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Internet of Things

V. Time Synchronization

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Internet of Things: Time Synchronization

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1. Introduction

1. Time Synchronization

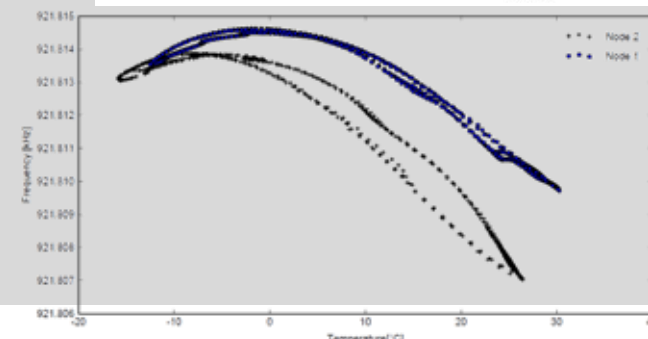
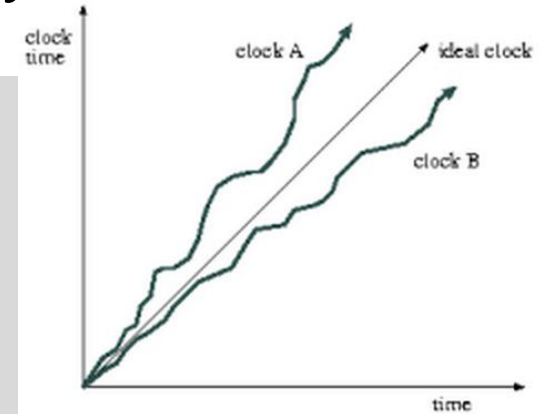
Clocks at sensor nodes should be synchronized in order to

- transform events occurring at different sensor nodes into a common time frame.
- support synchronized sleep and duty cycles among nodes.
- enable localization.

1. Introduction

2.1 Clocks and Communication Delays

- Sensor clocks are based on oscillators.
- $C(t)$: clock at time t
- Derivative $dC(t)/dt$ is ideally 1.
If not, the clock has a drift.
- **Clock skew**:
difference between readings of 2 clocks
- **Clock drift**: difference in reading
between a clock and a nominal
perfect reference clock per unit
of time of the reference clock



1. Introduction

2.2 Clocks and Communication Delays

- Clock drift depends on environmental conditions such as temperature and humidity.

$$1 - \rho \leq \frac{dC(t)}{dt} \leq 1 + \rho$$

- Typical values for ρ :
 $20 \cdot 10^{-6} \text{ [s/s]} = 20 \text{ s in 11.6 days}$
- If drifts $d_{i,j}$ and initial offsets $o_{i,j}$ of two clocks are known

- Clock times can be “translated”:
for two nodes i, j :

$$C_i(t) = a_{i,j} C_j(t) + b_{i,j}$$

- Example:

$$C_i(t) = 1.1 \cdot t$$

$$C_j(t) = 0.9 \cdot t$$

$$\rightarrow C_i(t) = 0.8181 \cdot C_j(t)$$

$$C_i(t) = d_i \cdot t + o_i$$

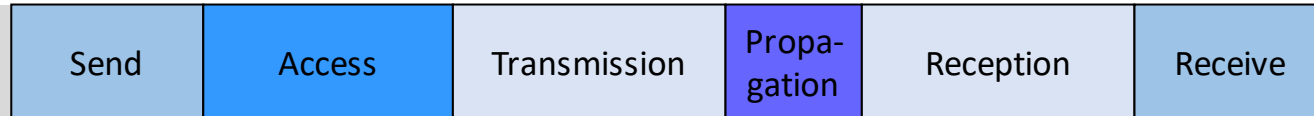
$$C_j(t) = d_j \cdot t + o_j$$

$$\Rightarrow (C_i(t) - o_i) \cdot d_j = (C_j(t) - o_j) \cdot d_i$$

$$C_i(t) = (d_i/d_j) \cdot C_j(t) - o_i \cdot (d_i/d_j) + o_{jj}$$

1. Introduction

3. Packet Delay



- Send time
 - Time needed by the packet from application to MAC layer
 - Variable because of software delays
- Access time
 - Delay resulting from MAC protocol
- Transmission time
 - Delay caused by bit-by-bit transmission
 - Can be calculated from packet length and radio speed, deterministic
- Propagation time
 - Time taken to traverse the wireless link from sender to receiver
 - Negligible
- Reception time
 - Time required to receive each bit of a packet
 - Deterministic
- Receive time
 - processing time between MAC and application layer
 - Variable

1. Introduction

4. Classes of Synchronization

- Internal vs. external
 - External: Nodes synchronize to an external master.
 - Internal: Nodes synchronize among each other.
- Scope: all nodes or sub-sets
- Rate vs. offset synchronization
- Time-scale transformation vs. clock synchronization
- Lifetime
 - Continuous: Network maintains synchronization at all times.
 - On-demand: No synchronization for a long time to save energy
 - Event-triggered: time-stamping of events and synchronization when event occurs, e.g., post-facto synchronization
 - Time-triggered: synchronization for a specific point of time

1. Introduction

5. Requirements for Time Synchronization Schemes

- Energy efficiency
- Memory usage
- Scalability
 - Deployment of large number of nodes
- Precision
 - Ordering of events vs. microsecond accuracy
- Robustness
 - Schemes should be robust to node failures.
- Lifetime
- Scope
 - Global vs. local
- Cost and size
 - GPS receivers are relatively large and costly.
- Immediacy
 - requires pre-synchronization

1. Introduction

6. Global Positioning System

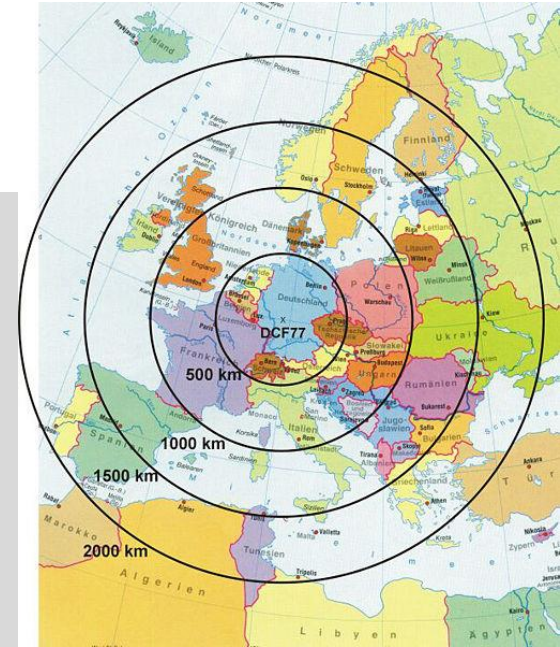
- consists of 32 operational satellites in 6 different planes broadcasting their exact location and precisely synchronized on-board clock time
- requires line-of-sight and does not work inside buildings.
- requires at least 4 visible satellites to calculate x , y , z , and Δt .
- Receiver consumes non-negligible power.

Component	Power (mW)
MCU	18
Radio (TX)	79.2
Radio (RX)	29.7
GPS	165
Switch-mode Regulator	6
Linear Regulator	3.3
Audio	3

1. Introduction

7. Time Signals

- Time signals transmitted by dedicated radio stations
- Example: DCF77
 - $D=Deutschland$ (Germany), $C=$ long wave signal, $F=$ Frankfurt, $77=$ frequency: 77.5 kHz.
 - Frequency synchronous with controlling atomic clock
 - Time information by amplitude modulation, 59 bits per minute
- Prototype receiver consumes 0.266 mW for an average reporting frequency of 1Hz
- Synchronization error ~ 1 ms for 500 s update intervals on TelosB motes



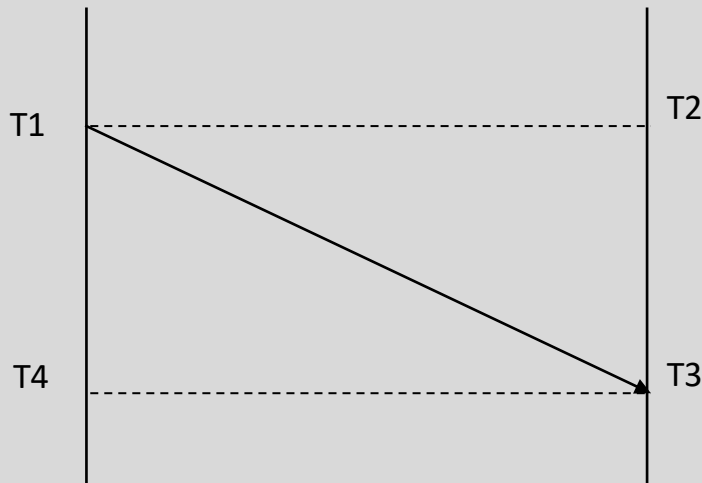
2. Synchronization Techniques

1. Taking 1 sample
 - Unidirectional synchronization
 - Round-trip synchronization
 - Reference broadcasting
2. Combining multiple estimates
3. Synchronization of multiple nodes

2. Synchronization Techniques

1.1 Unidirectional Synchronization

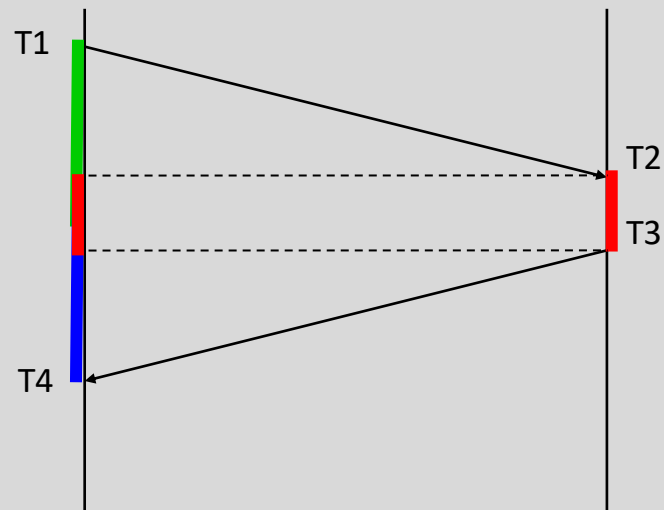
- Time-stamping of message
- Receiving node
 - knows $T1$ and $T3$
 - needs to estimate $T2$ or $T4$
 - Example:
 - estimated delay d
 - $T2 \approx T3 - d$
- Example: DCF77



2. Synchronization Techniques

1.2 Round-Trip Synchronization

- Δ : skew (offset)
- d : communication delay
- $T2 - T1 = d + \Delta$
- $T4 - T3 = d - \Delta$
- $\Delta = ((T2 - T1) - (T4 - T3)) / 2$
- $d = ((T2 - T1) + (T4 - T3)) / 2$
- Example
 - $\Delta = 10 \text{ s}, d = 0.1 \text{ s}$
 - $T1 = 0 \text{ s}, T2 = 10.1 \text{ s}$
 - $T3 = 11.1 \text{ s}, T4 = 1.2 \text{ s}$
 - $\Delta = (10.1 \text{ s} - (-9.9 \text{ s})) / 2 = 10 \text{ s}$
 - $d = (10.1 \text{ s} + (-9.9 \text{ s})) / 2 = 0.1 \text{ s}$

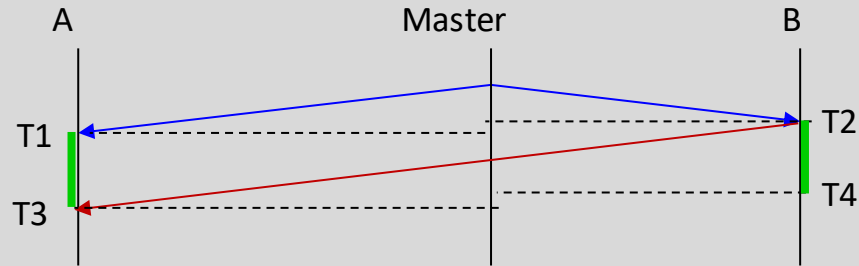


Example: NTP (Network Time Protocol)

2. Synchronization Techniques

1.3 Reference Broadcasting

- Broadcast of master received at T_1 by A and at T_2 by B with almost equal delay.
- B sends T_2 to node A.
- A receives message from B with delay $D = T_3 - T_1$ at T_3 and estimates $T_3 = T_1 + D \approx T_2 + D = T_4$
- Smaller synchronization error because of nearly simultaneous broadcast message reception
- Master reaches A and B but not vice versa.

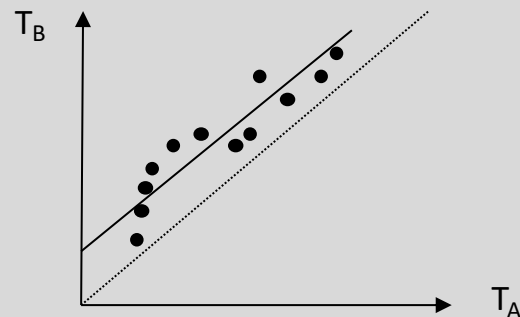


2. Synchronization Techniques

2. Combining Multiple Estimates

- Synchronization can be performed several times.
- Each point denotes a single estimate of the time relation between two nodes A and B.
- Multiple samples and interpolation techniques can decrease estimation error.
 - Example: linear regression: $T_B = a \cdot T_A + b$
 - Problem: requires large amount of memory, and much processing!
 - SS: sum of squares
- Examples
 - Tiny-Sync: Round-trip synchronization using multiple estimates
 - Reference Broadcast Synchronization: reference broadcasting using multiple estimates

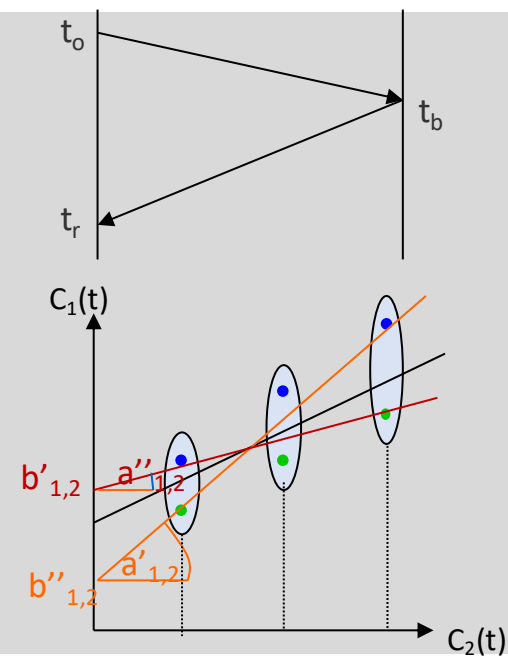
$$b = \frac{SS_{xy}}{SS_{xx}} = \frac{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2}$$
$$a = \bar{y} - b\bar{x} = \frac{\sum_{i=1}^n x_i^2 \sum_{i=1}^n y_i - \sum_{i=1}^n x_i \sum_{i=1}^n x_i y_i}{n \sum_{i=1}^n x_i^2 - (\sum_{i=1}^n x_i)^2}$$



2. Synchronization Techniques

2.1 Tiny-Sync

- $C_1(t) = a_{1,2} C_2(t) + b_{1,2}$ (*)
- $t_o < a_{1,2} t_b + b_{1,2}$
- $t_r > a_{1,2} t_b + b_{1,2}$
- $(t_o, t_b, t_r) = \text{data point}$
- Several data points are collected:
- Line corresponding to (*) must lie between the vertical intervals of each data point.
- Two lines indicate upper and lower bound.
- $a''_{1,2} \leq a_{1,2} \leq a'_{1,2}$
- $b''_{1,2} \leq b_{1,2} \leq b'_{1,2}$
- The more data points the tighter are the bounds.
- Problem
 - Estimation is computationally expensive and requires significant memory.
- Solution
 - Keep only data points contributing to the bounds
 - Problem: Optimal solution might not be found.



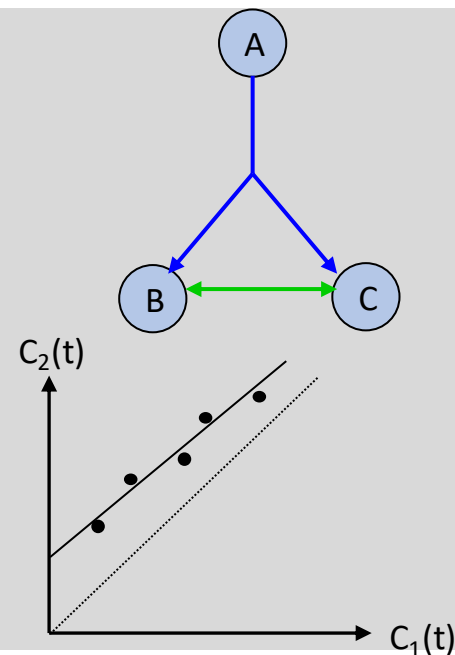
2. Synchronization Techniques

2.2 Reference Broadcast Synchronization

- Third party A transmits beacon message (without timestamp!) to neighbors.
- A may have unlimited power resources and reaches B, C, but not vice-versa!
- Neighbors timestamp the packet on reception and exchange timestamps.
- Neighbors can estimate the clock skew and clock drift using m beacons.
 - Each receiver i can calculate its offset to its neighbor j .

$$Offset_{i,j} = \frac{1}{m} \sum_{k=1}^m (T_{i,k} - T_{j,k})$$

- Averaging for offset estimation
 - Least square linear regression for offset/drift estimation
- Case Study
 - Mutual synchronization of a 30 nodes network in the range of $5 \mu s$



2. Synchronization Techniques

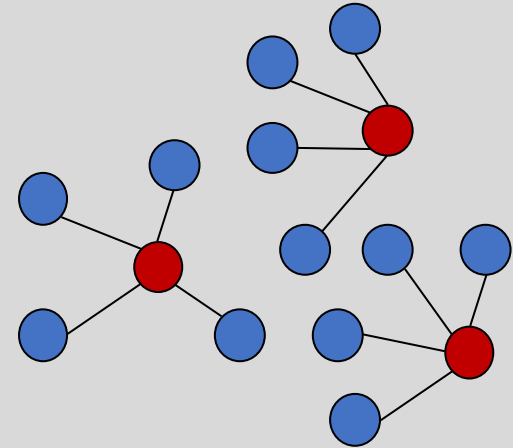
3. Synchronization of Multiple Nodes

- Typically, more than two nodes need to be synchronized.
 - Not all nodes to be synchronized can directly communicate to each other.
- Multi-hop synchronization approaches
- Out-of-band synchronization
 - Structured approaches
 - Clustering
 - Tree Construction
 - Unstructured approaches
 - Diffusion-based Synchronization
 - Gradient Clock Synchronization

2. Synchronization Techniques

3.1 Out-of-Band Synchronization

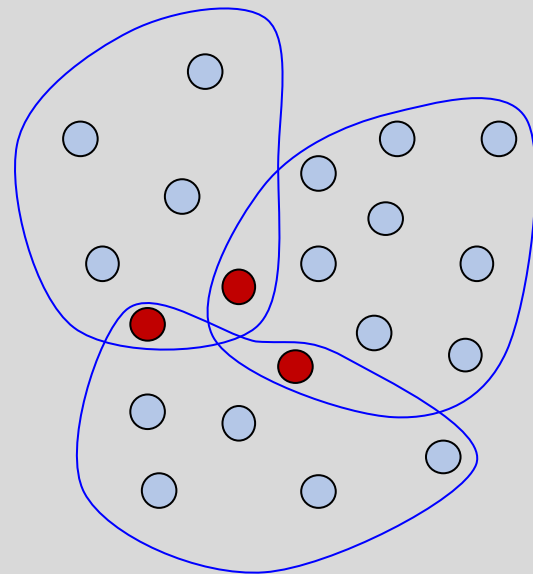
- Each node is connected to at least 1 **master**
- Masters are synchronized by out-of-band mechanisms, e.g., GPS.



2. Synchronization Techniques

3.2.1 Clustering

- All members of a **cluster** can synchronize, e.g., by reference broadcasting
- **Time gateways** belonging to different clusters can translate time-stamps between clusters.
- Tradeoff for cluster size
 - Many translations for small clusters
 - Higher energy consumption for large clusters
- Examples with RBS
 - Multi-Hop Synchronization
 - Time Routing in Multi-Hop Networks



2. Synchronization Techniques

3.2.1.1 Multi-Hop Synchronization with RBS

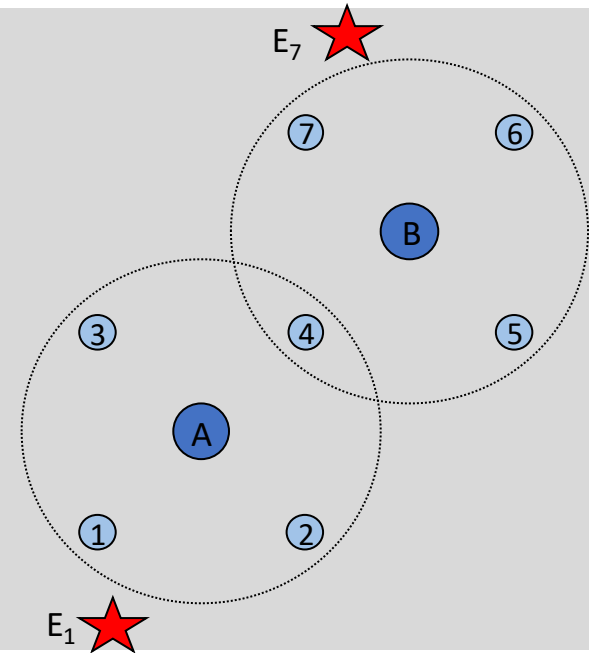
- Nodes A and B send synchronization beacons (pulses) P_A and P_B .
- Two events E_1 and E_7 are close to receivers 1 and 7.
- Receiver 1 observes E_1 2s after P_A .
- Receiver 7 observes E_7 4s prior to P_B .
- Receiver 4 observes P_A 10s after P_B .

$$E_1 = P_A + 2$$

$$E_7 = P_B - 4; E_7 + 4 = P_B$$

$$P_A = P_B + 10$$

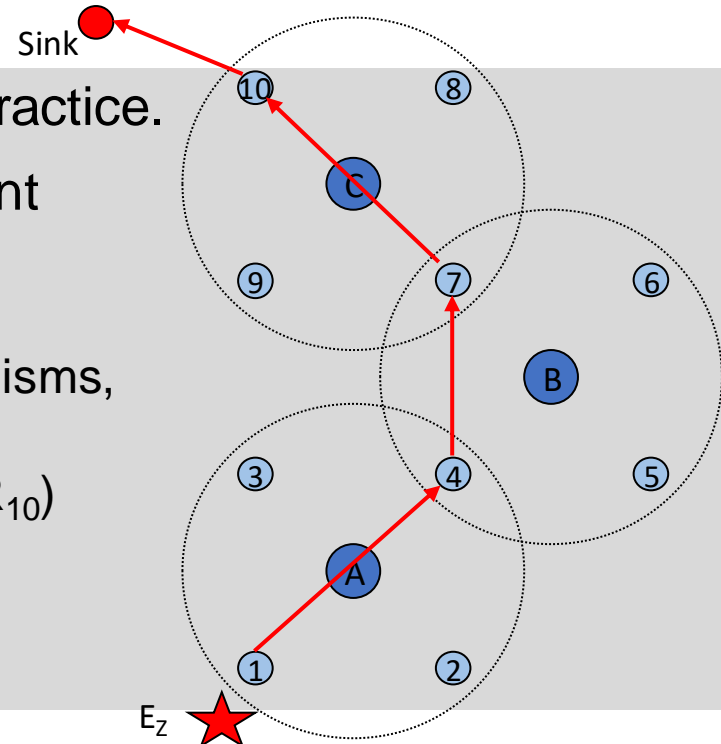
$$\begin{aligned} \rightarrow E_1 &= P_A + 2 = P_B + 10 + 2 \\ &= E_7 + 4 + 10 + 2 = E_7 + 16 \end{aligned}$$



2. Synchronization Techniques

3.2.1.2 Time Routing in Multi-Hop Networks with RBS

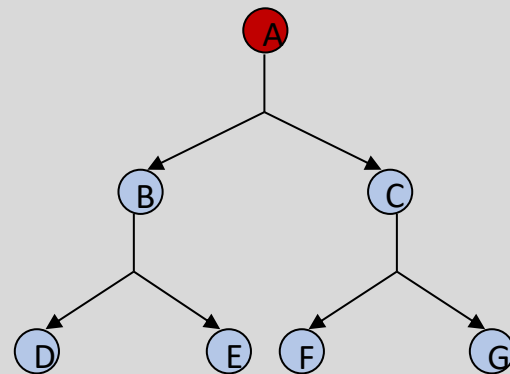
- Single time gateways are not desirable in practice.
- Approach: Dynamic time route establishment
 - Each node can convert time relationships (drift and offset).
 - Time route can be set up by routing mechanisms, e.g., shortest path routing
 - Example: $E_Z(R_1) \rightarrow E_Z(R_4) \rightarrow E_Z(R_7) \rightarrow E_Z(R_{10})$



2. Synchronization Techniques

3.2.2 Tree Construction

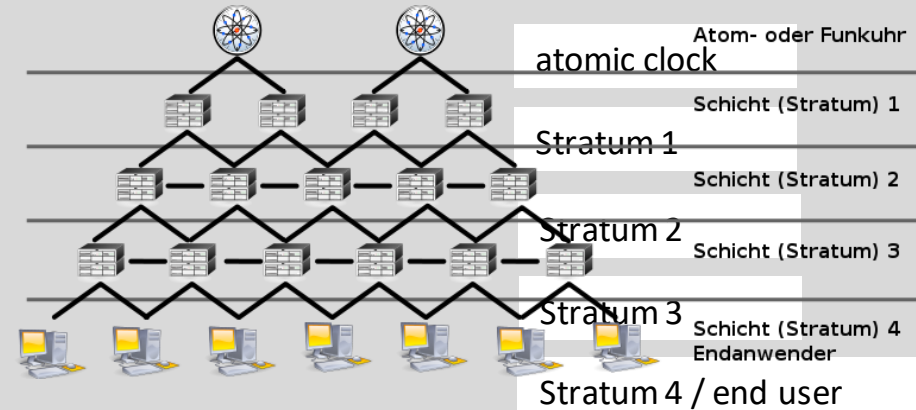
- Synchronization tree with master as the root
- Single-hop synchronization along tree
- Accuracy degrades with distance from root.
- Low tree level desired, but puts burden to nodes in order to synchronize other nodes.
- Tree formation is difficult in dynamic environments.
- Example: Timing-Sync Protocol for Sensor Networks



2. Synchronization Techniques

3.2.2.1.1 Timing-Sync Protocol for Sensor Networks

- TPSN inspired by Network Time Protocol
- NTP
 - Global time is injected to the network by time servers (Stratum 1).
 - Stratum 1 servers are synchronized in an out of band manner by atomic clocks (Stratum 0).
 - Nodes form a hierarchy. Stratum 1 server list publicly available at <http://support.ntp.org>.

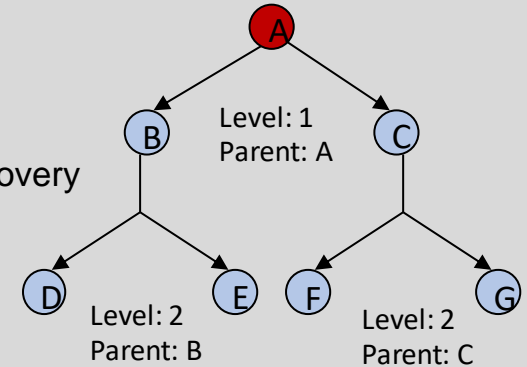


2. Synchronization Techniques

3.2.2.1.2 Timing-Sync Protocol for Sensor Networks

Protocol Steps

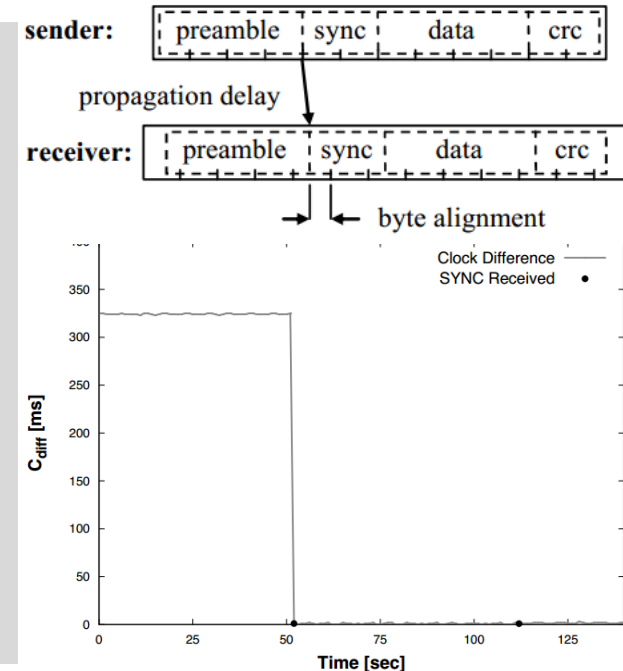
- Level Discovery
 - Root node on level 0 broadcasts Level_Discovery packet.
 - Neighbors assign level 1 and rebroadcast
 - ...
- Synchronization
 - Pair wise synchronization along hierarchy established during level discovery
 - Root node sends Time_sync packet.
 - Nodes back off randomly to avoid collisions and start message exchange (round trip synchronization).
 - Level $n+1$ nodes adapt clock to level n nodes.
- Implementation on MICA motes results in synchronization errors $< 20 \mu\text{s}$.



2. Synchronization Techniques

3.2.2.2 Flooding Time-Synchronization Protocol

- Node with lowest ID is used to synchronize the network as a leader.
- A leader periodically floods the network with a synchronization message including the leader's current time (time stamp, recorded on MAC level).
- Nodes record time stamp of message and time of arrival.
- Nodes rebroadcast after updating the time stamp.
- Linear regression (typically with 8 data points) for estimating offset and rate difference to leader.
- Experiments with motes: $< 2 \mu\text{s}$ synchronization error per node pair, synchronization messages every 30 s.



2. Synchronization Techniques

3.3 Unstructured Approaches

- Unstructured approaches do not establish a certain structure, but exchange time information between nodes that can communicate with each other.
- Completely localized solution
- Often: time information exchange using piggy-backing
→ very low overhead

Examples:

- Diffusion-based Synchronization
- Gradient Clock Synchronization

2. Synchronization Techniques

3.3.1 Diffusion-based Synchronization

Rate-based Synchronous Diffusion

- achieves global synchronization, convergence takes longer in larger networks
- Diffusion rate r_{ij} , $\sum_{j \neq i} r_{ij} \leq 1$, r_{ij} random

```
for each sensor node  $n_i$  in the network {  
  exchange clock time with  $n_i$ 's neighbors  
  for each neighbor  $n_j$  {  
     $c_i := \text{time of } n_i$ ;  $c_j := \text{time of } n_j$   
     $c_j := c_j + r_{ij} (c_i - c_j);$   
  }  
   $c_i := c_i - \sum_{\text{all } n_j} r_{ij} \cdot (c_i - c_j);$ 
```

Asynchronous Diffusion

- achieves global synchronization; convergence takes longer in larger networks

```
for each node  $n_i$  with uniform  
  probability {  
    ask clock readings from  $n_i$ 's  
    neighbors;  
    average clock readings;  
    send back new value to  
    neighbors;  
  }
```

2. Synchronization Techniques

3.3.2 Gradient Clock Synchronization

- Definitions
 - Hardware clock H_i with rate h_i and offset Φ
 - Logical clock L_i with rate l_i and offset θ
- Goal: precise time synchronization among neighbors
- No adaptation of hardware clock, but of logical clock (rate and offset), e.g., implemented by software timer
- No adaptation to reference clock, but completely distributed algorithm
- Nodes periodically broadcast L_i , l_i
- Evaluation on motes: 4 μ s synchronization error between neighbors with 30 s synchronization interval

$$H_i(t) = \int_{t_0}^t h_i(\tau) d\tau + \phi_i(t_0)$$

$$1 - \rho \leq h(t) \leq 1 + \rho$$

$$L_i(t) = \int_{t_0}^t h_i(\tau) \cdot l_i(\tau) d\tau + \theta_i(t_0)$$

$$l_i(t_{k+1}) = \frac{\left(\sum_{j \in N_i} l_j(t_k) \right) + l_i(t_k)}{|N_i| + 1}$$

$$\theta(t_{k+1}) = \theta(t_k) + \frac{\left(\sum_{j \in N_i} L_j(t_k) \right) + L_i(t_k)}{|N_i| + 1}$$

Thanks

for Your Attention

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