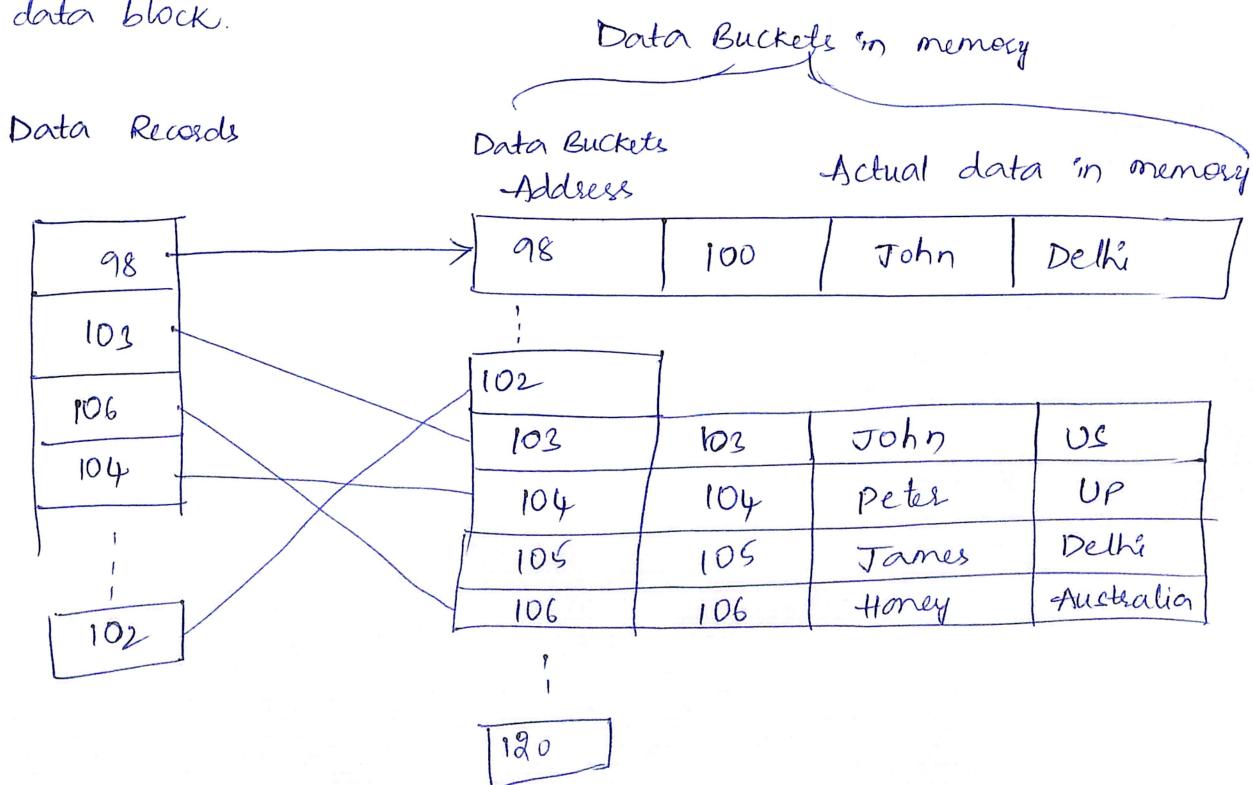


## UNIT-IV

1

- \* Static
- \* Hash

- In a huge DB structure, it is not so efficient to search all the index values & reach the desired data. Hashing technique is used to calculate the direct location of data record on the disk without using index structures.
  - Data is stored at the data blocks whose address is generated by using the hashing function. The memory location where these records are stored is known as data blocks.
  - A hash function can choose any of the column value to generate the address.
  - Hash function uses a primary key to generate the address of data block.
  - " " is a simple mathematical fn -> any complex mathematical fn.
  - we can consider PK itself as the address of the data block.
  - That means each row whose address will be the same as a PK stored in the data block.



Here, block address is same as  $\text{fK}$  value. This hash function can also be

a simple mathematical fn like exponential, mod, cos, sin, ...

- Suppose we have mod(5) hash fn to determine address of the data block.

It applies mod(5) hash fn on PK & generates 3, 3, 1, 4, 2, ...

records are stored in those data block addresses.

Eg:

Data records

98
104
106
:
102

Data Bucket address

1	106	James	Delhi
2	102	Jenny	US
3	98	John	UK
4	104	Honey	Australia
5			
6			

Data Buckets in memory

Actual data in memory

103	Albert	UK
-----	--------	----

## \* Hashing Types: (i) Static Hashing      (ii) Dynamic Hashing

- **Bucket**: A hash file stores data in bucket format. Bucket is considered as a unit of storage. A bucket typically stores one complete disk block, which in turn can store one or more records.

### - **Hash Function**:

" " h, is a mapping fn that maps all the set of search keys K to the address where actual records are placed. It is a fn from search keys to bucket addresses.

### i) Static Hashing:

In " ", the resultant data bucket address will always be the same. That means, for example if we generate an address for Emp\_id = 103 using hash fn mod(5) then it will give the bucket address as 3 always. Here, no change in the bucket address.

- In static hashing, the no of data buckets in memory remains constant throughout.

(7)

### Operations:

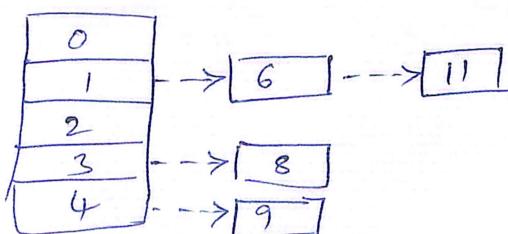
- Searching:** When a record needs to be searched, then the same hash fn retrieves the address of the bucket where the data is stored.
- Insert:** When a new record is inserted into the table, then we will generate an address for a new record based on the hash key & record is stored in that location.
- Delete:** We will first fetch the record which is supposed to be deleted. Then we will delete the records for that address in memory.
- Update:** To update a record, we will first search it using hash function, then data record will be updated.

- If we want to insert some new record into the file but the address of a data bucket generated by the hash fn is not empty or data already exists in that address. This situation is known as bucket overflow. To overcome bucket overflow, we have linear probing, overflow chaining.
- Bucket overflow, we can also call it as collision.

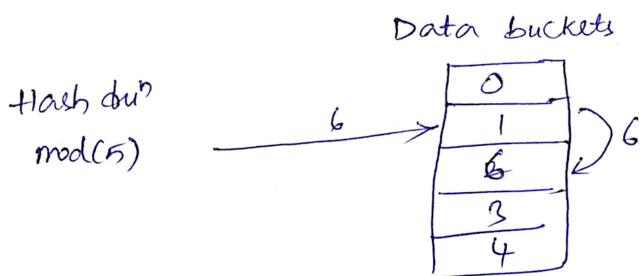
- **Overflow Chaining:** When buckets are full, a new bucket is allocated for the same hash result & is linked after the previous one. It is called closed hashing.

Data Buckets

Hash fn  
 $\text{mod}(5)$



Linear probing: when a hash fun generates an address at which data is already stored, the next free bucket is allocated to it. It is called as Open Hashing.



### (ii). Dynamic Hashing:

- To overcome the problems of static hashing like bucket overflow. we have dynamic hashing (or) Extensible hashing.
- In this method, data buckets grow or shrink as the records increases or decreases. It makes hashing dynamic ie., It allows insertion or deletion without resulting in poor performance.

### Searching:

i) calculate the hash address of the key

ii). Check how many bits are used in the directory & these bits are '1'.

iii). Take the least significant 'i' bits of the hash address. This gives index of the directory. directory.

iv). Using the index go to directory & find bucket address where the record might be.

### Insertion:

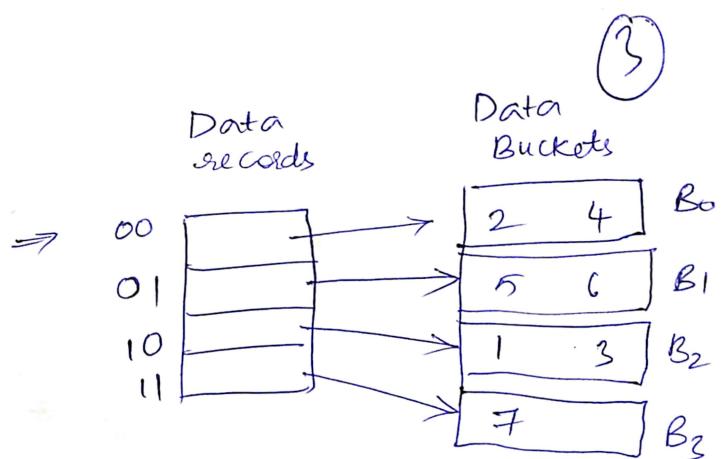
i). Follow same procedure for retrieval, ending up in some bucket.

ii). If there is still space in that bucket then place record in it.

iii). If bucket is full, then we will split the bucket & redistribute the records.

Eg.

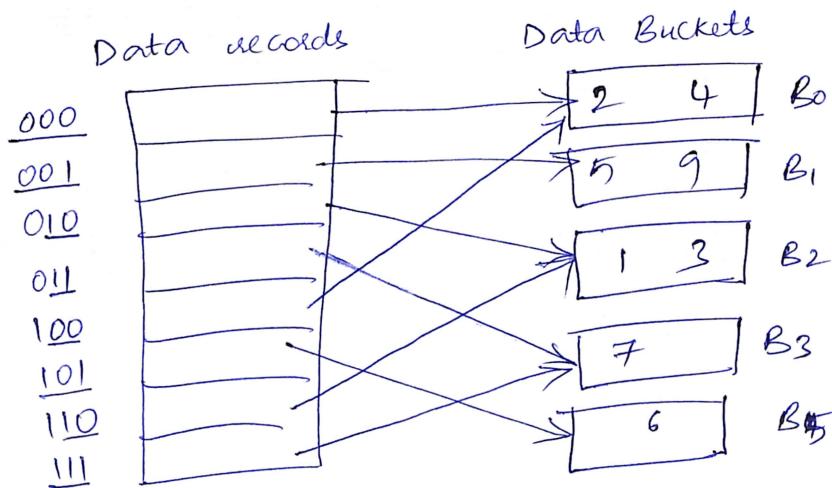
key	hash address
1	11010
2	00000
3	11110
4	00000
5	01001
6	10101
7	10111



Here, last two bits need to be considered

Suppose, if we want to insert 9 with hash address 10001

Here 9 must be stored in B<sub>1</sub> as it is ending with 01 But B<sub>1</sub> is full. So it will get split. But which element needs to be removed from B<sub>1</sub>. we need to consider last 3 digits.



### Advantages of dynamic hashing:

- performance doesn't decrease as the data grows in the system. It simply increases the size of memory to accommodate the data.
- Memory is well utilized as it grows & shrinks with the data.
- Good for dynamic DB.

### Disadvantages of dynamic hashing:

- If data size increases then bucket size also increased. These addresses of data will be maintained in the bucket address table. Because data ad. will keep on changing as bucket grow & shrink.
- Bucket overflow situation will also occur. But it takes little time to search than static.

(u)

## \* Transaction:

" is set of logically related operations. It contains a group of tasks. A transaction is an action or series of actions. It is performed by a single user to perform operations for accessing the contents of the database.

Eg: Suppose bank employee transfers 500/- from A's account to B's account.

A's account

B's account

Open\_Account(A)

Open\_Account(B)

old\_balance = A.balance

old\_balance = B.balance

New\_balance = old\_balance - 500

New\_balance = Old\_balance + 500

A.balance = New\_balance

B.balance = New\_balance

close\_Account(A)

close\_Account(B)

## Operations of Transaction:

① Read: used to read the value of X from DB & stores it in buffer in main memory.

② Write: used to write the value back to DB from buffer.

## \* ACID properties:

A = Atomicity — The entire transaction takes place at once or doesn't happen at all.  
 C = Consistency — DB must be consistent before & after transaction.  
 I = Isolation — Multiple transactions occur independently without interference.  
 D = Durability — changes of successful transaction occurs even if system failure occurs.

i). Atomicity: If any operation is performed on the data, either it should be performed or executed completely or should not be executed at all.

It involves the following two operations:

- Abort: If transaction aborts, changes made to DB are not visible.

- Commit: " " " Commit, changes made are visible.

Consider the following transaction T consisting of T<sub>1</sub> & T<sub>2</sub>, transferring 100/- from X to Y.

	T <sub>1</sub>	T <sub>2</sub>
Before	X : 500	Y : 200
	Read(X)	Read(Y)
	X := X - 100	Y := Y + 100
	Write(X)	Write(Y)
After	X : 400	Y : 300

Here, 2<sup>nd</sup> transaction fails after completion of T<sub>1</sub> (after write(X)) but before completion of T<sub>2</sub> (before write(Y)), then amount has been deducted from X but not added to Y. This results in an inconsistent DB. The transaction must be executed in its entirety in order to ensure the correctness of DB.

### (ii). Consistency:

Integrity constraints must be maintained so that the DB is consistent before & after transaction. It refers to the correctness of DB.

In the above example, total amount before and after transaction must be maintained.

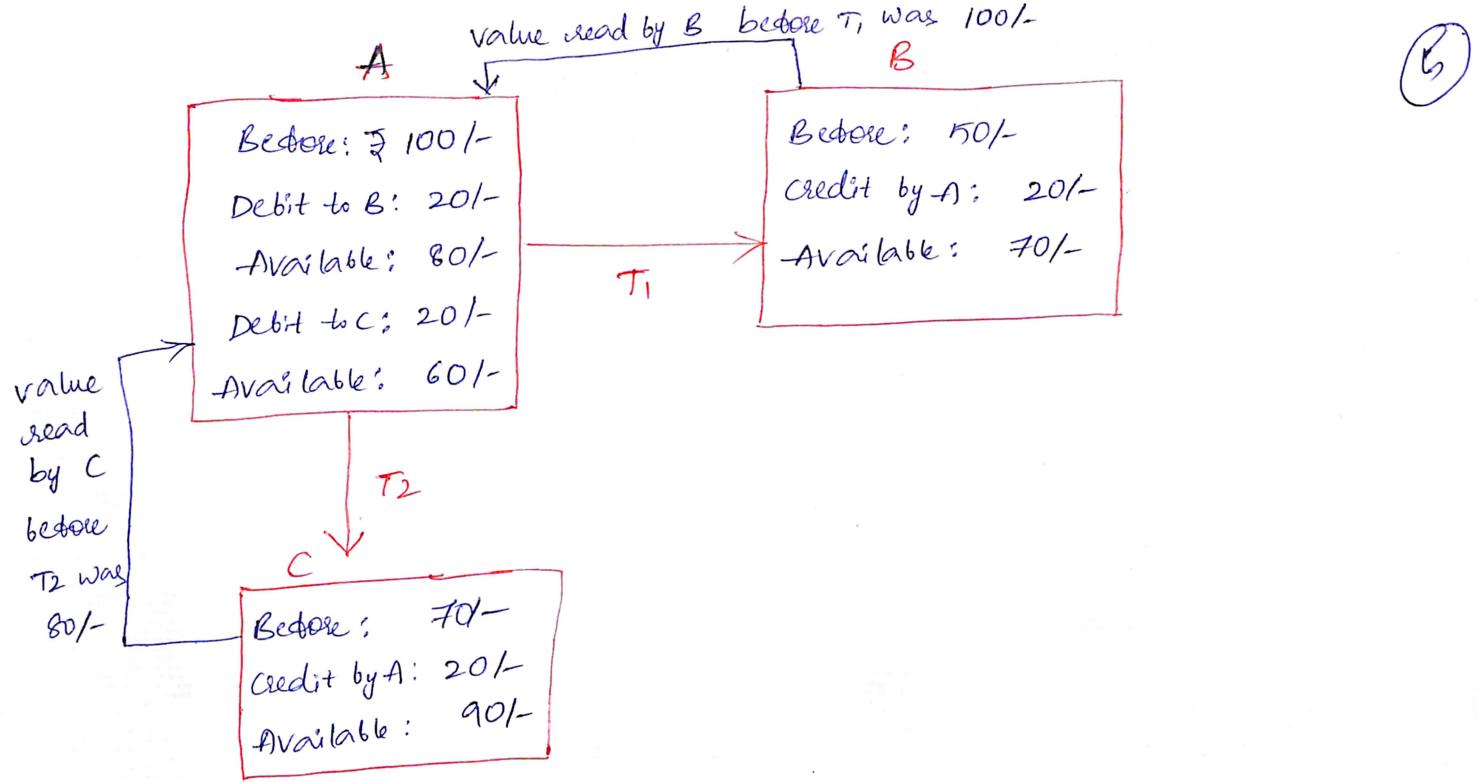
$$\text{Before } T_1 + T_2 = 500 + 200 = 700$$

$$\text{After} : 400 + 300 = 700$$

So, DB is consistent. Inconsistency occurs when either of transaction fails.

### (iii). Isolation:

" is a property of DB where no data should affect the other one & may occur concurrently. i.e., multiple transactions can occur concurrently without leading to the inconsistency of DB. Transactions occur independently without interference.



Here,  $T_1$  &  $T_2$  are not affecting each other. So, transaction is in isolation.

#### (iv) Durability:

It ensures that once transaction has completed execution, the modifications or updates to DB are stored in & written to disk & they persist even if a system failure occurs. These & updates become permanent & stored in non volatile memory.

If anything lost, it will be rectified by recovery manager.

Atomicity - Transaction manager

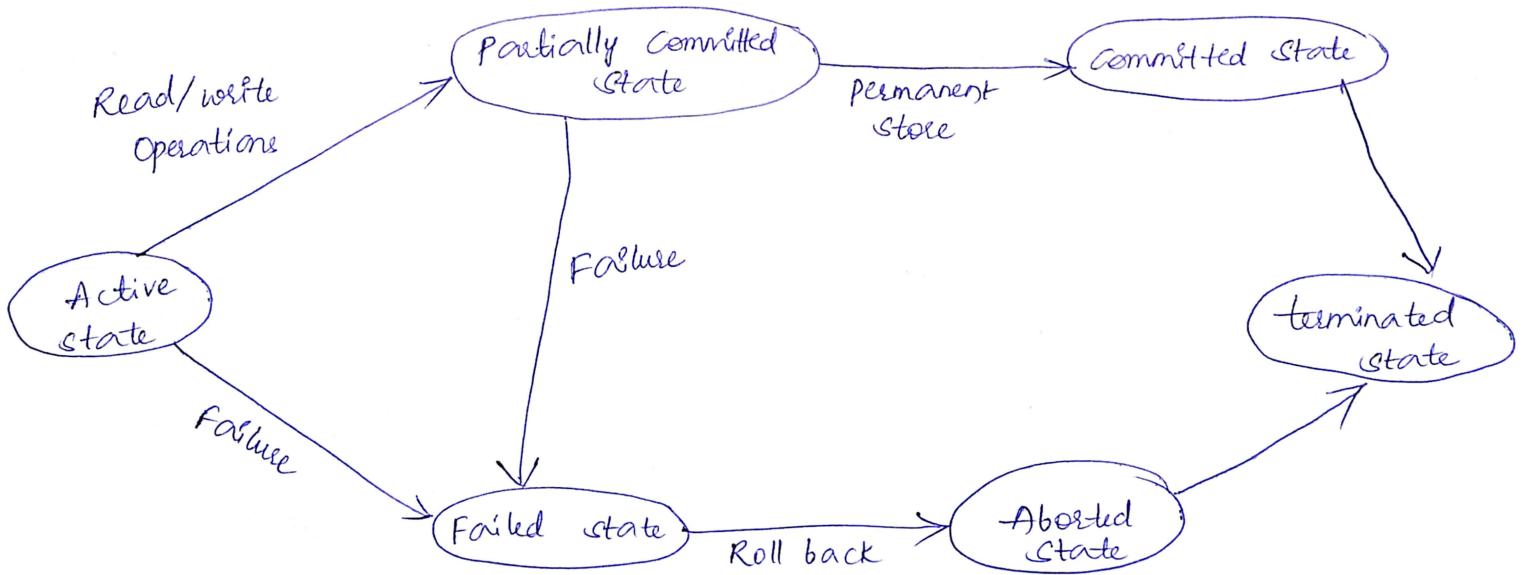
Consistency - Application programmes

Isolation - Concurrency control manager

Durability - Recovery manager.

#### \* States of transaction:

States through which a transaction goes during its lifetime. State will tell the current state of transaction.



### i). Active state:

- First state of every transaction. In this state, transaction is being executed.
- If all read & write operations are performed without any error then it goes to the "partially committed state". If transaction fails, it goes to the "aborted state".

### ii). partially Committed state:

- After completion of all read & write operation the changes are made in main memory or local buffer. If changes are made permanent on the DB then the state will change to "committed state" & in case of failure it will go to aborted state.
- Final statement of transaction is executed.

### iii). Committed state:

- It is the state when the changes are made permanent on the DB & the transaction is complete & therefore terminated in the "terminated state".

### iv). Failed state:

- When any instruction of transaction fails, it goes to the 'aborted state'.
- If failure occurs in making a permanent change of data on DB.

### v). Aborted state: terminated:

- If there isn't any rollback or transaction comes from "committed state"

then the system is consistent & ready for new transaction & old transaction is terminated. When transaction finished, terminated. (6)

#### (vi) terminated state: Aborted state:

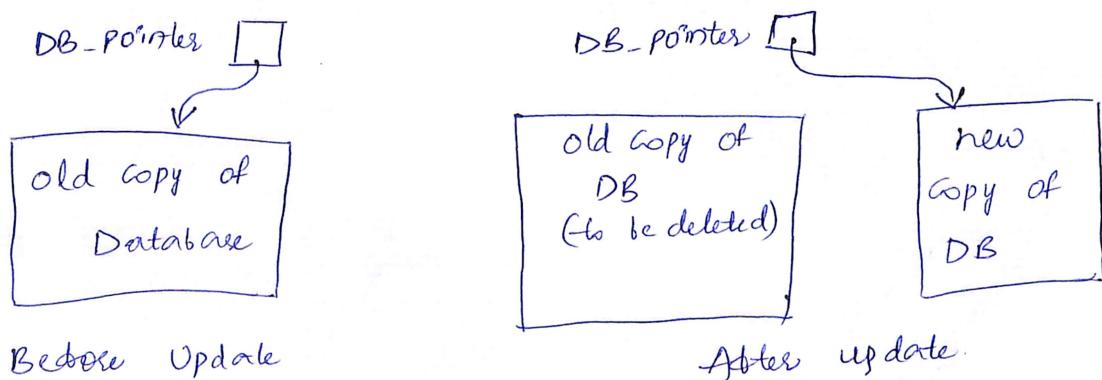
- When changes made by transaction are cancelled.
- After having any type of failure the transaction goes from "failed state" to "aborted state". Since in previous states, the changes are only made to local buffers or main memory & hence these changes are deleted or rolled back.

#### \* Implementation of Atomicity & Durability:

- Durability & Atomicity can be ensured by using recovery manager
- we can achieve atomicity using shadow copying technique.
  - " " " Durability using logs.

#### (i) Shadow copying technique:

- maintaining a shadow copy of original DB & reflecting all changes to the DB as a result of any transaction after committing transaction.



- DB is simply a file on disk. A pointer called DB-pointer is maintained on disk. It points to the current copy of the DB.
- In shadow copy technique, a transaction that wants to update the DB - first creates complete copy of DB. All updates done on the new

DB copy, leaving the original copy, the shadow copy. If at any point the transaction has to be aborted, the system detects the new copy. The old copy of DB has not been affected.

- If transaction completed, it is committed as follows

i). OS asks to make sure that all pages of new copy of DB have been written out to disk.

ii). After that, the DB system updates the pointer to point to the new copy of DB. The new copy then becomes the current copy of DB. The old copy deleted.

- If transaction failure occurs at any time before db-pointer is updated, old contents are not affected. We can abort the transaction by deleting new copy of DB.

- If system fails at any time before updated db-pointer written to disk. Then, when system restarts, it will read db-pointer & will see original contents of DB. Once file is written to disk, its contents will not be damaged even if there is system failure.

### iii. Logs:

- logs keep track of actions carried out by transactions which can be used for the recovery of DB in case of failure. Log files will be stored on stable storage devices.

- When transaction begins its execution it is recorded in log file  $\langle T_n, start \rangle$

- When " performs an operation. It is recorded in log as follows

$\langle T_n, X, V_1, V_2 \rangle$

- When transaction finishes its execution  $\langle T_n, commit \rangle$

## \* Concurrent Executions:

(7)

- Executing a set of transactions simultaneously in a preemptive & time shared method.
- Concurrency Control is the management procedure that is required for controlling concurrent execution of the operations that take place on a DB.
- Concurrency Control deals with interleaved execution of more than one transaction.
- In a multi user system, multiple users can access & use the same DB at one time, known as concurrent execution of the DB. It means that the same DB is executed simultaneously on a multi user system by different users.
- While working on the DB transactions, there occurs the requirement of using the DB by multiple users for performing different operations.
- Simultaneous execution should be in interleaved manner & no operation should affect the other executing operations, thus maintaining consistency of the DB.

## problems with concurrent execution:

### i) Lost update problems (W-W conflict):

This problem occurs when two different DB transactions perform the read/write operations on the same DB items in an interleaved manner that makes the values of the items incorrect hence making the DB inconsistent.

Ex: Two transactions  $T_x$  &  $T_y$  are performed on the same account A where balance of A is 300/-

Time	<u><math>T_x</math></u>	<u><math>T_y</math></u>
$t_1$	Read(A)	-
$t_2$	$A = A - 50$	Read(A)
$t_3$	-	$A = A + 100$
$t_4$	-	-
$t_5$	-	-
$t_6$	Write(A)	-
$t_7$	-	Write(A)

- At time  $t_1$ ,  $T_x$  reads the value of account A i.e., 300/-
- $t_2$ ,  $T_x$  deducts 50/- from A i.e., 250/- (not updated/ write)
- $t_3$ ,  $T_y$  reads value of A i.e., 300/- because  $T_x$  didn't update value yet.
- $t_4$ ,  $T_y$  adds 100/- to A i.e., 400/- (not updated/write)
- $t_5$ ,  $T_x$  writes value of A i.e., 250/-
- $t_7$ ,  $T_y$  writes value of A i.e., 400/- . Here, the value written by  $T_x$  is lost i.e., 250/- lost. Hence data becomes incorrect & DB inconsistent

### Dirty Read problems (W-R Conflict):

" " occurs when one transaction updates an item of the DB & somehow the transaction fails & before the data gets rollback, the updated DB item is accessed by another transaction. This comes the Read-write conflict b/w both transactions.

e.g.: two transactions  $T_x$  and  $T_y$  performing read/write operations on account A & balance of A is 300/-

<u>time</u>	<u><math>T_x</math></u>	<u><math>T_y</math></u>
$t_1$	Read(A)	-
$t_2$	$A = A + 50$	-
$t_3$	Write(A)	-
$t_4$	-	Read(A)
$t_5$	Server Down Rollback	-

- At time  $t_1$ ,  $T_x$  reads value of account A i.e., 300/-
- " "  $t_2$ ,  $T_x$  adds 50/- to A i.e., 350/- (not updated)
- $t_3$ , updated in A i.e., 350/-
- $t_4$ ,  $T_y$  reads account A i.e., 350/-
- $t_5$ ,  $T_x$  rollbacks due to server problem & value changes back to 300/- (initial value)
- But value of account A remains 350/- as  $T_y$  committed

## Unrepeatable Read problem (W-R Conflict):

(8)

Also called as Inconsistent Retrievals problem that occurs when in a transaction, two different values are read for the same DB item.

Eg:

<u>Time</u>	<u>tx</u>	<u>ty</u>	Initial A = 300/-
$t_1$	Read(A)	-	
$t_2$	-	Read(A)	
$t_3$	-	$A = A + 100$	
$t_4$	-	Write(A)	
$t_5$	Read(A)	-	

- At time  $t_1$ , tx reads value from account A i.e., 300/-

-  $t_2$ , ty reads A ie, 300/-

-  $t_3$ , ty adds 100/- to A so 400/- (not updated)

-  $t_4$ , ty updated value of A, 400/-

-  $t_5$ , tx reads value of A, 400/-

- that means, In tx, it reads two different values of account of A ie, 300/- initially after it reads 400/. this unrepeatable read problem.

## \* Serializability:

A transaction is said to be serializable if it is equivalent to serial schedule. It leaves database in a consistent state.

- A serial schedule is always serializable because, a transaction starts when the other transaction finished execution.
- Two types of serializability (i) Conflict (ii) View.

## (i) Conflict Serializability Schedule:

- A schedule is called " " if after swapping of non conflicting operations, it can transform into a serial schedule.

- The schedule will be a conflict serializable if it is conflict equivalent to a serial schedule.
- Two operations become conflicting if all conditions satisfy below:
  - Both belong to separate transactions
  - They have the same data item
  - They contain atleast one write operation.

Eg: Swapping is possible only if  $S_1 \& S_2$  are logically equal.

Schedule S<sub>1</sub>

T <sub>1</sub>	T <sub>2</sub>
Read(A)	Read(A)

Schedule S<sub>2</sub>

T <sub>1</sub>	T <sub>2</sub>
Read(A)	Read(A)

Here,  $S_1 = S_2$  means it is non-conflict.

Eg:

Schedule S<sub>1</sub>

T <sub>1</sub>	T <sub>2</sub>
Read(A)	write(A)

Schedule S<sub>2</sub>

T <sub>1</sub>	T <sub>2</sub>
Read(A)	write(A)

Here,  $S_1 \neq S_2$ . It is conflict

- In conflict equivalent, one can be transformed to another by swapping non conflicting operations

Two schedules are said to be conflict equivalent if and only if,

- They contain the same set of transaction
- If each pair of conflict operations are ordered in the same way.

Eg: Non serial Schedule

$T_1$	$T_2$
Read(A) write(A)	Read(A) write(A)
Read(B) write(B)	Read(B) write(B)

Serial Schedule

$T_1$	$T_2$
Read(A) write(A) Read(B) write(B)	Read(A) write(A) Read(B) write(B)

(9)

$S_2$  is serial schedule because all operations of  $T_1$  are performed before starting any operation of  $T_2$ .  $S_1$  can be transformed into a serial schedule by swapping non conflicting operations of  $S_1$ . After swapping of non conflict operations,  $S_1$  becomes

$T_1$	$T_2$
Read(A)	
write(A)	
Read(B)	
write(B)	

Read(A)
write(A)
Read(B)
write(B)

$S_1$  is conflict serializable.

(ii) View Serializability:

- If a schedule is view equivalent to a serial schedule,  $\Rightarrow$  view serializable
- If a schedule is conflict serializable, then it will be view serializable
- The view serializable which does not conflict serializable contains blind writes.

Two schedules  $S_1$  &  $S_2$  are said to be view equivalent if they satisfy following conditions.

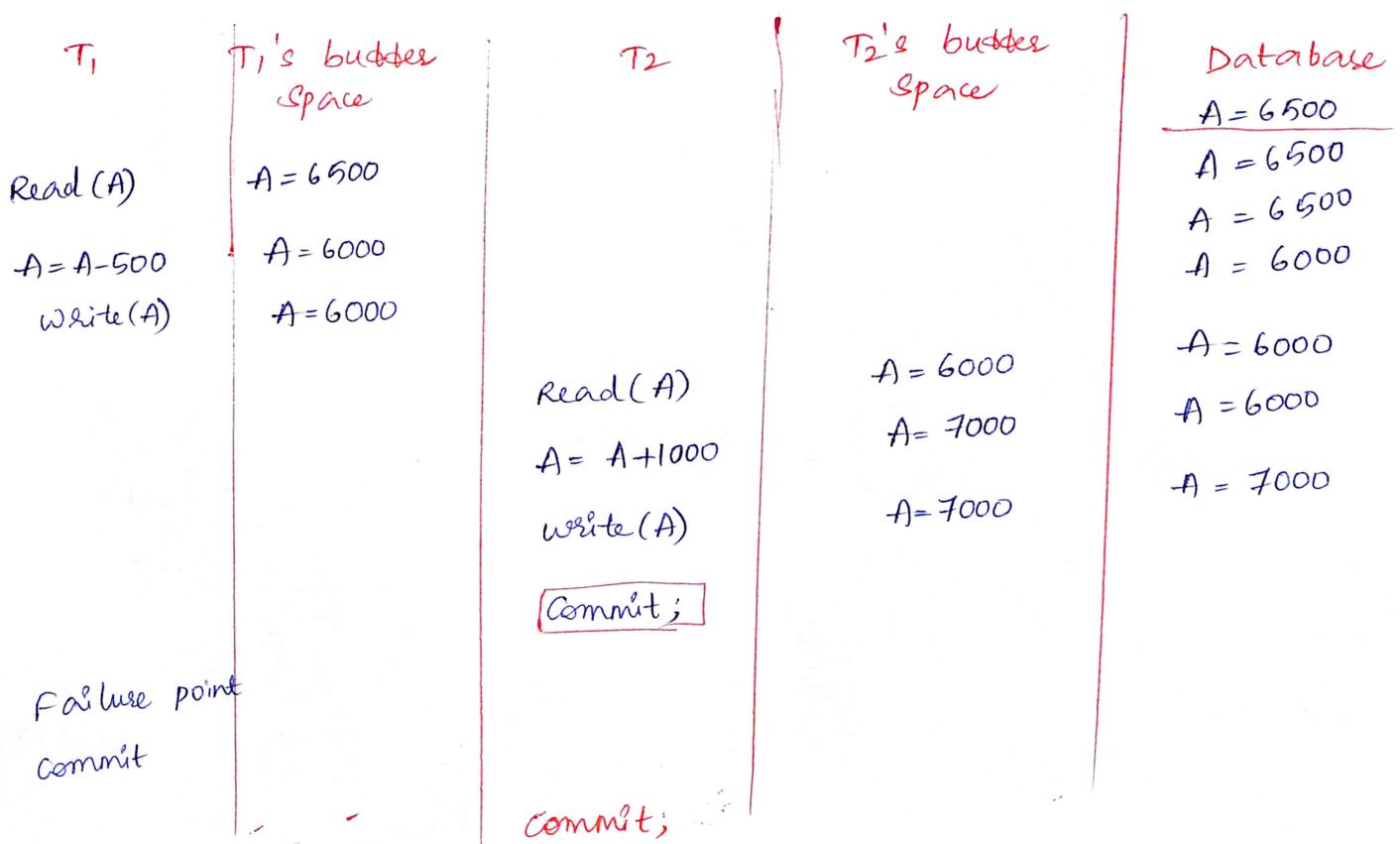
Initial Read:

- Initial read of both schedules must be the same.

Updated Read: In S1, if  $T_1$  is reading A which is updated by  $T_2$  then in S2 also,  $T_1$  should read A which is updated by  $T_2$ .

### \* Recoverability:

- Sometimes a transaction may not execute completely due to a software issue, system crash or hardware failure. In that case, the failed transaction has to be rollback. But some other transaction may also have used value produced by the failed transaction. So we have to rollback those transactions.



Here, we have two transactions.  $T_1$  reads & writes the value of A & that value is read & written by  $T_2$ .  $T_2$  commits. Due to failure, we have to rollback  $T_1$ .  $T_2$  also should rollback because it reads the value written by  $T_1$ , but  $T_2$  can't be rollback because it is already committed. This is irrecoverable schedule.

- If we have commit in  $T_2$ , after  $T_1$ 's commit then, we can roll back both  $T_1, T_2$  due to failure in  $T_1$ . It is recoverable with cascade rollback.
- Recoverable Cascading rollback: The schedule will be recoverable with Cascading rollback if  $T_j$  reads the updated value of  $T_i$ . Commit of  $T_j$  is delayed till Commit of  $T_i$ .

$T_1$	$T_1$ 's buffer space	$T_2$	$T_2$ 's buffer space	Database
Read(A)	$A = 6500$			$A = 6500$
$A = A - 500$	$A = 6000$			$A = 6500$
Write(A)	$A = 6000$			$A = 6000$
Commit;		Read(A); $A = A + 1000$ Write(A) Commit;	$A = 6000$ $A = 7000$ $A = 7000$	$A = 6000$ $A = 6000$ $A = 6000$ $A = 7000$

- $T_1$  reads & writes A & commits & that value is read & written by  $T_2$ . This is Cascadless recoverable schedule.

### \* Lock based protocol:

- Any transaction can't read or write data until it acquires an appropriate lock on it. There are 2 types of lock

#### (i) Shared lock:

- It is also known as Read only lock. In Shared lock, the data item can only read by the transaction.

- It can be shared b/w the transactions because when the transaction holds a lock, then it can't update the data on data item.

### (ii). Exclusive lock:

- The data item can be both reads as well as written by transaction.
- This lock is exclusive & in this lock, multiple transactions do not modify the same data simultaneously.

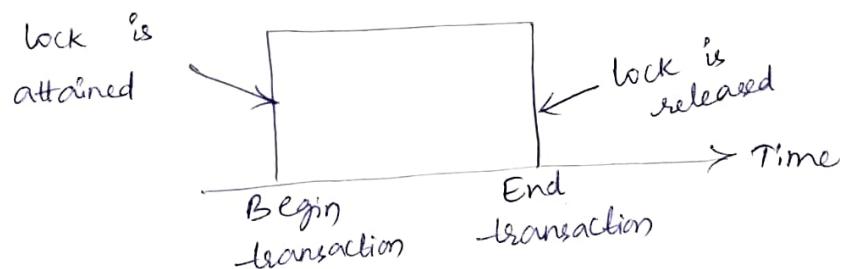
### types of lock protocols:

#### i). Simplistic lock protocol:

- It is the simplest way of locking the data while transaction.
- It allows all the transactions to get the lock on the data before insert or update or delete on it. It will unlock the data item after completing the transaction.

#### ii). pre-claiming lock protocol:

- Before initiating the transaction, it requests DBMS for the lock.
- If locks are granted then this protocol allows the transaction to begin. When the transaction is completed then it releases the lock.
- If all the locks are not granted then it allows the transaction to rolls back & wait until all locks are granted.



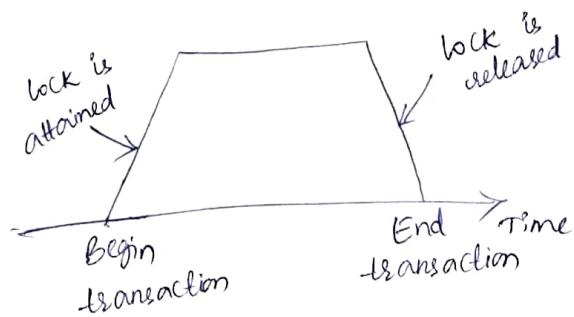
### (iii). Two-phase locking protocol:

(11)

- It divides the execution phase into 3 parts
- In first part, when the execution of the transaction starts, it seeks permission over the lock it requires.
- In second part, transaction acquires all the locks.
- In third part, transaction can't demand any new locks. It only releases the acquired locks.

#### Growing phase:

- In " ", a new lock on the data item may be acquired by the transaction.
- But none can be released.

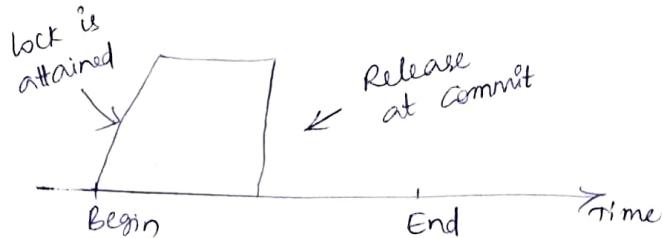


#### Chinking phase:

- existing lock held by the transaction will be released, but no new locks can be acquired.

### (iv). Strict two-phase locking protocol (Strict-2PL):

- In first phase, after acquiring all the locks, transaction continues to execute normally
- Strict 2PL doesn't release the lock after using it. So, it does not have chinking phase of lock release.
- Strict 2PL waits for the whole transaction to commit



## \* Time Stamp based protocols:

- " " " " is used to order the transactions based on (ascending) their timestamps.
  - priority of the older transaction is higher that's why it executes first.
  - To determine the timestamp of the transaction, it uses system time or logical counter.
  - $TS(T_i)$  denotes the timestamp of transaction  $T_i$ .
  - $R\_TS(x)$  denotes the read time stamp of data item  $x$ .
  - $W\_TS(x)$  denotes the write time stamp of data item  $x$ .
  - i). whenever  $T_i$  issues a read( $x$ ) operation:
    - If  $W\_TS(x) > TS(T_i)$  then the operation is rejected.
    - If  $W\_TS(x) \leq TS(T_i)$  " " " " executed.
    - Timestamps of all data items are updated.
  - ii). whenever  $T_i$  issues a write( $x$ ) operation:
    - If  $TS(T_i) < R\_TS(x)$  then the operation is rejected.
    - If  $TS(T_i) < W\_TS(x)$  " " " " &  $T_i$  is rolled back otherwise operation is executed, sets  $w\_TS(x)$  to  $TS(T_i)$ .

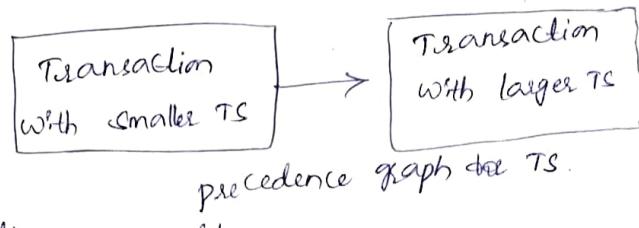
**Advantages**

  - i). It ensures serializability
  - ii). It ensures freedom from deadlock that means no transaction ever waits.

```

graph LR
    A[Transaction with smaller TS] --> B[Transaction with larger TS]
  
```

precedence graph due to TS.



## Advantages

- i). It ensures serializability

- iii. It ensures freedom from

- (ii). It ensures deadlock that means no transaction ever waits

## Disadvantage

- (ii). Schedule may not be recoverable & may not even be cascade-free.

- \* Validation based protocols: (2)
- " , also called as optimistic concurrency control technique.
  - The transaction is executed in following three phases.
    - Read phase:** The transaction  $T_i$  is read & executed. It is used to read the value of various data items & stores them in temporary local variables. It can perform all write operations on temporary variables without an update to the actual DB.
    - Validation phase:** The temporary variable value will be validated against the actual data to see if it violates the serializability.
    - Write phase:** If validation of the transaction is validated, then the temporary results are written to the DB or system otherwise the transaction is rolled back.
  - Each phase has the following different timestamps:
    - $\text{start}(T_i)$ : It contains the time when  $T_i$  started its execution.
    - $\text{validation}(T_i)$ : " " " ,  $T_i$  finishes its read phase & starts its validation phase.
    - $\text{finish}(T_i)$ : It contains the time when  $T_i$  finishes its write phase.
  - Validation phase will check the following:
    - $\text{Finish}(T_j) < \text{start}(T_i)$
    - $T_j$  finishes its execution means completes its write phase before  $T_i$  started its execution (read phase). Then the serializability maintained.
    - $T_i$  begins its write phase after  $T_j$  completes its write phase, & the read\_set of  $T_i$  should be disjoint with write\_set of  $T_j$ .
    - $T_j$  completes its read phase before  $T_i$  completes its read & read\_set & write\_set of  $T_i$  are disjoint with the write\_set of  $T_j$ .

### Advantages:

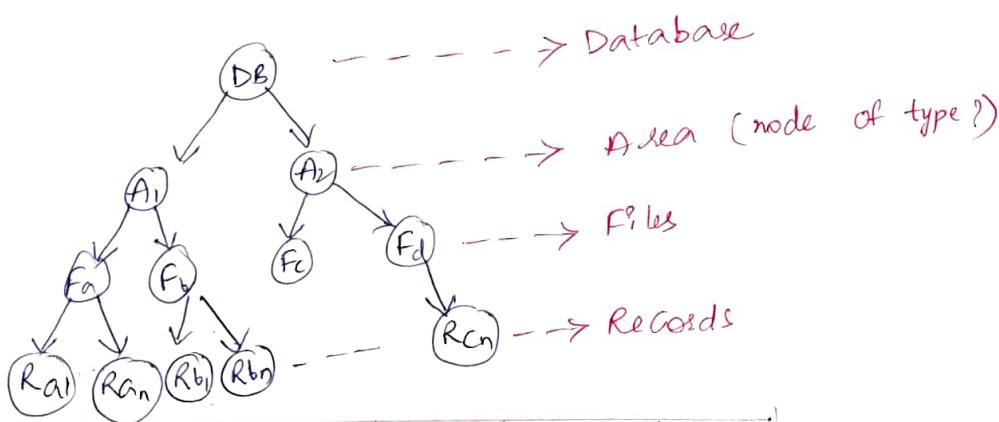
- Avoids cascading rollbacks
- Avoids deadlock

### Disadvantage:

- Starvation:  
↳ when a transaction has to wait for an indefinite period of time to acquire lock.

### \* Multiple granularity:

- Granularity is the size of data item allowed to lock.
- Multiple granularity is defined as hierarchically breaking up the DB into blocks which can be locked.
- It enhances concurrency & reduces lock overhead.
- It maintains the track of what to lock & how to lock.
- It makes easy to decide either to lock a data item or to unlock a data item. This type of hierarchy graphically represented as a tree.



	IS	IX	S	SIX	X
IS	✓	✓	✓	✓	✗
IX	✓	✓	✗	✗	✗
S	✓	✗	✓	✗	✗
SIX	✓	✗	✗	✗	✗
X	✗	✗	✗	✗	✗

IS - Intention Shared

IX - Intention Exclusive

S - Shared

SIX - Shared & Intention Exclusive

X - Exclusive

Intention shared (IS): It contains explicit locking at a lower level of tree but only with shared locks. (13)

Intention - Exclusive (IX): " at lower level with exclusive or shared locks.

Shared & Intention exclusive (SIX): Here, the mode is locked in shared mode. Some node is locked in exclusive mode by same transaction.

- Multiple granularity uses intention lock modes to ensure serializability. It requires that a transaction  $T_i$  that attempts to lock a node must follow these protocols:

- (i).  $T_i$  must follow lock compatibility matrix.
- (ii).  $T_i$  must lock the root first & it can lock any node.
- (iii).  $T_i$  can lock any node in S or IS only if  $T_i$  currently has the parent of the node locked in either IX or IS mode.
- (iv).  $T_i$  can lock a node in X, SIX or IX mode, if  $T_i$  currently has the parent of the node locked in either IX or SIX modes.
- (v).  $T_i$  can lock a node only if  $T_i$  has not previously unlocked any node.
- (vi).  $T_i$  can unlock a node only if  $T_i$  currently has none of the children of the node locked.

Eg:  $T_1$  transaction reads record R<sub>02</sub> in file F<sub>a</sub>. Then,  $T_2$  needs to lock DB, area A<sub>1</sub>, F<sub>a</sub> in 'IS' mode & finally lock R<sub>02</sub> in 'S' mode.