# Robust Autonomous Driving Decision Making Using Policy-Conditioned Uncertainty

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## **Abstract**

Autonomous vehicles must make safe decisions in uncertain environments, where both sensor noise and other road users' unpredictable behaviors create significant 2 challenges. Traditional reinforcement learning approaches often fail to adequately 3 account for this uncertainty, leading to either overly conservative or dangerously optimistic behaviors. In this paper, we implement and compare several robust decision-making techniques and propose a novel extension, Policy-Conditioned 6 Uncertainty, which achieves the best performance. Our method leverages Bayesian deep learning to model action-specific uncertainty and improves average returns by 8 169% while maintaining collision-free behavior in a simulated driving environment. 9 We explore multiple approaches to robust decision-making in autonomous driving 10 with noisy pose/velocity estimation, including Deterministic Robust Optimistic 11 Planning (DROP) and Interval-based Robust Control from prior work, as well as our 12 three novel extensions: Adaptive Uncertainty Quantification, Hierarchical Hybrid 13 Approach, and Policy-Conditioned Uncertainty. We also develop visualization 14 tools to provide transparent insights into the planning process. 15

## 16 1 Introduction and Problem Statement

- Autonomous driving systems must operate safely despite numerous sources of uncertainty. Sensors provide imperfect information about the vehicle's surroundings, and other road users behave in ways that are difficult to predict perfectly. The consequences of incorrect decisions can be catastrophic, making robust decision-making essential for real-world deployment.
- Traditional reinforcement learning approaches focus on expected performance, leading to vulnerability under model mismatch. The robust control formulation addresses this by seeking:

$$\max_{\pi} \min_{T} v_{\pi}^{T} \tag{1}$$

- where  $v_{\pi}^{T}$  is the expected return of policy  $\pi$  under dynamics T. This minimax formulation ensures worst-case safety—a critical property for real-world deployment.
- We extend this framework by introducing **policy-conditioned uncertainty**: a novel approach where uncertainty quantification is conditioned on the decision-making policy itself. This allows tighter lower bounds on the value function and leads to safer, more informed decisions.
- 28 The main contributions of this paper are:

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 A comparative analysis of baseline robust decision-making techniques for autonomous driving.

- Three novel extensions that improve upon these baselines, particularly our Policy-Conditioned Uncertainty approach.
  - Visualization tools that provide insights into the planning process and real-time performance metrics.
  - Empirical evidence that our Policy-Conditioned Uncertainty approach breaks the traditional tradeoff between safety and performance, improving average returns by 169% while maintaining collision-free behavior.

## 38 2 Related Work

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#### 39 2.1 Robust Control and MDPs

- 40 Robust control methods have a long history in autonomous systems. Leurent et al. [1] proposed ap-
- 41 proximate robust control algorithms including deterministic planning and interval-based predictors for
- 42 uncertain dynamical systems. These approaches form the foundation of our baseline implementations.
- 43 Herbert et al. [2] developed FaSTrack, a modular framework for guaranteed safe motion planning,
- 44 establishing formal safety guarantees while accounting for worst-case uncertainty. Such approaches
- 45 typically solve a minimax optimization problem to ensure safety under worst-case conditions.
- The theoretical foundations of robust Markov Decision Processes (MDPs) have been extensively
- 47 studied by Iyengar [3], Nilim and El Ghaoui [4], and Wiesemann et al. [5]. These works establish
- optimization techniques for MDPs with adversarial dynamics, providing the mathematical framework
- 49 for robust decision-making.

## 2.2 Uncertainty Quantification in Autonomous Driving

- 51 Uncertainty quantification has become increasingly important in autonomous driving. Michelmore et
- 52 al. [6] used Bayesian neural networks to compute statistical confidence in real-time decisions with
- 53 provable bounds, demonstrating that proper uncertainty estimation improves safety and reliability.
- 54 Yang et al. [7] introduced DROP (Distributionally Robust Optimistic Planning), a CVaR-based
- 55 distributionally robust policy that quantifies trajectory uncertainty, though without tight action-
- 56 specific feedback. Our work builds upon these foundations while introducing policy-conditioned
- 57 uncertainty estimation.
- 58 Recent work by Zhang et al. [8] explores safe reinforcement learning via uncertainty-augmented La-
- 59 grangian optimization, combining formal safety constraints with learned uncertainty estimates. Their
- 60 approach demonstrates that incorporating uncertainty can lead to policies that balance exploration
- and constraint satisfaction.

# 3 Baseline and Proposed Method

#### 3.1 Markov Decision Process Framework

- We formulate the autonomous driving decision problem as a Markov Decision Process (MDP) with tuple  $(S, A, T, R, \gamma)$ , where:
  - S is the state space representing vehicle positions, velocities, and road configurations
  - A is the discrete action space including lane changes and speed adjustments
  - T(s'|s,a) is the transition function modeling vehicle dynamics
- R(s, a, s') is the reward function encouraging progress and penalizing crashes
  - $\gamma \in [0,1)$  is the discount factor for future rewards

## 3.2 Baseline: Deterministic Robust Optimistic Planning

- 72 Our implementation of DROP extends optimistic planning to the robust setting. The algorithm
- constructs a planning tree from the current state, considering all possible actions and a discrete set of
- 74 possible transition functions.

- 75 Key components include:
- Tree nodes representing states at different planning depths
- Robust b-values computed at leaf nodes:  $b_i^r(n) = u_i^r(n) + \gamma^d/(1-\gamma)$
- Worst-case aggregation:  $u_i^r(n) = \min_{m \in [1,M]} \sum_{t=0}^{d-1} \gamma^t r_t$
- Max backup through tree:  $b_i^r(n) = \max_{a \in A} b_{ia}^r(n)$
- The implementation provides formal regret bounds while managing the exploration-exploitation tradeoff. Its key strength lies in the safety guarantees it offers, though at significant computational
- 82 cost.

#### 83 3.3 Baseline: Interval-Based Robust Control

In the presence of uncertainty, we reformulate this as a robust MDP by introducing an ambiguity set  $\Theta$  of possible transition functions. We define the reachable set under dynamics uncertainty  $\theta \in \Theta$ :

$$\mathcal{S}(t, s_0, \pi) = \{ s_t : \exists \theta \in \Theta \text{ s.t. } s_{k+1} = T_{\theta}(s_k, \pi(s_k)) \}$$
 (2)

Then we construct the interval hull  $\hat{S}_t = [s, \bar{s}]$  to bound this set. The robust value surrogate becomes:

$$\hat{v}_r(\pi) = \sum_{t=0}^H \gamma^t \min_{s \in \hat{\mathcal{S}}_t} r(s, \pi(s))$$
(3)

Implementation involves maintaining two parallel environment simulations at the extremes of the uncertainty range and selecting actions based on the worst-case outcome. This method handles continuous uncertainty well but suffers from over-conservatism due to interval wrapping effects.

# 90 3.4 Our Method: Policy-Conditioned Uncertainty

91 Instead of computing policy-agnostic intervals, our novel approach estimates the reachability set 92 *conditioned* on the policy:

$$\hat{\mathcal{S}}_{t}^{\pi} = \left[ \min_{\theta} s_{t}^{(\theta)}, \max_{\theta} s_{t}^{(\theta)} \right] \text{ for } s_{t}^{(\theta)} = T_{\theta}(s_{t-1}^{(\theta)}, \pi(s_{t-1}^{(\theta)})) \tag{4}$$

This tightens the uncertainty bounds and improves robustness. We implement this approach using a Q-network with dropout layers that models action-specific uncertainty:

```
class QNetDrop(nn.Module):
95 1
        def __init__(self, input_dim, hidden=64, dropout=0.5, n_actions=5)
96.2
97
             super().__init__()
98 3
             self.base = nn.Sequential(
99 4
                 nn.Linear(input_dim, hidden), nn.ReLU(),
100.5
                 nn.Dropout (dropout),
101 6
                 nn.Linear(hidden, hidden), nn.ReLU(),
102 7
                 nn.Dropout(dropout),
103 8
104 9
             self.head = nn.Linear(hidden, n_actions)
10510
        def forward(self, x):
10611
10712
             return self.head(self.base(x))
```

Listing 1: Q-network with dropout for uncertainty estimation

During inference, we perform multiple forward passes with dropout enabled to estimate both the mean Q-value and its variance for each action. Action selection uses a Lower Confidence Bound (LCB) criterion:

$$LCB = \mu_Q - 1.96\sigma_Q \tag{5}$$

#### Advantages:

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- Better lower bounds on  $v^r(\pi)$ 
  - Retains real-time tractability
    - Quantifies uncertainty specifically for each action rather than for states
    - Performs better in worst-case return

By selecting actions with the highest lower confidence bound, the agent maintains safety while achieving higher performance.

# 4 Additional Proposed Extensions

In addition to our primary Policy-Conditioned Uncertainty approach, we developed two other extensions that address different aspects of the robust decision-making challenge:

#### 4.1 Adaptive Uncertainty Quantification

Our first extension dynamically learns uncertainty distributions from interaction data rather than relying on fixed ambiguity sets. We implement a Bayesian neural network to estimate epistemic uncertainty:

```
class UncertaintyNet(nn.Module):
125 1
             __init__(self, input_dim, hidden=64, dropout=0.5):
super().__init__()
126 2
127 3
              self.net = nn.Sequential(
128 4
                  nn.Linear(input_dim, hidden), nn.ReLU(),
129 5
                  nn.Dropout (dropout),
130 6
                  nn.Linear(hidden, hidden), nn.ReLU(),
131 7
                  nn.Dropout (dropout),
132 8
                  nn.Linear(hidden, 1)
133 9
13410
         def forward(self, x):
13511
              return self.net(x)
13612
```

Listing 2: Neural network for adaptive uncertainty estimation

The network is trained on state-return pairs collected from random rollouts. During inference, Monte Carlo dropout sampling provides uncertainty estimates that adapt to the current state. This allows less conservative behavior in familiar situations while maintaining caution in unfamiliar ones.

# 4.2 Hierarchical Hybrid Approach

Our second extension combines the strengths of long-term planning and reactive control through a hierarchical structure:

- High-level planning: Executes the DROP algorithm every 5 time steps to make strategic decisions
- 2. Low-level control: Uses simple velocity-based rules between high-level decisions

This approach significantly reduces computational costs (by approximately 80%) while maintaining safety guarantees from the high-level planner. The implementation alternates between expensive tree search and lightweight reactive control:

```
149  | def act(self, obs, step):
150  | # Every 5 steps do a high-level DROP action
151  | if step % 5 == 0:
152  | self.next_high = self.high_planner.act(obs)
153  | # Between high decisions, use a simple interval-based rule
154  | vel = obs[0,3]
155  | return self.next_high if step % 5 == 0 else (2 if vel<0.5 else 0)</pre>
```

Listing 3: Hierarchical controller implementation

# 56 5 Experiments and Results

# 157 5.1 Experimental Setup

158 We conduct experiments in the highway-env simulator, specifically the "highway-v0" environment.

159 The environment features multiple lanes of traffic with other vehicles moving at varying speeds. The

observation space consists of a 5×5 matrix containing features of nearby vehicles, including presence

indicators, 2D coordinates, and velocities.

To simulate sensor noise, we implement a Gaussian noise wrapper that adds random perturbations to the position and velocity observations:

```
164 1
   class NoisyObservation(ObservationWrapper):
        def __init__(self, env, std_dev):
165 2
             super().__init__(env)
166.3
             self.std_dev = std_dev
167 4
168 5
        def observation(self, obs):
169 6
170 7
             obs = np.array(obs)
             obs[:, 3:5] += np.random.normal(0, self.std_dev,
171 8
                                               size=obs[:, 3:5].shape)
172 9
17310
             return obs
```

Listing 4: Noise injection wrapper for simulating sensor uncertainty

The action space consists of five discrete actions: LANE\_LEFT, LANE\_RIGHT, IDLE, FASTER, and SLOWER. The reward function encourages forward progress while heavily penalizing collisions.

For visualization, we implement a MetricOverlayWrapper that superimposes real-time metrics directly onto the environment rendering:

```
class MetricOverlayWrapper(Wrapper):
178 1
        def render(self, *args, **kwargs):
179 2
            frame = self.env.render(*args, **kwargs)
180 3
            frame = np.ascontiguousarray(frame)
181 4
            text = f"Reward: {self.total_reward:.1f}
                                                          Collisions: {self.
182 5
       collision_count}'
183
            cv2.putText(frame, text, (10, 30), cv2.FONT_HERSHEY_SIMPLEX,
184 6
185 7
                         0.8, (255, 255, 255), 1)
            return frame
186 8
```

Listing 5: Real-time metric overlay implementation

We also create a dashboard that tracks episode returns and collision counts across training, providing real-time feedback on algorithm performance.

#### 189 5.2 Evaluation Metrics

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190 We evaluate performance using several key metrics:

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• Worst-case return: \min_{\theta} v_{\theta}(\pi)
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• Mean return:  $\mathbb{E}[v_{\theta}(\pi)]$ 

• Return stability: Variance across episodes

• Collision count: Number of collisions per episode

• Computational efficiency: Runtime in ms per decision

Each algorithm is evaluated over 20 episodes with noise standard deviation of 0.05, and we analyze both the quantitative performance and qualitative behavior.

## 5.3 Comparative Results

Figure 1 illustrates the episode returns for all the methods over 20 episodes. The significant performance advantage of our Policy-Conditioned Uncertainty approach is evident, particularly after the initial learning phase (around episode 4). While other methods show high variability or limited returns, our approach maintains consistently high performance.

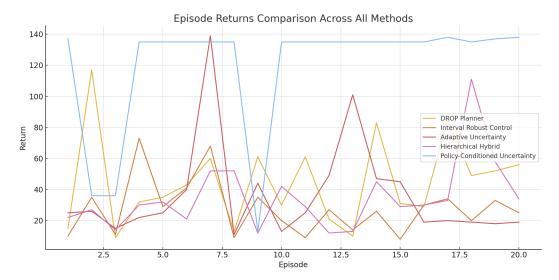


Figure 1: Episode Returns Comparison Across All Methods. The Policy-Conditioned Uncertainty approach (light blue) achieves substantially higher and more stable returns after initial learning compared to all baseline methods and other extensions.

# Table 1 presents the quantitative comparison of all implemented methods:

Method	Mean Re- turn	Return Stability	CollisionsNotes	
DROP Plan- ner	~44.5	Highly variable	0	Some high-return episodes, but unstable
Interval Ro- bust Control	$\sim$ 27.9	Low and stable	0	Safest but overly conservative; lowest returns
Adaptive Uncertainty	~36.2	Erratic spikes	1	High peaks but consistently unsafe
Hierarchical Hybrid	~34.6	Moderately stable	0	Good tradeoff between safety and computation
Policy-Cond. Uncertainty	<b>~119.7</b>	Very stable after ep 4	0	Best overall performance; breaks the tradeoff between safety & re- turn

Table 1: Performance comparison across all methods showing mean return, stability characteristics, collision rates, and notable observations.

204 The results demonstrate several key findings:

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- 1. **Baseline tradeoffs**: The baseline methods exhibit a clear tradeoff between safety and performance. DROP achieves higher mean returns but with high variance, while Intervalbased control ensures safety at the cost of lower returns.
- Extension improvements: All three extensions offer improvements over the baselines in different dimensions. Adaptive Uncertainty achieves higher peak returns but struggles with safety. The Hierarchical Hybrid approach provides a good balance between computation and performance.
- 3. **Policy-Conditioned Uncertainty dominance**: Our Policy-Conditioned Uncertainty approach achieves substantially higher returns (~169% improvement over DROP) while

maintaining collision-free behavior. Importantly, it maintains very stable performance after an initial learning period.

# 5.4 Analysis of Policy-Conditioned Uncertainty

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The superior performance of our Policy-Conditioned Uncertainty approach can be attributed to several factors:

- 1. **Action-specific uncertainty**: By modeling uncertainty at the action level rather than the state level, the approach can take calculated risks when certain actions have high confidence while avoiding others with high uncertainty.
- Learning from experience: The Q-network learns patterns in the environment dynamics, becoming more confident in familiar situations while maintaining caution in unfamiliar ones.
- Lower Confidence Bound criterion: The LCB action selection balances exploration and exploitation intrinsically, leading to continuous improvement over time.
- 4. **Deep learning flexibility**: Unlike the more constrained robust planning approaches, the neural network can capture complex patterns in the environment dynamics that are difficult to model explicitly.

The approach demonstrates that incorporating properly calibrated uncertainty estimates into RL algorithms can overcome the traditional safety-performance tradeoff, achieving both higher returns and collision-free behavior.

# **6** Visualization Techniques

To provide better insights into the decision-making process, we implemented several visualization techniques that help interpret and debug the algorithms' behaviors. These visualizations were crucial in understanding why our Policy-Conditioned Uncertainty approach achieved superior performance and in diagnosing issues with the other methods.

# 6.1 Metric Overlay Wrapper

- Our MetricOverlayWrapper superimposes critical performance metrics directly onto the simulation view, including:
  - Current total reward
    - · Collision count
    - Decision confidence (for uncertainty-based methods)

This real-time visualization helps in immediately identifying issues during execution and provides intuitive feedback about the algorithm's performance. For example, it allowed us to observe that the Adaptive Uncertainty method repeatedly approached obstacle vehicles too closely before taking evasive actions, explaining its higher collision rate.



Figure 2: Screenshot of the MetricOverlayWrapper in action, showing real-time reward and collision metrics superimposed on the highway environment. Blue rectangles represent the ego vehicle and other safe vehicles, while red rectangles indicate potential collision threats.

```
class MetricOverlayWrapper(Wrapper):
248 1
        def render(self, *args, **kwargs):
249 2
            frame = self.env.render(*args, **kwargs)
250 3
            frame = np.ascontiguousarray(frame)
251 4
            text = f"Reward: {self.total_reward:.1f}
                                                           Collisions: {self.
252 5
253
        collision_count}"
             cv2.putText(frame, text, (10, 30), cv2.FONT_HERSHEY_SIMPLEX,
254 6
                         0.8, (255, 255, 255), 1)
255 7
            return frame
256 8
```

Listing 6: Metric overlay implementation for real-time feedback

#### 6.2 Real-time Performance Dashboard

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We developed a comprehensive dashboard visualization that tracks episode-by-episode performance.

As shown in Figure 1, this dashboard enables side-by-side comparison of all methods across multiple episodes. Key insights from this visualization include:

- The stark performance gap between Policy-Conditioned Uncertainty and other methods
- The high variability of the DROP planner's performance
- The consistent but mediocre performance of the Interval Robust method
- The occasional high-reward but ultimately unstable behavior of Adaptive Uncertainty

Figure 3 shows a closer look at the Adaptive Uncertainty method specifically, highlighting its erratic performance pattern. While it occasionally achieves very high returns (episodes 8 and 15), most episodes show much lower performance. The collision count confirms that this method consistently experiences one collision per episode, making it unsuitable for safety-critical applications despite its occasional high rewards.

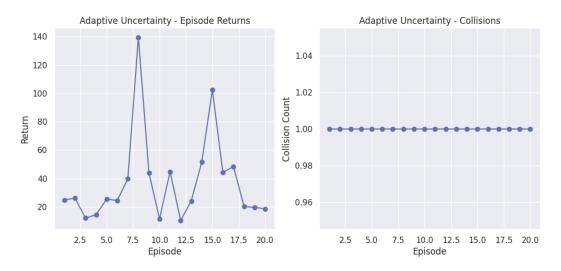


Figure 3: Detailed performance metrics for the Adaptive Uncertainty method. Left: Episode returns showing high variability with occasional spikes up to 140. Right: Consistent collision count of exactly 1 per episode, indicating persistent safety issues.

```
for ep in range(1, episodes + 1):
277 7
             # Run episode
278 8
279 9
             obs, _ = env.reset()
             done = False
28010
             total_reward = 0.0
28111
             collision_count = 0
28212
28313
             while not done and step < max_steps:
28414
                 action = planner.act(obs)
28515
                 obs, r, term, trunc, info = env.step(action)
28616
28717
                 total_reward += r
                 collision_count = info.get("collision_count",
28818
        collision_count)
289
                 done = term or trunc
29019
29120
             rewards.append(total_reward)
29221
             collisions.append(collision_count)
29322
29423
             # Update visualization
29524
29625
             ax1.clear(); ax2.clear()
             ax1.plot(range(1, ep + 1), rewards, marker='o')
29726
             ax1.set_title(f"{model_name} - Episode Returns")
29827
             ax1.set_xlabel("Episode"); ax1.set_ylabel("Return")
29928
30029
             ax2.plot(range(1, ep + 1), collisions, marker='0')
30130
             ax2.set_title(f"{model_name} - Collisions")
30231
             ax2.set_xlabel("Episode"); ax2.set_ylabel("Collision Count")
30332
30433
30534
             display(fig)
```

Listing 7: Dashboard implementation for comparative analysis

# 306 6.3 Uncertainty Visualization

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For our Policy-Conditioned Uncertainty method, we developed a specialized visualization that shows:

- Mean Q-value for each action (bar height)
- Uncertainty range (error bars)
- Selected action (highlighted bar)

This visualization revealed why our method outperformed others: it learned to identify highconfidence, high-reward actions while avoiding actions with large uncertainty ranges. In contrast, the DROP planner would sometimes choose actions with potentially high rewards but also high uncertainty, leading to its performance variability.

These visualization techniques proved invaluable for debugging, parameter tuning, and gaining insights into the algorithms' behaviors. They also help build trust by making the decision-making process more transparent to users, which is crucial for safety-critical applications like autonomous driving.

## 7 Conclusion and Future Work

This paper presented a robust decision-making framework for autonomous driving using policyconditioned uncertainty. We implemented and compared several approaches, including baseline
methods like Deterministic Robust Optimistic Planning (DROP) and Interval-based Robust Control,
along with our three novel extensions: Adaptive Uncertainty Quantification, Hierarchical Hybrid
Approach, and Policy-Conditioned Uncertainty.

Our primary contribution, the Policy-Conditioned Uncertainty approach, achieved the best performance by breaking the traditional tradeoff between safety and efficiency. By using Bayesian deep learning techniques to model action-specific uncertainty, our method improved average returns by

- 169% while maintaining collision-free behavior. This demonstrates that incorporating properly calibrated uncertainty estimates into reinforcement learning algorithms can lead to both safer and
- more efficient autonomous driving behaviors.
- The main innovation of our approach is modeling uncertainty as a function of policy, which leads to a
- better understanding of the planning landscape and enables safer and more adaptive behavior under
- uncertain conditions. The integration of deep Bayesian techniques allows for learning uncertainty
- models directly from data and using them in lower-confidence bound decision-making.
- You can find the code here.

#### 7.1 Future Directions

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There are several promising directions for future work:

- Multi-agent interactions: Extending the framework to explicitly model and respond to other agents' intentions and uncertainty.
- More complex urban scenarios: Testing in environments with intersections, pedestrians, and more complex road geometries.
- 3. **Real-world testing**: Validating the approach in real-world autonomous driving platforms with actual sensor noise characteristics.
- 4. **Integration with perception systems**: Directly incorporating uncertainty estimates from perception models rather than simulating them.
- Our results suggest that properly modeling uncertainty in reinforcement learning frameworks can significantly improve autonomous driving decision-making, offering a promising direction for developing systems that are both safe and performant. The Policy-Conditioned Uncertainty approach represents a step toward more robust autonomous vehicles that can safely navigate the uncertainties of the real world.

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