

# Problem Set 7

*Computer Vision*  
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## 1 Registration, Outlier Rejection

In image registration the corresponding point coordinates are related by homography,  $\lambda p' = Hp$ , where  $p = (x, y, 1)$  and  $p' = (x', y', 1)$  are the coordinates on image  $I$  and  $I'$ . Note that  $H$  is equivalent to  $H' = \beta H$  for any  $\beta > 0$  because all equations can be satisfied by multiplying  $\lambda$  for all matching points by an appropriate number. It is therefore justified to set  $\|H\| = 1$  for its estimation. Estimate  $H$  by eliminating  $\lambda$  and writing the equations in an appropriate linear system, where the entries of  $H$  are the unknowns. Solve the system by enforcing  $\|H\| = 1$ . What is the minimum number of correspondences needed?

## 2 Interest Points

Consider the following two images:

$$I^1 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1(*) & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 1 \\ 0 & 0 & 0 & 1(**) & 1 & 1 \end{bmatrix}, \quad I^2 = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0.5(*) & 0.5 & 0.5 \\ 0 & 0 & 0 & 0.5 & 0.5 & 0.5 \\ 0 & 0 & 0 & 0.5(**) & 0.5 & 0.5 \end{bmatrix}. \quad (1)$$

1. Compute the Harris corner score at the points denoted with  $(*)$  and  $(**)$  using  $k = 0.05$ . Approximate the second moment matrix by averaging

over a  $3 \times 3$  neighborhood around the points. Moreover, for boundary pixels assign 0 to their gradients.

2. Use the Hessian detector for the same images of the previous exercise.