# 4.2 Question 2

**4.2.A** Consider the following hash function. Messages are in the form of a sequence of numbers in  $\mathcal{Z}_n$ ,  $M=(a_1a_2...a_t)$ . The hash value is calculated as  $\sum_{i=1}^t a_i$  for some predefined value n. Does this hash function satisfy any of the requirements for a hash function listed in Table 1.

**4.2.B** Repeat part (A) for the hash function  $h = \left(\sum_{i=1}^{t} (a_i)^2\right) \mod n$ .

**4.2.C** Calculate the hash function of part (B) for M = (189, 632, 900, 722, 349) and n = 989.

$$h = \left(\sum_{i=1}^{5} (a_i)^2\right) \mod 989$$

$$= (189^2 + 632^2 + 900^2 + 722^2 + 349^2) \mod 989$$

$$= (35'721 + 399'424 + 810'000 + 521'284 + 121'801) \mod 989$$

$$= 1'888'230 \mod 989$$

$$= 229$$

## 4.3 Question 3

**4.3.A** State the value of the padding field in SHA-512 if the length of the message is: 5000 bits

1. Calculate size of the data in the last block:

$$5000 \ mod \ 1024 = 904$$

2. Add the size of the length field (128 bit) to the last block size:

$$904 + 128 = 1032$$

3. Because 1032 > 1024 the last block is now:

$$1032 \ mod \ 1024 = 8$$

4. The length of the padding field is therefore:

$$1024 - 8 = 1016 bits$$

5. Therefore the padding consists of one 1 and 1015 zeros, hence the value is:

Exercise 04

### **5001** bits

1. Calculate size of the data in the last block:

$$5001 \mod 1024 = 905$$

2. Add the size of the length field (128 bit) to the last block size:

$$905 + 128 = 1033$$

3. Because 1032 > 1024 the last block is now:

$$1033 \ mod \ 1024 = 9$$

4. The length of the padding field is therefore:

$$1024 - 9 = 1015 bits$$

5. Therefore the padding consists of one 1 and 1014 zeros, hence the value is:

#### **5002 bits**

1. Calculate size of the data in the last block:

$$5002 \ mod \ 1024 = 906$$

2. Add the size of the length field (128 bit) to the last block size:

$$906 + 128 = 1034$$

3. Because 1032 > 1024 the last block is now:

$$1034 \ mod \ 1024 = 10$$

4. The length of the padding field is therefore:

$$1024 - 10 = 1014 \ bits$$

5. Therefore the padding consists of one 1 and 1013 zeros, hence the value is:

## 4.3.B State the value of the length field in SHA-512 if the length of the message is:

#### **5000** bits

0x00000000000000000000000000001388

#### **5001** bits

#### **5002 bits**

0x0000000000000000000000000000138A

## 4.4 Question 4

# 4.4.A Explain the differences in the algorithms of SHA-3 and MD-5. Which one is used today? Why?