

## CLL:113-Tut-7(16.12.20)

Q1 A. Develop a user-friendly computer program for multiple segments (a) Trapezoidal and (b) Simpson's 1/3 rule and (c) Simpson's 3/8 rule Test it by integrating:

$$\int_0^1 x^{0.1} (1.2 - x) (1 - e^{20(x-1)}) dx$$

Use the true value of 0.602298 to compute  $\epsilon_t$

B. For each case, draw the true error as a function of the number of segments. Does the error always decrease with increase in number of segments ?

Part B has to be done in the report

Q2. The following relationships can be used to analyze uniform beams subject to distributed loads,

$$\frac{dy}{dx} = \theta(x), \quad \frac{d\theta}{dx} = \frac{M(x)}{EI}, \quad \frac{dM}{dx} = V(x), \quad \frac{dV}{dx} = -w(x)$$

Where  $x$  = distance along beam (m),  $y$  = deflection (m),  $\theta(x)$  = slope (m/m),  $E$  = modulus of elasticity (Pa = N/m<sup>2</sup>),  $I$  = moment of inertia (m<sup>4</sup>),  $M(x)$  = moment (N m),  $V(x)$  = shear (N), and  $w(x)$  = distributed load (N/m). For the case of a linearly increasing load, the slope can be computed analytically as

$$\theta(x) = \frac{w_0}{120EI} \left( -5x^4 + 6L^2x^2 - L^4 \right) \dots\dots\dots(1)$$

Employ (a) numerical integration to compute the deflection (in m) And (b) numerical differentiation to compute the moment (in N m) and shear (in N). Base your numerical calculations on values of the slope computed with Eq. 1 at equally spaced intervals of  $\Delta x = 0.125$  m along a 3-m beam. Use the following parameter values in your computation:  $E = 200$  GPa,  $I = 0.0003$  m<sup>4</sup>, and  $w_0 = 2.5$  kN/cm. In addition, the deflections at the ends of the beam are set at  $y(0) = y(L) = 0$ .

part(a) use each of the three numerical integration methods utilized in Q1 to compute the deflection

part(b) for  $x = 0$  -use forward difference

$x = 3$  -use backward difference

rest all other  $x$  -use central difference method