# Task 7.1D: Function approximation implementation

### Introduction

The following task is another extension to the environment we have seen from Task 1.1P, but this time it implements two algorithms that incorporate Function Approximation. We implemented these two algorithms on the 'Pendulum-v0' Environment. Please refer to this link for further details about the environment: Pendulum - Gym Documentation (gymlibrary.dev).

Our report aims to talk in detail about the environment and the results we have received from it while creating the environment and the algorithms from scratch. These algorithms are as follows:

- Semi-Gradient SARSA (0)
- Semi-Gradient TD(Lambda)

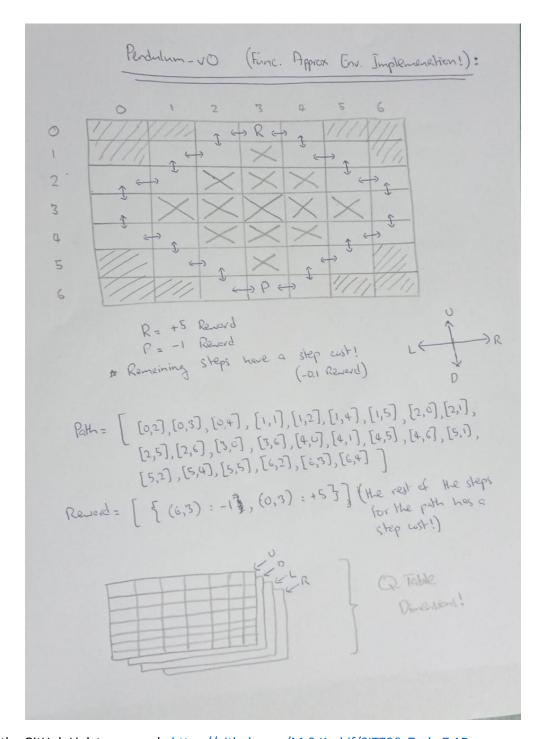
We have also appended our Python Jupyter Notebook with this report. Please refer to the end of this report.

#### About our Fnvironment

Our Environment resembles the Grid World Environment we have worked through the workshops in the past couple of weeks. In fact, I have attached an Image and the Jupyter Notebook File of the 'Grid World' Environment in the GitHub Repository mentioned below under this sub-heading. Our observation space comprises a 3D Array this time, where we have the Grid Environment's x and y coordinates and the actions to be taken within the Grid. This is shown below in the following picture below.

I have happened to also mention the actions and rewards per state in the figure. Please note three important aspects of the environment. Firstly, the states we have mentioned in the environment below happened to resemble the circular path in which our pendulum moves around, in order to balance itself from the fixed end. They are enlisted as shown in the picture below. Secondly, each state comprises a pair of actions pointing outwards (although the actions I should like a double arrow). So, for example, the actions of the initial state S(6,3) are left (L) and right(R). please also know that I have shown the directions within the picture, in initials. All of the actions for each state are mentioned within the Jupyter Notebook. And thirdly, each state also has a reward associated with it. So for the starting state S(6,3) and the terminal state S(0,3), the rewards are -1 and +5 respectively. And as for the remaining states, they have a step cost of -0.1. Finally, the Q-Table derived for this environment is a 3D environment, where the x, y, and z coordinates are the x and y coordinates of the 7x7 grid along with the number of all possible actions, which are 4. The third coordinate of the environment is exempted from Semi-gradient TD(Lambda).

In order to compute the results, we have taken 200 timesteps per episode. In the later heading, we computed a graph of average rewards received by the agent per episode. We have computed two trends with different colors in order to get the results we need.



This is the GitHub Link to my work: <a href="https://github.com/M-S-Kashif/SIT796">https://github.com/M-S-Kashif/SIT796</a> Task 7.1D

# Results

The following are some of the results we have taken from our Notebook. We have taken the mean value of the reward after 100 episodes, and the final Q-Table after the 100<sup>th</sup> episode, to justify the working of our Model. These are how the results look like:

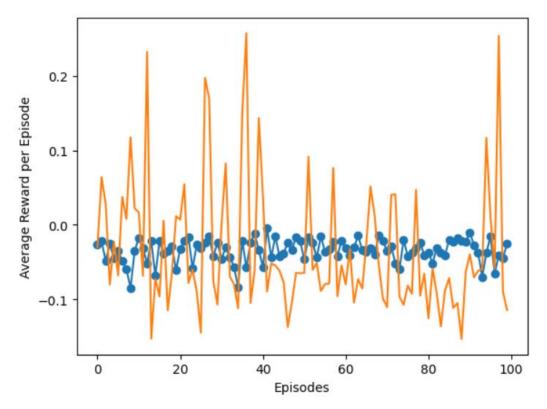
# (Semi-Gradient SARSA(0))

```
Q-Table in the 100th Episode:
Episode --- [47/100] | Reward ---- -4.7
                                                      0.
Episode --- [48/100]
                                                                             0.
                                                                                       0.
                     Reward ---- -6.79999999999997
                                                                   0.
                                                      [ 0.
                                                                0.
0.
0.
0.
                                                       [ 0.
[ 0.
Episode --- [49/100]
                     Reward ---- -3,20000000000000000
                                                                              0.
                                                                                        0.
                                                                                                 1
                                                                            0.
Episode --- [50/100]
                     Reward ---- -4.399999999999999
                                                                                        0.
Episode --- [51/100]
                     Reward ---- -9.29999999999999
                                                       [ 0.
[ 0.
                                                                            0.
0.
0.
                                                                                        0.
                                                      [ 0.
[ 0.
                     Reward ---- -3,3000000000000001
Episode --- [52/100]
                                                                                        0.
Episode --- [53/100]
                     Reward ---- -4.7000000000000001
                                                                                        0.
                                                                                                 ]]
Episode --- [54/100]
                     Reward ---- -8.79999999999999
Episode --- [55/100]
                     Reward ---- -3.1000000000000001
                                                      [[ 0.
                                                                  0.
                                                                            0.
                                                                                        0.
                                                                                                 1
                                                               0.
0.
0.
0.
0.
Episode --- [56/100]
                     Reward ---- -7.19999999999999
                                                                          0.
                                                      [ 0.
                                                                                        0.
Episode --- [57/100]
                     Reward ---- -6.399999999999999
                                                       [ 0.
                                                                             0.
                                                                                        0.
Episode --- [58/100]
                     Reward ---- -4.599999999999999
                                                                                        0.
Episode --- [59/100]
                     Reward ---- -8.39999999999997
                                                       [ 0.
[ 0.
                                                                            0.
0.
0.
                                                                                        0.
                     Reward ---- -4.2
Episode --- [60/100]
                                                                                        0.
                                                      [ 0.
Episode --- [61/100]
                     Reward ---- -6.2
                                                                                        0.
                                                                                                  11
Episode --- [62/100]
                     Reward ---- -8.09999999999999
                                                      Episode --- [63/100]
                     Reward ---- -6.1
                                                                                        0.
                                                                                                 1
Episode --- [64/100]
                     Reward ---- -2.90000000000000001
                                                                                        0.
Episode --- [65/100]
                     Reward ---- -6.79999999999998
                                                                                        0.
Episode --- [66/100]
                     Reward ---- -7.19999999999998
                                                                                        0.
Episode --- [67/100]
                     0.
                                                                                                 1
Episode --- [68/100]
                     Reward ---- -7.89999999999998
                                                                                        0.
Episode --- [69/100]
                     Reward ---- -2.9000000000000001
                                                                                        0.
                                                                                                  11
Episode --- [70/100]
                     Reward ---- -4.2
                                                                 0.
0.
0.
0.
0.
Episode --- [71/100]
                     Reward ---- -7.09999999999998
                                                                            0.
                                                      [[ 0.
                                                                                        0.
                                                                            0.
                                                      [ 0.
Episode --- [72/100]
                     Reward ---- -5.6999999999999975
                                                                                        0.
                                                                                                 1
Episode --- [73/100]
                     Reward ---- -10.29999999999999
                                                                                        0.
Episode --- [74/100]
                     Reward ---- -11.899999999999983
                                                       [ 0.
                                                                                        0.
                                                                            0.
Episode --- [75/100]
                     Reward ---- -4.0000000000000001
                                                                           0.
0.
0.
                                                       [ 0.
                                                                                        0.
                                                       [ 0.
Episode --- [76/100]
                     Reward ---- -8.49999999999999
                                                                                        0.
                                                      [ 0.
Episode --- [77/100]
                     Reward ---- -7.599999999999998
                                                                                        0.
                                                                                                  11
Episode --- [78/100]
                     Reward ---- -6.299999999999997
                                                      Episode --- [79/100]
                     Reward ---- -4.7
                                                                                        0.
                                                                                                 1
Episode --- [80/100]
                     Reward ---- -8.2
                                                                                        0.
Episode --- [81/100]
                     Reward ---- -7.499999999999999
                                                                                                 ]
Episode --- [82/100]
                     Reward ---- -10.29999999999995
                                                                                        0.
Episode --- [83/100]
                     Reward ---- -6.19999999999995
                                                                                        0.
Episode --- [84/100]
                     Reward ---- -7.49999999999998
                                                                                        0.
Episode --- [85/100]
                     Reward ---- -8.09999999999987
                                                                                        0.
                                                                                                 11
Episode --- [86/100]
                     Reward ---- -4.0000000000000001
                                                      [[ 0.
[ 0.
                                                                 0. 0.
0. 0.
Episode --- [87/100]
                     Reward ---- -4.60000000000000000
                                                                                        0.
                                                                                                 1
Episode --- [88/100]
                     Reward ---- -3.500000000000000000
                                                                                        0.
                                                       [ 0.
Episode --- [89/100]
                     Reward ---- -4.4
                                                                  -0.0199181 0.
0. 0.
0. 0.
                                                                                        0.
                                                       Episode --- [90/100]
                     0.
Episode --- [91/100]
                     Reward ---- -2.0
                                                                                        0.
                                                                            0.
0.
0.
Episode --- [92/100]
                     0.
0.
Episode --- [93/100]
                     Reward ---- -7.499999999999998
                                                                                                  11
Episode --- [94/100]
                     Reward ---- -13.99999999999968
                                                                  0. 0.
0.
                                                      [[ 0.
[ 0.
Episode --- [95/100]
                    Reward ---- -7.499999999999999
                                                                                        0.
                                                                                                 1
Episode --- [96/100]
                    Reward ---- -3.1
                                                                                        0.
Episode --- [97/100] |
                    Reward ---- -12,9999999999997
                                                       [-0.02999181 -0.00616232 -0.04406767 -0.35249578]
Episode --- [98/100]
                    Reward ---- -8.09999999999998
                                                      [ 0.
[ 0.
                                                                   0. -0.04935613 0.
0. 0. 0.
Episode --- [99/100] | Reward ---- -8.99999999999999
                                                                                                 1
Episode --- [100/100] | Reward ---- -5.0
                                                       [ 0.
                                                                  0.
0.
                                                                                        0.
                                                                             0.
                                                                                        0.
Average Reward after 100 Episodes: -6.88999999999997
                                                                             0.
                                                                                                  111
```

# (Semi-Gradient TD(Lambda))

```
Q-Table in the 100th Episode:
Episode --- [50/100]
                     Reward ---- -12.99999999999999
                                                             [[[ 0.
                                                                          0.
                                                                                     0.
                                                                                                 0.
Episode --- [51/100]
                       Reward ---- -12.8999999999998
                                                             [ 0.
                                                                          0.
Episode --- [52/100]
                       Reward ---- 18.300000000000002
                                                              [ 0.
                                                                          0.
                                                                                                0.
                                                                                     0.
Episode --- [53/100]
                       Reward ---- -12,09999999999977
                                                              Γ0.
                                                                          0.
                                                                                     0.
                                                                                                0.
Episode --- [54/100]
                       Reward ---- -10.2000000000000031
                                                                          0.
                                                             [ 0.
                                                                                     0.
                                                                                                0.
                                                                                                          1
Episode --- [55/100]
                       Reward ---- -17.8
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
Episode --- [56/100]
                       Reward ---- -15.8999999999998
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                                                                                                          11
Episode --- [57/100]
                       Reward ---- -15.8000000000000042
Episode --- [58/100]
                       Reward ---- 15.3000000000000004
                                                             [[ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
Episode --- [59/100]
                                                             [ 0.
                       Reward ---- -19.200000000000014
                                                                          0.
                                                                                                0.
                                                                                     0.
Episode --- [60/100]
                                                              [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                       Reward ---- -10.89999999999977
                                                              Γ0.
                                                                                                0.
                                                                          0.
                                                                                     0.
Episode --- [61/100]
                       [ 0.
                                                                          0.
Episode --- [62/100]
                       Reward ---- -6.399999999999755
                                                                                     0.
                                                                                                0.
                                                                                     0.
                                                              [ 0.
                                                                          0.
                                                                                                0.
Episode --- [63/100]
                       Reward ---- -20.89999999999984
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                                                                                                          11
Episode --- [64/100]
                       Reward ---- -14.599999999999975
Episode --- [65/100]
                       [[ 0.
                                                                                     0.
                                                                          0.
                                                                                                0.
Episode --- [66/100]
                       Reward ---- -4.79999999999976
                                                                          0.
                                                             [ 0.
                                                                                     0.
                                                                                                0.
                                                                                                          1
Episode --- [67/100]
                       Reward ---- 10.300000000000027
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                                                                                                          1
Episode --- [68/100]
                       Reward ---- 2.5000000000000187
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
Episode --- [69/100]
                       Reward ---- -10.89999999999977
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
Episode --- [70/100]
                       Reward ---- -19.8000000000000004
                                                              Γ0.
                                                                          0.
                                                                                     0.
                                                                                                0.
Episode --- [71/100]
                       Reward ---- -22.100000000000001
                                                                                     0.
                                                             [ 0.
                                                                          0.
                                                                                                0.
                                                                                                          11
Episode --- [72/100]
                       Reward ---- 8.0000000000000023
Episode --- [73/100]
                       Reward ---- 8.200000000000028
                                                             [[ 0.
                                                                         -0.07648783 0.
                                                                                                -0.01323737]
Episode --- [74/100]
                       Reward ---- -19.300000000000001
                                                                                                0.
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                          1
                                                                                     0.
Episode --- [75/100]
                       Reward ---- -21.5
                                                              [ 0.
                                                                          0.
                                                                                                0.
                                                             [ 0.
                                                                          0.
                                                                                                0.
Episode --- [76/100]
                       Reward ---- -16.29999999999976
                                                                                     0.
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                                                                                                          ]
Episode --- [77/100]
                       Reward ---- -18.50000000000000004
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
Episode --- [78/100]
                       Reward ---- 9.4000000000000022
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
Episode --- [79/100]
                       Reward ---- -18.99999999999996
Episode --- [80/100]
                       Reward ---- -13,099999999999973
                                                             [[-0.04232098 0.
                                                                                    -0.03281617 -0.104069971
Episode --- [81/100]
                       Reward ---- -25.100000000000003
                                                              [-0.04631232 -0.15434664 -0.07426049 -0.04351224]
Episode --- [82/100]
                       Reward ---- -11.69999999999998
                                                                          0.
                                                              Γ0.
                                                                                     0.
                                                                                                0.
Episode --- [83/100]
                       Reward ---- -18.400000000000001
                                                             [ 0.
                                                                          a.
                                                                                     0.
                                                                                                0.
Episode --- [84/100]
                       Reward ---- -27.300000000000005
                                                                                     0.
                                                              [ 0.
                                                                          0.
                                                                                                0.
Episode --- [85/100]
                       Reward ---- -17.59999999999998
                                                                                     0.
                                                             [ 0.
                                                                          0.
                                                                                                0.
Episode --- [86/100]
                       Reward ---- -14.299999999999999
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                                                                                                          11
Episode --- [87/100]
                       Reward ---- -22,3000000000000047
Episode --- [88/100]
                       Reward ---- -21.0000000000000036
                                                             [[ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                                                              [-0.02259149 -0.03279831 -0.01135903 -0.27378823]
Episode --- [89/100]
                       Reward ---- -30.700000000000056
Episode --- [90/100]
                       Reward ---- -12.69999999999997
                                                              [-0.09638018 -0.60425686  0.00279311 -0.04032602]
                                                             [ 0.
Episode --- [91/100]
                       Reward ---- -7.89999999999955
                                                                         0.
                                                                                    0.
                                                                                                0.
                                                              [-0.03387165 -0.31171903 -0.08025988 -0.01443011]
Episode --- [92/100]
                       Reward ---- -14.09999999999966
                                                             [ 0. -0.00886022 -0.01772045 0.
Episode --- [93/100]
                       Reward ---- -12.39999999999983
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                                                                                                          11
Episode --- [94/100]
                       Reward ---- -11,799999999999983
Episode --- [95/100]
                       Reward ---- 23.39999999999963
                                                             [[ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
Episode --- [96/100]
                       Reward ---- 2.1000000000000016
                                                             [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                     Reward ---- -11.800000000000005
Episode --- [97/100]
                                                              [ 0.00978951 -0.15654161 -0.12990104 -0.83839656]
Episode --- [98/100] | Reward ---- 50.7999999999999
                                                              [-0.06156678 -0.08406764 -0.41077049 -0.11807476]
Episode --- [99/100] | Reward ---- -18.0
                                                              [-0.08995889 -0.0097468 -0.56850924 -0.09019683]
Episode --- [100/100] | Reward ---- -22.900000000000023
                                                                          0.
                                                              [ 0.
                                                                                     0.
                                                                                                0.
Average Reward after 100 Episodes: -6.69299999999999
                                                              [ 0.
                                                                          0.
                                                                                     0.
                                                                                                0.
                                                                                                          111
```

# (Semi-Gradient SARSA(0) vs Semi-Gradient TD(Lambda))



Our final results apparently show for now that the Semi-gradient TD(Lambda) outperforms its SARSA (0) counterpart. We can also see that the trend of the TD(Lambda) is more diverse compared to the SARSA (0) trend. The rewards in the episodes in the above results show positive values in rewards after some of the episodes. They also show that with the element of eligibility traces, we are capable of making the agent learn better about the model.

# References

- https://www.gymlibrary.dev/environments/classic control/
- <a href="https://www.gymlibrary.dev/environments/classic control/pendulum/">https://www.gymlibrary.dev/environments/classic control/pendulum/</a>
- https://numpy.org/doc/stable/reference/
- https://www.learndatasci.com/tutorials/reinforcement-q-learning-scratch-python-openai-gym/
- Sutton, R. S., & Barto, A. G. (2018). Reinforcement learning: An introduction. MIT Press. Semi-Gradient SARSA:
- https://web.stanford.edu/class/psych209/Readings/SuttonBartoIPRLBook2ndEd.pdf (p. 152-154)
- Class Slides (Week 7, Week07\_01\_Function\_Approximation1, Slides 9,14)

#### Task 7.1D: Function approximation implementation

Objective: To implement Task 1.1P with the following methods:

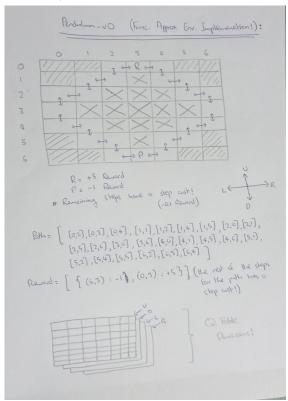
#Loading all of our libraries...
import numpy as np
import matplotlib.pyplot as plt
# import gym
import sys

drive.mount('/content/drive')
sys.path.insert(0,'/content/drive/MyDrive/Colab Notebooks/')

#Importing our GridWorld Module after connection.
from GN import Grid, print\_values, print\_policy

### Creating our Environment

```
MALL the Constants...
ALL_POSSIBLE_ACTIONS = ('U', 'D', 'L', '8')
OLD GAPWA = 0.9
ALPHA = 0.1
eps = 0.1
```



```
pendulue - Grid(7, 7, (6, 3))

stop.cost - 0.1.

Bolizionary of the rewards assigned at every step of the path...

(0, 1): 5, (0, 2): step.cost, (1, 2): step.cost, (1, 2): step.cost, (1, 2): step.cost, (1, 4): step.cost, (1, 4): step.cost, (1, 5): step.cost, (2, 5): step.cost, (3, 5): step.cost, (4, 5): step.cost, (4, 6): step.cost, (5, 6): step.cost, (6, 6): step.cost, (
                   pendulum = Grid(7, 7, (6, 3))
step_cost = -0.1
```

```
----Rewards per state in the Environment
            0.00 |
0.00 |
-0.10 |
5.00 |
-0.10 |
0.00 |
            0.00 |
-0.10 |
-0.10 |
-0.10 |
-0.10 |
-0.10 |
-0.10 |
            -0.10 |
-0.10 |
0.00 |
0.00 |
0.00 |
-0.10 |
         -0.10 |
0.00 |
0.00 |
0.00 |
0.00 |
0.00 |
-0.10 |
            -0.10 |
-0.10 |
0.00 |
0.00 |
0.00 |
-0.10 |
            0.00 |
-0.10 |
-0.10 |
-0.10 |
-0.10 |
-0.10 |
-0.10 |
      #Enlisting all the possible of
         state = list(actions.keys())
possible_actions = list(actions.values())
      (6, 2) | ('0', '8')

(6, 3) | ('1', '8')

(6, 4) | ('1', '8')

(6, 4) | ('1', '8')

(7, 4) | ('1', '1')

(7, 4) | ('1', '1')

(7, 4) | ('1', '1')

(7, 4) | ('1', '1')

(7, 4) | ('1', '1')

(8, 4) | ('1', '8')

(8, 4) | ('1', '8')

(8, 4) | ('1', '8')

(8, 4) | ('1', '8')

(8, 4) | ('1', '8')

(8, 4) | ('1', '8')

(8, 4) | ('1', '8')

(8, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')

(9, 4) | ('1', '8')
         Semi-Gradient Sarsa(0)
   # #Function for getting the actions of our Optimal Policy...
   # def max.dict(d):
# def max.dict(d):
# max.by = None
# max.by = None
# max.by = None
# max.by = None
# for b, v in d.tten(f):
# for b, v in d.tten(f):
# max.by = None
# max.by = None
# cetter max.by, max.voi
      def option_greedy_action(trate, epsilon):
    #SEMICOUTION
    #If option_greedy_action(trate, epsilon):
    #If option_greedy_action(trate)    #If option_greedy_action(trate)
    #If option_greedy_action(trate(all_POSSBNE_ACTIONS)    ##If option_greedy_action(trate(all_possBNE_ACTIONS)    ##If option_greedy_action(trate(all_possBNE_ACTIONS)    ##If option_greedy_action(trate(all_possBNE_ACTIONS)    ##If option_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_action_greedy_
Function to return reward with self-step function(s,a):
s = r + products.seve(a)
i, j = s
if s in actions.seve(j):
i = a = v^{(i)}
i = 1 - v^{(i)}
i = r - v^{(i)}
i = v^{(i
      #Function to return reward with from a certain state with Grid Pr
                                       \begin{aligned} & \text{special case } L_s^{-r, \cdots, r} \\ & \text{subso} & \text{the sour}... \\ & \text{if } s = w^r. \end{aligned} 
                         else:
    r = 0
    sprint("\nOut of bounds. Move Undone...")
    return s, r
   print(next_5, r)
(5, 3) 0

Stantion for computing the gradient of the model.
def grad(0, state, action):
(1, c) = state
gradient = np.zeros_like(0)
gradient = 1
return gradient
```

For our Semi-Gradient SARSA(0), this is the psuedocode for us to implement:

num\_actions = len(ALL\_POSSIBLE\_ACTIONS)

# Number of Actions

# Q-table/weights Initialized

Total Q = np\_reros((7, 7, num\_actions))

eligibility\_trace = np\_zeros((7,7,4))

# Resetting Eligibility Trace

total\_reward = 0
# a = np.argmax(predict(state, weights))
for t in range(200):

```
Input:
                                                                    A differentiable state-action value function \hat{q} \colon \mathcal{S} \times \mathcal{A} \times \mathbb{R}^d \to \mathbb{R}
                                                                    A policy \pi if predicting or q_\pi if estimating (e.g. using \varepsilon-greedy)
                                        Algorithm Parameter
                                                                    Step size \alpha \in (0.1]
                                     Initialise: w \in \mathbb{R}^d \text{ arbitrarily e.g. } w = 0 Loop forever (for each episode): S, A \leftarrow \text{Initial state and action of episode (e.g. using } \varepsilon - greedy) Loop for each step of the episode until S \in S(\text{Terminal}): \text{Take action } A, \text{ observe } R, S' If S' \in S^{\text{terminal}} then: w = w + \alpha [R + \gamma \hat{q}(S, A, w)] \nabla \hat{q}(S, A, w), \text{ special case for terminal state can't include future state also:
                                        Initialise:
                                                                                                             else: Choose A' as a function of \hat{q}(S', w) (e.g. using \varepsilon = greedy) \mathbf{w} = \mathbf{w} + \alpha [R + \gamma \hat{q}(S', A', \mathbf{w}) - \hat{q}(S, A, \mathbf{w})] \nabla \hat{q}(S, A, \mathbf{w})S + S'A + A'
                                      semi_gradient_sarsa(num_episodes, alpha, gamma, epsilon):
total_reward_per_episode = []
average_reward_per_episode = []
                                      for i in range(num_episodes):
                                                action = epsilon_greedy_action(state, epsilon)
for t in range(200):
                                                            # Getting next state and reward...
next_state, reward = step_function(state, action)
                                                           #Getting dimensions of the current and next state in order to update the Q-Table. ci, cj = state nl, nj = next_state
                                                            #Get the next action...
next_action = epsilon_greedy_action(next_state, epsilon)
                                                            #Mapping the current and next action.

a = action_map(action)

next_a = action_map(next_action)
                                                            #Update the Q-Table...

td_err = reward + gamma * Q[ni][nj][next_a] - Q[ci][cj][a]
Q[ci][cj][a] += alpha * td_err * grad(Q[ci][cj][a], state, a)
                                                            #Creating the total sum of the reward...
total_reward += reward
                                                            #Assign the new state and action and repeat.
state = next_state
action = next_action
                                                  average_reward_per_episode.append(total_reward/200)
total_reward_per_episode.append(total_reward)
print("Episode --- {{}}".format(i + 1, total_reward)
                                        return total_reward_per_episode, average_reward_per_episode, Total_Q
                          Semi-Gradient TD(\lambda)
   In [7]: weights = np.zeros((7, 7, 4)) # Q-table/weights Initialized
weights[3,2,:]
                         array([0., 0., 0., 0.])
  In [8]: # Function for predicting the weights...
def predict(state, weights):
    i, j = state
    return np.dot(weights[i,j,:], np.ones(4))
                               next_s = (i,j)
if next_s in actions.keys():
r = rewards.get(next_s, 0)
# print(next_s, "----",r)
return next_s, r
                                     else:

r = 0

#print(next_s,"----",r)
                                        else: r = 0 ** **print("\nOut of bounds. Move Undone...") return s, r
                         #Running a small test for the function next_S, r = step\_function((0,2),3) print(next_S, r)
                             (0, 3) 5
                                      Input: The policy \pi to be evaluate A differentiable function \theta\colon \mathcal{S}\times\mathbb{R}^d\to\mathbb{R} Algorithm Parameter: Step size a\in (0,1] Trace decay rate \lambda\in [0,1]
                                      we find a point of the second second
                                                                   Reset z = 0
                                                                   Neset \mathbf{z} = \mathbf{0}

Loop for each step of the episode until S \in S(\text{Terminal}):

Choose A \sim \pi(\cdot \mid S)

Take action A, observe R, S'

\mathbf{z} \leftarrow \gamma 2 \mathbf{z} + 7 \theta(S, \mathbf{w})

\delta \leftarrow R + \gamma \theta(S', \mathbf{w}) - \theta(S, \mathbf{w})

\mathbf{w} = \mathbf{w} + \alpha \delta \mathbf{z}

S \leftarrow S'
for i in range(num_episodes):
#pendulum.set_state(s) / state = env.reset()
state = (6,3) #Starting point of the Agent in the Envir
```

```
#Taking a Random Action... 
 a = np.random.choice(\{\theta,1,2,3\}) # To kick-start the algorithm
        #Getting dimensions of the current and next state in order to update the ci, cj = state
# ni, nj = next state
        #Get the next action...
next_a = predict(next_state, weights)
       #Computing TD Error (delta)...
delta = reward + gamma * predict(next_state, weights) - predict(state, weights)
        #Creating the total sum of the reward.
total_reward += reward
       #Assign the new state and action and repeat
state = next_state
a = next_a
   return total_reward_per_episode, average_reward_per_episode, Total_Q
```

#### Comparison of Results

#### SARSA(0) Results

```
trpe, sarsa_arpe, Total_Q = semi_gradient_sarsa(num_episodes, ALPHA, GAMMA, eps)
print("Average Reward after 100 Episodes: ",np.mean(trpe))
```

In [32]: print("Q-Table in the 100th Episode: \n", Total\_Q)

### TD(Lambda) Results

-Table in the				
[[[ 0.	0.	0.	0.	]
[ 0.	0.	0.	0.	]
[ 0.	0.	0.	0.	]
[ 0.	Θ.	0.	0.	]
[ 0.	0.	0.	0.	]
[ 0.	0.	0.	0.	]
[ 0.	θ.	0.	θ.	]]
[[ 0.	θ.	θ.	0.	1
	0.	0.	0.	1
[ 0.	0.	0.	0.	1
[ 0.	0.	0.	0.	1
0.	0.	0.	0.	1
[ 0.	0.	0.	0.	1
[ 0.	0.	0.	0.	'n
[ 0.	0.	0.	٥.	11
[[ 0.	0.	θ.	Θ.	1
[ 0.	θ.	θ.	θ.	]
[ 0.	θ.	θ.	θ.	]
[ 0.	θ.	θ.	θ.	]
[ 0.	θ.	θ.	θ.	j
[ 0.	θ.	θ.	θ.	]
[ 0.	0.	0.	0.	]]
[[ 0. +0.07648783 0. +0.01323737]				
[[ 0.				
[ 0.	θ.	0.	0.	]
[ 0.	θ.	0.	θ.	]
[ 0.	0.	0.	0.	]
[ 0.	0.	0.	0.	]
[ 0.	0.	0.	0.	]]
[[-0.04232098 00.03281617 -0.10406997]				
			-0.04351224]	
[ 0.	0.	Θ.	θ.	í
[ 0.	θ.	Θ.	θ.	í
0.	θ.	0.	0.	í
0.	θ.	0.	0.	i
0.	θ.	0.	0.	11
[[ 0.	0.	0.	θ.	]
[-0.02259149				
[-0.09638018				2]
[ 0.	0.	0.	0.	]
[-0.03387165				
[ 0.		-0.01772045		]
[ 0.	θ.	0.	0.	]]
[[ 0.	θ.	θ.	θ.	1
[0.	0.	0.	0.	í
0.00978951				61
[-0.06156678				
[-0.08995889		-0.56850924		
0.	0.	0.	0.	i
[ 0.	0.	0.	0.	in

### Semi-Gradient SARSA(0) vs Semi-Gradient TD(Lambda)

```
In (3): #Flotting the overage reperts per options...

x = [x for x is range(180)]

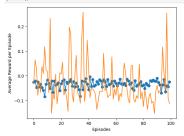
y1 = strat_upes

pl.eq.(x) = shortband for "per current exis"

pl.eq.(x) = shortband for "per current exis"

pl.eq.(x) = shortband for "per current exis"

pl.eq.(x) = pl.eq.(x
```



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