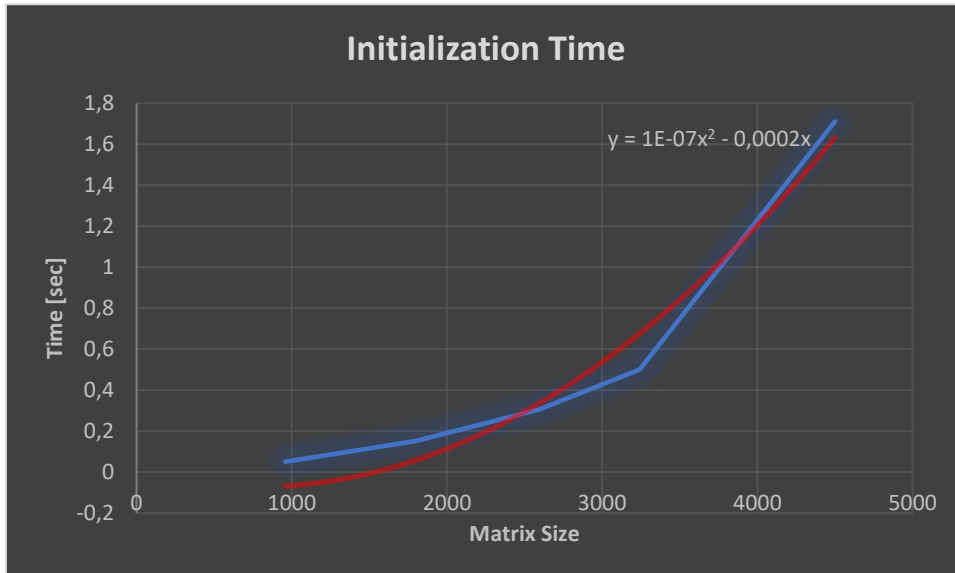


### 3.1 Computation of Sequential References Times

#### 3.2.1 Initialization Time

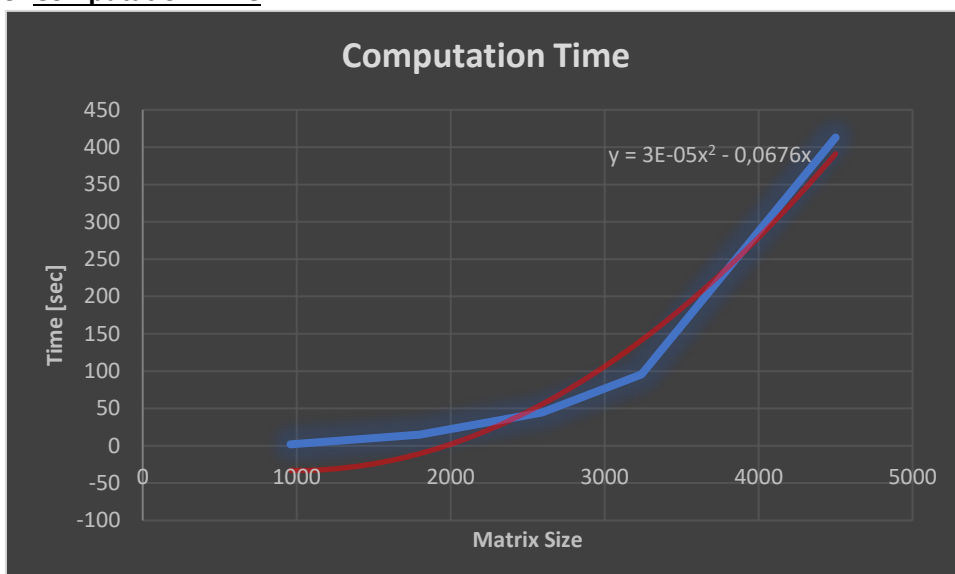


| Matrix Size | Initialization Time [sec] |
|-------------|---------------------------|
| 960         | 0,0512                    |
| 1800        | 0,1524                    |
| 2592        | 0,3056                    |
| 3240        | 0,5004                    |
| 4500        | 1,7108                    |

#### 3.2.2 Sending Time

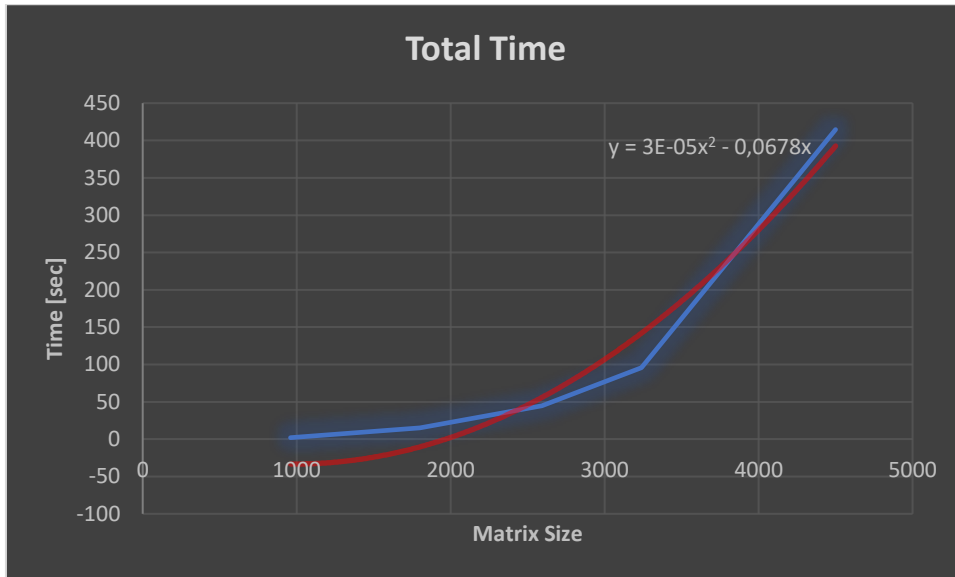
There is no sending in the sequential procedure.

#### 3.2.3 Computation Time



| Matrix Size | Computation Time [sec] |
|-------------|------------------------|
| 960         | 1,9536                 |
| 1800        | 14,824                 |
| 2592        | 44,4602                |
| 3240        | 95,3732                |
| 4500        | 412,9508               |

### 3.2.4 Total Time



| Matrix Size | Total Time [sec] |
|-------------|------------------|
| 960         | 2,0048           |
| 1800        | 14,9764          |
| 2592        | 44,7658          |
| 3240        | 95,8736          |
| 4500        | 414,6616         |

### 3.2 Computation of Parallel Times

#### 3.2.1 Tables

##### i. 4 Workers

| Matrix Size | Initialization Time | Sending Time | Computation Time | Total Time |
|-------------|---------------------|--------------|------------------|------------|
| 1260        | 0,9044              | 2,117        | 0,7096           | 3,731      |
| 1728        | 0,9258              | 3,3672       | 1,6556           | 5,9486     |
| 2520        | 1,0348              | 6,2454       | 4,7676           | 12,0478    |
| 4140        | 0,9828              | 15,2366      | 17,433           | 33,6524    |
| 5040        | 0,9836              | 21,0324      | 30,8148          | 52,8308    |

##### ii. 12 Workers

| Matrix Size | Initialization Time | Sending Time | Computation Time | Total Time |
|-------------|---------------------|--------------|------------------|------------|
| 1260        | 0,96                | 2,3982       | 0,3472           | 3,7054     |
| 1728        | 0,9906              | 3,7224       | 0,5726           | 5,2856     |
| 2520        | 1,0596              | 7,5266       | 1,375            | 9,9612     |
| 4140        | 1,137               | 22,0286      | 6,031            | 29,1966    |
| 5040        | 1,0064              | 36,1374      | 11,463           | 48,6068    |

##### iii. 20 Workers

| Matrix Size | Initialization Time | Sending Time | Computation Time | Total Time |
|-------------|---------------------|--------------|------------------|------------|
| 1260        | 1,0746              | 2,9          | 0,4156           | 4,3902     |
| 1728        | 1,1022              | 4,4074       | 0,5536           | 6,0632     |
| 2520        | 1,1694              | 8,2476       | 1,0502           | 10,4672    |
| 4140        | 1,2338              | 23,013       | 3,508            | 27,7548    |
| 5040        | 1,124               | 41,1854      | 6,584            | 48,8934    |

##### iv. 28 Workers

| Matrix Size | Initialization Time | Sending Time | Computation Time | Total Time |
|-------------|---------------------|--------------|------------------|------------|
| 1260        | 1,1558              | 3,4254       | 0,4944           | 5,0756     |
| 1728        | 1,1356              | 4,7834       | 0,6216           | 6,5406     |
| 2520        | 1,2372              | 8,7378       | 1,0696           | 11,0446    |
| 4140        | 1,3608              | 26,7766      | 2,8848           | 31,0222    |
| 5040        | 1,1138              | 40,0966      | 4,9106           | 46,121     |

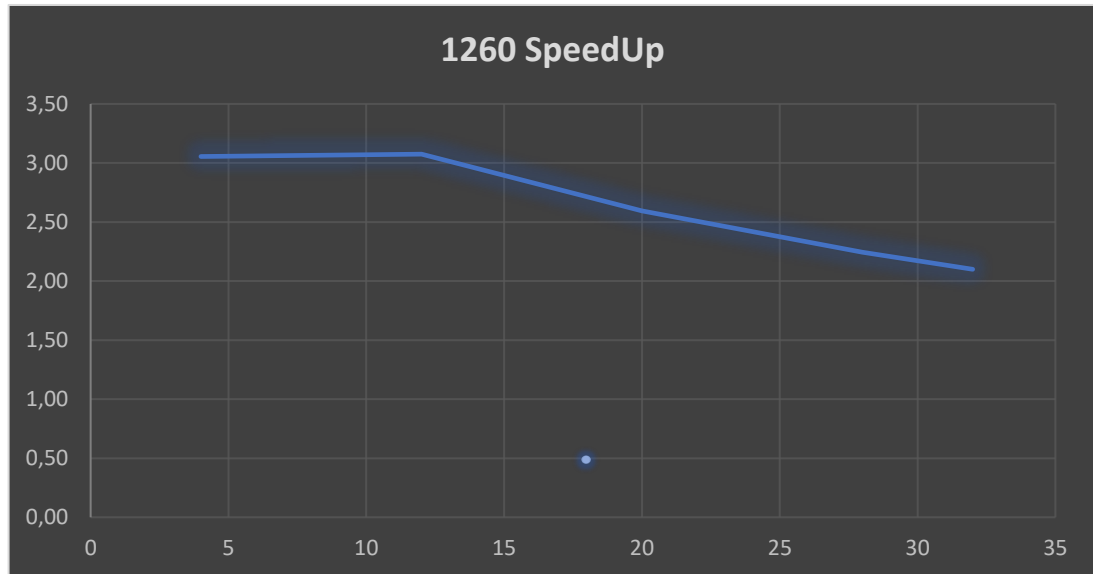
##### v. 32 Workers

| Matrix Size | Initialization Time | Sending Time | Computation Time | Total Time |
|-------------|---------------------|--------------|------------------|------------|
| 1260        | 1,129               | 3,7532       | 0,5434           | 5,4256     |
| 1728        | 1,1398              | 5,157        | 0,6818           | 6,9786     |
| 2520        | 1,2244              | 9,2518       | 1,0472           | 11,5234    |
| 4140        | 1,3154              | 28,3296      | 3,9762           | 33,6212    |
| 5040        | 1,1632              | 41,6344      | 5,6076           | 48,4052    |

### 3.2.2 Plots

#### i. Matrix Size 1260

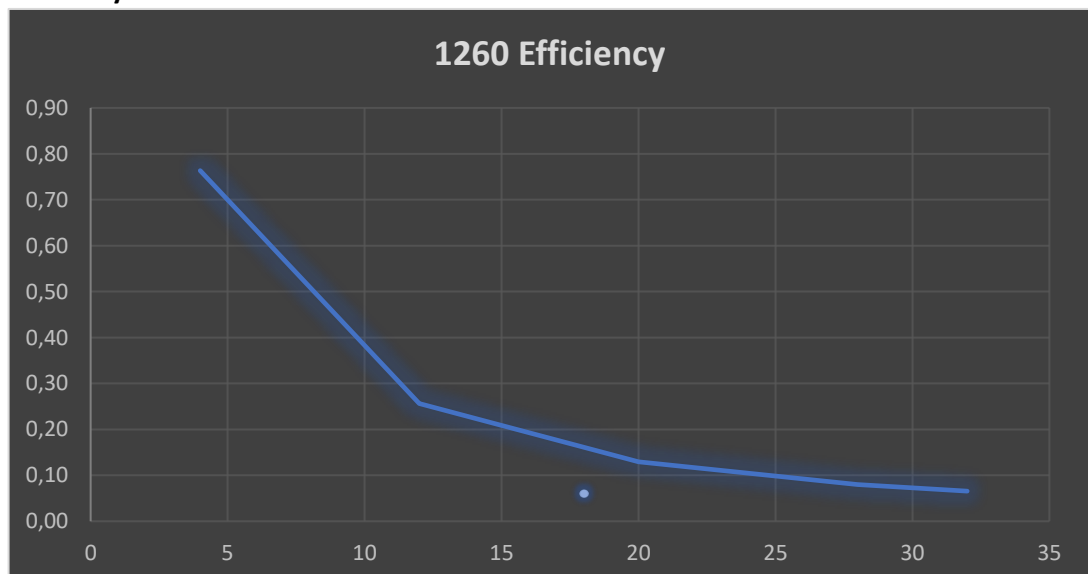
##### a. SpeedUp



We can see that the SpeedUp in the beginning is approximately constant but when using more workers it is lessened. This is because the sending time increases the more workers are used which is negatively influencing the total time for the computation as well as the speedup.

Therefore when the matrix size is small it is better to use few workers, because otherwise the communication between the workers takes too much time in comparison to the actual computation time.

##### b. Efficiency

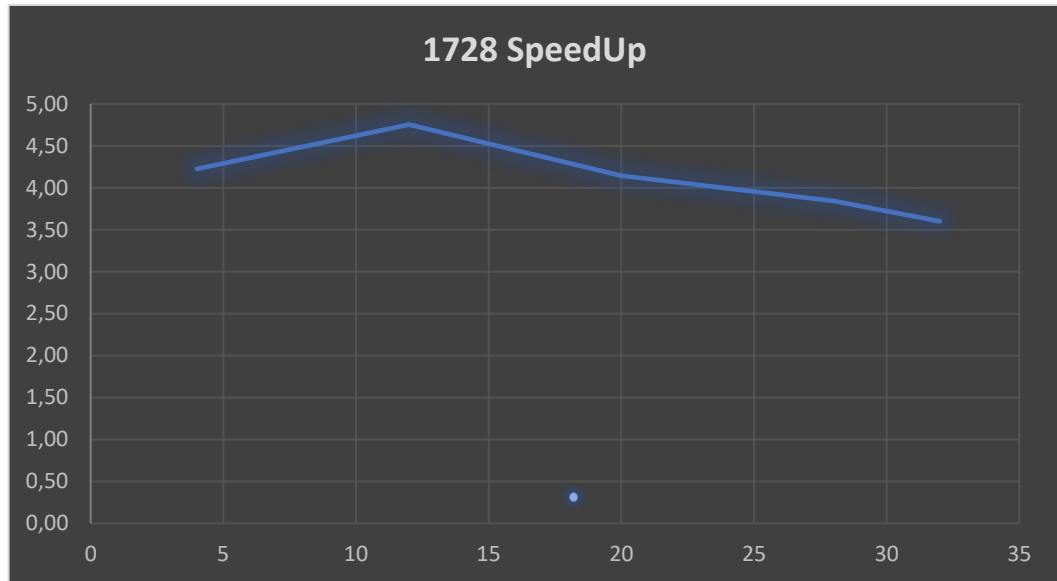


When looking at the efficiency plot it is obvious that less workers are more efficient than when using a lot of workers. This is mainly because when more workers are working on the same task they have to synchronize and eventually wait for each other, therefore if the speedup is not significantly increased the more workers are added the less efficient one worker would be.

In this example even when using 4 workers, one worker would not reach the efficiency of one worker.

## ii. Matrix Size 1728

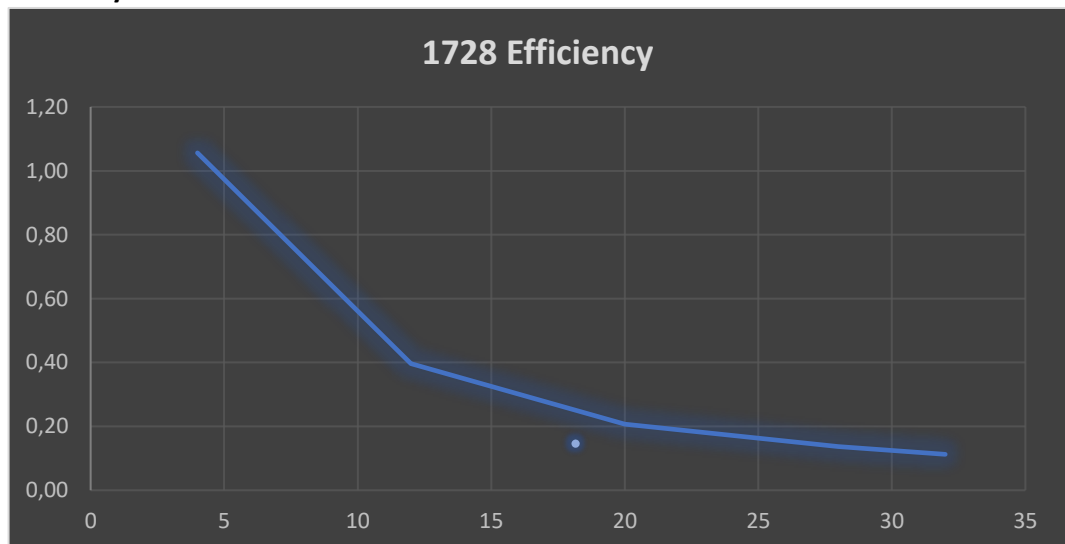
### a. SpeedUp



We can see that the SpeedUp in the beginning is increasing but when using more workers it is lessened. This is because the sending time increases the more workers are used which is negatively influencing the total time for the computation as well as the speedup.

Therefore for this matrix size it is faster when using 12 workers. When using 20 workers the communication takes too much time, but when using 4 workers each of them still needs to do plenty of work.

### b. Efficiency

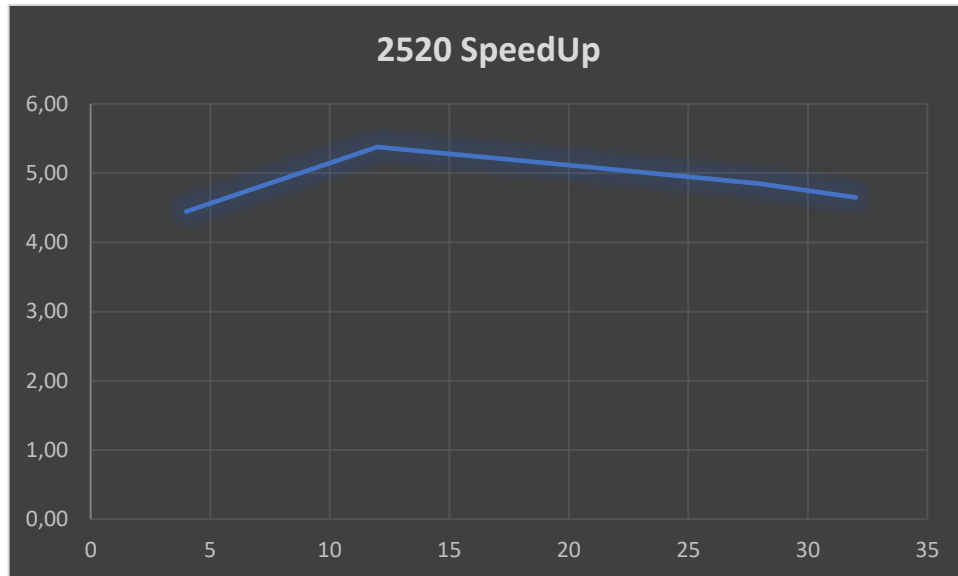


When looking at the efficiency plot it is obvious that less worker are more efficient than when using a lot of workers. This is mainly because when more workers are working on the same task they have to synchronize and eventually wait for each other, therefore if the speedup is not significantly increased the more workers are added the less efficient one worker would be.

In this example when using 4 workers, one of them is nearly as efficient as when using one worker.

### iii. Matrix Size 2520

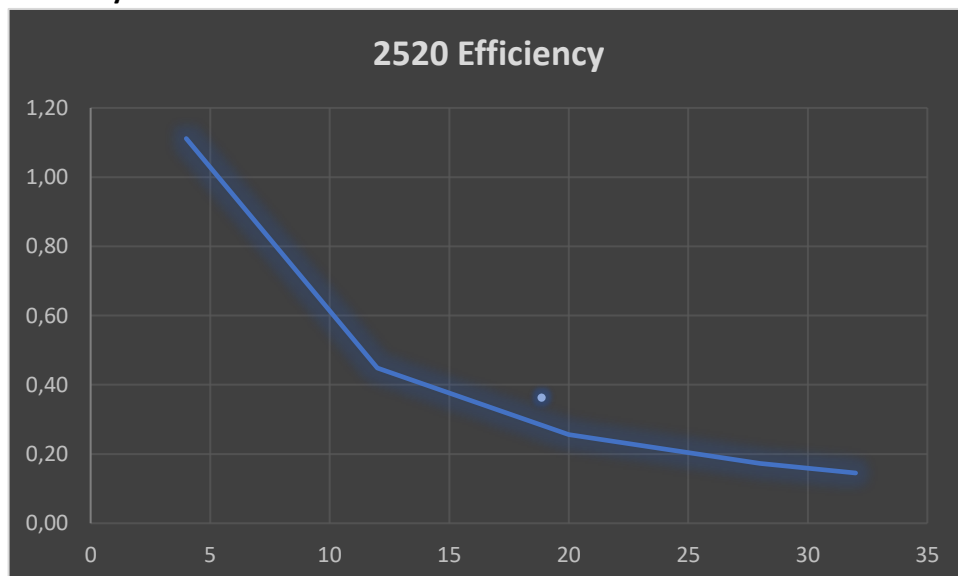
#### a. SpeedUp



We can see that the SpeedUp in the beginning is increasing but when using more workers it is lessened. This is because the sending time increases the more workers are used which is negatively influencing the total time for the computation as well as the speedup.

Therefore for this matrix size it is faster when using 12 workers. When using 20 workers the communication takes too much time, but when using 4 workers each of them still needs to do plenty of work.

#### b. Efficiency



When looking at the efficiency plot it is obvious that less worker are more efficient than when using a lot of workers. This is mainly because when more workers are working on the same task they have to synchronize and eventually wait for each other, therefore if the speedup is not significantly increased the more workers are added the less efficient one worker would be.

In this example when using 4 workers, one of them is slightly more efficient as when using one worker.

#### iv. Matrix Size 4140

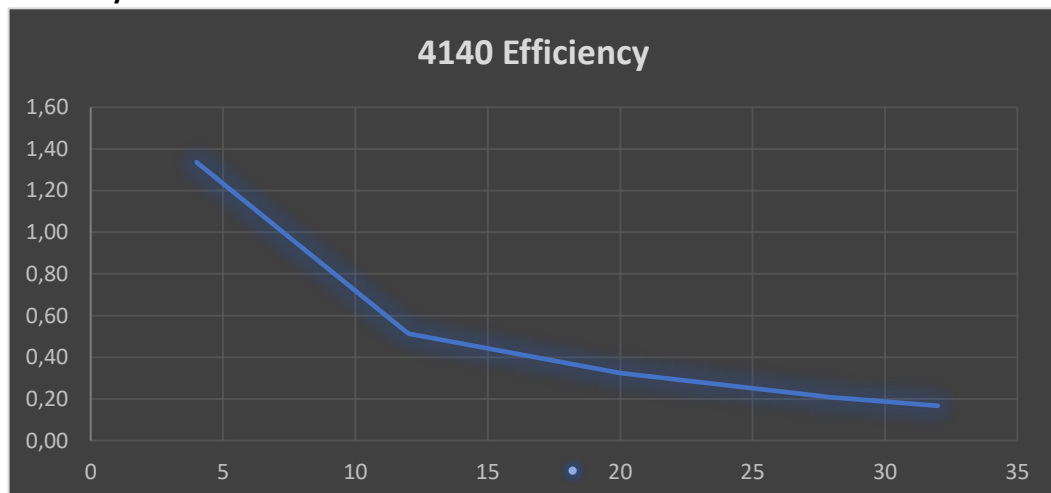
##### a. SpeedUp



For the matrix size of 4140 it is faster when using 20 workers because the sending time is not so significant but for less workers there is still a huge amount of work to do. When using more workers the sending time is too significant to be efficient and the speedup decreases.

Therefore for this matrix size 20 workers are optimal because a size 4140 leads to a huge amount of work.

##### b. Efficiency

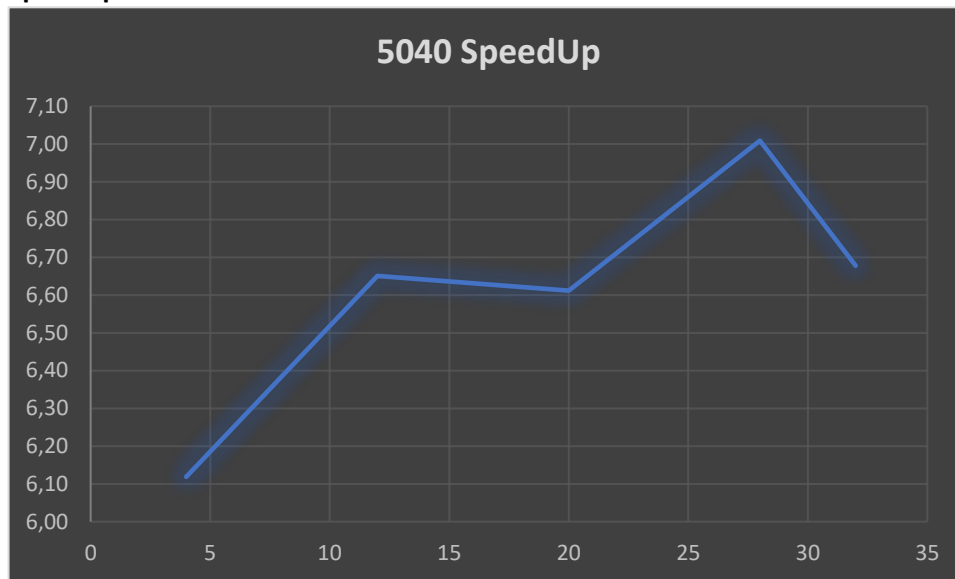


When looking at the efficiency plot it is obvious that less worker are more efficient than when using a lot of workers. This is mainly because when more workers are working on the same task they have to synchronize and eventually wait for each other, therefore if the speedup is not significantly increased the more workers are added the less efficient one worker would be.

In this example when using 4 workers, one of them is significantly more efficient as when using one worker.

**v. Matrix Size 5040**

**a. SpeedUp**



For the matrix size of 5040 it is faster to use 28 workers because it is a lot of work to compute the result. When using 32 workers the sending time gets too significant so that the speedup decreases.

Therefore for a huge amount of work it is better to have more workers because the sending time does not affect the speedup as much anymore.

The decrease of the speedup when using 20 workers could be due to some delay while sending between the workers.

**b. Efficiency**



When looking at the efficiency plot it is obvious that less worker are more efficient than when using a lot of workers. This is mainly because when more workers are working on the same task they have to synchronize and eventually wait for each other, therefore if the speedup is not significantly increased the more workers are added the less efficient one worker would be.

In this example when using 4 workers, one of them is nearly as efficient as one and a half workers.