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CSE-DS D1
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DAA Exp :- 7

AIM: Experiment based on backtracking strategy: N-Queens problem

Algorithm:

If two queens are placed at position (i, j) and (k, l).

Then they are on same diagonal only if $(i - j) = k - l$ or $i + j = k + l$.

The first equation implies that $j - l = i - k$.

The second equation implies that $j - l = k - i$.

Therefore, two queens lie on the duplicate diagonal if and only if $|j-l|=|i-k|$

Place (k, i) returns a Boolean value that is true if the kth queen can be placed in column i.

x[] is a global array whose final k - 1 values have been set. Abs (r) returns the absolute value

of r.

Place (k, i)

```
{  
  For j ← 1 to k - 1  
  do if (x [j] = i) or (Abs (x [j] - i)) == (Abs (j - k))  
  then return false;  
  return true;  
}
```

N - Queens (k, n):

```
{  
  For i ← 1 to n  
  do if Place (k, i) then  
  {  
    x [k] ← i;  
    if (k == n) then  
      write (x [1....n]);  
    else  
      N - Queens (k + 1, n);  
  }  
}
```

Code :-

```
#include <stdio.h>  
#include <stdlib.h>  
#include <stdbool.h>  
#include <math.h>  
int *  
deepCopy (int *arr, int len)  
{  
  
  int *newarr = malloc (sizeof (int) * len);
```

```
for (int i = 0; i < len; i++)

newarr[i] = arr[i];

return newarr;

}
```

```
int *
printArray (int *arr, int len)
{

for (int i = 0; i < len; i++)

printf ("%8d", arr[i]);

printf ("\n");

}
```

```
typedef struct node
```

```
{

int *data;

struct node *next;

} *pnode;
```

```
typedef struct list
{
```

```
pnode head;
```

```
pnode tail;
```

```
int n;
```

```
} *plist;
```

```
void
addNodetoList (plist l, int *data)
{
```

```
if (l->head != NULL)
```

```
{
```

```
l->tail->next = malloc (sizeof (struct node));
```

```
l->tail = l->tail->next;
```

```
l->tail->next = NULL;
```

```

l->tail->data = data;

}

else

{

l->head = malloc (sizeof (struct node));

l->tail = l->head;

l->tail->next = NULL;

l->tail->data = data;

}
}
plist createList (int n)
{

plist l = malloc (sizeof (struct list));

l->head = NULL;

l->tail = NULL;

l->n = n;

return l;

}

typedef struct NQueensSolutions
{

int count;

plist solutions;           // linked list of solutions
} *pNQueensSolutions;

void
printSolutions (pNQueensSolutions sol)
{

int n = sol->solutions->n;

printf ("\n");

for (pnode temp = sol->solutions->head; temp != NULL; temp =
temp->next)

printArray (temp->data, n);

}

```

```

bool queenCanBePlaced (int n, int k, int pos, int *curr_board)

{

int a, b;

for (int i = 1; i < k; i++)

    {

a = abs (i - k);           // x1 - x2
    b = abs (curr_board[i - 1] - pos); // y1 - y2
    if (a == b || a == 0 || b == 0)

return false;

    }

return true;

}


void
placeKthQueen (int k, int n, int *curr_board, pNQueensSolutions
solutions)
{

for (int i = 1; i <= n; i++)

    {

if (queenCanBePlaced (n, k, i, curr_board))

        {

curr_board[k - 1] = i;

if (k == n)           // this is a complete solution
        {

addNodetoList (solutions->solutions,
deepCopy (curr_board, n)); // add a deep copy of current board to the list of solutions
        solutions->count++;

        }

        else           // place the next queen
        placeKthQueen (k + 1, n, curr_board, solutions);

        }

    }

}

```

```
}
```

```
pNQueensSolutions NQueens (int n)  
{
```

```
pNQueensSolutions nqs = malloc (sizeof (struct NQueensSolutions));
```

```
nqs->count = 0;
```

```
nqs->solutions = createList (n);
```

```
int curr_board[n];
```

```
curr_board[0] = 1;
```

```
placeKthQueen (1, n, curr_board, nqs);
```

```
return nqs;
```

```
}
```

```
int  
main ()  
{
```

```
int n;
```

```
printf ("Enter number of queens: ");
```

```
scanf ("%d", &n);
```

```
pNQueensSolutions sol = NQueens (n);
```

```
printf ("\nNumber of solutions: %d\n", sol->count);
```

```
if (sol->count > 0)
```

```
{
```

```
printf ("All solutions:");
```

```
printSolutions (sol);
```

```
}
```

```
}
```

OUTPUT:

The screenshot displays the OnlineGDB beta web interface. The left sidebar contains navigation links: IDE, My Projects, Classroom (new), Learn Programming, Programming Questions, Jobs (new), Sign Up, and Login. The main console area shows the following output:

```
Enter number of queens: 8
Number of solutions: 92
All solutions:
1 5 8 6 3 7 2 4
1 6 8 3 7 4 2 5
1 7 4 6 8 2 5 3
1 7 5 8 2 4 6 3
2 4 6 8 3 1 7 5
2 5 7 1 3 8 6 4
2 5 7 4 1 8 6 3
2 6 1 7 4 8 3 5
2 6 8 3 1 4 7 5
2 7 3 6 8 5 1 4
2 7 5 8 1 4 6 3
2 8 6 1 3 5 7 4
3 1 7 5 8 2 4 6
3 5 2 8 1 7 4 6
3 5 2 8 6 4 7 1
3 5 7 1 4 2 8 6
3 5 8 4 1 7 2 6
3 6 2 5 8 1 7 4
3 6 2 7 1 4 8 5
3 6 2 7 5 1 8 4
3 6 4 1 8 5 7 2
3 6 4 2 8 5 7 1
3 6 8 1 4 7 5 2
3 6 8 1 5 7 2 4
3 6 8 2 4 1 7 5
3 7 2 8 5 1 4 6
3 7 2 8 6 4 1 5
3 8 4 7 1 6 2 5
4 1 5 8 6 3 7 2
4 1 5 8 6 3 7 2
4 2 5 8 6 1 3 7
4 2 7 3 6 8 5 1
4 2 7 5 1 8 6 3
4 2 8 5 7 1 3 6
```

The bottom of the console shows the message: "...Program finished with exit code 0 Press ENTER to exit console.[]". The Windows taskbar at the bottom indicates the system time as 12:16 AM on 19-04-2023, with a temperature of 31°C and a "Smoke" status.