

Three-Factor ANOVA

PSYC214: Statistics For Group Comparisons

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Week 9

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Three-Factor
ANOVA

Memory and
Context

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Recall Interaction Effects
Recognition ANOVA Table
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Learning Objectives

- Procedures for analysing and interpreting three-factor ANOVA
- How to decompose a three-way interaction:
 - splitting the design and analysing it as a series of two-factor ANOVAs
- Examples:
 - $2 \times 2 \times 2$ fully within-participants ANOVA
 - $2 \times 2 \times 2$ mixed ANOVA
- General things to consider

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Three-Factor ANOVA

- Three-factor ANOVAs are common in psychology
- In such designs, there are three possible **two-way interactions**:
 - $A \times B$
 - $A \times C$
 - $B \times C$
- There is also the possibility of a **three-way interaction**:
 - $A \times B \times C$
- Complexity of interpreting these designs arises when the three-way interaction is significant

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Three-Factor ANOVA

- Basic design principles of earlier lectures still apply
- A between-participants design is still relatively simple, with only a single error term for all effects
- However, a $2 \times 2 \times 2$ design would require at least 160 participants (obeying our maxim of $N = 20$ per cell)
- Problems with fully within-participants and mixed designs apply equally to three-factor designs
- Try to avoid exceeding two levels per factor where possible

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Three-Factor ANOVA

- The most straightforward outcome is when the three-way interaction is not significant
- Where this occurs, one or more of the two-way interactions may be significant
- In which case, each significant two-way interaction should be investigated separately of the others
- The procedures for interpreting each interaction are the same as those discussed in previous lectures
- For example, if the $A \times B$ two-way interaction is significant, the simple main effects of factor A at B, and factor B at A can be investigated

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Three-Factor ANOVA

- The simplest case arises when none of the interactions are significant
- In this case, the outcome must be interpreted in terms of the main effects, if any of these are significant
- If nothing is significant, then unless specific pairwise comparisons are planned, the analysis is complete

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Dealing With A Significant Three-Way Interaction

- A significant three-way interaction occurs when there are different two-way interactions between two of the factors according to the levels of the third factor
- The simplest way to analyse a significant three-way interaction is to reanalyse it as a series of two-factor ANOVAs, e.g. :
 - 1 a 2 (factor A: level A_1 vs. level A_2) \times 2 (factor B: level B_1 vs. level B_2) ANOVA at level C_1 of factor C
 - 2 a 2 (factor A: level A_1 vs. level A_2) \times 2 (factor B: level B_1 vs. level B_2) ANOVA at level C_2 of factor C
- Any significant interactions would be followed up with a simple main effects analysis

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Memory and Context: A $2 \times 2 \times 2$ Fully Within-Participants Design

- A memory researcher wants to know if memory is better when material is tested in the same context it was learned in
- They also want to know whether recall and recognition memory are equally context dependent
- The researcher manipulates three factors in a $2 \times 2 \times 2$ fully within-participants design:
 - 1 memory test (recall vs. recognition)
 - 2 learning context (learn under water vs. learn land)
 - 3 testing context (test under water vs. test land)
- Participants given words to remember in a learning context → memory for the words tested via recall or recognition
- Dependent measure is the number of words remembered correctly

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Raw Data For Memory and Context Study

Table: A $2 \times 2 \times 2$ factorial design

| Factor A: Task | | Level A ₁ recall | | | Level A ₂ recognition | | |
|--------------------|----------------------------|-----------------------------|----------------------|----------------------------|----------------------------------|---------------------|---|
| Factor B: Learning | Level B ₁ under | Level B ₂ land | | Level B ₁ under | Level B ₂ land | | |
| Factor C: Testing | C ₁ under | C ₂ land | C ₁ under | C ₂ land | C ₁ under | C ₂ land | |
| P ₁ | 8 | 5 | 3 | 7 | 5 | 5 | 7 |
| P ₂ | 9 | 6 | 3 | 8 | 7 | 6 | 5 |
| P ₃ | 7 | 5 | 4 | 6 | 6 | 7 | 5 |
| P ₄ | 8 | 4 | 4 | 5 | 7 | 5 | 6 |
| P ₅ | 6 | 3 | 3 | 8 | 5 | 4 | 6 |

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Aggregate Data For Memory and Context Study

Table: A $2 \times 2 \times 2$ factorial design

| | Level A ₁ recall task | | | Level A ₂ recognition task | | | Overall |
|----------------------------------|----------------------------------|---------------------------|---------|---------------------------------------|---------------------------|---------|---------|
| | Level B ₁ under | Level B ₂ land | Overall | Level B ₁ under | Level B ₂ land | Overall | |
| Level C ₁ under water | 7.6 | 3.4 | 5.5 | Level C ₁ under water | 6 | 5.8 | 5.9 |
| Level C ₂ on land | 4.6 | 6.8 | 5.7 | Level C ₂ on land | 5.4 | 5.8 | 5.6 |
| Overall | 6.1 | 5.1 | 5.6 | | 5.7 | 5.8 | 5.8 |

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ANOVA Table For Memory and Context Study

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|----------------------|----------------|--------------------|-------------|--------|-------|
| A (memory task) | 0.225 | 1 | 0.225 | 1.000 | 0.374 |
| Error A × P | 0.900 | 4 | 0.225 | | |
| B (learning context) | 2.025 | 1 | 2.025 | 1.588 | 0.276 |
| Error B × P | 5.100 | 4 | 1.275 | | |
| C (testing context) | 0.025 | 1 | 0.025 | 0.014 | 0.911 |
| Error C × P | 7.100 | 4 | 1.775 | | |
| A × B | 3.025 | 1 | 3.025 | 2.951 | 0.161 |
| Error A × B × P | 4.100 | 4 | 1.025 | | |
| A × C | 0.625 | 1 | 0.625 | 0.714 | 0.446 |
| Error A × C × P | 3.500 | 4 | 0.875 | | |
| B × C | 30.625 | 1 | 30.625 | 27.222 | 0.006 |
| Error B × C × P | 4.500 | 4 | 1.125 | | |
| A × B × C | 21.025 | 1 | 21.025 | 27.129 | 0.006 |
| Error A × B × C × P | 3.10 | 4 | 0.775 | | |
| P (participants) | 10.900 | 4 | 2.733 | | |

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| Error A × P | 0.900 | 4 | 0.225 | | |
| B (learning context) | 2.025 | 1 | 2.025 | 1.588 | 0.276 |
| Error B × P | 5.100 | 4 | 1.275 | | |
| C (testing context) | 0.025 | 1 | 0.025 | 0.014 | 0.911 |
| Error C × P | 7.100 | 4 | 1.775 | | |
| A × B | 3.025 | 1 | 3.025 | 2.951 | 0.161 |
| Error A × B × P | 4.100 | 4 | 1.025 | | |
| A × C | 0.625 | 1 | 0.625 | 0.714 | 0.446 |
| Error A × C × P | 3.500 | 4 | 0.875 | | |
| B × C | 30.625 | 1 | 30.625 | 27.222 | 0.006 |
| Error B × C × P | 4.500 | 4 | 1.125 | | |
| A × B × C | 21.025 | 1 | 21.025 | 27.129 | 0.006 |
| Error A × B × C × P | 3.10 | 4 | 0.775 | | |
| P (participants) | 10.900 | 4 | 2.733 | | |

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Interpreting The Significant Three-Way Interaction

- To decompose our significant three-way interaction, we first need to decide which factor to split our design by
- The obvious choice is factor A (memory task: recall vs. recognition)
- Next, we perform two two-factor ANOVAs:
 - 2 (learning context: learn under water vs. learn land) \times 2 (testing context: test under water vs. test land) ANOVA for the **recall** memory test condition only
 - 2 (learning context: learn under water vs. learn land) \times 2 (testing context: test under water vs. test land) ANOVA for the **recognition** memory test condition only

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ANOVA Table For Recall Memory Task

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|-------------------------------|----------------|--------------------|-------------|--------|-------|
| B (learning context) | 5.000 | 1 | 5.000 | 3.636 | 0.129 |
| Error B \times P | 5.500 | 4 | 1.375 | | |
| C (testing context) | 0.200 | 1 | 0.200 | 0.186 | 0.688 |
| Error C \times P | 4.300 | 4 | 1.075 | | |
| B \times C | 51.200 | 1 | 51.200 | 62.061 | 0.001 |
| Error B \times C \times P | 3.300 | 4 | 0.825 | | |
| P (participants) | 5.300 | 4 | 1.333 | | |

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ANOVA Table For Recall Memory Task

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|-------------------------------|----------------|--------------------|-------------|--------|-------|
| B (learning context) | 5.000 | 1 | 5.000 | 3.636 | 0.129 |
| Error B \times P | 5.500 | 4 | 1.375 | | |
| C (testing context) | 0.200 | 1 | 0.200 | 0.186 | 0.688 |
| Error C \times P | 4.300 | 4 | 1.075 | | |
| B \times C | 51.200 | 1 | 51.200 | 62.061 | 0.001 |
| Error B \times C \times P | 3.300 | 4 | 0.825 | | |
| P (participants) | 5.300 | 4 | 1.333 | | |

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Simple Main Effects Table For Recall Memory Task

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|----------------------------|----------------|--------------------|-------------|--------|-------|
| learning context at | | | | | |
| test under water | 44.100 | 1 | 44.100 | 32.073 | 0.005 |
| test land | 12.100 | 1 | 12.100 | 8.800 | 0.041 |
| Error term | 5.50 | 4 | 1.375 | | |
| testing context at | | | | | |
| learn under water | 22.500 | 1 | 22.500 | 20.930 | 0.010 |
| learn land | 28.900 | 1 | 28.900 | 26.884 | 0.007 |
| Error term | 4.300 | 4 | 1.075 | | |

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ANOVA Table For Recognition Memory Task

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|----------------------|----------------|--------------------|-------------|-------|-------|
| B (learning context) | 0.050 | 1 | 0.050 | 0.054 | 0.828 |
| Error B × P | 3.700 | 4 | 0.925 | | |
| C (testing context) | 0.450 | 1 | 0.450 | 0.286 | 0.621 |
| Error C × P | 6.300 | 4 | 1.575 | | |
| B × C | 0.450 | 1 | 0.450 | 0.419 | 0.553 |
| Error B × C × P | 4.300 | 4 | 1.075 | | |
| P (participants) | 6.500 | 4 | 1.633 | | |

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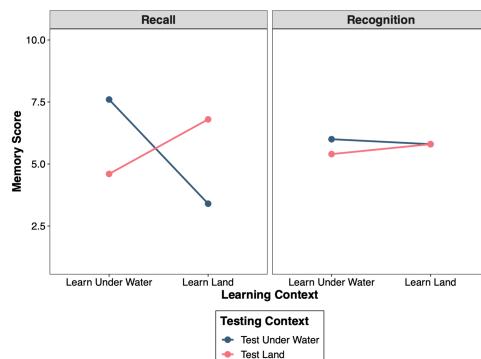
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Interaction Plots For Memory and Context Study



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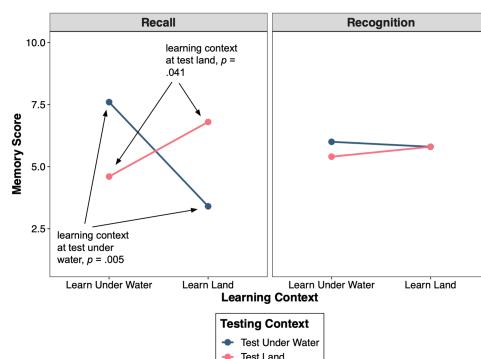
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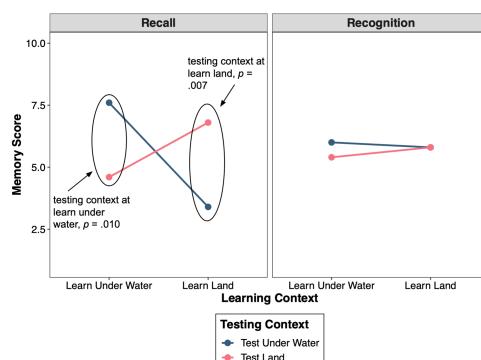
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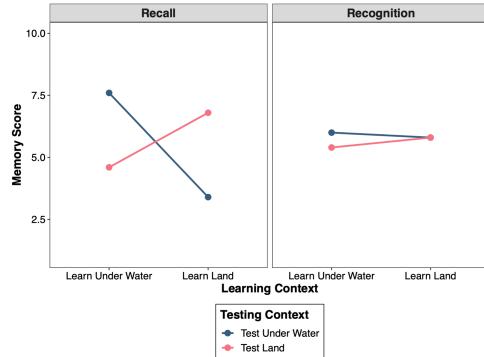
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Learning To Pronounce Irregular Words: A $2 \times 2 \times 2$ Mixed Design

- A researcher wants to investigate the development in children's ability to pronounce regular and irregular words
- The researcher adopts a $2 \times 2 \times 2$ mixed design:
 - age (7 years old vs. 9 years old) is between-participants
 - word frequency (low vs. high) is within-participants
 - word type (regular vs. irregular) is within-participants
- Participants are given 10 words to pronounce in each category (40 words in total)
- Dependent measure is the number of pronunciation errors

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Raw Data For Word Pronunciation Study

Table: A $2 \times 2 \times 2$ factorial design

| Factor A: Age | Level A ₁ 7-years-old | | | | Level A ₂ 9-years-old | | | | |
|----------------|----------------------------------|--------------------|---------------------------|--------------------------|----------------------------------|--------------------|--------------------|--------------------|---|
| | Factor B: Frequency | | Level B ₁ high | Level B ₂ low | Factor C: Word type | | C ₁ reg | C ₂ irr | |
| | C ₁ reg | C ₂ irr | C ₁ reg | C ₂ irr | C ₁ reg | C ₂ irr | C ₁ reg | C ₂ irr | |
| P ₁ | 6 | 7 | 5 | 6 | P ₆ | 4 | 4 | 3 | 6 |
| P ₂ | 7 | 5 | 6 | 7 | P ₇ | 3 | 4 | 4 | 7 |
| P ₃ | 5 | 6 | 7 | 6 | P ₈ | 4 | 3 | 5 | 9 |
| P ₄ | 6 | 7 | 5 | 7 | P ₉ | 5 | 5 | 3 | 8 |
| P ₅ | 6 | 6 | 5 | 7 | P ₁₀ | 3 | 4 | 3 | 7 |

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Aggregate Data For Word Pronunciation Study

Table: A $2 \times 2 \times 2$ factorial design

| | Level A ₁ 7-years-old | | | Level A ₂ 9-years-old | | |
|--------------------------------|----------------------------------|--------------------------------|---------|----------------------------------|--------------------------------|--------------------------|
| | Level B ₁ high | | Overall | Level B ₁ high | | Level B ₂ low |
| | Level C ₁ regular | Level C ₂ irregular | | Level C ₁ regular | Level C ₂ irregular | Overall |
| Level C ₁ regular | 6.0 | 5.6 | 5.8 | 3.8 | 3.6 | 3.7 |
| Level C ₂ irregular | 6.2 | 6.6 | 6.4 | 4.0 | 7.4 | 5.7 |
| Overall | 6.1 | 6.1 | 6.1 | 3.9 | 5.5 | 4.7 |

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ANOVA Table For Word Pronunciation Study

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|-------------------|----------------|--------------------|-------------|--------|--------|
| A (age) | 19.600 | 1 | 19.600 | 34.844 | < .001 |
| Between error S/A | 4.500 | 8 | 0.562 | | |
| B (frequency) | 6.400 | 1 | 6.400 | 5.885 | 0.042 |
| Error B × S/A | 8.700 | 8 | 1.087 | | |
| C (word type) | 16.900 | 1 | 16.900 | 36.541 | < .001 |
| Error C × S/A | 3.700 | 8 | 0.462 | | |
| A × B | 6.400 | 1 | 6.400 | 5.885 | 0.042 |
| Error B × S/A | 8.700 | 8 | 1.087 | | |
| A × C | 4.900 | 1 | 4.900 | 10.595 | 0.012 |
| Error C × S/A | 3.700 | 8 | 0.462 | | |
| B × C | 12.100 | 1 | 12.100 | 17.600 | 0.003 |
| Error B × C × S/A | 5.500 | 8 | 0.688 | | |
| A × B × C | 4.900 | 1 | 4.900 | 7.127 | 0.028 |
| Error B × C × S/A | 5.500 | 8 | 0.688 | | |

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ANOVA Table For Word Pronunciation Study

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|-------------------|----------------|--------------------|-------------|--------|--------|
| A (age) | 19.600 | 1 | 19.600 | 34.844 | < .001 |
| Between error S/A | 4.500 | 8 | 0.562 | | |
| B (frequency) | 6.400 | 1 | 6.400 | 5.885 | 0.042 |
| Error B × S/A | 8.700 | 8 | 1.087 | | |
| C (word type) | 16.900 | 1 | 16.900 | 36.541 | < .001 |
| Error C × S/A | 3.700 | 8 | 0.462 | | |
| A × B | 6.400 | 1 | 6.400 | 5.885 | 0.042 |
| Error B × S/A | 8.700 | 8 | 1.087 | | |
| A × C | 4.900 | 1 | 4.900 | 10.595 | 0.012 |
| Error C × S/A | 3.700 | 8 | 0.462 | | |
| B × C | 12.100 | 1 | 12.100 | 17.600 | 0.003 |
| Error B × C × S/A | 5.500 | 8 | 0.688 | | |
| A × B × C | 4.900 | 1 | 4.900 | 7.127 | 0.028 |
| Error B × C × S/A | 5.500 | 8 | 0.688 | | |

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Interpreting The Significant Three-Way Interaction

- To decompose our significant three-way interaction, we first need to decide which factor to split our design by
- The obvious choice is our between-participants factor A (age: 7 year olds vs. 9 year olds)
- Next, we perform two two-factor ANOVAs:
 - 2 (frequency: low vs. high) × 2 (word type: regular vs. irregular) ANOVA for the 7 year olds only
 - 2 (frequency: low vs. high) × 2 (word type: regular vs. irregular) ANOVA for the 9 year olds only

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ANOVA Table For 7 Year Olds

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|------------------|----------------|--------------------|-------------|-------|-------|
| B (frequency) | 0.000 | 1 | 0.000 | 0.000 | 1.000 |
| Error B × P | 2.500 | 4 | 0.625 | | |
| C (word type) | 1.800 | 1 | 1.800 | 5.885 | 0.178 |
| Error C × P | 2.700 | 4 | 0.675 | | |
| B × C | 0.800 | 1 | 0.800 | 5.885 | 0.405 |
| Error B × C × P | 3.700 | 4 | 0.925 | | |
| P (participants) | 0.300 | 4 | 0.075 | | |

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ANOVA Table For 9 Year Olds

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|------------------|----------------|--------------------|-------------|--------|-------|
| B (frequency) | 12.800 | 1 | 12.800 | 8.258 | 0.045 |
| Error B × P | 6.200 | 4 | 1.550 | | |
| C (word type) | 20.000 | 1 | 20.000 | 80.000 | <.001 |
| Error C × P | 1.000 | 4 | 0.250 | | |
| B × C | 16.200 | 1 | 16.200 | 36.000 | 0.004 |
| Error B × C × P | 1.800 | 4 | 0.450 | | |
| P (participants) | 4.200 | 4 | 1.050 | | |

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ANOVA Table For 9 Year Olds

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|------------------|----------------|--------------------|-------------|--------|-------|
| B (frequency) | 12.800 | 1 | 12.800 | 8.258 | 0.045 |
| Error B × P | 6.200 | 4 | 1.550 | | |
| C (word type) | 20.000 | 1 | 20.000 | 80.000 | <.001 |
| Error C × P | 1.000 | 4 | 0.250 | | |
| B × C | 16.200 | 1 | 16.200 | 36.000 | 0.004 |
| Error B × C × P | 1.800 | 4 | 0.450 | | |
| P (participants) | 4.200 | 4 | 1.050 | | |

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Simple Main Effects Table For 9 Year Olds

| Source | Sum of Squares | Degrees of Freedom | Mean Square | F | P |
|-------------------|----------------|--------------------|-------------|---------|-------|
| word frequency at | | | | | |
| regular words | 0.100 | 1 | 0.100 | 0.065 | 0.812 |
| irregular words | 28.900 | 1 | 28.900 | 18.645 | 0.013 |
| Error term | 6.200 | 4 | 1.550 | | |
| word type at | | | | | |
| low frequency | 36.100 | 1 | 36.100 | 144.400 | <.001 |
| high frequency | 0.100 | 1 | 0.100 | 0.400 | 0.561 |
| Error term | 1.000 | 4 | 0.250 | | |

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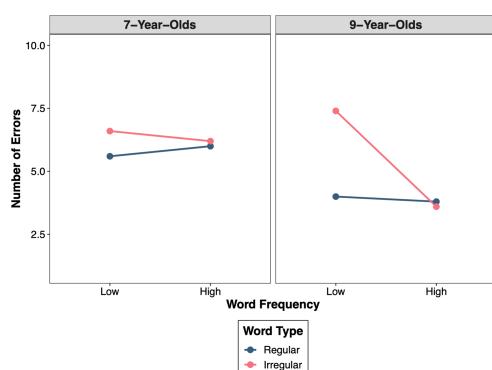
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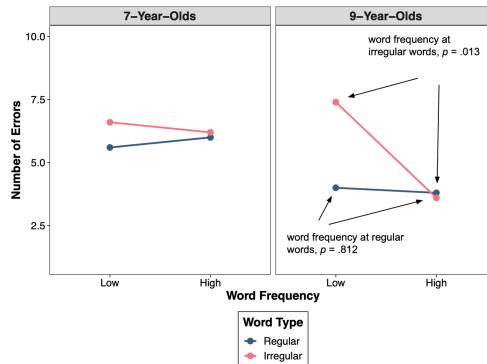
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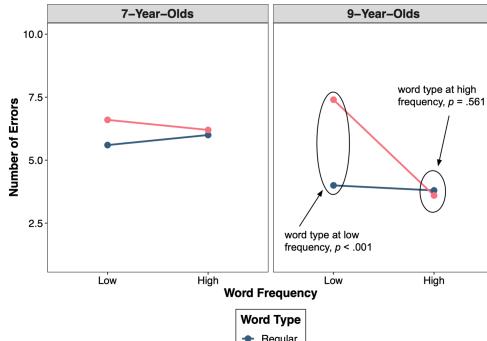


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A Final Note On Interpreting Three-Way Interactions

- In both of these examples, one of the two-factor ANOVAs returned a significant interaction, whereas the other returned a non-significant interaction
- This will **not** always be the case
- Sometimes the interaction for each two-factor ANOVA will be significant and both will need to be followed up with a simple main effects analysis
- Under these conditions, the simple main effects for the two interactions will differ in direction and/or size of their trends

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- As always, start at the bottom of the ANOVA table and work your way up
- If the three-way interaction is significant, then this must be analysed
- If not, then each of the significant two-way interactions should be analysed independently
- If none of the two-way interactions is significant, the ANOVA results may be described in terms of the main effects, with follow-up tests for any factors with three or more levels

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In Next Week's Lab ...

- Running a three-factor (fully within-participants and mixed) ANOVA in R



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References

Roberts, M. J., & Russo, R. (1999, Chapter 12). *A student's guide to Analysis of Variance*. Routledge: London.



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