Rate-Monotonic utilization bound

$$U = (2.5 / 5) + (4.5 / 15) + (3.5 / 20) = 0.975$$

$$Urm = 3 * (2^{(1/3)} - 1) = 0.799$$

- ∵ U > Urm
- ∴ System guaranteed not schedulable

Time demand analysis

Assuming T1 is the highest priority, then T2, then T3.

Time Demand for T1

- $W(1) = 2.5 + \Gamma(0) = 2.5$
- $W(2) = 2.5 + \Gamma(0) = 2.5$
- $W(3) = 2.5 + \Gamma(0) = 2.5$
- $W(4) = 2.5 + \Gamma(0) = 2.5$
- $W(5) = 2.5 + \Gamma(0) = 2.5$
- W(5) < D = 2.5 < 5
- .. T1 is schedulable.

Time Demand for T2

- $W(1) = 4.5 + \Gamma(1/5) * 2.51 = 7$
- $W(2) = 4.5 + \lceil (2/5) * 2.5 \rceil = 7$
- $W(3) = 4.5 + \Gamma(3/5) * 2.51 = 7$
- $W(4) = 4.5 + \Gamma(4/5) * 2.57 = 7$
- $W(5) = 4.5 + \lceil (5/5) * 2.5 \rceil = 7$
- $W(6) = 4.5 + \Gamma(6/5) * 2.51 = 9.5$
- $W(7) = 4.5 + \Gamma(8/5) * 2.57 = 9.5$
- $W(8) = 4.5 + \Gamma(7/5) * 2.57 = 9.5$
- $W(9) = 4.5 + \Gamma(9/5) * 2.57 = 9.5$
- $W(10) = 4.5 + \Gamma(10/5) * 2.51 = 9.5$
- $W(11) = 4.5 + \Gamma(11/5) * 2.57 = 12$
- $W(12) = 4.5 + \Gamma(12/5) * 2.57 = 12$
- $W(13) = 4.5 + \Gamma(13/5) * 2.57 = 12$
- $W(14) = 4.5 + \Gamma(14/5) * 2.57 = 12$
- $W(15) = 4.5 + \Gamma(15/5) * 2.57 = 12$
- :: W(15) < D = 12 < 15
- T2 is schedulable.

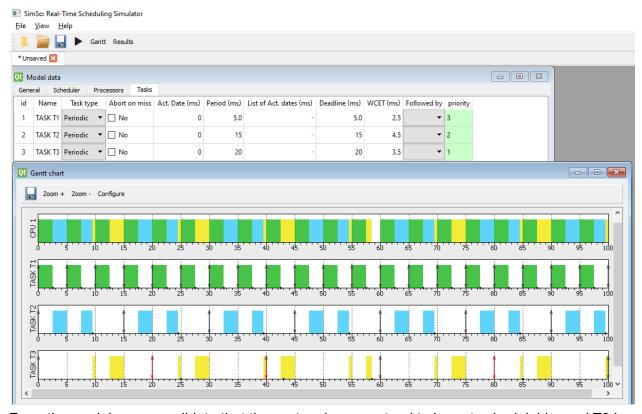
Time Demand for T3

```
• W(1) = 3.5 + \lceil (1/5) * 2.5 \rceil + \lceil (1/15) * 4.5 \rceil = 10.5
• W(2) = 3.5 + \lceil (2/5) * 2.5 \rceil + \lceil (2/15) * 4.5 \rceil = 10.5
• W(3) = 3.5 + \Gamma(3/5) * 2.57 + \Gamma(3/15) * 4.57 = 10.5
• W(4) = 3.5 + (4/5) * 2.57 + (4/15) * 4.57 = 10.5
• W(5) = 3.5 + \lceil (5/5) * 2.5 \rceil + \lceil (5/15) * 4.5 \rceil = 10.5
• W(6) = 3.5 + \lceil (6/5) * 2.5 \rceil + \lceil (6/15) * 4.5 \rceil = 13
• W(7) = 3.5 + \lceil (7/5) * 2.5 \rceil + \lceil (7/15) * 4.5 \rceil = 13
• W(8) = 3.5 + \lceil (8/5) * 2.5 \rceil + \lceil (8/15) * 4.5 \rceil = 13
• W(9) = 3.5 + \lceil (9/5) * 2.5 \rceil + \lceil (9/15) * 4.5 \rceil = 13
• W(10) = 3.5 + \Gamma(10/5) * 2.51 + \Gamma(10/15) * 4.51 = 13
• W(11) = 3.5 + \Gamma(11/5) * 2.5 + \Gamma(11/15) * 4.5 = 15.5
• W(12) = 3.5 + \Gamma(12/5) * 2.57 + \Gamma(12/15) * 4.57 = 15.5
• W(13) = 3.5 + \Gamma(13/5) * 2.57 + \Gamma(13/15) * 4.57 = 15.5
• W(14) = 3.5 + \Gamma(14/5) * 2.5 + \Gamma(14/15) * 4.5 = 15.5
• W(15) = 3.5 + \Gamma(15/5) * 2.57 + \Gamma(15/15) * 4.57 = 15.5
• W(16) = 3.5 + \Gamma(16/5) * 2.51 + \Gamma(16/15) * 4.51 = 22.5
• W(17) = 3.5 + \Gamma(17/5) * 2.5 + \Gamma(17/15) * 4.5 = 22.5
• W(18) = 3.5 + \Gamma(18/5) * 2.57 + \Gamma(18/15) * 4.57 = 22.5
• W(19) = 3.5 + \Gamma(19/5) * 2.5 + \Gamma(19/15) * 4.5 = 22.5
```

• $W(20) = 3.5 + \Gamma(20/5) * 2.51 + \Gamma(20/15) * 4.51 = 22.5$

- W(15) > D = 22.5 > 20
- ∴ T3 is not schedulable.

Simso Model



From the model we can validate that the system is guaranteed to be not schedulable, and T3 is the one that is not schedulable.