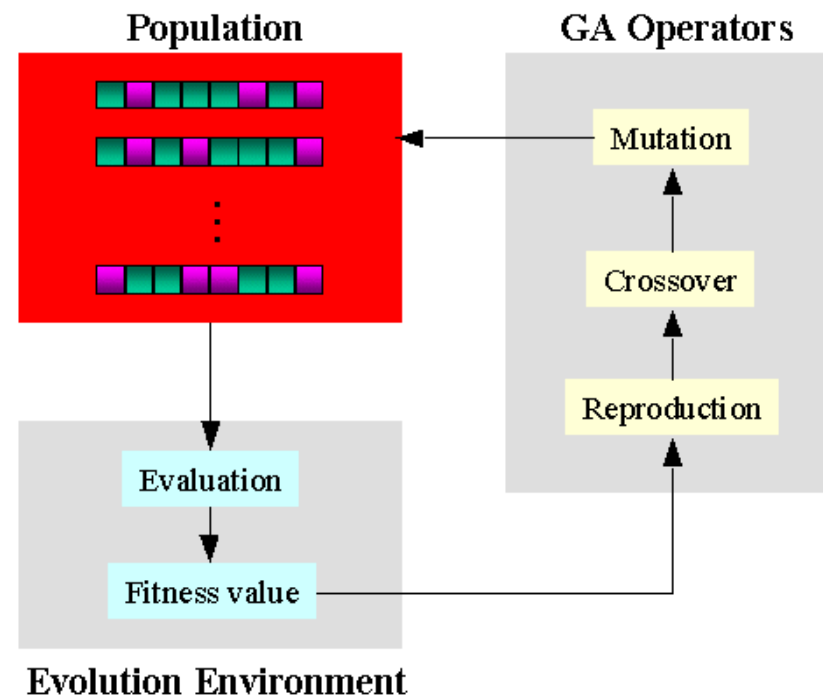


Lecture 12

Artificial Intelligence

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Genetic Algorithm

- Genetic algorithms are defined as a type of computational optimization technique inspired by the principles of natural selection and genetics
- They are used to solve complex problems by mimicking the process of evolution to improve a population of potential solutions iteratively.
- Charles Darwinian Evolution – 1859
- **Theory of natural selection**
 - It proposes that the plants and animals that exist today are the result of millions of years of adaptation to the demands of the environment
- Over time, the entire population of the ecosystem is said to evolve to contain organisms that, on average, are fitter for environment than those of previous generations of the population

Genetic Algorithm

➤ Genetic algorithms



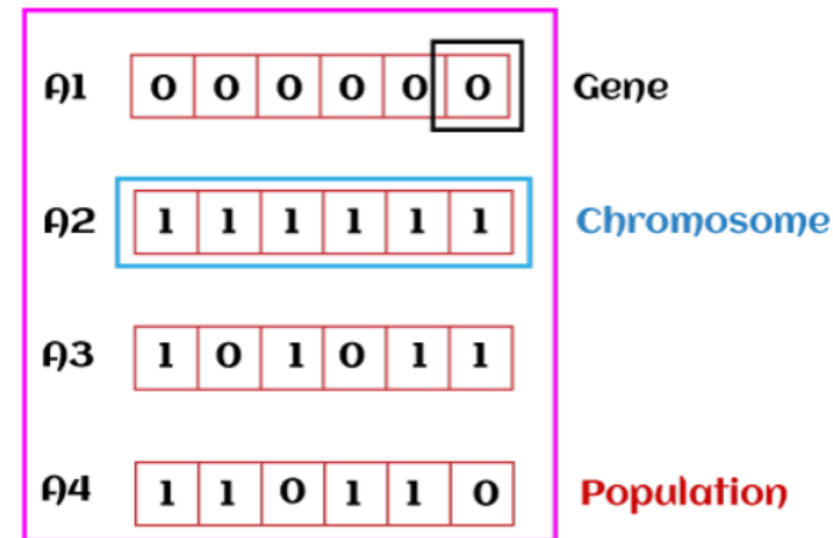
Charles Darwin – Evolution by *Descent with Modification* (1859)

Long-necked giraffes are randomly born and have more offspring due to their competitive advantage

➤ Focus on optimization

Genetic Algorithm

- The concepts of GAs are directly derived from natural evolution.
- In the early 70's John Holland introduced this concept (Holland, 1975).
- GAs emulate ideas from genetics and natural selection and can search potentially large spaces
- Based on: survival of the most fittest individual
- Two key steps: reproduction, survive
- Try to simulate life.
 - Individual = solution
 - Environment = problem

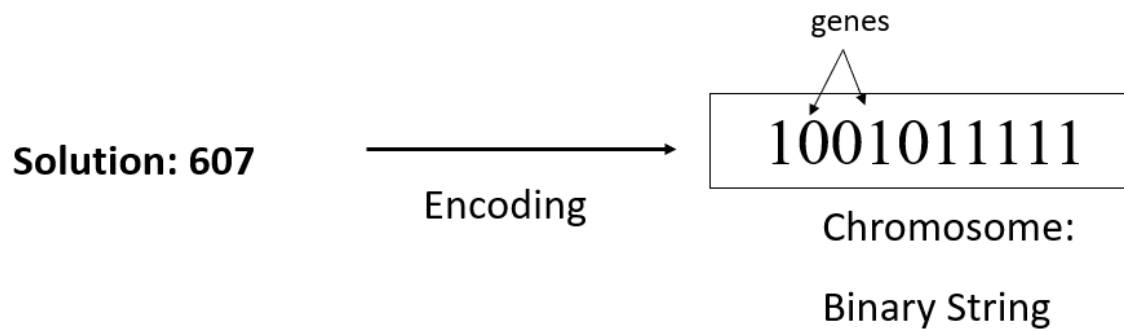


Genetic Algorithm

- Before we can apply Genetic Algorithm to a problem, we need to answer:
 - How can an individual be represented?
 - What is the fitness function?
 - How are individuals selected?
 - How do individuals reproduce?

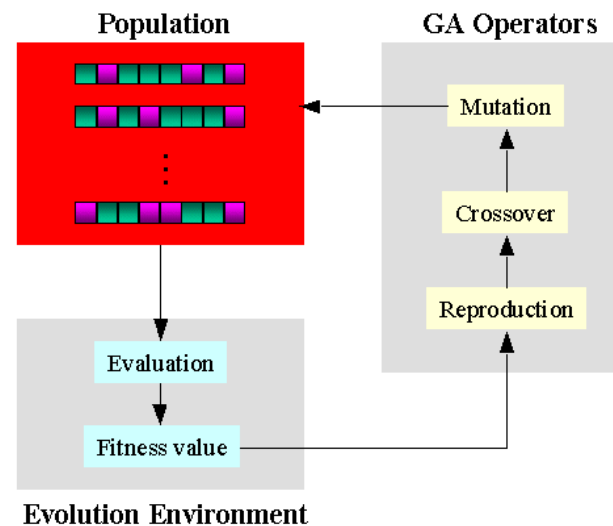
Representation of states (solutions)

- State as sequence of strings
- Each state or individual is represented as a string over a finite alphabet $\{0,1\}$. It is also called chromosome which contains genes.



Reproduction: building new states

- After representing States (solutions)
- Build a population of random solutions
- Let them reproduce using genetic operators
 - At each generation: apply "survival of the fittest"
 - Hopefully better and better solutions evolve over time
 - The best solutions are more likely to survive and more likely to produce even better solutions



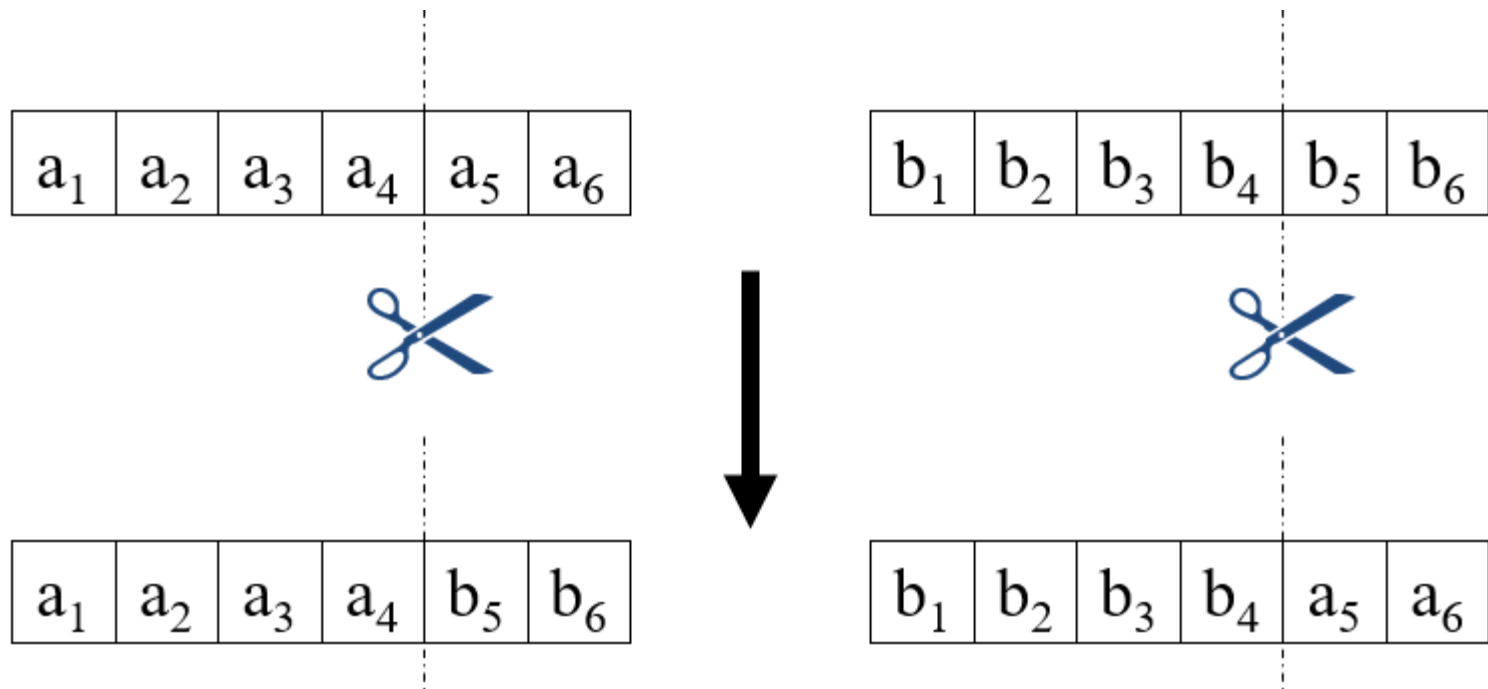
Genetic Operators

- Crossover
- Mutation
- These operators mimic what happens to our genetic material when we reproduce

Genetic Operators

➤ Crossover

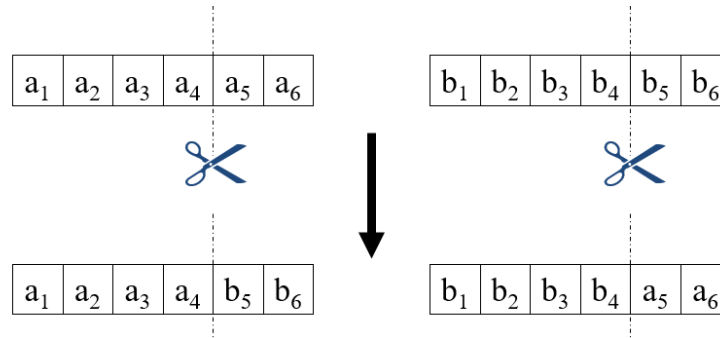
- Cut two solutions at a random point and switch the respective parts
- Typically a value of 0.7 for crossover probability gives good results.



Genetic Operators

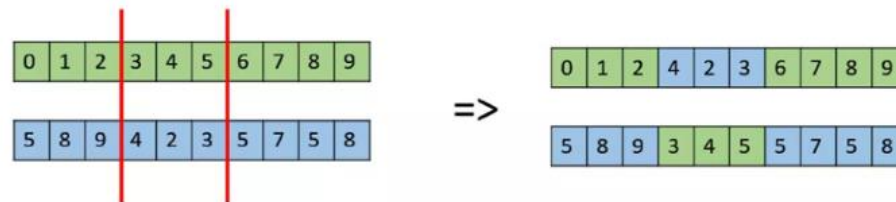
➤ Crossover

➤ Single point



➤ Multi point:

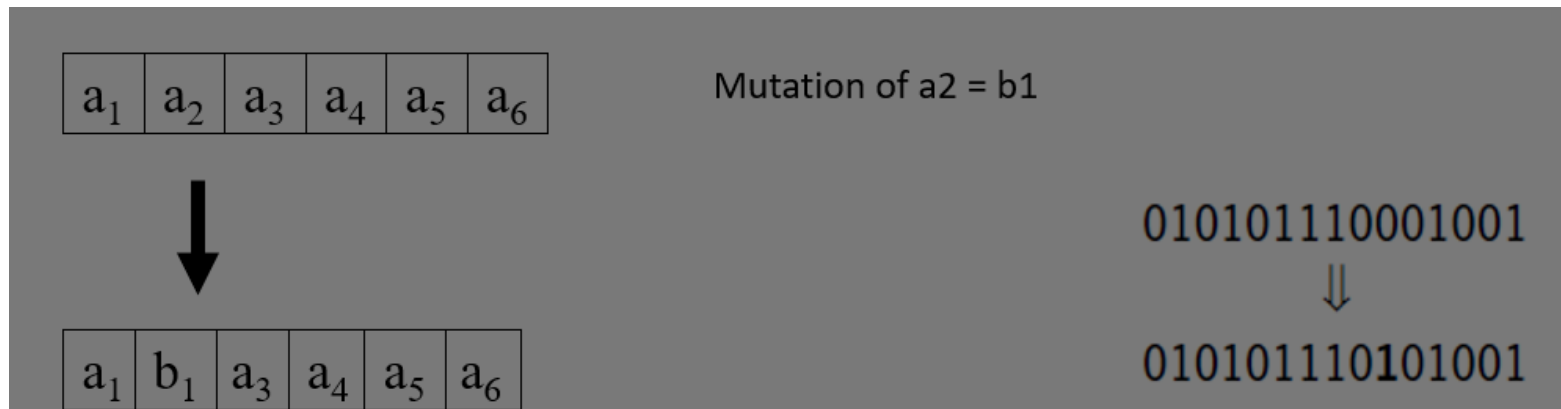
• Multi Point Crossover



➤ Uniform point

Genetic Operators: Mutation operator

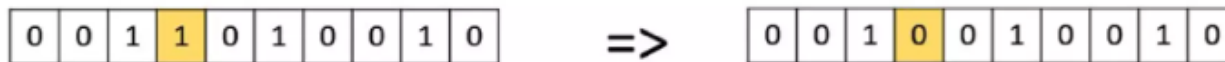
- Randomly change one bit in the solution
- Mutation is a unary operator (i.e., applied to just one argument—a single gene)
- Occasional mutation makes the method much less sensitive to the original population and also allows "new" solutions to emerge



Genetic Operators: Mutation operator

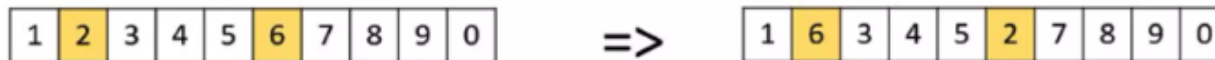
➤ Different types

-Bit Flip Mutation

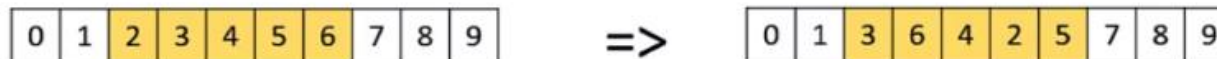


-Random Resetting

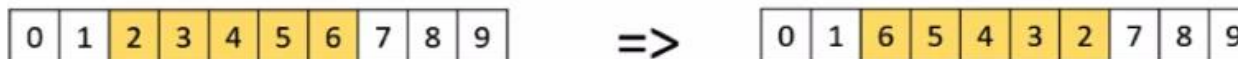
-Swap Mutation



• Scramble Mutation

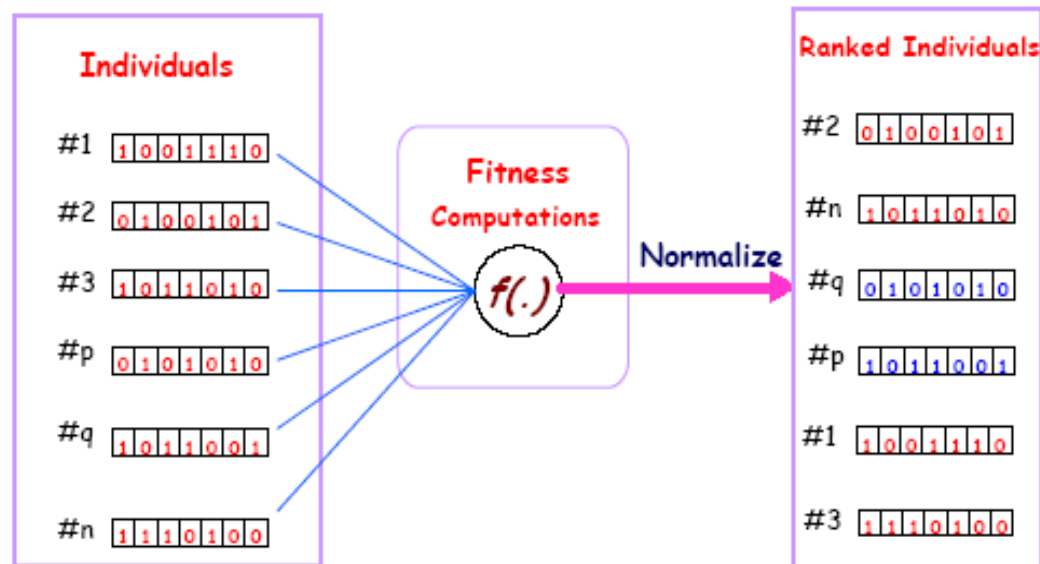


• Inversion Mutation



Evaluation and Selection

- We then see how good the solutions are, using an evaluation function (recall $f(n)$ in informed search)
- Often it is a heuristic, especially if it is computationally expensive to do a complete evaluation
- The final population can then be evaluated more deeply to decide on the best solution



Survival of the Fittest

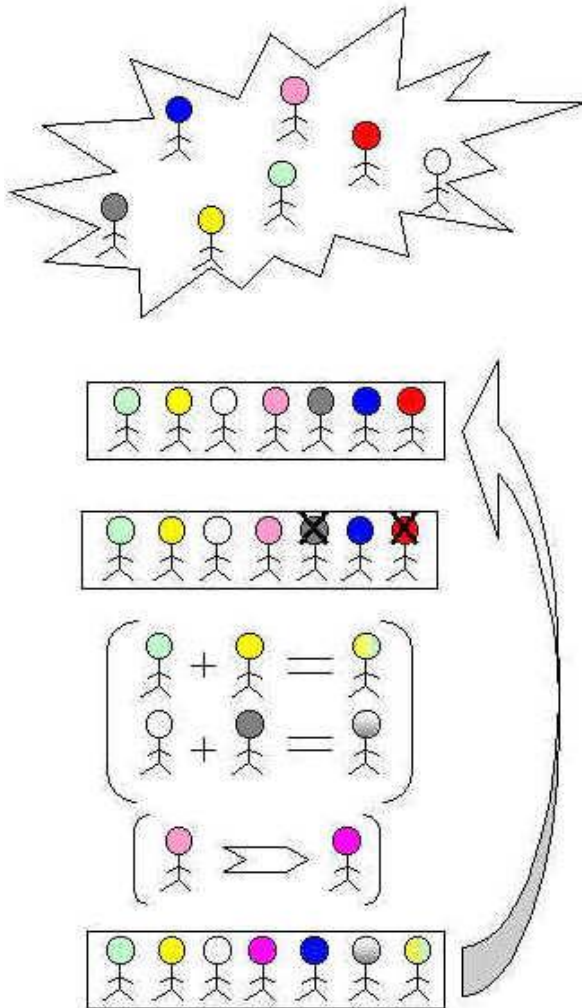
- Select the surviving population
- Likelihood of survival is related in some way to your score on the fitness function
 - The most common technique is roulette wheel selection
 - In roulette wheel selection, individuals are given a probability of being selected that is directly proportionate to their fitness.
- Note we always keep the best solution so far
- Remember: Its local search

Process:

- The most common type of genetic algorithm works like this:
- a population is created with a group of individuals created randomly.
- The individuals in the population are then evaluated.
- The evaluation function is provided by the programmer and gives the individuals a score based on how well they perform at the given task.
- Two individuals are then selected based on their fitness, the higher the fitness, the higher the chance of being selected.
- These individuals then "reproduce" to create one or more offspring, after which the offspring are mutated randomly.
- This continues until a suitable solution has been found or a certain number of generations have passed, depending on the needs of the programmer.

Process:

➤ Genetic Algorithm

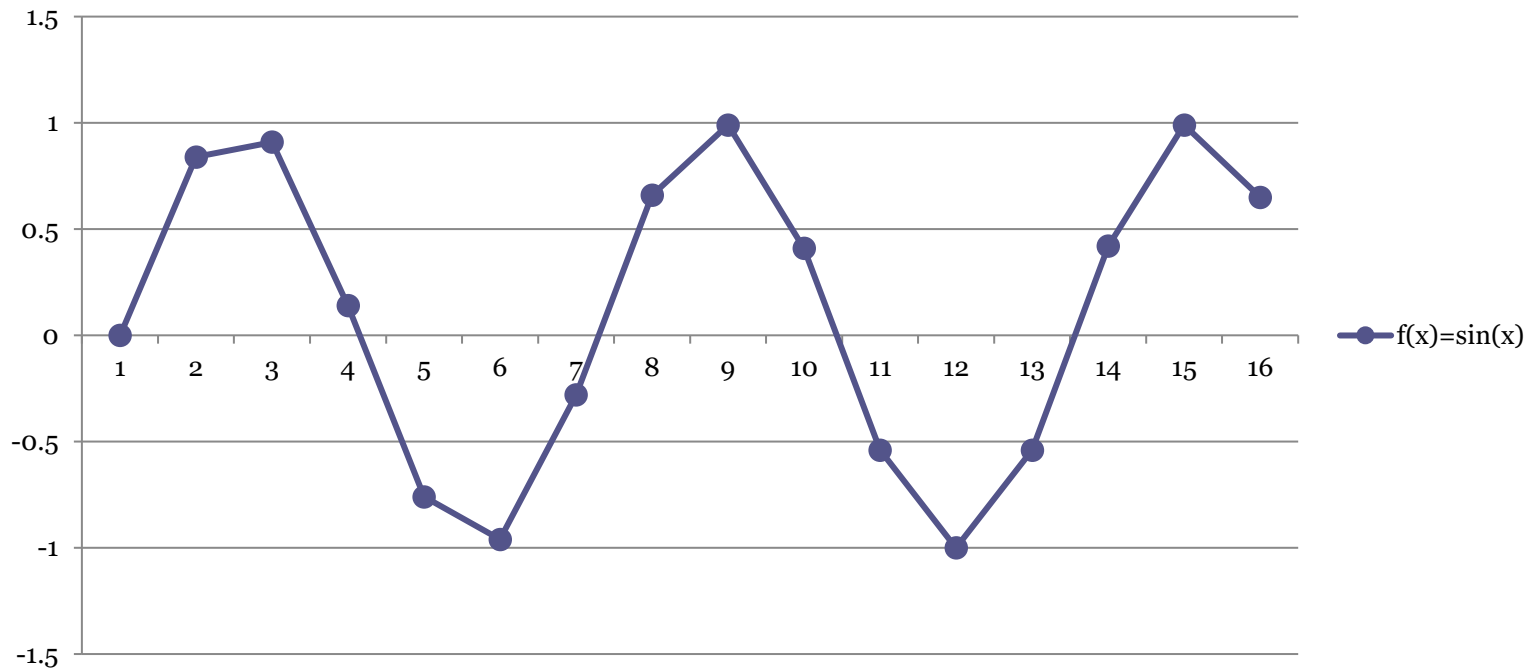


Termination:

- This generational process is repeated until a termination condition has been reached.
- Common terminating conditions are:
 - A solution is found that satisfies minimum criteria
 - Fixed number of generations reached
 - Allocated budget (computation time/money) reached
 - The highest ranking solution's fitness is reaching or has reached a plateau such that successive iterations no longer produce better results
 - Manual inspection
 - Any Combinations of the above

Fitness Function (Optimization):

- Fitness Function for a mathematic function
- Ex. attempt to maximize the function:
 - $f(x) = \sin(x)$ in range $0 \leq x \leq 15$



Fitness Function (Optimization):

- Using population size of 4 chromosomes
- First Generation: Generate a random population:

$$\begin{array}{ll} c1 = 1001 & (9) \\ c2 = 0011 & (3) \end{array} \qquad \begin{array}{ll} c3 = 1010 & (10) \\ c4 = 0101 & (5) \end{array}$$

- To calculate fitness of a chromosome, we calculate $f(x)$ for its decimal value
- Assign fitness as a numeric value from 0 to 100
 - 0 is the least fit
 - 100 is the most fit.

Fitness Function (Optimization):

Fitness of x , $f'(x)$:

$$f'(x) = 50(f(x) + 1)$$

$$f'(x) = 50(\sin(x) + 1)$$

➤ 1 generation

Table 14.1 Generation 1

| Chromosome | Genes | Integer value | $f(x)$ | Fitness $f'(x)$ | Fitness ratio |
|------------|-------|---------------|--------|-----------------|---------------|
| c1 | 1001 | 9 | 0.41 | 70.61 | 46.3% |
| c2 | 0011 | 3 | 0.14 | 57.06 | 37.4% |
| c3 | 1010 | 10 | -0.54 | 22.80 | 14.9% |
| c4 | 0101 | 5 | -0.96 | 2.05 | 1.34% |

Fitness Function (Optimization):

- The range of real numbers from 0 to 100 is divided up between the chromosomes proportionally to each chromosome's fitness.
- In first generation:
- c1 has 46.3% of the range (i.e., from 0 to 46.3)
- c2 37.4% of the range (i.e., from 46.4 to 83.7)
- 1 generation

Table 14.1 Generation 1

| Chromosome | Genes | Integer value | $f(x)$ | Fitness $f'(x)$ | Fitness ratio |
|------------|-------|---------------|--------|-----------------|---------------|
| c1 | 1001 | 9 | 0.41 | 70.61 | 46.3% |
| c2 | 0011 | 3 | 0.14 | 57.06 | 37.4% |
| c3 | 1010 | 10 | -0.54 | 22.80 | 14.9% |
| c4 | 0101 | 5 | -0.96 | 2.05 | 1.34% |

Fitness Function (Optimization):

➤ Fitness ratio of c1:

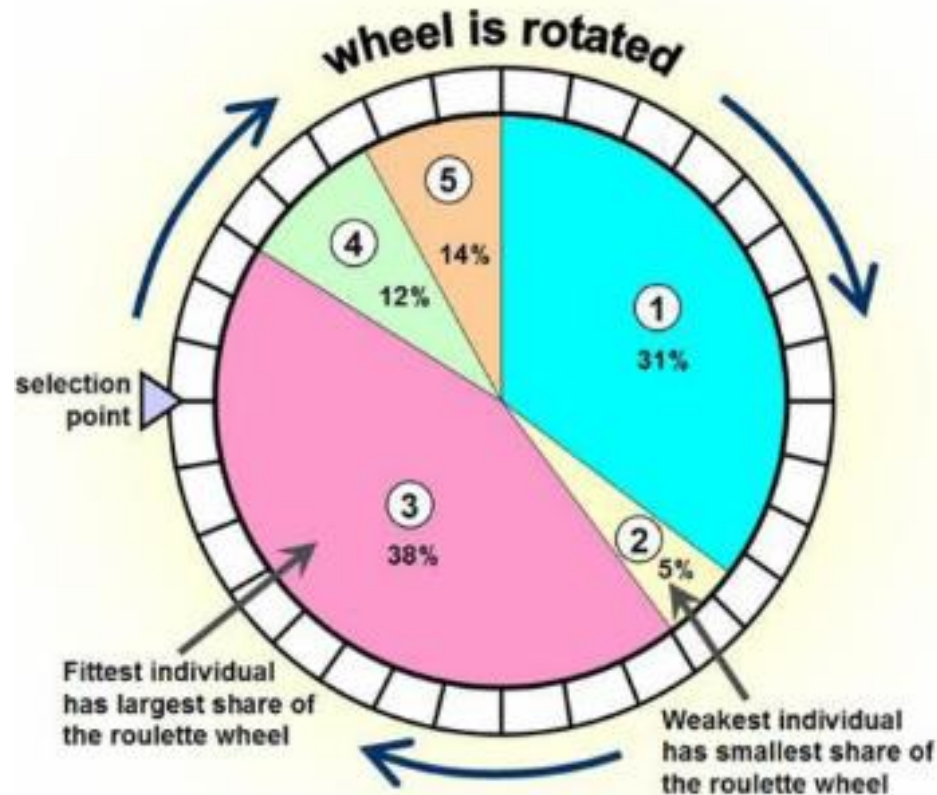
$$\text{➤ } 70.61 / (70.61 + 57.06 + 22.8 + 2.05) \times 100 = 46.29$$

➤ Fitness ratio of c2:

$$\text{➤ } 57.06 / (70.61 + 57.06 + 22.8 + 2.05) \times 100 = 37.4$$

Idea behind Roulette Selection

- Generate 4 random number



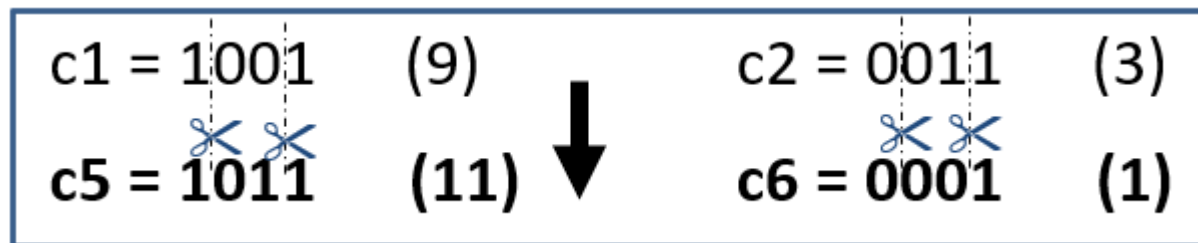
Next Generation

- Need 4 random numbers for next generation
- Assume that:
 - First random number is 56.7 (c2 is chosen)
 - Second random number is 38.2 (c1 is chosen)
 - Third random number is 20 (c1 is chosen)
 - Fourth random number is 85 (c3 is chosen)

Next Generation

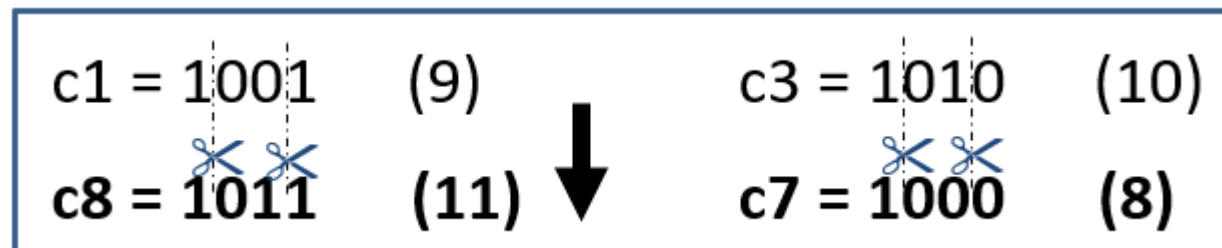
➤ Combine first two to produce two new offspring:

➤ Crossover point



➤ Combine last two to produce two new offspring:

➤ Crossover point



Second generation: c5 to c8

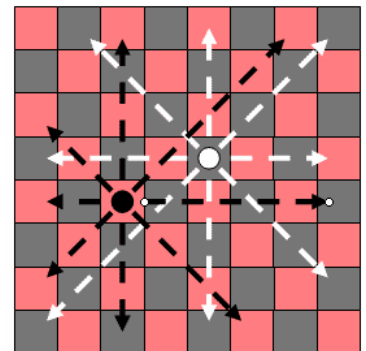
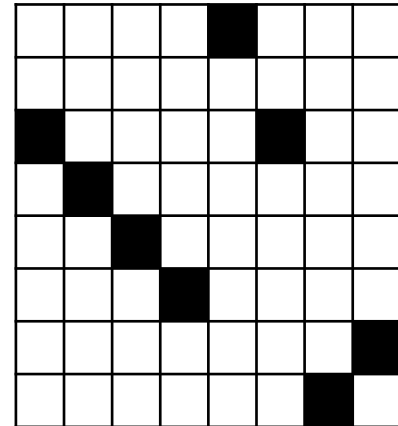
- c4 did not have a chance to reproduce (its genes will be lost)
- Fittest chromosome in the first generation (c1), able to reproduce twice
- Passing on its highly fit genes to all members of the next generation

Table 14.2 Generation 2

| Chromosome | Genes | Integer value | $f(x)$ | Fitness $f'(x)$ | Fitness ratio |
|------------|-------|---------------|--------|-----------------|---------------|
| c5 | 1011 | 11 | -1 | 0 | 0% |
| c6 | 0001 | 1 | 0.84 | 92.07 | 48.1% |
| c7 | 1000 | 8 | 0.99 | 99.47 | 51.9% |
| c8 | 1011 | 11 | -1 | 0 | 0% |

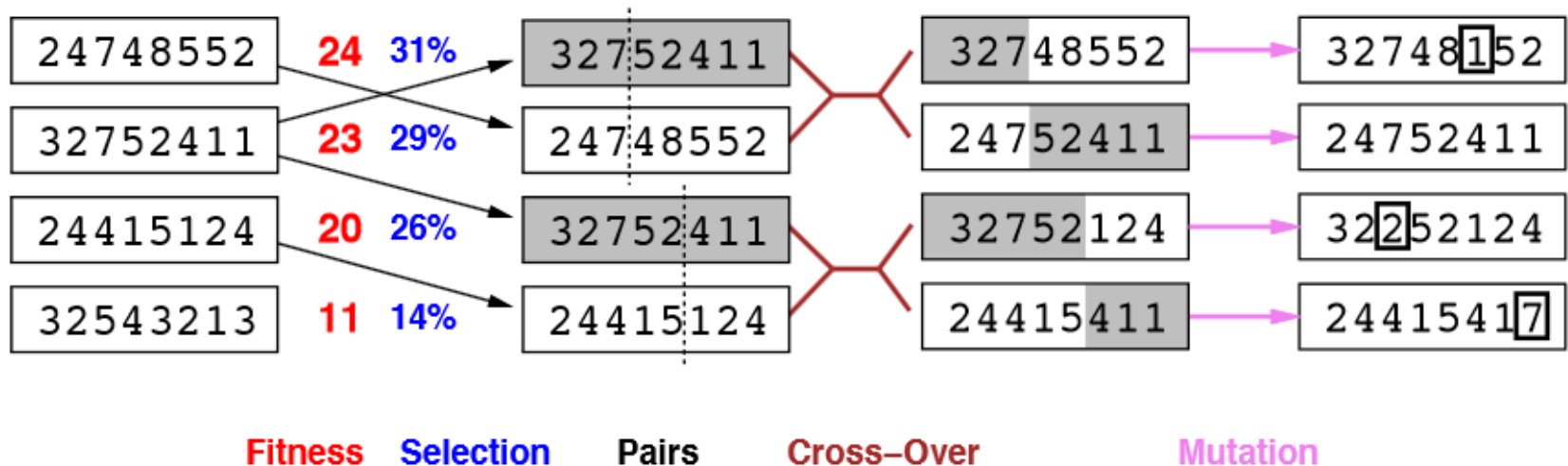
8-Queens Problem

- State = position of 8 queens each in a column
 - 3 4 5 6 1 3 8 7
- Start with k randomly generated states (population)
- Evaluation function (fitness function).
- Higher values for better states.
- Produce the next generation of states
- Random selection
 - Crossover
 - Random mutation



8-Queens Problem

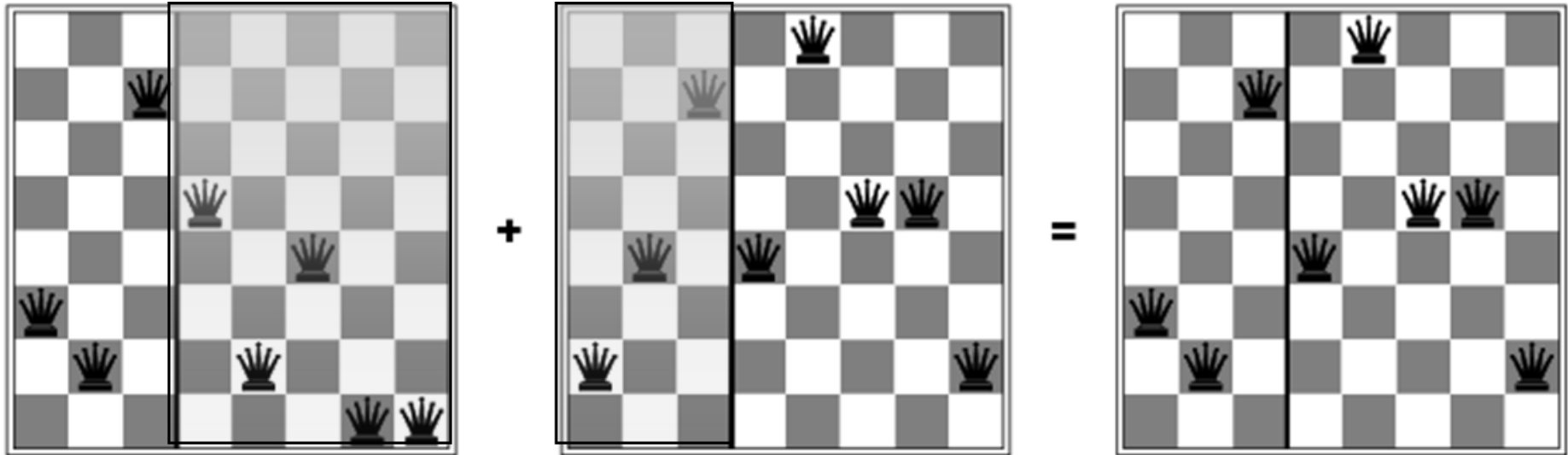
- State = position of 8 queens each in a column



Note: $24 / (24 + 23 + 20 + 11) = 31\%$

8-Queens Problem

➤ Effect of Crossover on 8-Queens



Has the effect of “jumping” to a completely different new part of the search space

Advantages:

- They are Robust
- Provide optimization over large space state.
- Unlike traditional AI, they do not break on slight change in input or presence of noise

Example:

➤ Example

➤ Input:

```
GENES = '''abcdefghijklmnopqrstuvwxyzABCDEFGHIJKLMNOPQRSTUVWXYZ  
QRSTUVWXYZ 1234567890, .-;:_!"#%&/()=?@${[]}'''
```

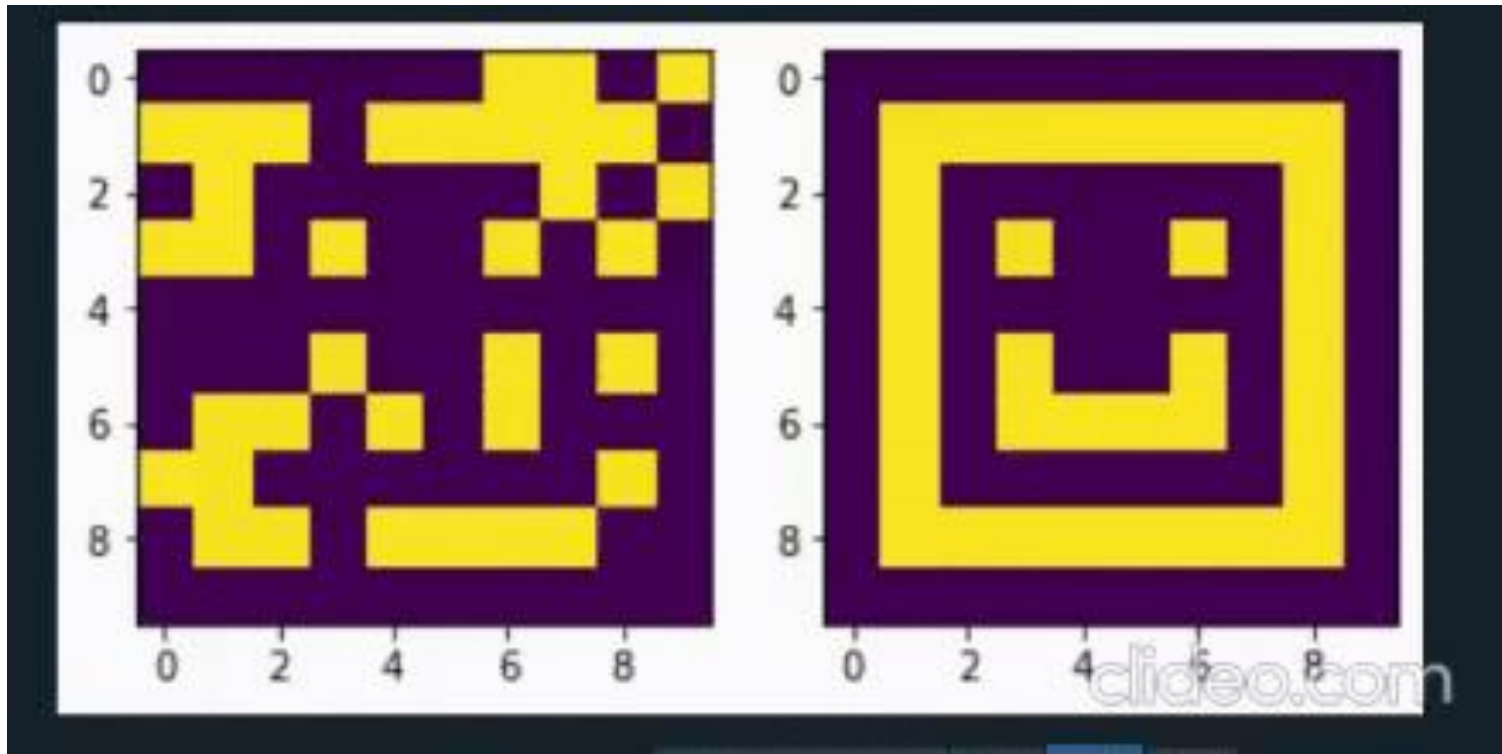
```
# Target string to be generated  
TARGET = "I love GeeksforGeeks"
```

| | | |
|----------------|-------------------------------|-------------|
| Generation: 1 | String: t0{"-?=jH[k8=B4]Oe@} | Fitness: 18 |
| Generation: 2 | String: t0{"-?=jH[k8=B4]Oe@} | Fitness: 18 |
| Generation: 3 | String: .#lRWf9k_Ifslw #0\$k_ | Fitness: 17 |
| Generation: 4 | String: .-1Rq?9mHqk3Wo]3rek_ | Fitness: 16 |
| Generation: 5 | String: .-1Rq?9mHqk3Wo]3rek_ | Fitness: 16 |
| Generation: 6 | String: A#ldW) #lIkslw cVek) | Fitness: 14 |
| Generation: 7 | String: A#ldW) #lIkslw cVek) | Fitness: 14 |
| Generation: 8 | String: (, o x _x%Rs=, 6Peek3 | Fitness: 13 |
| | . | |
| | . | |
| | . | |
| Generation: 29 | String: I lope Geeks#o, Geeks | Fitness: 3 |
| Generation: 30 | String: I loMe GeeksfoBGeeks | Fitness: 2 |
| Generation: 31 | String: I love Geeksfo0Geeks | Fitness: 1 |
| Generation: 32 | String: I love Geeksfo0Geeks | Fitness: 1 |
| Generation: 33 | String: I love Geeksfo0Geeks | Fitness: 1 |
| Generation: 34 | String: I love GeeksforGeeks | Fitness: 0 |

➤ <https://www.geeksforgeeks.org/genetic-algorithms/>

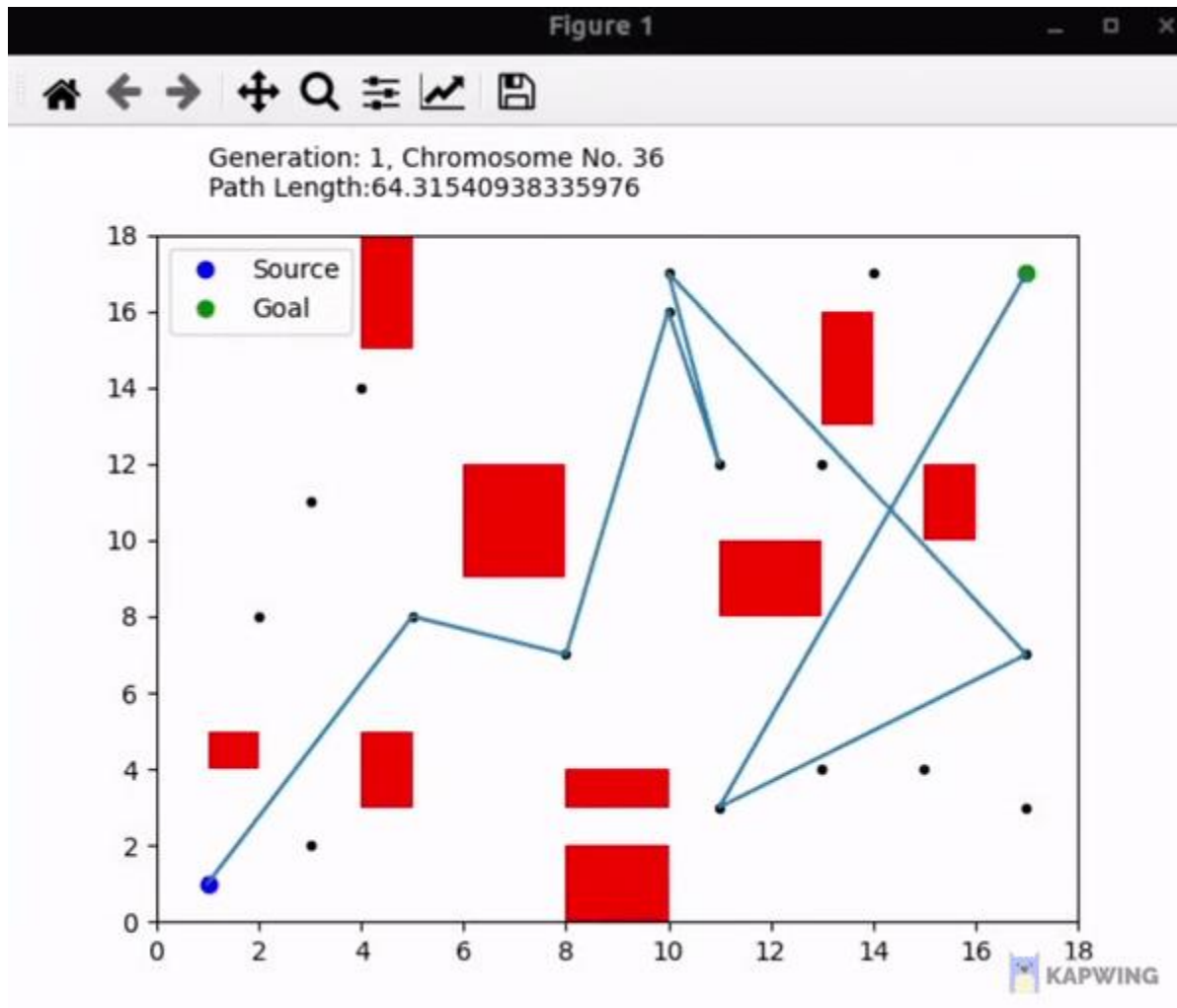
Example:

➤ Example



Example:

➤ Example



Example:

➤ Example

