

**inputs:**  $up, down$ : pure  
**output:**  $count: \{0, \dots, M\}$

