

SPLEX TME 8

Partial Least Squares and Canonical Correlation Analysis

The goal of the TME is to understand and get skills in Partial Least Squares (PLS) and Canonical Correlation Analysis (CCA).

Data

- Data provided during the TME

Analysis

- **Canonical correlation.**

Short description: Canonical correlations analysis (CCA) is an exploratory statistical method to highlight correlations between two data sets acquired on the same experimental units. CCA is most appropriate when a researcher desires to examine the relationship between two variable set.

X and Y are matrices of order $n \times p$ and $n \times q$. The columns correspond to variables and the rows correspond to experimental units (patients). Find two vectors a and b that maximize the correlation between the linear combinations

$$\begin{aligned}U &= a_1X^1 + a_2X^2 + \dots + a_pX^p \\V &= b_1Y^1 + b_2Y^2 + \dots + b_qY^q\end{aligned}$$

The problem consists in solving

$$\rho = \text{cor}(U, V) = \max_{a,b} \text{cor}(Xa, Yb)$$

Canonical correlations ρ are the positive square roots of the eigenvalues λ of $P_X P_Y$ ($\rho = \sqrt{\lambda}$), where

$$\begin{aligned}P_X &= X(X^T X)^{-1} X^T \\P_Y &= Y(Y^T Y)^{-1} Y^T\end{aligned}$$

The canonical correlation coefficient is the Pearson relationship between the two synthetic variables on a given canonical function. Because of the scaling created by the standardized weights in the linear equations, this value cannot be negative and only ranges from 0 to 1. Visualization of the results of canonical correlation is usually through bar plots of the coefficients of the two sets of variables for the pairs of canonical variates showing significant correlation.

- **Partial least squares.** *Short description:* PLS regression is a recent technique that generalizes and combines features from principal component analysis and multiple regression. It is particularly useful when we need to predict a set of dependent variables from a (very) large set of independent variables (i.e., predictors). SPLS is its sparse version.

1. Explore the canonical correlation analysis of Python: find relations between groups of variables

http://scikit-learn.org/stable/modules/generated/sklearn.cross_decomposition.CCA.html

2. http://scikit-learn.org/stable/modules/generated/sklearn.cross_decomposition.PLSCanonical.html
3. Estimate accuracy of the methods on the heterogeneous data