variable: $c: \{0, \cdots, M\}$
inputs: $up, down$: pure
output: $count: \{0, \cdots, M\}$