the foreign keys of the referencing tuples automatically
  - Updating a foreign key (FK) may violate referential integrity
  - Updating an ordinary attribute (neither PK nor FK):
    - Can only violate domain or NOT NULL constraints



### Summary

- Presented Relational Model Concepts
  - Definitions
  - Characteristics of relations
- Discussed Relational Model Constraints and Relational Database Schemas
  - Domain constraints'
  - Key constraints
  - Entity integrity
  - Referential integrity
- Described the Relational Update Operations and Dealing with Constraint Violations



### **In-Class Exercise**

(Taken from Exercise 3.16)

Consider the following relations for a database that keeps track of student enrollment in courses and the books adopted for each course:

STUDENT(SSN, Name, Major, Bdate)

COURSE(Course#, Cname, Dept)

ENROLL(<u>SSN</u>, <u>Course</u>#, <u>Quarter</u>, Grade)

BOOK\_ADOPTION(Course#, Quarter, Book\_ISBN)

TEXT(Book\_ISBN, Book\_Title, Publisher, Author)

Draw a relational schema diagram specifying the foreign keys for this schema.

