Supplementary Material: SQL queries for CFD^ps

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Below we show how the SQL queries Q_i^c and Q_i^v are generated for validating CFD p s in $\Sigma^i_{\text{cfd}^p}$, which is an extension of the SQL techniques for CFDs and eCFDs discussed in [2] and [1], respectively.

The queries Q_i^c and Q_i^v for the violations of $\Sigma_{\mathsf{cfd}^p}^i$ are given as follows, which capitalize on the data table enc_L , enc_R and enc_{\neq} that $\mathsf{encode}\ \mathsf{CFD}^p\mathsf{s}$ in $\Sigma_{\mathsf{cfd}^p}^i$.

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\begin{array}{l} Q_i^c\text{: select }R_i.*\text{ from }R_i, \text{ enc}_L\ L, \text{enc}_R\ R, \text{enc}_\neq\ N\\ \text{where }L.\text{cid}=R.\text{cid and }R_i.X\asymp L\text{ and }R_i.X\asymp N\text{ and }\\ \text{not }(R_i.Y\asymp R\text{ and }R_i.Y\asymp N) \end{array}
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 Q_i^v : select distinct X_L

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\begin{array}{l} \text{from (select $L$.cid as cid, $X_L$, $Y_R$ from $R_i$, $\operatorname{enc}_L$ $L$, $\operatorname{enc}_R$ $R$, $\operatorname{enc}_{\neq}$ $N$} \\ \text{where $L$.cid} = R.{\operatorname{cid}} \text{ and } R_i.X \asymp L$ and \\ R_i.X \asymp N$ and $R.Y = '\_'$ ) as $M$} \\ \text{group by cid, $X_L$ having count (distinct $Y_R$)} > 1 \end{array}
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Here (1) $X = \{A_1, \dots, A_{m1}\}$ and $Y = \{B_1, \dots, B_{m2}\}$ are the sets of attributes in LHS and RHS of Σ_{cfd}^i respectively; (2) $R_i \cdot X \times L$ is the conjunction of

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\begin{array}{l} L.A_j \text{ is null or } R_i.A_j = L.A_j \text{ or } (L.A_j = \begin{subarray}{c} -c \\ and & (L.A_{j>} \text{ is null or } R_i.A_j > L.A_{j>}) \\ and & (L.A_{j\geq} \text{ is null or } R_i.A_j \geq L.A_{j\geq}) \\ and & (L.A_{j<} \text{ is null or } R_i.A_j < L.A_{j<}) \\ and & (L.A_{j\leq} \text{ is null or } R_i.A_j \leq L.A_{j\leq})) \end{array}
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for each $j \in [1, m_1]$; (3) $R_i \cdot Y \times R$ is defined similarly for attributes in Y; (4) $R_i \cdot X \times N$ is the conjunction of

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\begin{array}{c} \textbf{not exists (select}* \textbf{ from } N \\ \textbf{ where } L. \textbf{cid} = N. \textbf{cid and } N. \textbf{pos} = \text{'LHS'} \textbf{ and} \\ N. \textbf{att} = \text{'}A_j\text{'} \textbf{ and } R_i. A_j = N. \textbf{val}) \end{array}
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for each $j \in [1, m_1]$; (5) $R_i \cdot Y \times N$ is defined similarly, but with $N.\mathsf{pos} = '\mathsf{RHS}'$; (6) X_L is the set of following attributes

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(case when L.A_j is not null then R_i.A_j end) as A_{Lj}
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for each j \in [1, m_1]; (7) Similarly, Y_R is the set of (case when R.B_k is not null then R_i.B_k end) as B_{Rk}
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for each $k \in [1, m_2]$; (8) $R.Y = '_'$ is the disjunction of $R.B_k = '_'$ for each $k \in [1, m_2]$.

Intuitively, detecting violations of CFD^ps is a two-step process. First, query Q_i^c detects single-tuple violations, *i.e.*,

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the tuples t in I_i that match the LHS of a CFD p in $\Sigma^i_{\mathsf{cfd}^p}$, but do not match its RHS. Second, query Q^v_i finds multi-tuple violations, *i.e.*, the tuples t in I_i such that (a) there exists another tuple t' in I_i , t and t' match and agree on the LHS of a CFD p in $\Sigma^i_{\mathsf{cfd}^p}$, but do not agree on the RHS of the CFD p .

Example 1: Using the coding of Fig. 4, two SQL queries for checking CFD^ps φ_2 , φ_3 and φ_4 of Fig. 2 are given as follows:

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Q_1^c: select R_1.* from item R_1, enc<sub>L</sub> L, enc<sub>R</sub> R, enc\neq N
    where L.cid = R.cid and
               (L.sale is null or R_1.sale = L.sale or L.sale = ' _') and
               not exists (select * from N
                        where N.\operatorname{cid} = L.\operatorname{cid} and N.\operatorname{pos} =' \operatorname{LHS}' and
                         N.\mathsf{att} = 'sale' \ \mathsf{and} \ R_1.\mathsf{sale} = N.\mathsf{val} \ ) \ \mathsf{and} \ 
               (L.price is null or R_1.price = L.price or (L.price = '_' and
               (L.price> is null or R_1.price> L.price> ) and
               (L.\mathsf{price}_{<} \mathbf{is} \mathbf{null} \mathbf{or} R_1.\mathsf{price} \leq L.\mathsf{price}_{<}))) and
               not exists ( select * from N
                         where N.\operatorname{cid} = L.\operatorname{cid} and N.\operatorname{pos} =' \operatorname{LHS}' and
                         N.\mathsf{att} =' price' \text{ and } R_1.\mathsf{price} = N.\mathsf{val}) and
              not (( R.{\rm shipping} is null or R_1.{\rm shipping}=R.{\rm shipping} or R.{\rm shipping}=' _' ) and
               not exists ( select * from N
                         where N.\operatorname{cid} = R.\operatorname{cid} and N.\operatorname{pos} =' \operatorname{RHS}' and
                         N.\mathsf{att} =' \mathit{shipping'} \ \mathsf{and} \ R_1.\mathsf{shipping} = N.\mathsf{val}) \ \mathsf{and}
               (R.price is null or R_1.price = R.price or (R.price = ' _ ' and
               (R.\mathsf{price}_{>}\ \mathbf{is}\ \mathbf{null}\ \mathbf{or}\ R_1.\mathsf{price}_{\geq}\ R.\mathsf{price}_{\geq}\ ) and
               (R.\mathsf{price} \subset \mathsf{is} \; \mathsf{null} \; \mathsf{or} \; R_1.\mathsf{price} \subset R.\mathsf{price} \subset ))) \; \mathsf{and} \;
               not exists ( select * from N
                         where N.\operatorname{cid} = R.\operatorname{cid} and N.\operatorname{pos} =' \operatorname{RHS}' and
                         N.\mathsf{att} = 'price' \text{ and } R_1.\mathsf{price} = N.\mathsf{val} ))
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```
Q_1^v: select distinct sale<sub>L</sub>, price<sub>L</sub> from (
   select L.cid as cid,
   (case when L.sale is not null then R_1.sale end) as sale<sub>L</sub>,
   (case when L.price is not null then R_1.price end) as priceL,
   (case when R.shipping is not null then R_1.shipping end) as shipping R,
   (case when R.price is not null then R_1.price end) as price<sub>R</sub>
   from item R_1, enc<sub>L</sub> L, enc<sub>R</sub> R, enc\neq N
             where L.\operatorname{cid} = R.\operatorname{cid} and
             (L.sale is null or R_1.sale = L.sale or L.sale = ' _') and
             not exists ( select * from N
                          where N.\operatorname{cid} = L.\operatorname{cid} and N.\operatorname{pos} =' \operatorname{LHS}' and
                          N.\mathsf{att} = 'sale' \text{ and } R_1.\mathsf{sale} = N.\mathsf{val}) \text{ and }
             (L.price is null or R_1.price = L.price or (L.price = ' _ ' and
             (L.\mathsf{price}_{>} \mathbf{is} \; \mathbf{null} \; \mathbf{or} \; R_1.\mathsf{price} > L.\mathsf{price}_{>}) \; \mathbf{and} \;
             (L.\mathsf{price}_{<} \mathsf{is} \mathsf{null} \mathsf{or} R_1.\mathsf{price} \leq L.\mathsf{price}_{<}))) and
             not exists (select * from N
                          where N.\operatorname{cid} = L.\operatorname{cid} and N.\operatorname{pos} =' \operatorname{LHS}' and
                          N.\mathsf{att} =' price' \text{ and } R_1.\mathsf{price} = N.\mathsf{val}) and
             (R.\mathsf{shipping} = ' \_'\mathsf{or}\ R.\mathsf{price} = ' \_')) as M
   group by cid, saleL, priceL
```

having count (distinct shipping_R, price_R)> 1

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