

Information Security

10 domains of IS

Ceasar Cipher:

Plain text: meet me after toga party

Cipher text: PHHN PH DINHU WRJD SDUWB

→ Replacement w.r.t defined place

a b c d e f

For decryption, move backward.

Using Modulo Math:

$$C = E(3, P)$$

$$= (P+3) \bmod 26$$

$$P = D(k, C)$$

$$= (C-k) \bmod 26$$

Ceasar Cipher (ROT-13) Rotation - 13

A|B|C|D|E|...|M|

↓ ↓ ↓ ↓ ↓ ↑
N|O|P|Q|R|...|Z|

Plain → H E L L O

Cipher → U R Y X B

Problem with Caesar cipher

→ Brute force attack \Rightarrow try all possible combination

→ In case of Caesar cipher they are only 25. So encrypted message will be easily decrypted.

Substitution (Mono Alphabetic):

→ Decide yourself to replace a particular letter with other one

A \rightarrow B $k = +1$

B \rightarrow V $k = +20$

C \rightarrow G $k = +4$

D \rightarrow Q $k = +13$

Don't replace two letters with same

With keyword:

keyword = KEYWORD

P.L = A B C D E F G H I J
K E Y W O R D A B C

K L M N O P Q R S T
F G H I J L M N P Q
U V W X Y Z
S T U V X Z

P.t = a L K i n d i

C.t = K G F B I W B

Homophone Cipher :

A	B	C	D	E	F	G	H	I	J
D	X	S	F	Z	E	H	C	V	I
9				⁷ ₂				³	
K	L	M	N	O	P	Q	R	S	T
I	P	G	A	Q	L	K	J	R	U
			5	0				4	6
U	V	W	X	Y	Z				
O	W	M	Y	B	N				

M9PP

cipher = F7E25F UC2 1DR6 ↑ ØE SD4UP1

WALL

Plain = DEFEND THE EAST ↑ OF CASTLE

Playfair cipher:

→ Digraph Substitution cipher

keyword = MONARCHY

→ Matrix 5x5

→ I/J replacement

→ Repeating letter → (x)

M	O	N	A	R
C	H	X	B	D
E	F	G	I	J
K	L	P	Q	S

M	O	N	A	R
C	H	-Y	B	D
E	F	G	I/J	K
L	P	Q	S	T
U	V	W	X	Z

Keyword : Monarchy

Hello

Plaintext : Instruments

Helxlo

GATLMZCLRQXA

HS

→ With same row or column

BP

replace with next letter

EP → IM

→ with diagonals/non-dia → see in
corresponding in rows.

30-01-24

Hill Cipher :

msg : act → column vector

key : gybngkurf

(3)

Encryption :

$$C = KP \bmod 26$$

$$= \begin{bmatrix} 6 & 24 & 1 \\ 13 & 16 & 10 \\ 20 & 17 & 15 \end{bmatrix} \begin{bmatrix} 0 \\ 2 \\ 19 \end{bmatrix} \bmod 26$$

$$\begin{bmatrix} 67 \\ 222 \\ 319 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 15 \\ 14 \\ 7 \end{bmatrix}$$

$$C \cdot T = POH$$

Decryption:

$$P = K^{-1} C \text{ mod } 26$$

$$\begin{bmatrix} 6 & 24 & 1 \\ 23 & 16 & 10 \\ 20 & 17 & 15 \end{bmatrix}^{-1} = \begin{bmatrix} 8 & 5 & 10 \\ 21 & 8 & 21 \\ 21 & 12 & 8 \end{bmatrix} \begin{bmatrix} 15 \\ 14 \\ 7 \end{bmatrix} = \begin{bmatrix} 260 \\ 574 \\ 539 \end{bmatrix} \text{ mod } 26$$

$$\begin{bmatrix} 0 \\ 2 \\ 19 \end{bmatrix} \Rightarrow P \cdot T = ACT$$

(Example)

✓ Plain text P.T = Short Examples

Key = Hill. n=2

Cipher text = APADJTFWTLFJ *

$$C = KP \text{ mod } 26$$

$$C_1 = \begin{bmatrix} 7 & 8 \\ 11 & 11 \end{bmatrix} \begin{bmatrix} 18 \\ 7 \end{bmatrix} \text{ mod } 26 \quad (2)$$

$$= \begin{bmatrix} 126 + 56 \\ 198 + 77 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 182 \\ 275 \end{bmatrix} \text{ mod } 26$$

$$= \begin{bmatrix} 0 \\ 15 \end{bmatrix} \xrightarrow{\text{mod 26}} \boxed{AP}$$

$$C_2 = KP \text{ mod } 26 \quad C_2 = 0 \vee$$

$$= \begin{bmatrix} 7 & 8 \\ 11 & 11 \end{bmatrix} \begin{bmatrix} 14 \\ 17 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 234 \\ 341 \end{bmatrix} \text{ mod } 26 \Rightarrow \begin{bmatrix} 0 \\ 3 \end{bmatrix}$$

AD

- TE

$$C_3 = KP \bmod 26$$

$$= \begin{bmatrix} 7 & 8 \\ 11 & 11 \end{bmatrix} \begin{bmatrix} 19 \\ 4 \end{bmatrix} \bmod 26 \Rightarrow \begin{bmatrix} 165 \\ 253 \end{bmatrix} \bmod 26 = \begin{bmatrix} 9 \\ 19 \end{bmatrix}$$

$$\boxed{C \cdot T = JT}$$

$$C_4 = KP \bmod 26 \quad XA$$

$$= \begin{bmatrix} 7 & 8 \\ 11 & 11 \end{bmatrix} \begin{bmatrix} 23 \\ 0 \end{bmatrix} \bmod 26 \Rightarrow \begin{bmatrix} 161 \\ 253 \end{bmatrix} \bmod 26 = \begin{bmatrix} 5 \\ 19 \end{bmatrix}$$

$$\boxed{C \cdot T = FT}$$

$$C_5 = KP \bmod 26 \quad MP$$

$$= \begin{bmatrix} 7 & 8 \\ 11 & 11 \end{bmatrix} \begin{bmatrix} 12 \\ 15 \end{bmatrix} \bmod 26 = \begin{bmatrix} 204 \\ 297 \end{bmatrix} \bmod 26 = \begin{bmatrix} 22 \\ 11 \end{bmatrix}$$

$$\boxed{C \cdot T = WL}$$

$$C_6 = KP \bmod 26 \quad LE$$

$$= \begin{bmatrix} 7 & 8 \\ 11 & 11 \end{bmatrix} \begin{bmatrix} 11 \\ 4 \end{bmatrix} \bmod 26 = \begin{bmatrix} 109 \\ 165 \end{bmatrix} \bmod 26 = \begin{bmatrix} 5 \\ 9 \end{bmatrix}$$

$$\boxed{C \cdot T = FJ}$$

P.t - Short Example

C · t = APADJ TFTWL FJ

Decryption : Assignment

Vigenere Cipher:

* Vigenere Table / Square

plain ↑	A	B	C	D	Z → key
A	A	B	C	D	Z
B	B	C	D	E	A
C	C	D	E	F	B
D	D	E	F	G	C
:	:	:	:	:	:
Z	Z	A	B	C	Y

Encryption :

P.T = geekforgeeks

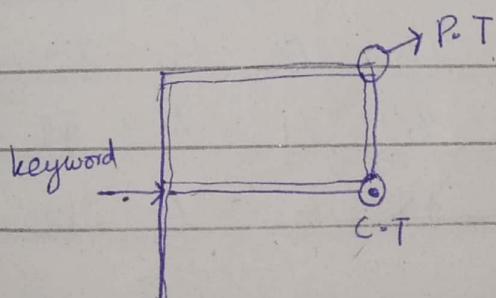
Key = xyz

[x]yzxyzxyzxyzxyz
GeekForGeeks

Decryption

keyword — ,

C.T — →



Keyword = UET

C.T = orbpikmms

$$= \begin{bmatrix} U & E & T & U & E & T & U & E & T & U \\ O & R & b & p & i & k & m & m & m & S \end{bmatrix}$$

= UNIVERSITY

Vernam Cipher

Encryption

P.T →	r	a	m	s	w	a	m	i
P.NO →	17	0	12	18	22	0	12	8
key →	r	a	n	g	e	e	l	a
K.NO →	17	0	13	6	4	4	11	0
J = P.NO + K.NO	034	0	25	24	26	4	23	8
If (J > 25)	-26				-26			
mod 26	8	0	(25)	24	0	4	23	8

C.T I A Z Y A E X I

DECRYPTION

C.T - K

18 0 25 24 0 4 23 8

-17 0 13 6 4 4 11 0

-9. 0 12 18 -4 0 12 8

mod 26

17 0 12 18 22 0 12 8

R A M S W A M I

Hill Cipher decryption

$$\text{Key} = \begin{bmatrix} 7 & 8 \\ 11 & 11 \end{bmatrix} \quad \det = (7)(11) - (4)(8) = 77 - 88 = -11$$

$$-11 \text{ mod } 26 \Rightarrow 15$$

$$\text{Adj.} \begin{bmatrix} 7 & 8 \\ 11 & 11 \end{bmatrix} = \begin{bmatrix} 11 & -8 \\ -11 & 7 \end{bmatrix}$$

$$K^{-1} = \frac{1}{15} = 15^{-1} \quad (15)(x) \text{ mod } 26 = 1$$

$$\text{P.T} = K^{-1} C \text{ mod } 26$$

$$= 7 \begin{bmatrix} 11 & 18 \\ 15 & 7 \end{bmatrix} [$$

$$(15)(7) \text{ mod } 26 = 1$$

$$105 \text{ mod } 26 = 1$$

$$1 \text{ mod } 26 = 1$$

VIC Cipher:

→ Straddling Checkerboard

→ Top Row → [0-9]

→ Second Row → Popular letter in any order

ESTONIAR									
0	1	2	3	4	5	6	7	8	9
E	T	X	A	O	N	X	R	I	S
B	C	D	F	G	H	J	K	L	M
P	Q	/	U	V	W	X	Y	Z	,

Encryption:

P.T → M A R Y Q U E E N O F

29 3 7 67 61 63 0 0 5 4 23

S C O T S

9 21 4 1 9

3 3 7 15 9 11 00 54 23
 AAR
 9 → 21 4 1 9 X

\rightarrow DDHPJLA AFEX JVERT

Step 1 → Number

Step 2 → Break 2 digits into Single digit

Step 3 → Add Key 1542 (result mod 10)

Step 4 → Pairing the result digit if their appears $\frac{2}{2}$

2	9	3	7	6	7	6	1	6	3
1	5	4	2	1	5	4	2	1	5
3	$14 \text{ mod } 10$	7	9	7	12	10	3	7	8
③	④	⑦	⑨	⑦	②	⑩	③	⑦	⑧
0	0	5	4	2	3	9	2	.1	4
4	2	1	5	4	2	1	5	4	2
4	2	6	9	6	5	10	7	5	6
④	②	⑥	⑨	⑥	⑤	⑩	⑦	⑤	⑧
1	9								

1 5

2 24

② ④

3	4	7	9	7	20	3	7	8	4	26	9	65	0	7	5	62	4
A	O	R	S	R	B	A	R	I	O	J	S	W	E	R	N	I	O

AORSRBARIOJSWERNIO

Decryption

$$10 - 1 = 9$$

A	O	R	S	R	B
3	4	7	9	20	8
1	5	4	2	1	20
2	-1	3	7		5

mod 10

2	9	3	7
29	3	7	
M	A	R	

A	R	I	O	J	S	W	E	R	N
3	7	8	26	9	65	0	7	5	
4	2	1	5	4	2	1	5	4	2

1 0
62 8.

Decryption

A	O	R	S	R	B	A	R	I	O
3	4	7	9	7	20	3	7	8	4
1	5	4	2	1	5	4	2	1	5
2	-1	11	11	8	7	4	5	8	4
J	S	W	E	R	N	I	O		
26	9	65	0	7	5	62	4		
21	5	42	1	5	4	21	5		

Transportation (Transposition) Permutation:

1- Scytale Cipher:
P.T \rightarrow send help!



C.T \Rightarrow SNUFLDEPA

2-Rail Fence Cipher:

Depth \rightarrow 2

P.T \rightarrow Meet me after class

M	E	M	A	T	R	L	S
E	T	E	F	E	C	A	S

C.T = MEMATRLSETEFECAS

3-Route Cipher:

key = 6

P.T \Rightarrow I am going to School

I	A	M	G	O	I
N	G	T	O	S	C
H	O	O	L	X	X

\rightarrow Clockwise

\rightarrow Anticlockwise

C.T \Rightarrow ICXXLOOHNIAMGOSOTG

Rail cipher Decryption

I	A	M	G	O	I	
N	G	T	O	S	C	
H	O	O	L	X	X	

↓ Insert from here

I am GOING TO SCHOOL.

② Rail Fence Decryption

depth = 2

C.T = M E M A T R L S E T J E F E C A S

2 X 16

→ Fill from left to right

M	E		M	A		T	R	L	S
E	T	M	E	F	T	E	R	C	A

Read zig-zag.

MEET ME AFTER CLASS

① Scytale cipher Decryption

Every ^{fifth} ~~second~~ element write.

C.T → S N H L ! E D E P

SEND HELP!

13-02-24

Number Theory

→ Division Algo:

if 'a' is 'b' → integers
 $b \geq 1$

then $a = qb + r$

Modular Form

$$a \equiv r \pmod{b}$$

$$r \equiv a \pmod{b}$$

→ Divisor & GCD

integers a, b, c

$c | a, c | b \rightarrow c$ is common divisor

$\text{GCD}(a, b) \rightarrow$ largest common divisor

→ coprime / relatively prime if their GCD is 1.

→ Congruences :-

If 'a' and 'b' are integers

the 'a' is said to be congruent

to " $b \pmod{m}$ " if $m | a-b$

$m \rightarrow$ modulus of congruence

Ex:

$$24 \equiv 9 \pmod{5} \quad \text{as } 5 | 24 - 9$$

$$-8 \equiv 5 \pmod{13} \quad \text{as } 13 | -8 - 5$$

Properties

1- $a \equiv b \pmod{n}$ if $n | a - b$

2- $a \equiv b \pmod{n}$ implies $b \equiv a \pmod{n}$

3- if $a \equiv b \pmod{n}$ and $b \equiv c \pmod{n}$ then

$$a \equiv c \pmod{n}$$

1- $(a \pm b) \pmod{n} = [(a \pmod{n}) \pm (b \pmod{n})] \pmod{n}$

$$(6 + 8) \pmod{12}$$

$$11^7 \pmod{13}$$

$$= 11^{4+2+1} \pmod{13}$$

$$= 11^4 \cdot 11^2 \cdot 11 \pmod{13}$$

$$= [(11^4 \pmod{13}) \cdot (11^2 \pmod{13}) \cdot (11 \pmod{13})] \pmod{13}$$

$$= [(11^2)^2 \pmod{13} \cdot (11^2 \pmod{13}) \cdot (11 \pmod{13})] \pmod{13}$$

$$= (4^2 \pmod{13} \cdot 4 \pmod{13} \cdot 11) \pmod{13}$$

$$= (3 \cdot 4 \cdot 11) \pmod{13}$$

$$= 132 \pmod{13} \Rightarrow 2$$

Multiplicative inverse

Let $a \in \mathbb{Z}_n$ then $\bar{a} \bmod n$ is

an integer $n \in \mathbb{N}$

$a \cdot x \bmod n = 1 \bmod n$ if $\gcd(a, n) = 1$

$a \in \mathbb{Z}_n$ is invertible

Calculating Multiplicative Inverse:

Euclidean Algorithm

If 'a' and 'b' are positive integers
with $a > b$ then

$$\text{GCD}(a, b) = \text{GCD}(b, a \bmod b)$$

→ Calculate GCD of 4864 & 3458

$$4864 = 1 \cdot 3458 + 1406$$

$$3458 = 2 \cdot 1406 + 646$$

$$1406 = 2 \cdot 646 + 114$$

$$646 = 5 \cdot 114 + 76$$

$$114 = 1 \cdot 76 + 38$$

$$76 = 2 \cdot 38 + 0$$

$$\text{GCD} = 38$$

✓

Extended Euclidean Algorithm

$$ax + by = d$$

$$4864(x) + 3458(y) = 38$$

$$38 = 114 \cdot 1 - 76 \cdot 1$$

$$38 = 114 \cdot 1 - [646 \cdot 1 - 114 \cdot 5] \cdot 1$$

$$= 114 \cdot 1 - 646 \cdot 1 + 114 \cdot 5$$

$$= 114 \cdot 6 - 646 \cdot 1$$

$$= [1406 - 646 \cdot 2] \cdot 6 - 646 \cdot 1$$

$$= 1406 \cdot 6 - 646 \cdot 12 - 646 \cdot 1$$

$$= 1406 \cdot 6 - 646 \cdot 13$$

$$= 1406 \cdot 6 - [3458 - 1406 \cdot 2] \cdot 13$$

$$= 1406 \cdot 6 - 3458 \cdot 13 + 1406 \cdot 26$$

$$= 1406 \cdot 32 - 3458 \cdot 13$$

$$= (4864 - 3458) \cdot 32 - 3458 \cdot 13$$

$$= 4864 \cdot 32 - 3458 \cdot 32 - 3458 \cdot 13$$

$$= 4864 \cdot 32 - 3458 \cdot 45$$

$$x = 32 \quad y = -45$$

GCD(1025, 35)

$$1025 = 35 \cdot 29 + 10$$

$$35 = 10 \cdot 3 + 5$$

$$10 = 5 \cdot 2 + 0$$

$$5 = GCD$$

$$45x + 130y = 5$$

C

$$GCD =$$

$$130 = 45 \cdot 2 + 40$$

$$\rightarrow 45 = 40 \cdot 1 + 5$$

$$40 = 5 \cdot 8 + 0$$

$$GCD = 5$$

$$5 = 40 - 5 \cdot 8$$

$$5 = 45 - 40 \cdot 1$$

$$5 = 45 - (130 - 45 \cdot 2) \cdot 1$$

$$5 = 45 - 130 \cdot 1 + 45 \cdot 2$$

$$5 = 45 \cdot 3 + 130 \cdot (-1)$$

$$x = 3$$

$$y = -1$$

$$513(x) + 144(y) = 9$$

G.C.D

$$513 = 144 \cdot 3 + 81$$

$$144 = 81 \cdot 1 + 63$$

$$81 = 63 \cdot 1 + 18$$

$$63 = 18 \cdot 3 + 9$$

$$18 = 9 \cdot 2 + 0$$

$$\text{G.C.D} = 9$$

Extended Euclidean

$$9 = 63 - 18 \cdot 3$$

$$9 = 63 - (81 - 63) \cdot 3$$

$$9 = 63 - 81 \cdot 3 + 63 \cdot 3$$

$$9 = 63 \cdot 4 - 81 \cdot 3$$

$$9 = (144 - 81 \cdot 1) \cdot 4 - 81 \cdot 3$$

$$9 = 144 \cdot 4 - 81 \cdot 4 - 81 \cdot 3$$

$$9 = 144 \cdot 4 - 81 \cdot 7$$

$$9 = 144 \cdot 4 - (513 - 144 \cdot 3) \cdot 7$$

$$9 = 144 \cdot 4 - 513 \cdot 7 + 144 \cdot 21$$

$$9 = -513 \cdot 7 + 144 \cdot 25$$

$$9 = 513 \cdot (-7) + 144 \cdot 25$$

$$x = -7$$

$$y = 25$$

\therefore

Affine Cipher:

- Mono-Alphabetic substitution cipher
- Each letter encrypts to one letter and back again.
- Working in $\text{mod } m \rightarrow$ length of alphabets used
- letters are mapped to integers in the range of $[0 - (m-1)]$.
- key consists of two numbers 'a' and 'b'.
- For 26 alphabets 'a' must be relatively prime to 'm'.

Encryption:

$$c = (ap + b) \text{ mod } m$$

$$b \rightarrow 1 \leq b \leq m$$

$$a \rightarrow 1 \leq a \leq m,$$

$$\gcd(a, m) = 1 \rightarrow \text{to find multiplicative inverse in decryption}$$

Decryption:

$$p = a^{-1} (c - b) \text{ mod } m$$

msg = I am a secret

$$m = 26$$

$$a = 15$$

$$b = 7$$

Encryption

$$C = (ap + b) \bmod m$$

$$I = (15 \cdot 8 + 7) \bmod 26$$

$$= 120 + 7 \bmod 26$$

$$= 127 \bmod 26$$

$$= 23 \Rightarrow X$$

$$A = (15 \cdot 0 + 7) \bmod 26$$

$$= 7 \bmod 26$$

$$= 7 = H$$

$$M = (15 \cdot 12 + 7) \bmod 26$$

$$= 187 \bmod 26$$

$$= 5 \bmod 26$$

$$= 5 \Rightarrow F$$

$$S = (15 \cdot 18 + 7) \bmod 26$$

$$= 277 \bmod 26$$

$$= 17 \bmod 26$$

$$= R$$

$$\begin{aligned} E &= (15 \cdot 4 + 7) \bmod 26 \\ &\equiv 67 \bmod 26 \\ &\equiv 15 \bmod 26 \\ &= 15 \Rightarrow P \end{aligned}$$

$$\begin{aligned} C &= (15 \cdot 2 + 7) \bmod 26 \\ &\equiv 37 \bmod 26 \\ &\equiv 11 \Rightarrow I \end{aligned}$$

$$\begin{aligned} R &\Rightarrow (15 \cdot 17 + 7) \bmod 26 \\ &\equiv (255 + 7) \bmod 26 \\ &\equiv 262 \bmod 26 \\ &\equiv 2 \Rightarrow B \end{aligned}$$

$$\begin{aligned} T &= (15 \cdot 19 + 7) \bmod 26 \\ &\equiv (285 + 7) \bmod 26 \\ &\equiv 292 \bmod 26 \\ &\equiv 6 \Rightarrow G \end{aligned}$$

XHFHRPLCPG

✓

Decryption

$$15^{-1} \bmod 26$$

$$\Rightarrow 15 \cdot x = 1 \bmod 26$$

$$\Rightarrow 26 = 15 \cdot 1 + 11$$

$$15 = 11 + 4$$

$$11 = 4 \cdot 2 + 3$$

$$4 = 3 + 1$$

$$3 = 1 \cdot 3 + 0$$

$$G.C.D = 1$$

$$1 = 4 - 3$$

$$= 4 - (11 - 4 \cdot 2)$$

$$= 4 - 11 \cdot 1 + 4 \cdot 2$$

$$\begin{aligned}
 &= 4 \cdot 3 - 11 \cdot 1 \\
 &= (15 - 11) \cdot 3 - 11 \cdot 1 \\
 &= 15 \cdot 3 - 11 \cdot 3 - 11 \cdot 1 \\
 &= 15 \cdot 3 - 11 \cdot 4 \\
 &= 15 \cdot 3 - (26 - 15) \cdot 4 \\
 &= 15 \cdot 3 - 26 \cdot 4 + 15 \cdot 4 \\
 &= 15 \cdot 7 - 26 \cdot 4 \\
 \rightarrow l_{\text{mod} 26} &= 15 \cdot 7 \bmod 26 - 26 \cdot 4 \bmod 26 \\
 \rightarrow x &= 7 \quad [1 = 15 \cdot 7 \bmod 26 - 0]
 \end{aligned}$$

$$\begin{aligned}
 \rightarrow P &= \vec{a}'(c - b) \bmod m \\
 P_x &= 7(23 - 7) \bmod 26 \\
 E &= 112 \bmod 26 \\
 &= 8 \bmod 26 \\
 &= 8 \Rightarrow I^C
 \end{aligned}$$

$$\begin{aligned}
 P_A &= 7(7 - 7) \bmod 26 \\
 &= 0 \bmod 26 \Rightarrow A
 \end{aligned}$$

$$\begin{aligned}
 P_F &= 7(5 - 7) \bmod 26 \\
 &= -14 \bmod 26 \\
 &\equiv 12 \Rightarrow M
 \end{aligned}$$

$$\begin{aligned} p_R &= 7(17-7) \bmod 26 \\ &= 70 \bmod 26 \\ &= 18 \Rightarrow S \end{aligned}$$

$$\begin{aligned} p_P &= 7(15-7) \bmod 26 \\ &= 56 \bmod 26 \\ &= 4 \Rightarrow E \end{aligned}$$

$$\begin{aligned} p_L &= 7(11-7) \bmod 26 \\ &= 28 \bmod 26 \\ &= 2 \Rightarrow C \end{aligned}$$

$$\begin{aligned} p_C &= 7(2-7) \bmod 26 \\ &= -35 \bmod 26 \\ &= -9 \bmod 26 \\ &= 17 \Rightarrow R \end{aligned}$$

$$\begin{aligned} p_G &= 7(6-7) \bmod 26 \\ &= 7(-1) \bmod 26 \\ &= -7 \bmod 26 \end{aligned}$$

Plain text,
I AM A SECRET

SECRET
SECRET
SECRET

$$13^{-1} \bmod 15$$

$$13^{-1} \bmod 15$$
$$13 \cdot x \bmod 15 = 1 \bmod 15$$

$$15 = 13 + 2$$

$$13 = 2 \cdot 6 + 1$$

$$2 = 1.2 + 0$$

$$G.C.D = 1$$

$$1 = 13 - 2 \cdot 6$$

$$1 = 13 - (15 - 13) \cdot 6$$

$$1 = 13 + 13 \cdot 6 - 15 \cdot 6$$

$$1 = 13.7 - 15.6$$

$$1 \equiv 13 \cdot 7 \pmod{15} - 15 \cdot 6 \pmod{15}$$

$$1 \bmod 15 = 7 \cdot 13 \bmod 15 - 0$$

$$13 \cdot x \bmod 15$$

$$13 \cdot 7 \bmod 15$$

$$x = 7$$

$$13^{-1} \bmod 15 = 7$$

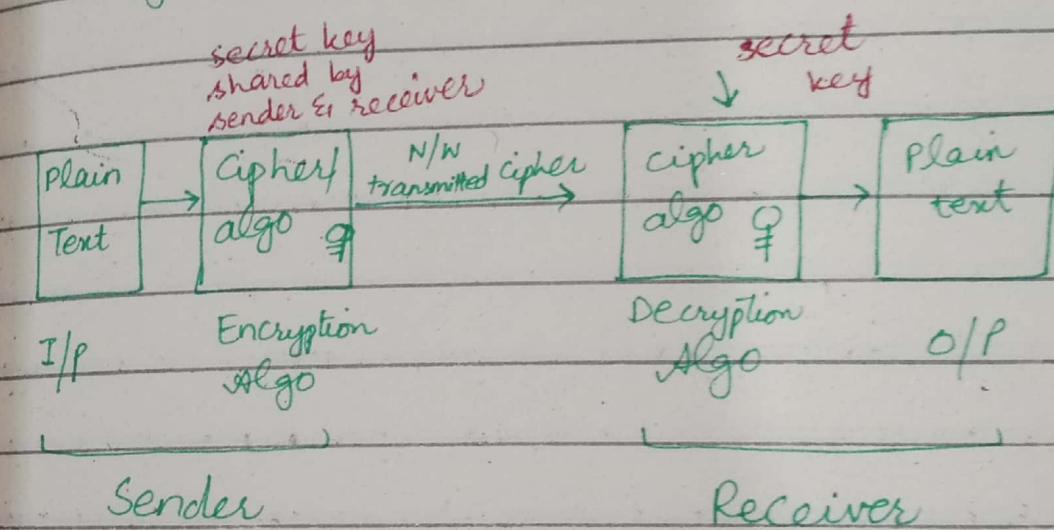
- ## Crypto-Dimensions
- Types of Operation
 - i - Substitution
 - ii - Transposition

 - Number of keys
 - i - Symmetric key
 - ii - Asymmetric key

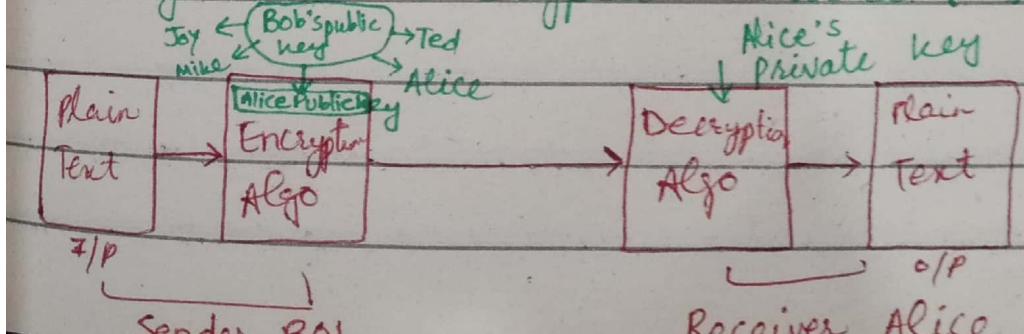
 - Processing ways
 - i - Block Cipher
 - ii - Stream Cipher

Basic Encryption Models:

1 - Symmetric Encryption Model:



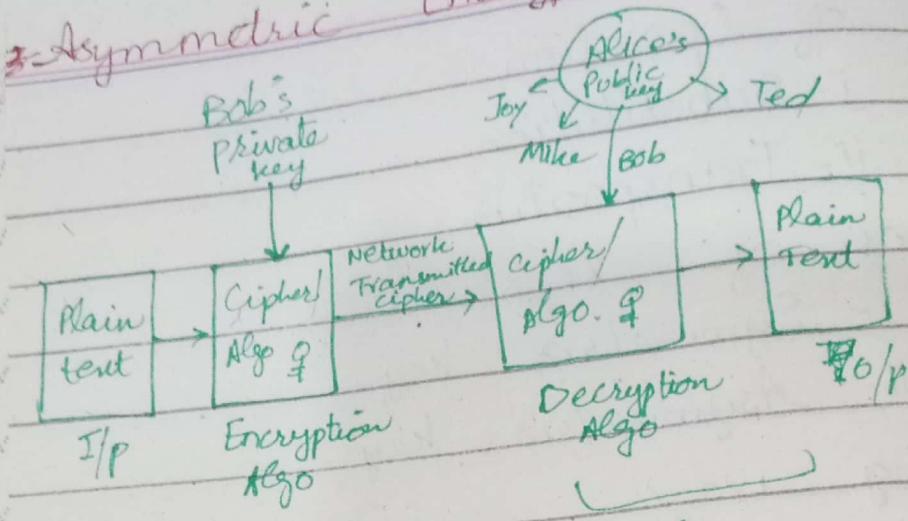
2 - Asymmetric Encryption Model (1):



Asymmetric

Encryption

Model (2)



Bob
sender

Alice

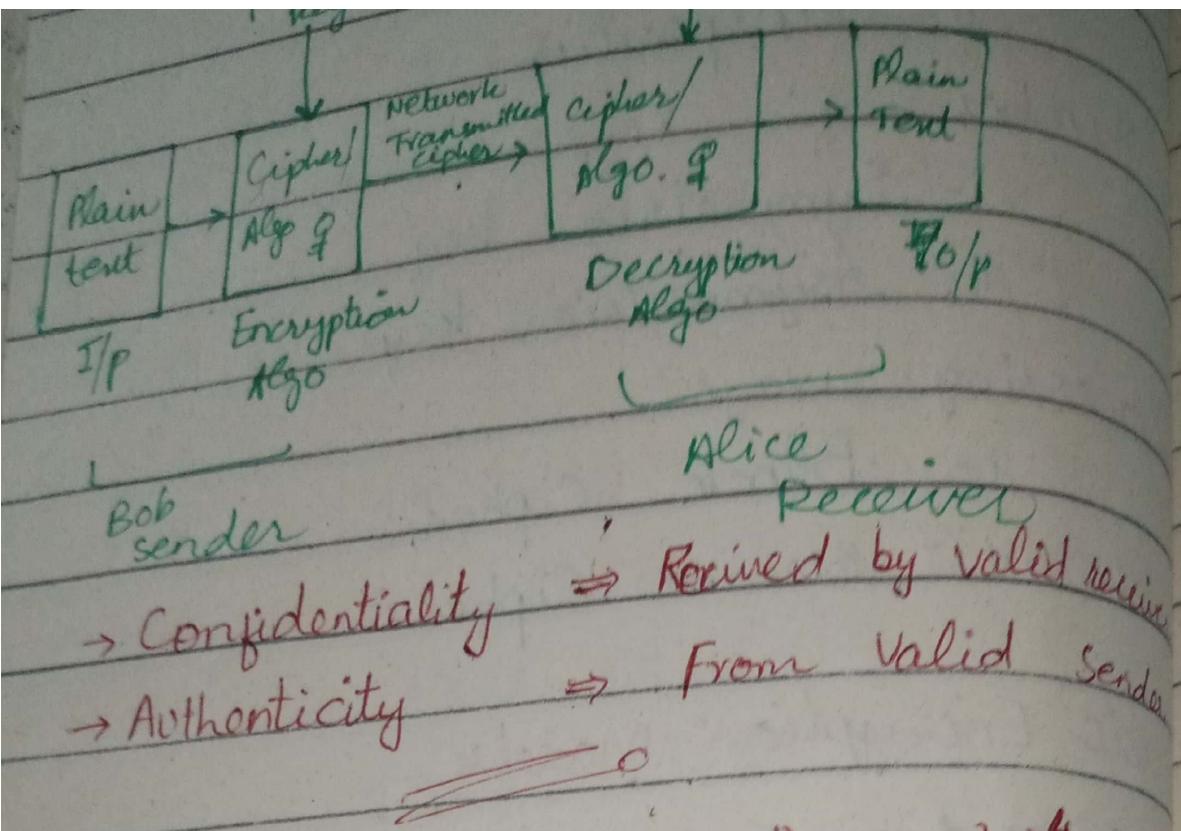
Received

→ Confidentiality

→ Received by valid receiver

→ Authenticity

→ From valid sender



20-02-2024

Secure Symmetric Encryption:

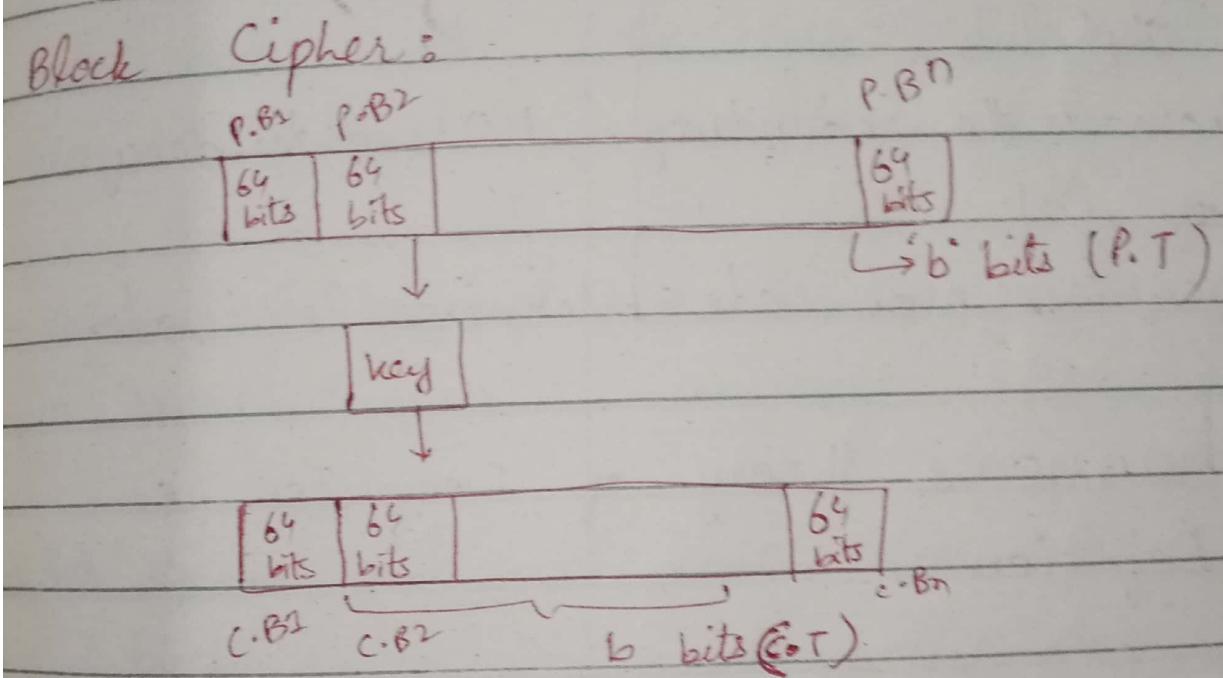
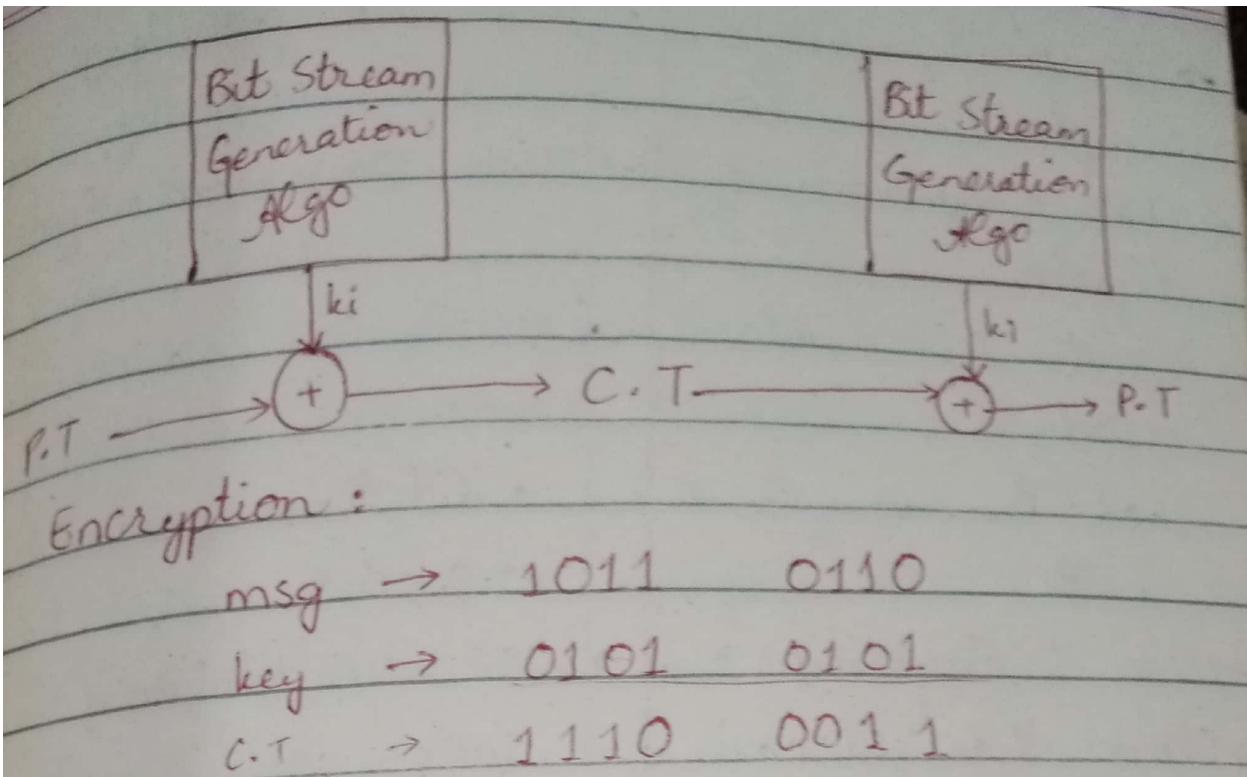
1. Strong Encryption Algo
2. Secret Key

Cryptanalytic Attacks:

1. Cypher/Cipher text only
2. Known plain text
3. Select plain text
4. Choose cipher text
5. Chosen text

unconditional Security (Can not break encrypted text)

Computational Security (



Block Cipher:	Stream Cipher
P.T. is grouped in blocks & then converted to C.T	\rightarrow 1 bit/1 byte of P.T. is converted into C.T
uses 64 or more bits	\rightarrow 8 bits are used

Block Cipher	Stream Cipher
→ Complexity is simple.	→ More Complex
→ Uses Confusion & diffusion	→ Uses Confusion or
→ algorithmic modes used:	→ algorithmic modes used:
<ul style="list-style-type: none"> • ECB • CBC 	<ul style="list-style-type: none"> • CFB • OFB
→ uses transposition	→ uses substitution
→ Slower than stream cipher	→ faster
→ Increases the redundancy of P.T	→ NO redundancy
→ requires more code	→ requires less code

Shannon's theory of Confusion & Diffusion

* Diffusion → Hide the relationship b/w C.T and P.T

* Confusion → Hides the relationship b/w C.T and key

Confusion

Cryptographic technique used to create faint cipher text.

Possible through substitution algorithms

In confusion, if one bit within the secret modified, most or all bits within the cipher text will also be modified

Vagueness is increased in resultant

Both stream cipher and block cipher use confusion.

rel. b/w cipher text & key is masked by confusion.

Diffusion

→ used to create cryptic plain texts.

→ Possible through transposition algorithms

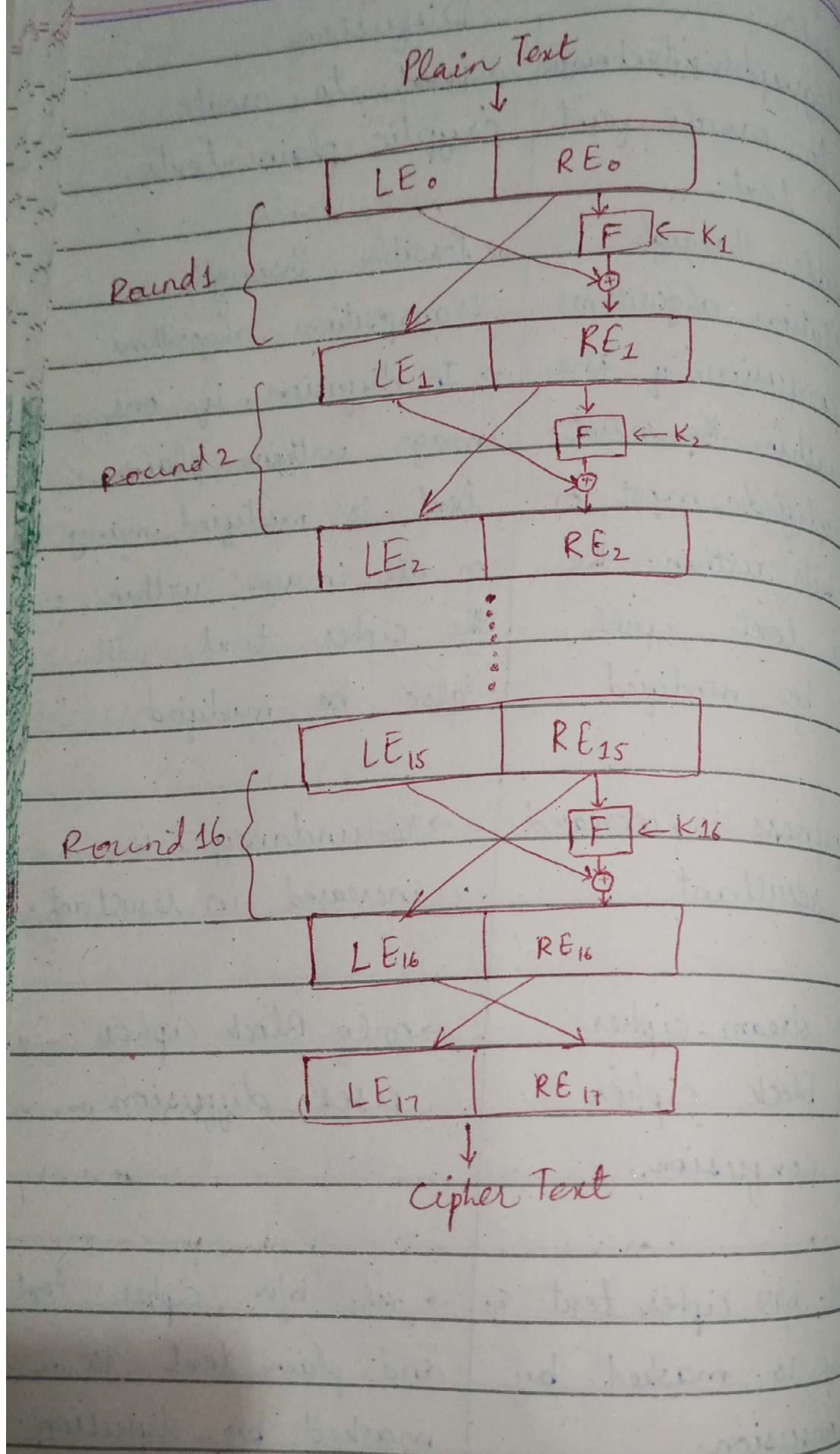
→ In diffusion, if one image within plain text is modified, many or all image within the cipher text will also be modified

→ redundancy is increased in resultant.

→ only Block cipher uses diffusion

→ rel. b/w cipher text and plain text is masked by diffusion.

Feistel Cipher Structure



Block Cipher Design Principles:

- Block Size (64 bits)
- Key Size
- No. of rounds (choose optimal no.) 16
- No. of subkey
- Round Function
- Plain text divided into 2 halves.

Data Encryption Standard (DES)

- Block Cipher
- Symmetric
- 64-bit Plain text block
- 16 rounds → each round is a feistal round.

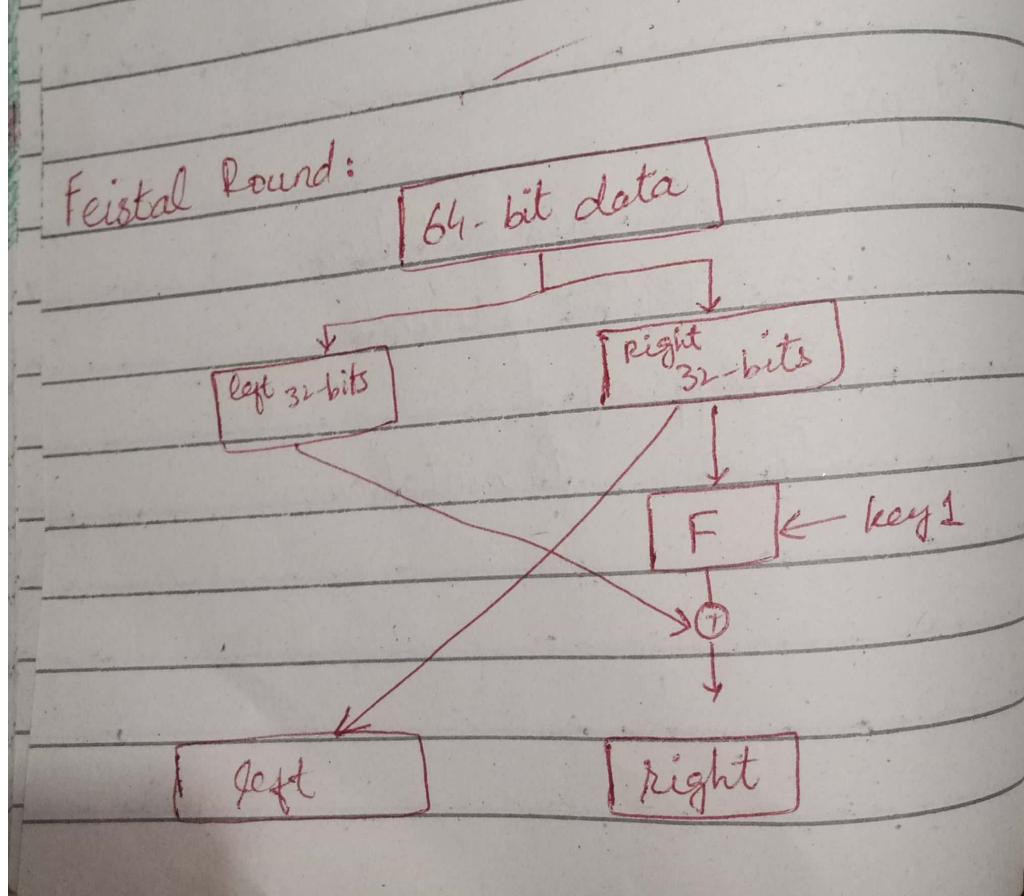
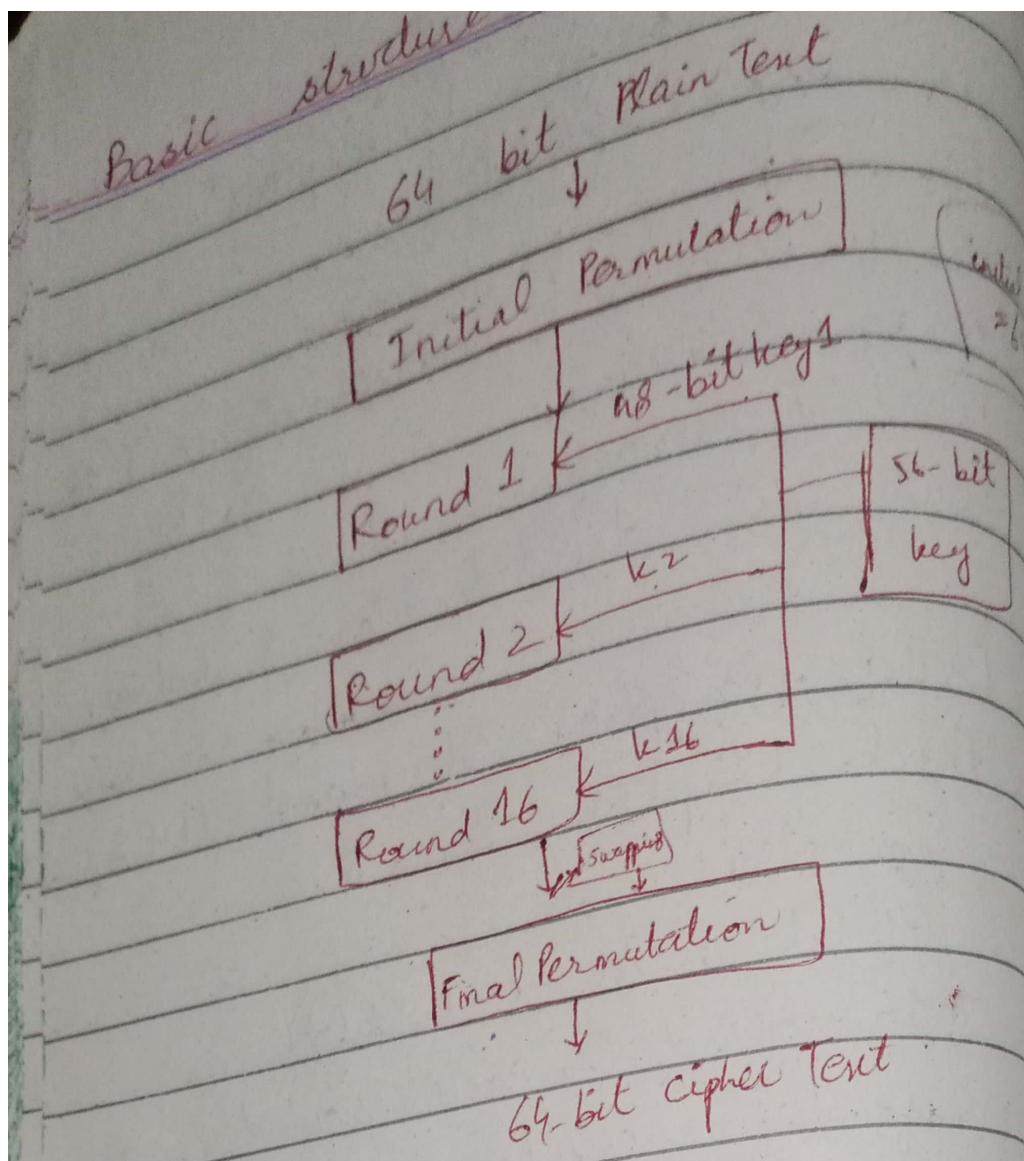
4 Steps:

Initial Permutation

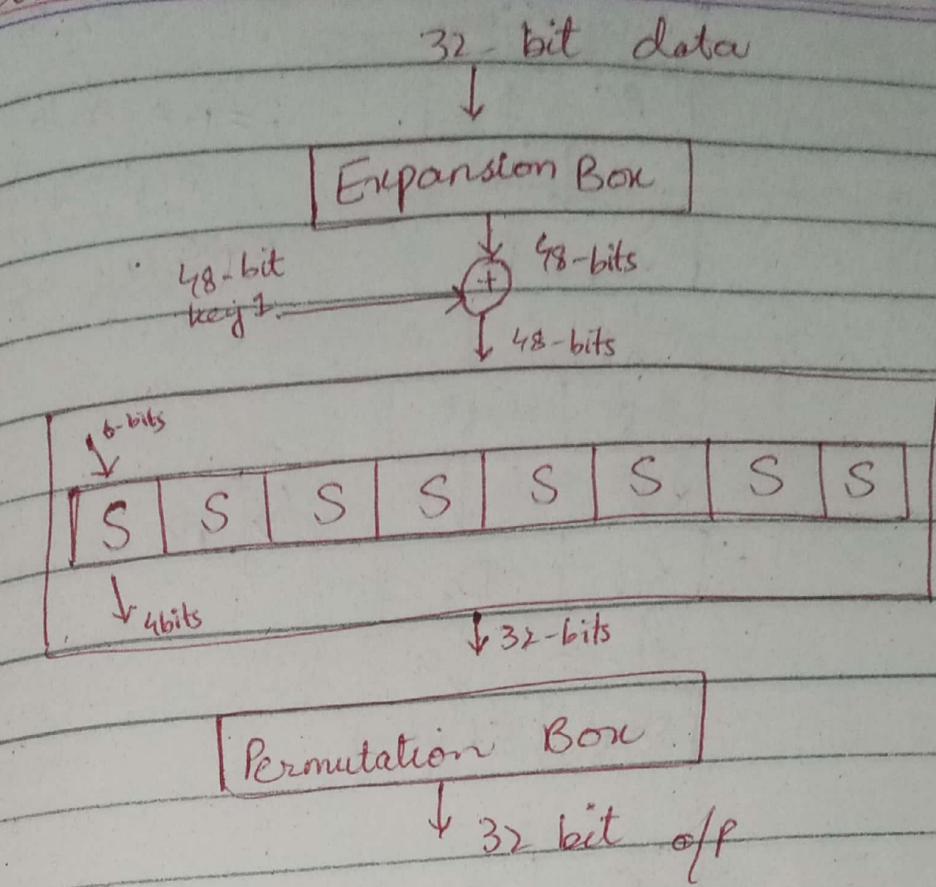
16 - feistal rounds

Swapping

Final Permutation



Round Function :



Expansion Box :

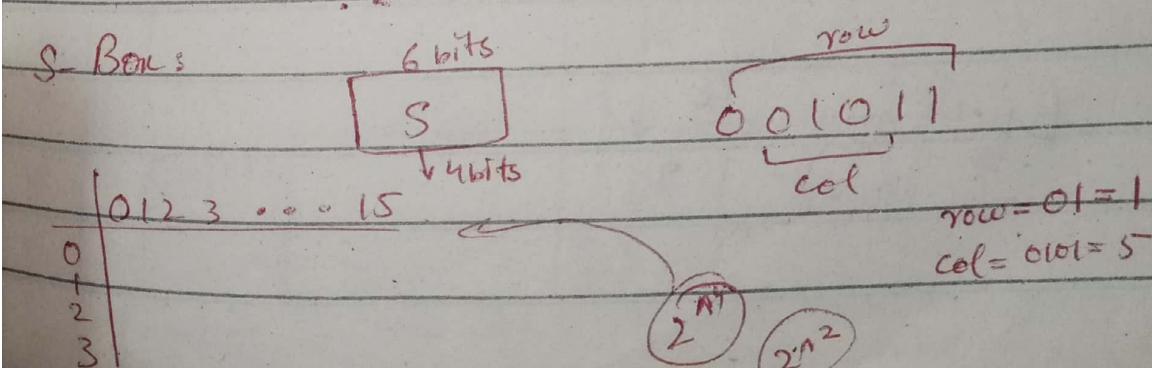
data \Rightarrow don't give the money to that person ever.

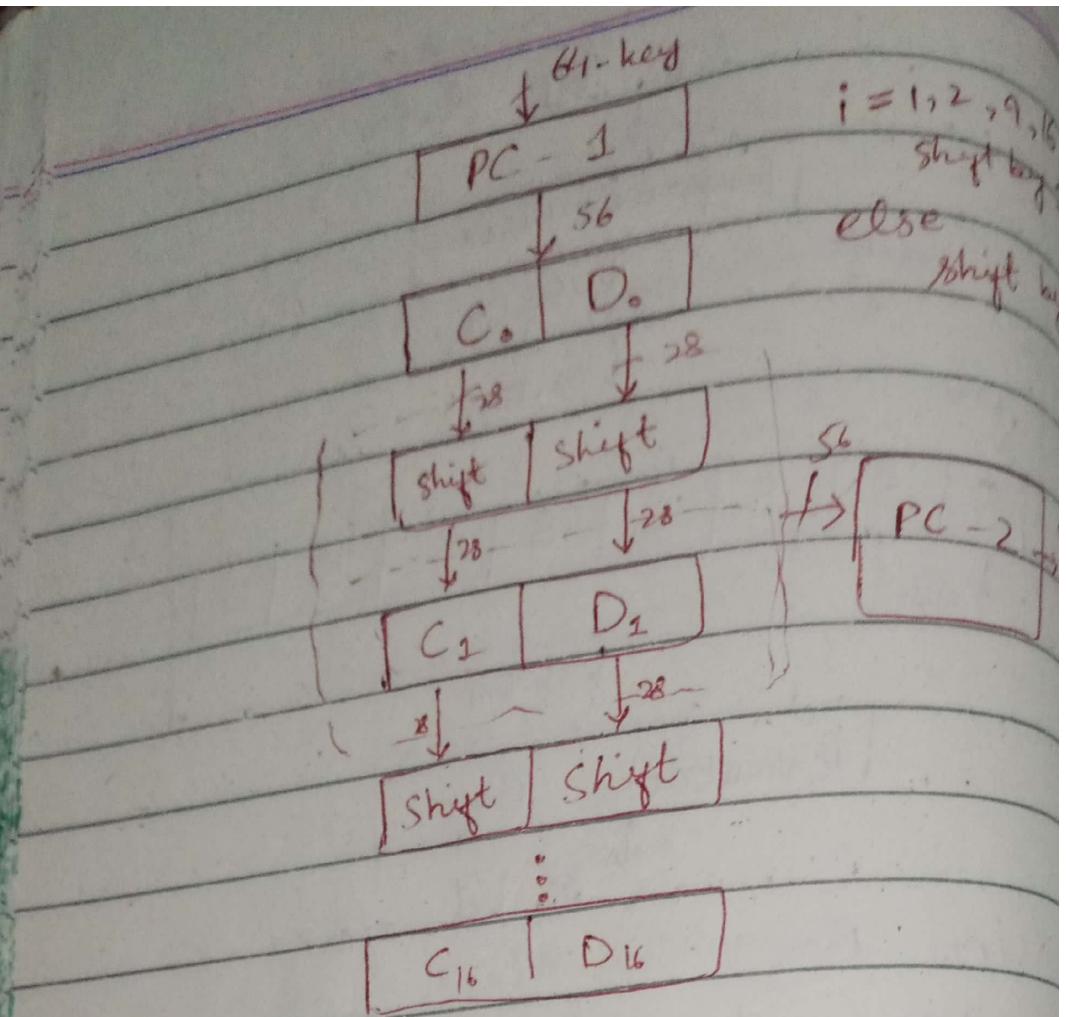
[DONT] [GIVE] [THEM] [ONEY] [TO TH] [ATPE] [RSON] [EVER]

R [DONT G T GIVE T E THEM O M ONE Y H] [N EVER]

$$8 \times 6 = 48$$

S Box :





PC - 2

$56 \rightarrow 48$

$C_1 \rightarrow 28 \text{ bits} \rightarrow (1 - 28)$

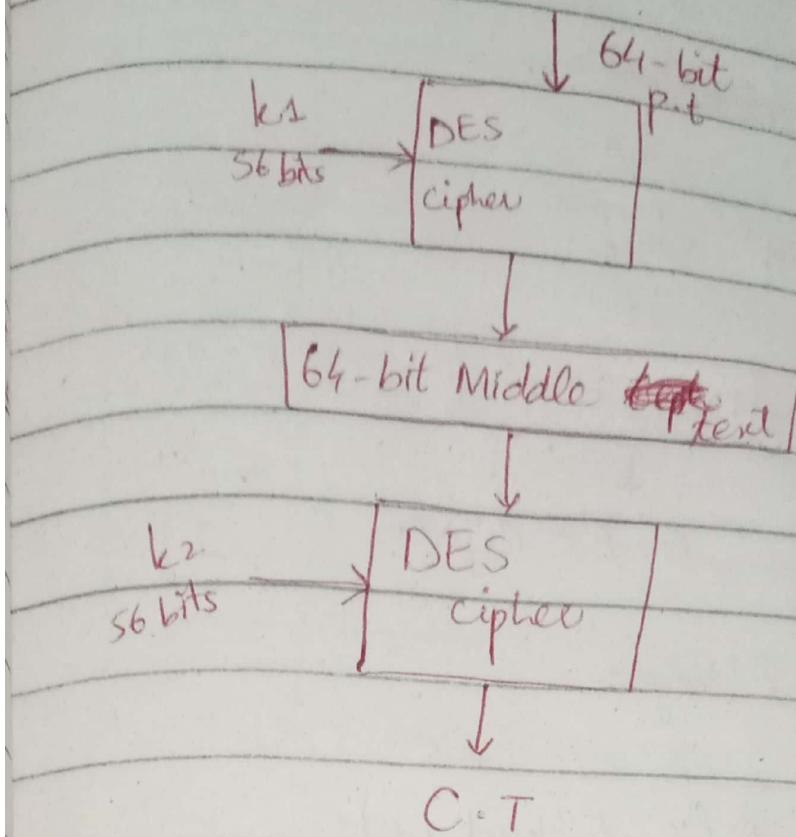
$D_1 \rightarrow 28 \text{ bits} \rightarrow (29 - 56)$

Left half $C_1 \rightarrow 9, 8, 22, 25$

right half $C_2 \rightarrow 35, 38, 43, 54$

Effective key length $\rightarrow \frac{48}{2} = 24$

1 - Double DES (2DES)



Encryption:

$$C.T = E(K_2, E(K_1, P.T))$$

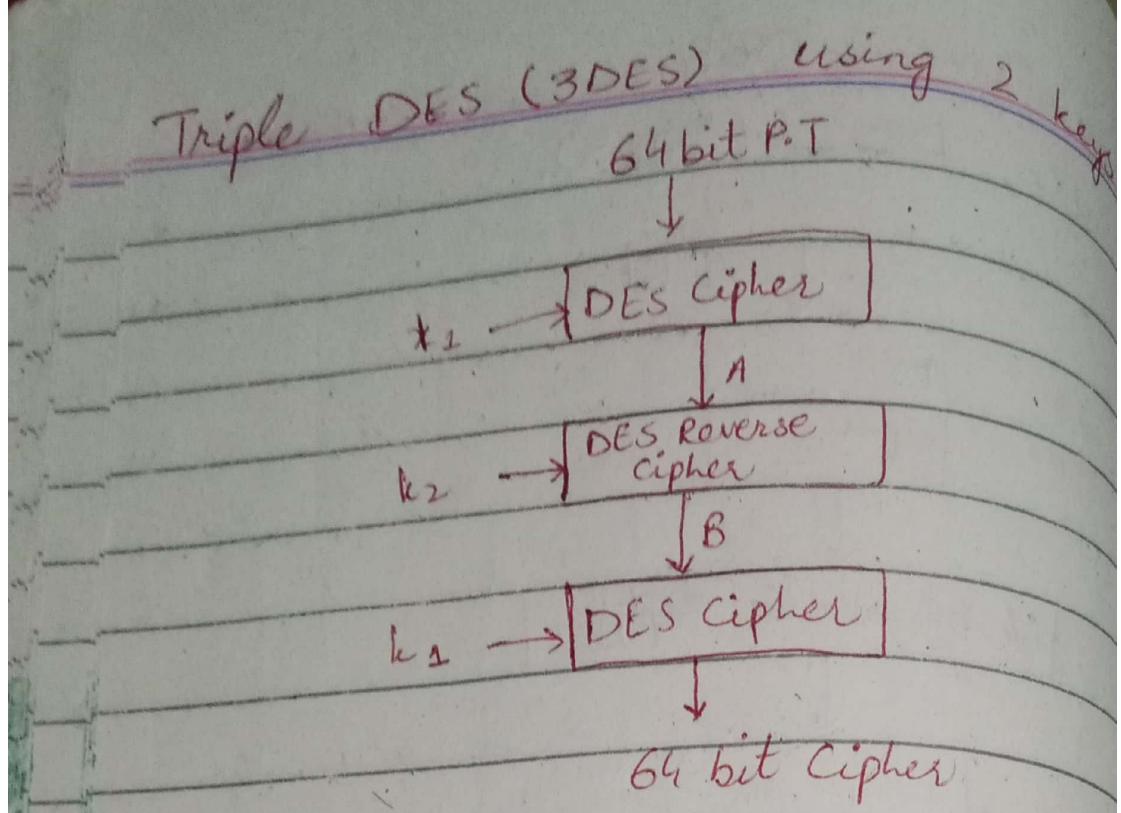
Decryption:

$$P.T = D(K_1, D(K_2, C.T))$$

Meet in the middle attack

	K_1		K_2	
key	P.T	Middle Text	C.T	Middle Text
1			1	
2			2	
..			..	
56			50	
		$k_1 = 10$		$k_2 = 50$

where middle text of both table is same
that will be values of k_1 and k_2 .



3DES using 3 keys:

$$C = E(k_3; D(k_2, E(k_1, P)))$$

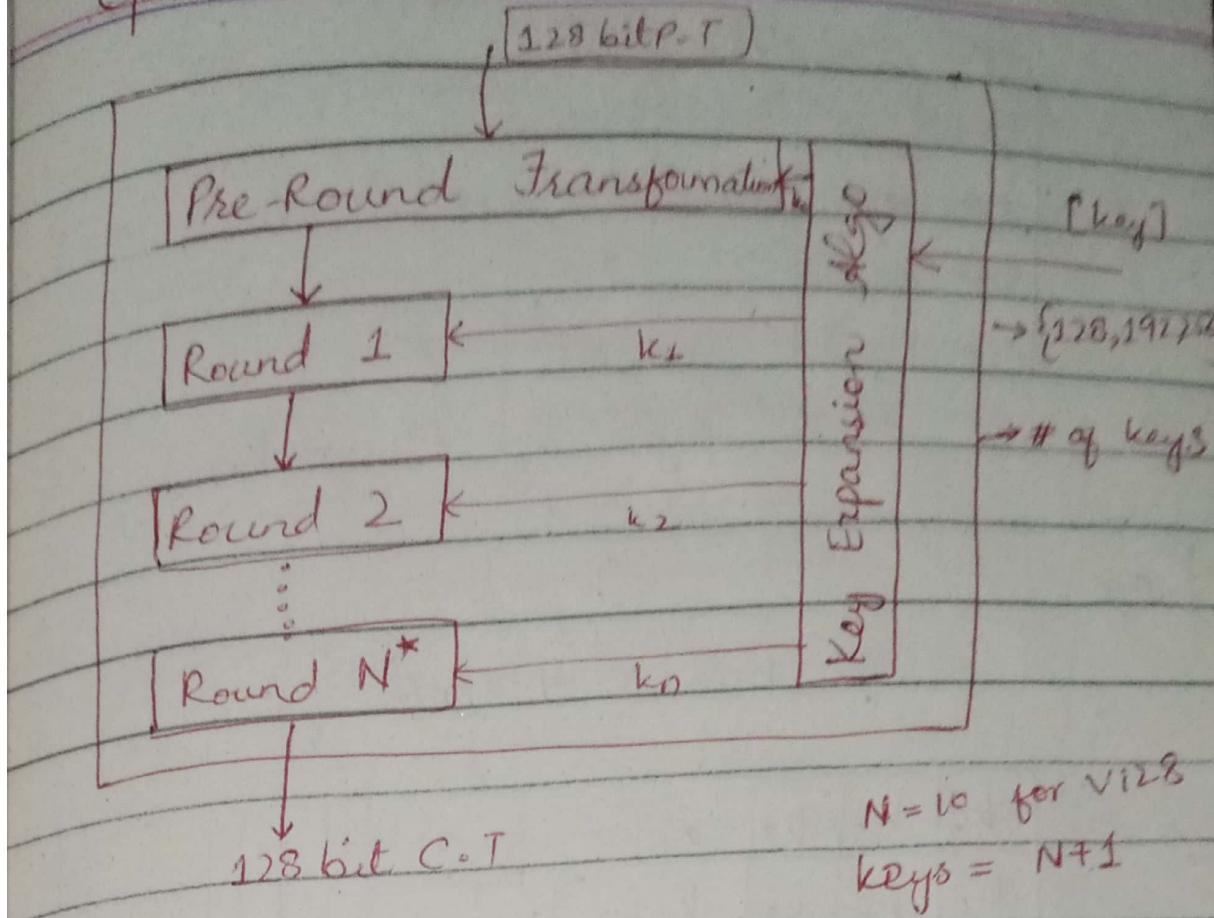
$$P = D(k_1, E(k_2, D(k_3, C)))$$

28-02-24

Advanced Encryption Standard (AES):

Rounds	No. of bits in key
version 128 → 10	128
version 192 → 12	192
version 256 → 14	256

General Structure:



$$N = 10 \text{ for } \text{Viz} \\ \text{keys} = N+1$$

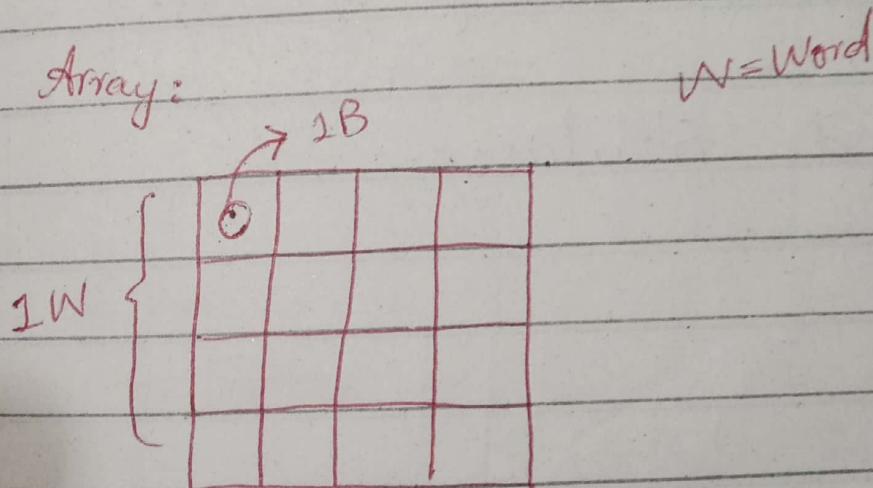
$$1B = 8 \text{ bits}$$

$$1W = 4B = 32 \text{ bits}$$

(State-Array) State \Rightarrow $[4 \times 4]$ matrix

$$\text{Array} \quad \Rightarrow \quad 16 \text{ Bytes} = 128 \text{ bits}$$

Input Array:



$$4 \times 4 = 16B = 128 \text{ bits}$$

State Array:

W_0	W_1	W_2	W_3
$S_{0,0}$	$S_{0,1}$	$S_{0,2}$	$S_{0,3}$
$S_{1,0}$	$S_{1,1}$	$S_{1,2}$	$S_{1,3}$
$S_{2,0}$	$S_{2,1}$	$S_{2,2}$	$S_{2,3}$
$S_{3,0}$	$S_{3,1}$	$S_{3,2}$	$S_{3,3}$

→ $[W_0 \ W_1 \ W_2 \ W_3]$

↳ 3rd byte of 1st word

Key:

128 bits = 4 words

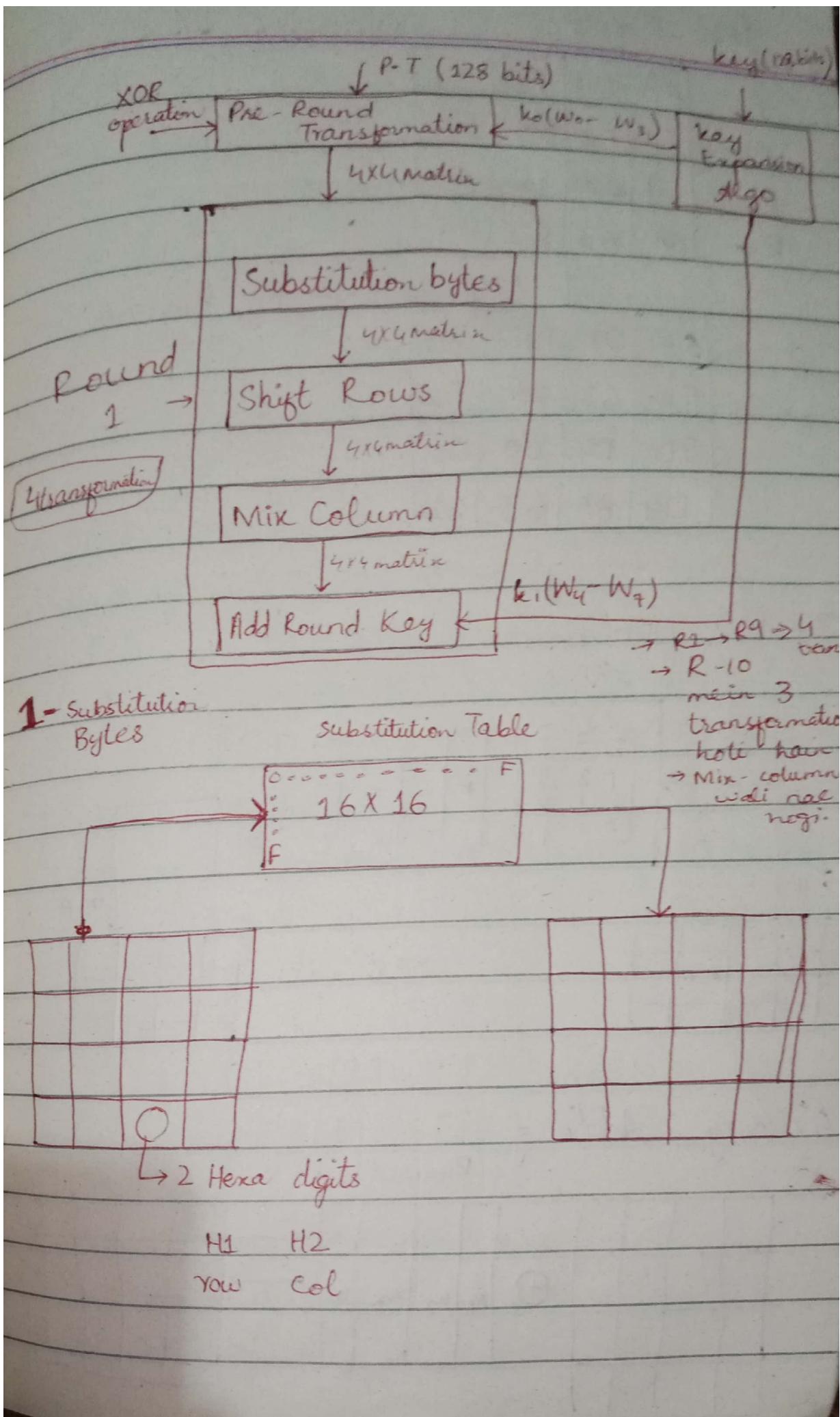
k_0	k_4	k_8	k_{12}	key Expansion Algo →	k_0
k_1	k_5	k_9	k_{13}		\dots
k_2	k_6	k_{10}	k_{14}		\dots
k_3	k_7	k_{11}	k_{15}		\dots

44 words

→ 11 keys generated

∴

Round Structure:



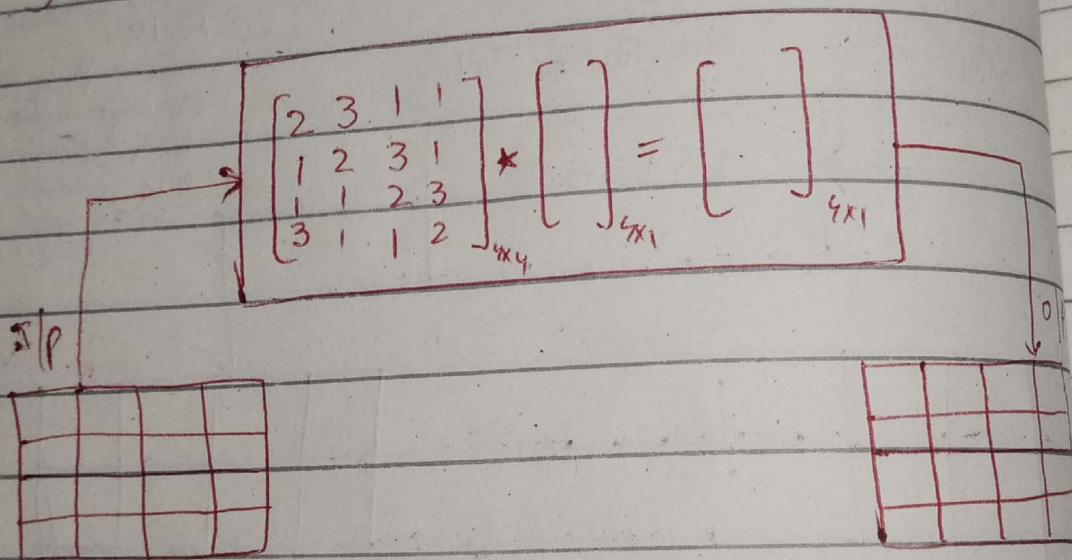
2- Shift

R ₀	63	C9	FE	30
R ₁	F2	F2	63	26
R ₂	C9	C3	7D	D4
R ₃	BA	63	82	D4

Shift to left By Row N

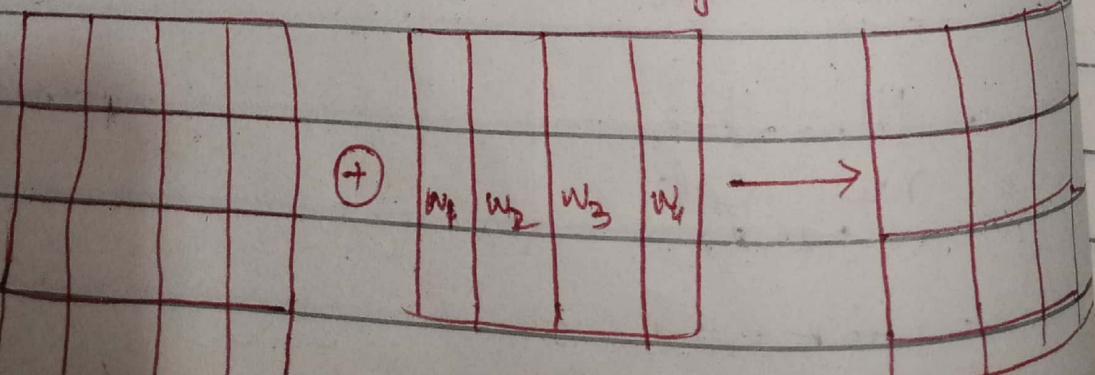
63	C9	FE	30
F2	63	26	F2
7D	D4	C9	C3
D4	BA	63	82

3- Mix Column:



4- Key Adding

Round key



05-03-24

RC4

- 1- Key Sch
- 2- Key sta
- 3- Encryption

$$S[i] = T[i]$$

$$S = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15]$$

key array =
P.T. \rightarrow

$$T[1]$$

1- Key
No. of

for i

do

j

S

2- Key

RC4

Stream Cipher

2- Key Scheduling

2- Key Stream Generation

3- Encryption and Decryption

$S[i]$ = State vector 0-255

$T[i]$ = key vector / Temporary array

$S = [0, 1, 2, 3, 4, 5, 6, 7]$

key array = [1 2 3 6]

P.T. $\rightarrow [1, 2, 2, 2]$

$T [1, 2, 3, 6, 1, 2, 3, 6]$

1- Key Scheduling

No. of iterations = Size of S-array

$j = 0$

for $i = 0$ to 255

do

$j = [j + S[i] + T[i]] \bmod 256$

swap($S[i], S[j]$)

2- Key Stream Generation

No. of iterations = Size of key

$i, j = 0$

$i = 10$
 $j = (j + S[i]) \bmod 256$
swap $[S[i], S[j]]$
 $t = [S[i] + S[j]] \bmod 256$
 $k_i = S[t];$

3. Encryption

Encryption \rightarrow P.T \oplus New Key

06-03-24

Euler's Totient Function

(Euler Phi function)

$\rightarrow \phi(n)$

\rightarrow no. of +ve integers less than ' n '
that are co-prime to ' n ' where
 $(n \geq 1)$.

Ex:

$$\phi(1) = 1$$

$$\phi(5) = ?$$

No. < 5 are $\rightarrow 1, 2, 3, 4$

$$GCD(1, 5) = 1$$

$$GCD(2, 5) = 1 \rightarrow \phi(5) = 4$$

$$\text{GCD}(3, 5) = 1$$

$$\text{GCD}(4, 5) = 1 \quad \phi(6) = ?$$

P1:

if 'n' is prime then
 $\phi(n) = n - 1$

P2:

$$\phi(a * b) = \phi(a) * \phi(b)$$

P3:

$$\phi(p^n) = p^n - p^{n-1}$$

Euler's Totient Theorem:

if 'x' and 'n' are positive coprime integers then

$$x^{\phi(n)} \equiv 1 \pmod{n}$$

$$\Rightarrow x^{\phi(n)} \pmod{n} = 1 \pmod{n}$$

Ex:

$$x = 11, \quad n = 10$$

$$11^{\phi(10)} \equiv 1 \pmod{10}$$

$$\begin{aligned}\therefore \phi(10) &= \phi(2) * \phi(5) \\ &= 1 * 4 = 4\end{aligned}$$

$$\Rightarrow 11^4 \equiv 1 \pmod{10}$$

$$1461 \equiv 1 \pmod{10}$$

L. $x^{\phi(n) \cdot a} \equiv 1 \pmod{n}$

Ex. $11^{4 \cdot 2} = 1 \pmod{10}$

$214358881 \equiv 1 \pmod{10}$

Ex. $11^{40} = 1 \pmod{10}$

Ex. $4^{99} \pmod{35}$

$x = 4, n = 35 \rightarrow \text{coprime}$

By Euler's Theorem

$$4^{\phi(35)} = 1 \pmod{35}$$

$$\begin{aligned}\therefore \phi(35) &= \phi(7) * \phi(5) \\ &= 6 * 4 = 24\end{aligned}$$

$\Rightarrow 4^{24} = 1 \pmod{35}$

$$4^{99} \rightarrow 4^{(24) \cdot 4 + 3}$$

$$= (4^{24})^4 \pmod{35} \cdot 4^3 \pmod{35}$$

$$= 1 \cdot 4^3 \pmod{35}$$

$$= 64 \pmod{35}$$

$$\therefore 29$$

Fermat's Little Theorem

→ Specific case where 'n' is prime

→ If 'n' is prime and 'x' is a positive integer not divisible by 'n' then

$$x^{n-1} \equiv 1 \pmod{n}$$

Ex:

$$x = 3, n = 5$$

$$3^{5-1} \equiv 1 \pmod{5}$$

$$3^4 \equiv 1 \pmod{5}$$

$$81 \equiv 1 \pmod{5}$$

Another way

$$x^n \equiv x \pmod{n}$$

$$3^5 \equiv 3 \pmod{5}$$

$$243 \equiv 3 \pmod{5}$$

$$\therefore 243 \% 5 = 3$$

Ex.

$$4^{532} \pmod{11}$$

$$x^{n-1} \equiv 1 \pmod{n}$$

$$x = 4, n = 11$$

$$4^{11-1} \equiv 1 \pmod{11}$$

$$4^{10} \equiv 1 \pmod{11}$$

$$\begin{aligned}
 & 4^{53} \mod 11 \\
 \Rightarrow & 4^{(4)(13)} \cdot 4^2 \mod 11 \\
 \Rightarrow & 1 \mod 11 \cdot 4^2 \mod 11 \\
 \Rightarrow & 16 \mod 11 \\
 = & 5
 \end{aligned}$$

vii - Private key

2. Encryption:

3. Decryption

RSA algo

→ Rivest - Shamir - Adleman → 1978

→ asymmetric (2 keys)

1 - Key Generation :

i - Select 2 large prime numbers P, q .

$$ii - n = P \cdot q$$

$$iii - \phi(n) = (P-1)(q-1)$$

iv - Choose value of 'e'
 $1 < e < \phi(n)$

$$\text{GCD } (\phi(n), e) = 1$$

v - Calculate

$$d = e^{-1} \mod \phi(n)$$

i.e

$$ed = 1 \mod \phi(n)$$

$$ed \mod \phi(n) = 1 \mod \phi(n)$$

vi - Public key {e, n}

$$P = 3 ,$$

$$\rightarrow n = P$$

$$\rightarrow \phi(n) =$$

Let

as

GC

$\rightarrow d$

de

$7 \times a$

$7d$

d -

vii- Private key {d, n}

2. Encryption:

$$C = M^e \text{ mod } n \quad (M < n)$$

3. Decryption:

$$M = C^d \text{ mod } n$$

$$p = 3, q = 11$$

$$\rightarrow n = p \times q = 3 \times 11 = 33$$

$$\rightarrow \phi(n) = (p-1)(q-1) \Rightarrow (3-1)(11-1) = 2 \times 10 = 20$$

$$\text{Let } e = 7$$

$$\text{as } 1 < 7 < 20$$

$$\text{GCD}(7, 20) = 1$$

$$\rightarrow d = e^{-1} \text{ mod } \phi(n)$$

$$de = 1 \text{ mod } \phi(n)$$

$$7d = 1 \text{ mod } 20$$

$$7d \text{ mod } 20 = 1$$

$d \rightarrow$ multiplicative inverse of 7 = 3

Public key = $\{e, n\} = \{7, 33\}$
Private key = $\{d, n\} = \{3, 33\}$

Encryption :

$$\text{Let } m = 31$$

then

$$C = 31^7 \pmod{33}$$
$$= 4$$

Decryption :

$$m = C^d \pmod{n}$$

$$m = 4^3 \pmod{33}$$

$$m = 31$$

~~0~~

$$3^{302} \mod 13$$

$x = 3$ and $n = 13$ are coprime
By Euler's theorem

$$3^{\phi(13)} \equiv 1 \pmod{13}$$

$$\Rightarrow \phi(13) = 12$$

$$3^{12} \equiv 1 \pmod{13}$$

$$3^{302} \mod 13 \Rightarrow 3^{(12)(25)+2} \mod 13$$

$$\Rightarrow 3^{(12)25} \mod 13 \cdot 3^2 \mod 13$$

$$= 1 \cdot 3^2 \mod 13$$

$$= 9 \mod 13$$

∴