

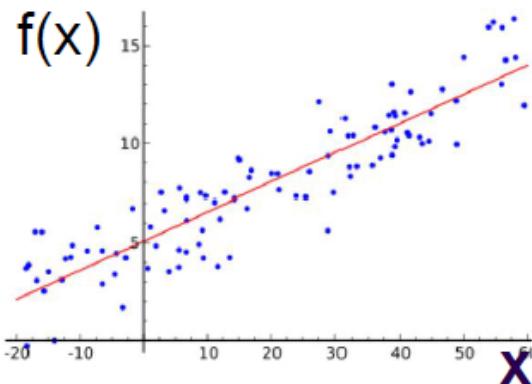
# INTRODUCTION TO DATA SCIENCE

11/12/2024

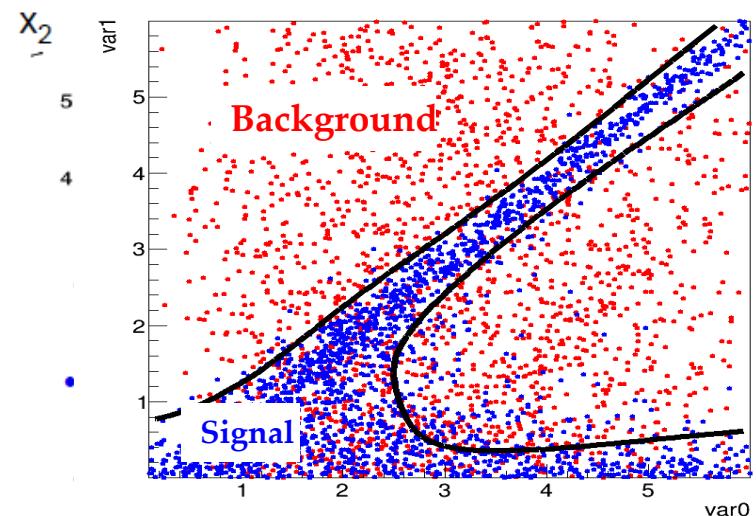
WFAiS UJ, Informatyka Stosowana  
I stopień studiów

# What are Multivariate Techniques

→ Many things ... starting from “linear regression” ...



to multivariate event classification



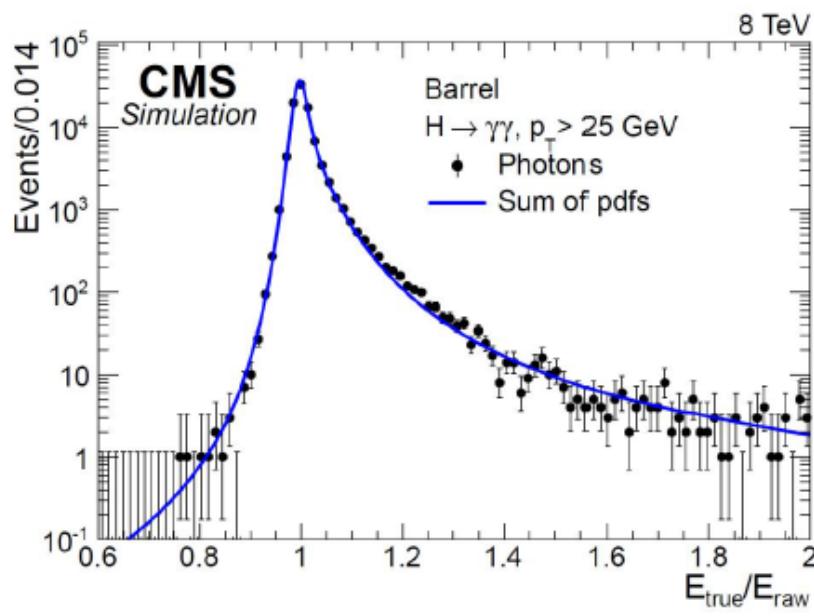
→ or w/o prior ‘analytic’ model

→ typically “multivariate”

- Parameters depend on the ‘joint distribution’  $f(x_1, x_2)$
- ‘learning from experience’ → known data points

# Machine Learning - Multivariate Techniques

- fitted (non-)analytic function may approximate:
  - target value → ‘regression’  
( e.g. calorimeter calibration/correction function)

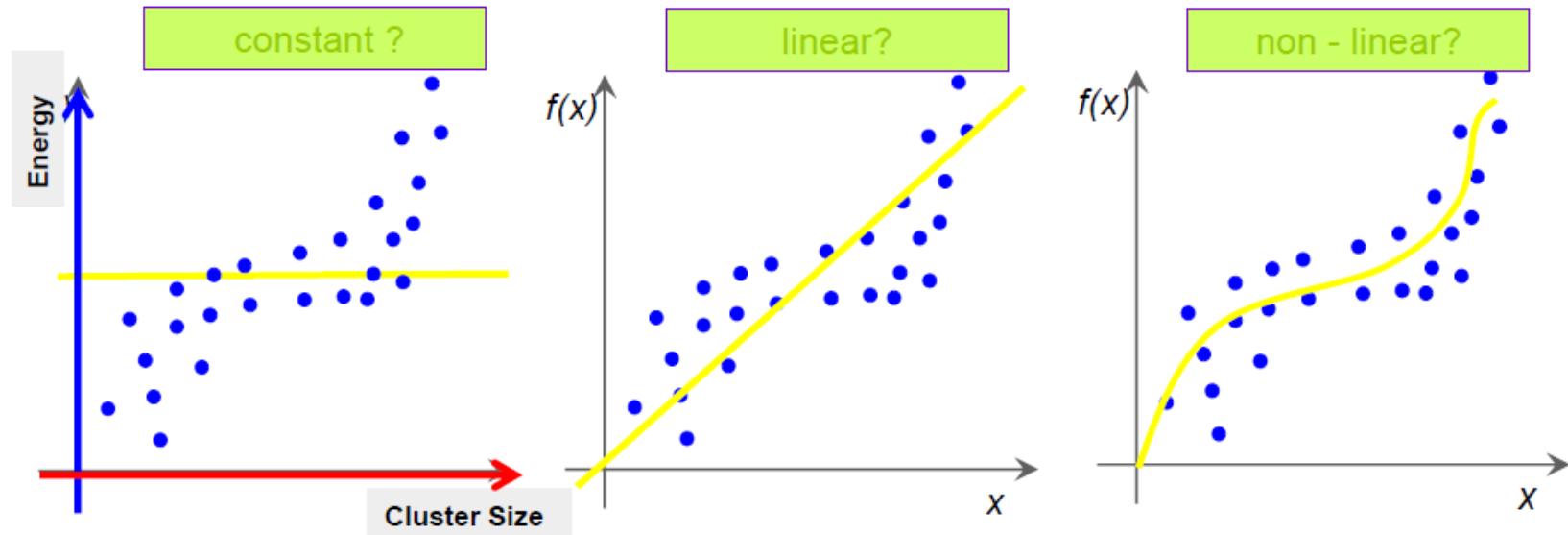


## MC sample: $\gamma + \text{jets}$

- Raw energy in crystals,  $\eta, \Phi$
- Cluster shape variables
- Local cluster position variables  
(energy leakage)
- Pile-up estimators
  - predict energy correction (i.e. parameters in crystal-ball: pdf for energy measurement)

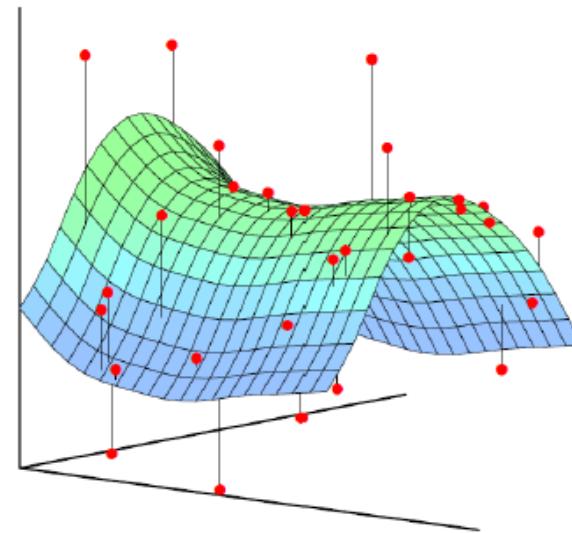
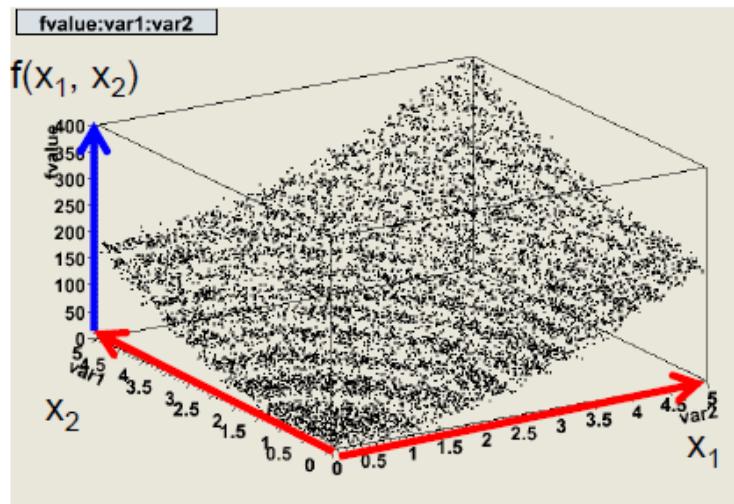
# Regression

- ‘known measurements’ → model “functional behaviour”
- e.g. : photon energy as function “D”-variables: ECAL shower parameters + ...



- known analytic model (i.e. nth -order polynomial) → Maximum Likelihood Fit)
- no model ?
  - “draw any kind of curve” and parameterize it?
- seems trivial ? → human brain has very good pattern recognition capabilities!
- what if you have **many** input variables?

# Regression -> model functional behaviour



- “standard” regression → fit a known analytic function
  - e.g.  $f(x) = ax_1^2 + bx_2^2 + c$
- BUT most times: don’t have a reasonable “model” ? → need something more general:
  - e.g. piecewise defined splines, kernel estimators, decision trees to approximate  $f(x)$

Note: we are not interested in the ‘fitted parameter(s)’, it is not: “Newton deriving  $F=ma$ ”  
→ just provide prediction of function values  $f(x)$  for new measurements  $x$

# Multi-Variate Classification

Consider events which can be either signal or background events.

Each event is characterized by  $n$  observables:

$$\vec{x} = (x_1, \dots, x_n) \quad \text{"feature vector"}$$

Goal: classify events as signal or background in an optimal way.

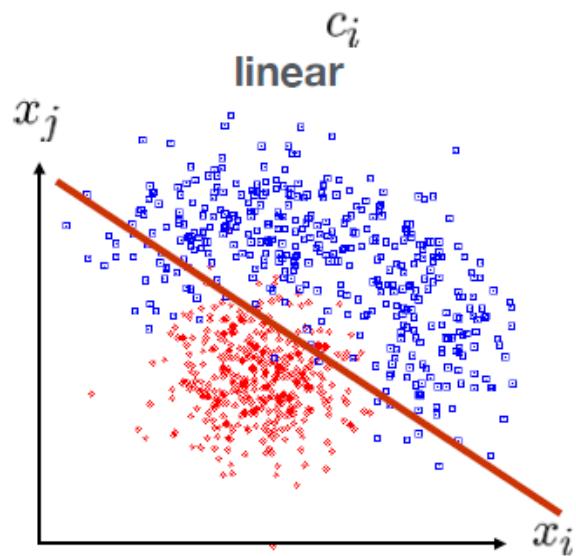
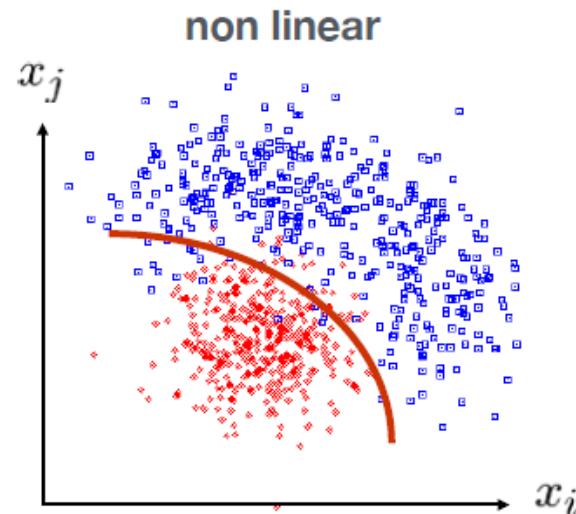
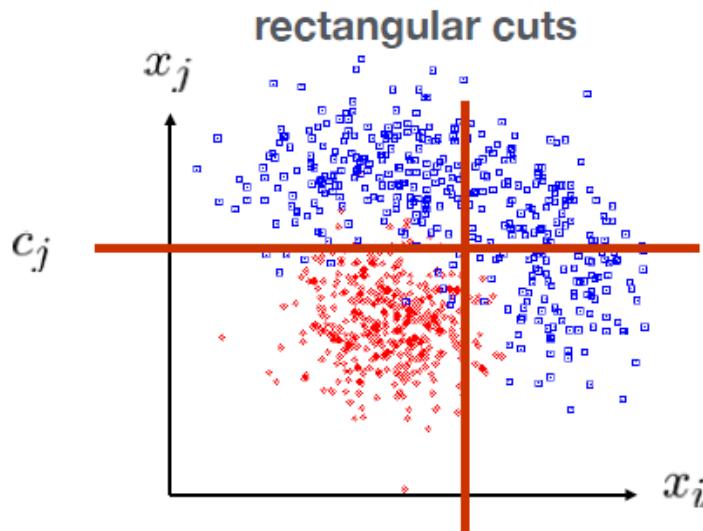
This is usually done by mapping the feature vector to a single variable, i.e., to scalar test statistic:

$$\mathbb{R}^n \rightarrow \mathbb{R} : \quad y(\vec{x})$$

A cut  $y > c$  to classify events as signal corresponds to selecting a potentially complicated hyper-surface in feature space. In general superior to classical "rectangular" cuts on the  $x_i$ .

Problem closely related to *machine learning (pattern recognition, data mining, ... )*

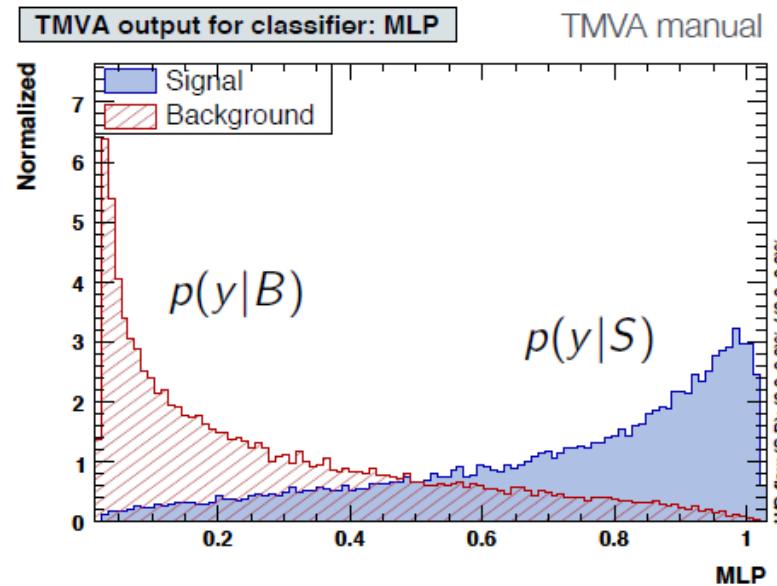
# Classification: Different Approaches



k-Nearest-Neighbor,  
Boosted Decision Trees,  
Multi-Layer Perceptrons,  
Support Vector Machines  
...

# Signal Probability Instead of Hard Decisions

Example: test statistic  $y$  for signal and background from a Multi-Layer Perceptron (MLP):



Instead of a hard yes/no decision one can also define the probability of an event to be a signal event:

$$P_s(y) \equiv P(S|y) = \frac{p(y|S) \cdot f_s}{p(y|S) \cdot f_s + p(y|B) \cdot (1 - f_s)}, \quad f_s = \frac{n_s}{n_s + n_b}$$

# Machine learning: Basic terminology

The goal of machine learning is to predict results based on incoming data.

**Features** (also parameters, or variables): these are the factors for a machine to look at. E.g.: cartesian coordinates, pixel colors, a car mileage, user's gender, stock price, word frequency in the text.

- Quantitative ( $x = \{1.02, 0.21, 0.12, 2\}$ )
- Qualitative *discrete* ( $x = \{\text{medium, small, large}\}$ ) or *categorical* ( $x=\{\text{red, blue, green}\}$ )

**Algorithms** (also models): Any problem can be solved in different ways. The method you choose affects the precision, performance, and size of the final model.

- If the data is insufficient/inappropriate (e.g. statistically limited or missing important features), even the best algorithm won't help. Pay attention to the accuracy of your results only when you have a good enough dataset.

# CLASSICAL MACHINE LEARNING

Data is pre-categorized or numerical

## SUPERVISED

Predict a category

### CLASSIFICATION

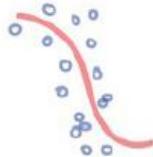
«Divide the socks by color»



Predict a number

### REGRESSION

«Divide the ties by length»



OUR FOCUS

Data is not labeled in any way

## UNSUPERVISED

Divide by similarity

### CLUSTERING

«Split up similar clothing into stacks»



Identify sequences

### ASSOCIATION

«Find what clothes I often wear together»



### DIMENSION REDUCTION (generalization)

«Make the best outfits from the given clothes»



Image credit: [https://vas3k.com/blog/machine\\_learning/](https://vas3k.com/blog/machine_learning/)

# Where are the neural networks?

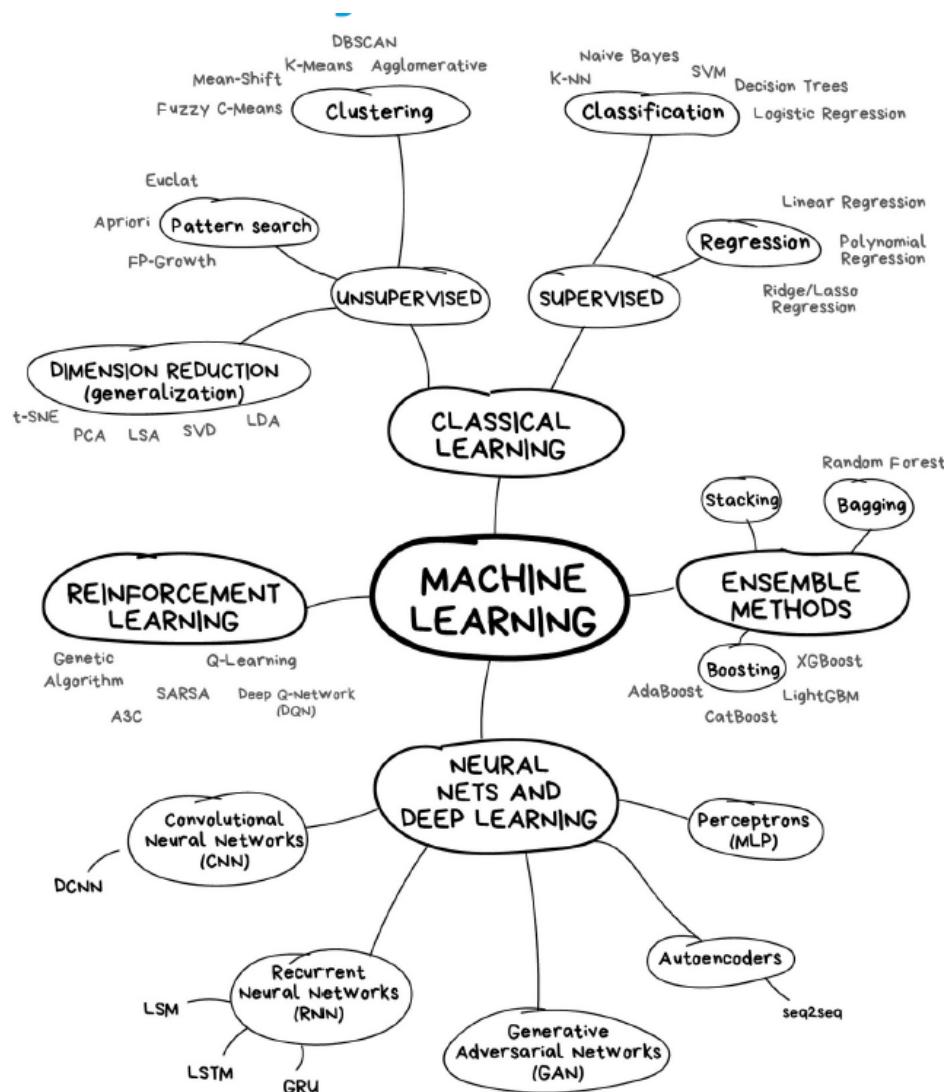


Image credit: [https://vas3k.com/blog/machine\\_learning/](https://vas3k.com/blog/machine_learning/)

# Neural Networks

Any neural network is a collection of **neurons** and **connections** between them.

**Neuron** is a function with a set of inputs and one output. Its task is to take all numbers from its input, apply a function on them and send the result to the output.

- Example: sum up all numbers from the inputs and if that sum is bigger than N give 1 as a result. Otherwise return zero.

**Connections** are like channels between neurons. They connect outputs of one neuron with the inputs of another so they can send digits to each other. Each connection has only one parameter the *weight*.

- These weights tell the neuron to respond more to one input and less to another. Weights are adjusted when training — that's how the network learns.

# Perceptron

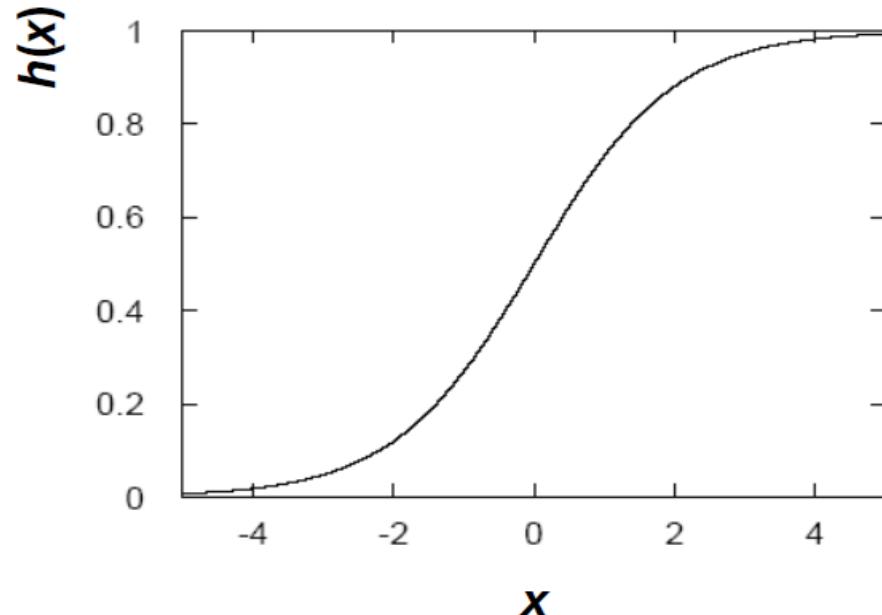
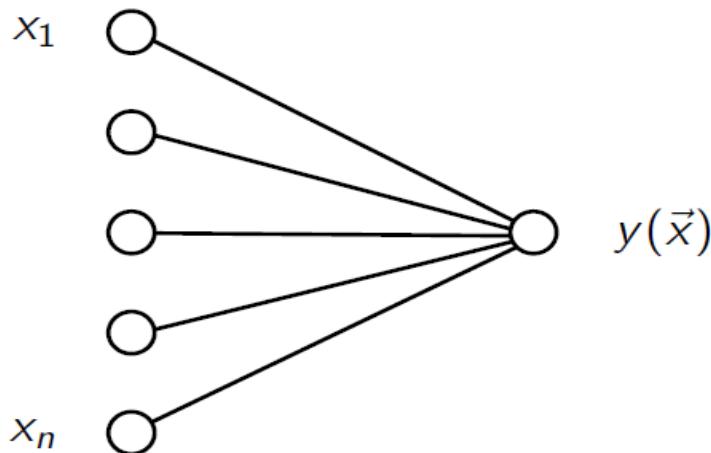
Discriminant:

$$y(\vec{x}) = h \left( w_0 + \sum_{i=1}^n w_i x_i \right)$$

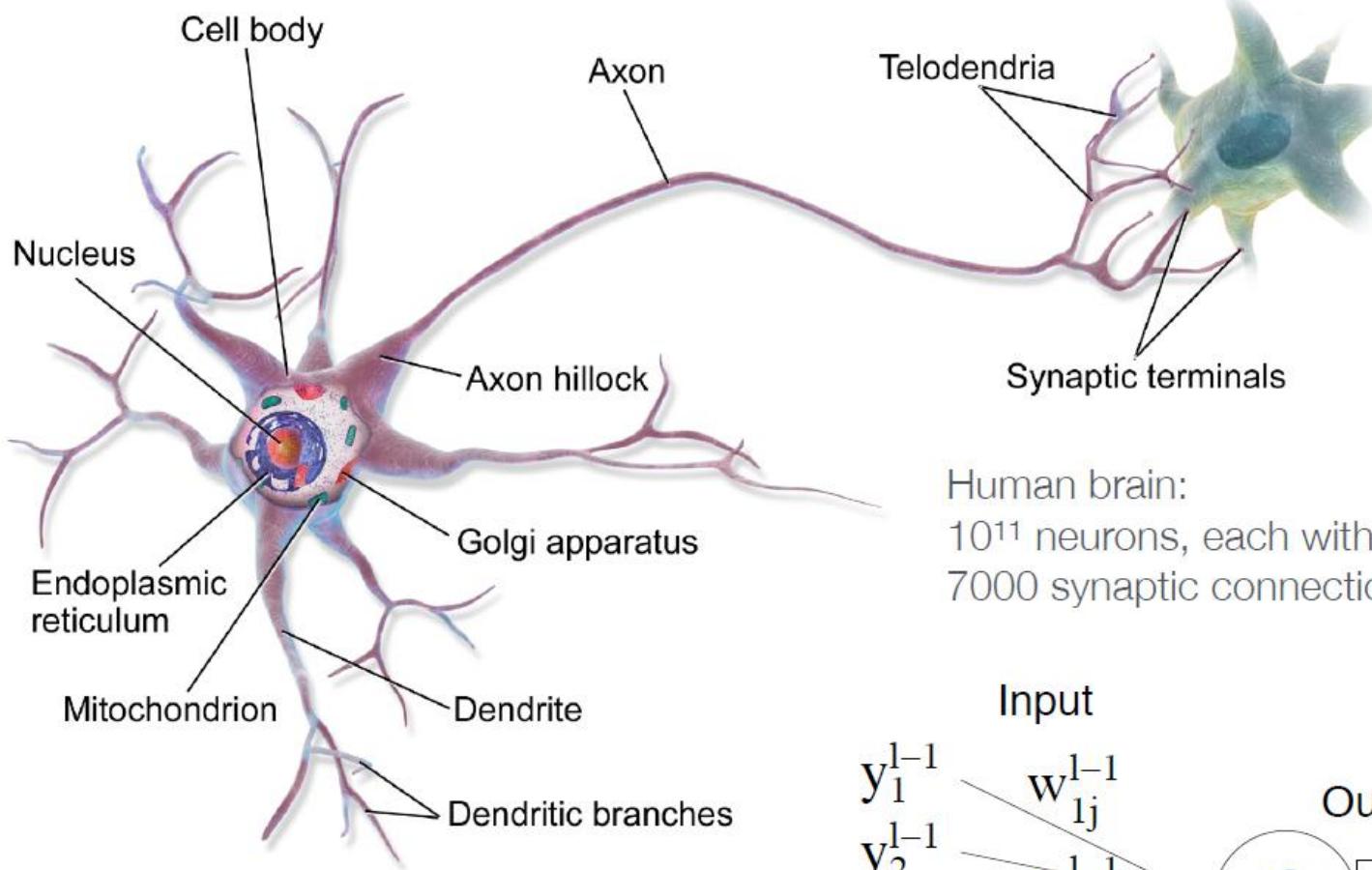
The nonlinear, monotonic function  $h$  is called *activation function*.

Typical choices for  $h$ :

$$\frac{1}{1 + e^{-x}} \text{ ("sigmoid")}, \quad \tanh x$$

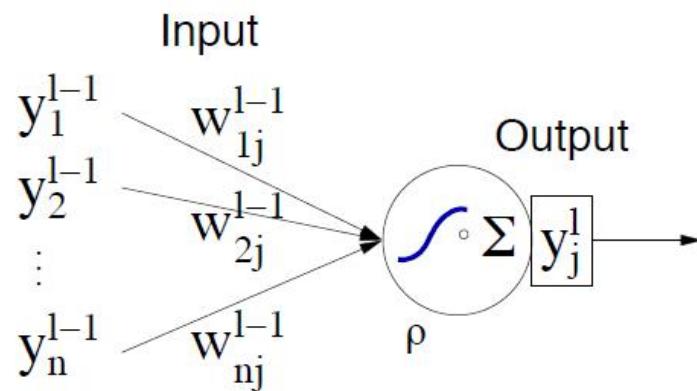


# The Biological Inspiration: the Neuron

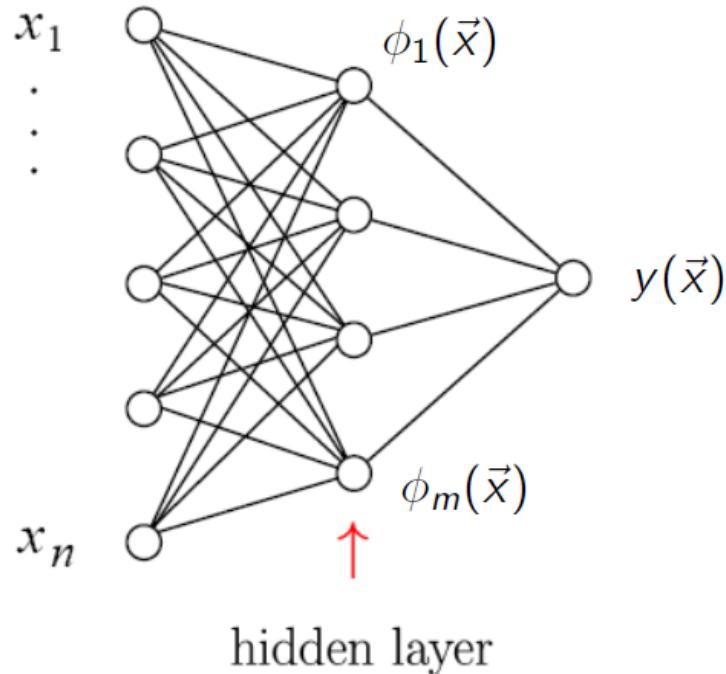


<https://en.wikipedia.org/wiki/Neuron>

Human brain:  
10<sup>11</sup> neurons, each with on average  
7000 synaptic connections



# Feedforward Neural Network with One Hidden Layer



superscripts indicates layer number

$$\phi_i(\vec{x}) = h \left( w_{i0}^{(1)} + \sum_{j=1}^n w_{ij}^{(1)} x_j \right)$$

$$y(\vec{x}) = h \left( w_{10}^{(2)} + \sum_{j=1}^m w_{1j}^{(2)} \phi_j(\vec{x}) \right)$$

Straightforward to generalize to multiple hidden layers

# Network Training

$\vec{x}_a$  : training event,  $a = 1, \dots, N$

$t_a$  : correct label for training event  $a$

\  
e.g.,  $t_a = 1, 0$  for signal and background, respectively

$\vec{w}$  : vector containing all weights

Error function:

$$E(\vec{w}) = \frac{1}{2} \sum_{a=1}^N (y(\vec{x}_a, \vec{w}) - t_a)^2 = \sum_{a=1}^N E_a(\vec{w})$$

Weights are determined by minimizing the error function.

# Backpropagation

Start with an initial guess  $\vec{w}^{(0)}$  for the weights and then update weights after each training event:

$$\vec{w}^{(\tau+1)} = \vec{w}^{(\tau)} - \eta \nabla E_a(\vec{w}^{(\tau)})$$

└── learning rate

Let's write network output as follows:

$$y(\vec{x}) = h(u(\vec{x})) \text{ with } u(\vec{x}) = \sum_{j=0}^m w_{1j}^{(2)} \phi_j(\vec{x}), \phi_j(\vec{x}) = h \left( \sum_{k=0}^n w_{jk}^{(1)} x_k \right) \equiv h(v_j(\vec{x}))$$

Here we defined  $\phi_0 = x_0 = 1$  and the sums start from 0 to include the offsets.

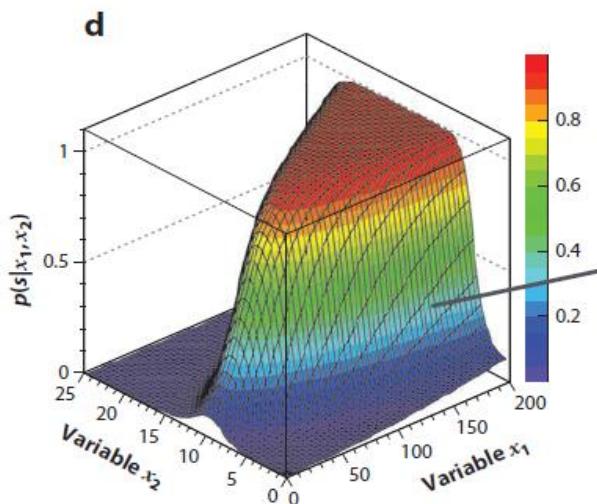
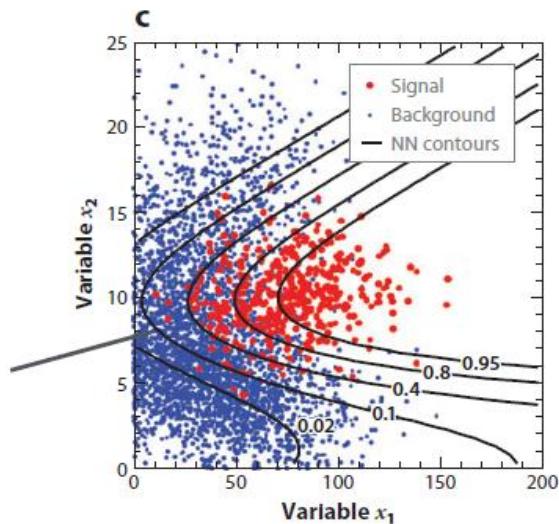
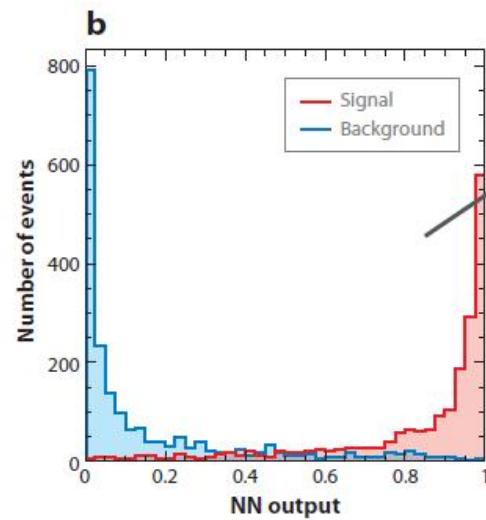
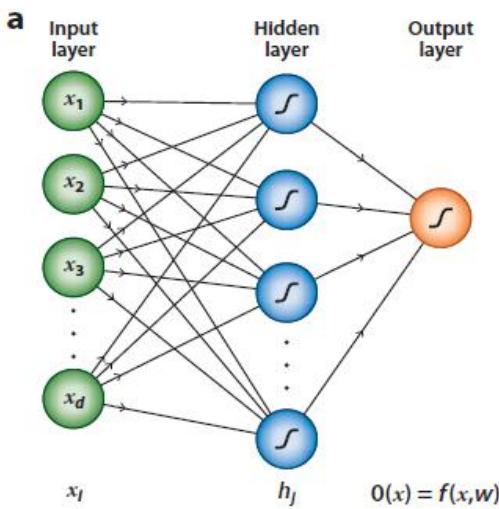
Weights from hidden layer to output:

$$E_a = \frac{1}{2}(y_a - t_a)^2 \rightarrow \frac{\partial E_a}{\partial w_{1j}^{(2)}} = (y_a - t_a)h'(u(\vec{x}_a)) \frac{\partial u}{\partial w_{1j}^{(2)}} = (y_a - t_a)h'(u(\vec{x}_a))\phi_j(\vec{x}_a)$$

Weights from input layer to hidden layer ( $\rightarrow$  further application of chain rule):

$$\frac{\partial E_a}{\partial w_{jk}^{(1)}} = (y_a - t_a)h'(u(\vec{x}_a))w_{1j}^{(2)}h'(v_j(\vec{x}_a))x_{a,k} \quad \vec{x}_a \equiv (x_{a,1}, \dots, x_{a,n})$$

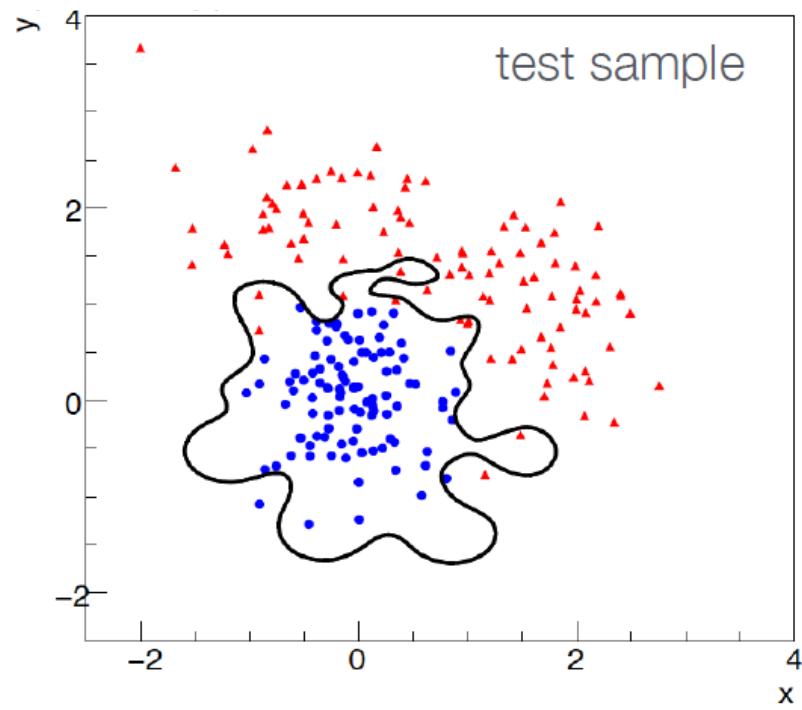
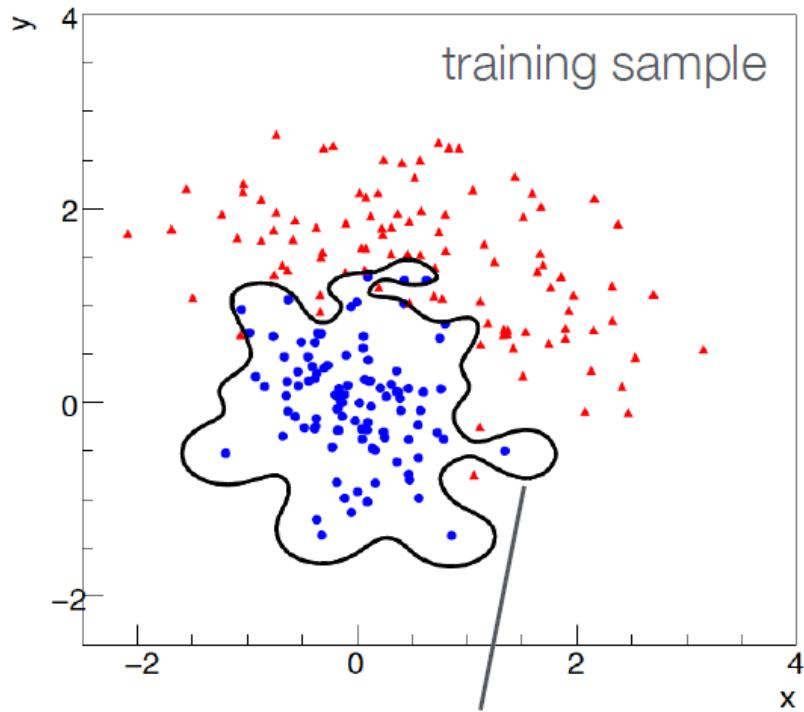
# Neural Network Output and Decision Boundaries



decision  
boundaries  
for different  
cuts on NN  
output

# Example of Overtraining

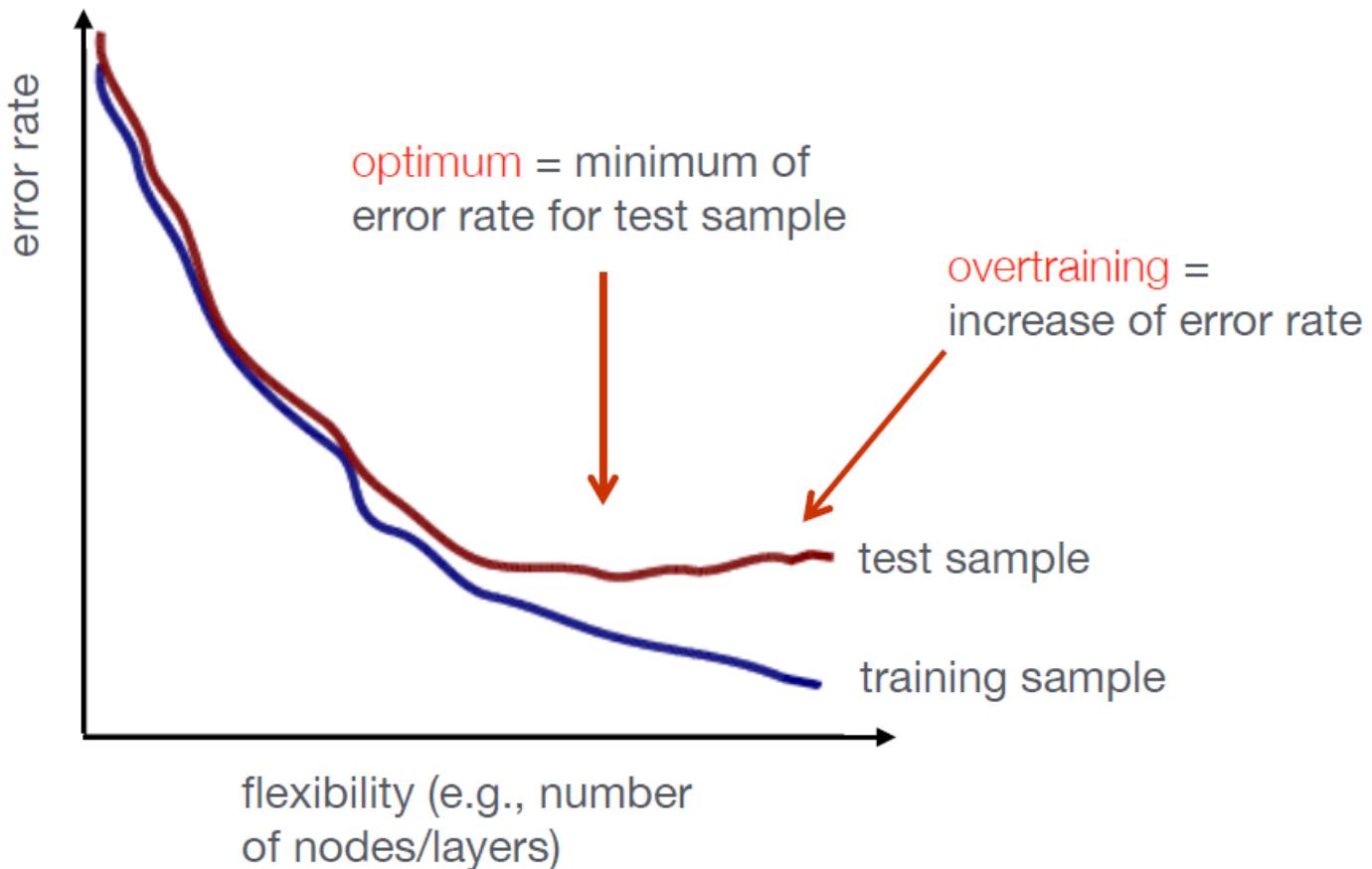
Too many neurons/layers make a neural network too flexible  
→ overtraining



Network "learns" features that are merely statistical fluctuations in the training sample

# Monitoring Overtraining

Monitor fraction of misclassified events (or error function):



# Deep Neural Networks

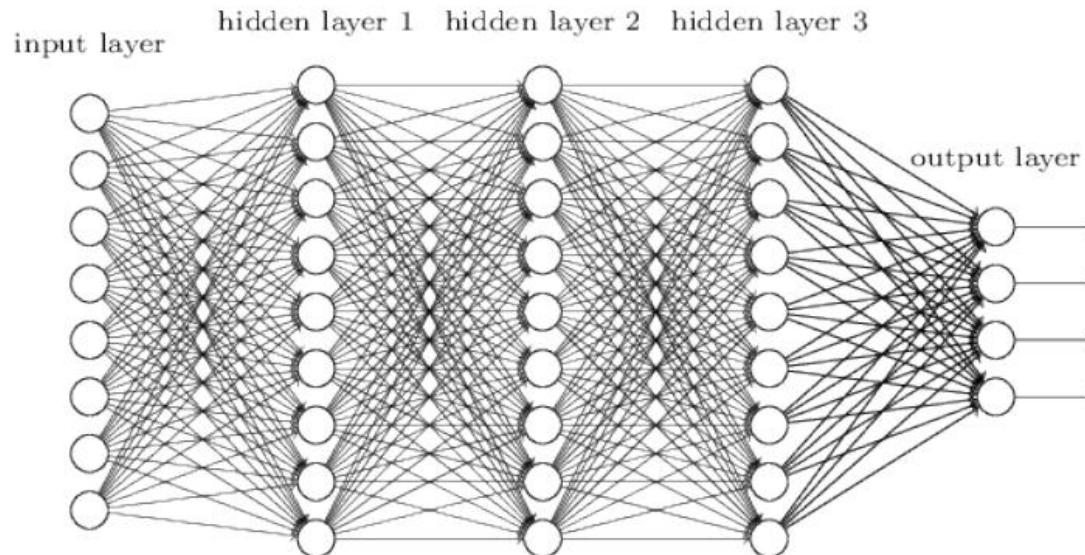
Deep networks: many hidden layers with large number of neurons

## Challenges

- ▶ Hard to train ("vanishing gradient problem")
- ▶ Training slow
- ▶ Risk of overtraining

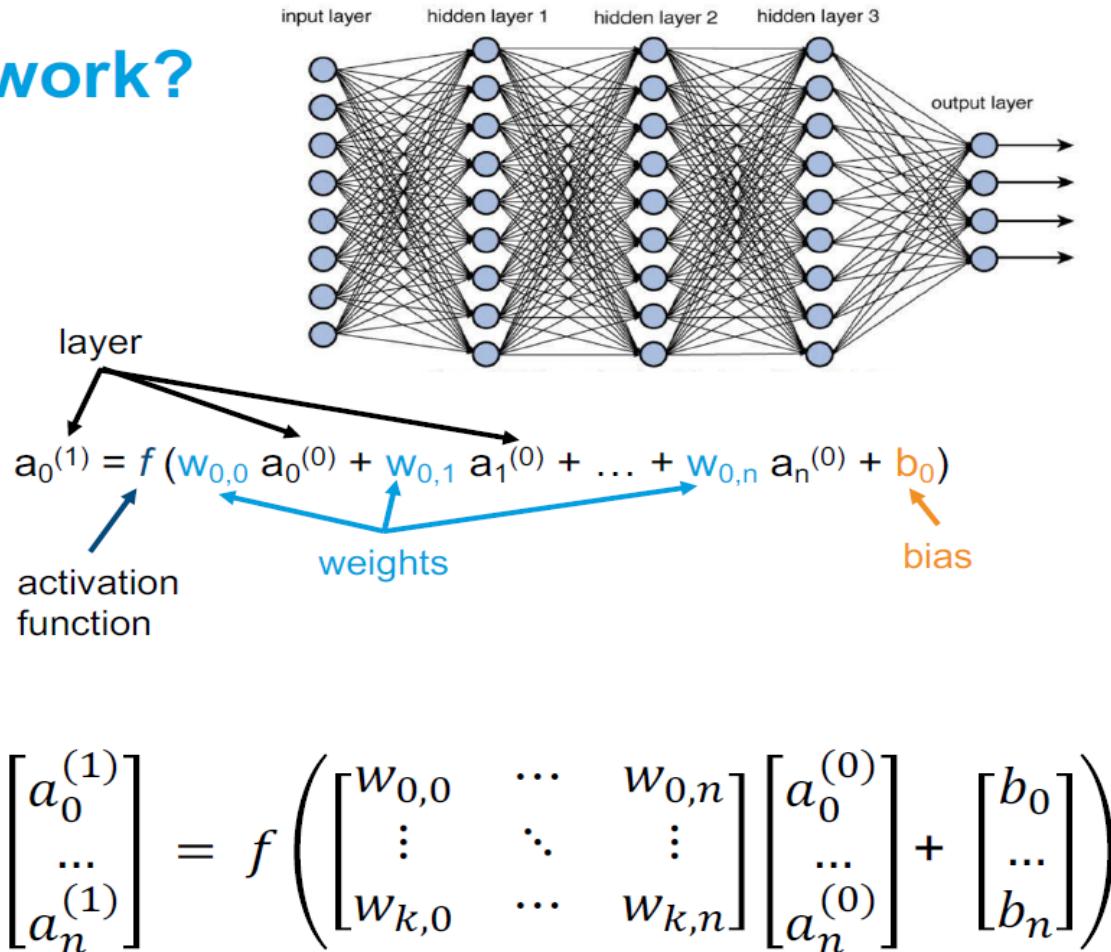
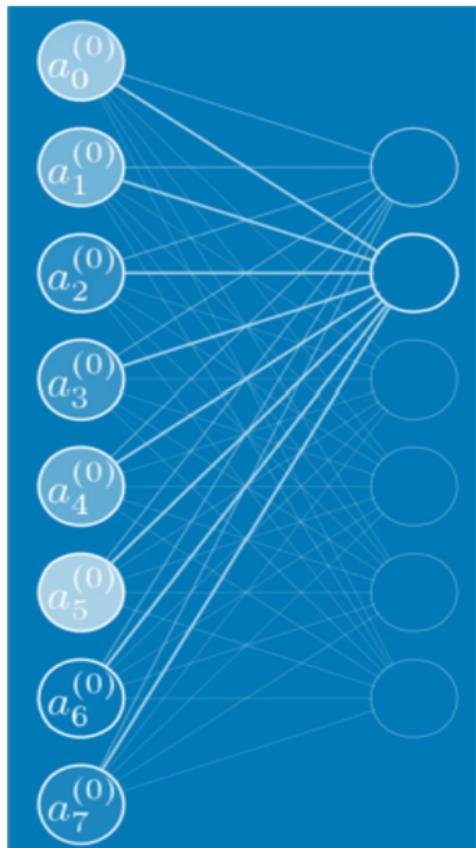
## Big progress in recent years

- ▶ Interest in NN waned before ca. 2006
- ▶ Milestone: paper by G. Hinton (2006): "learning for deep belief nets"
- ▶ Image recognition, AlphaGo, ...
- ▶ Soon: self-driving cars, ...



# How do NNs work?

## How do NNs work?



# How do NNs learn?

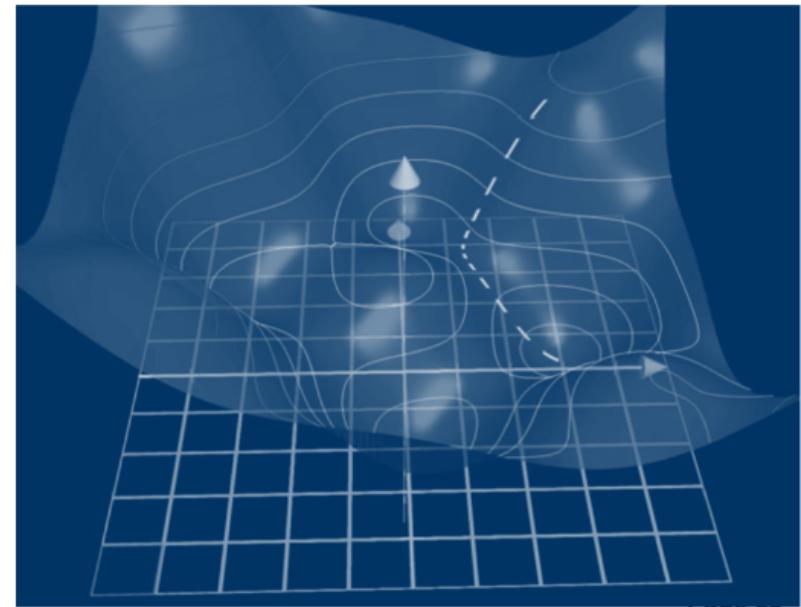
After we constructed a network, our task is to **assign proper weights** so neurons will react correctly to incoming signals.

- define a loss function to measure how far the response is from the truth

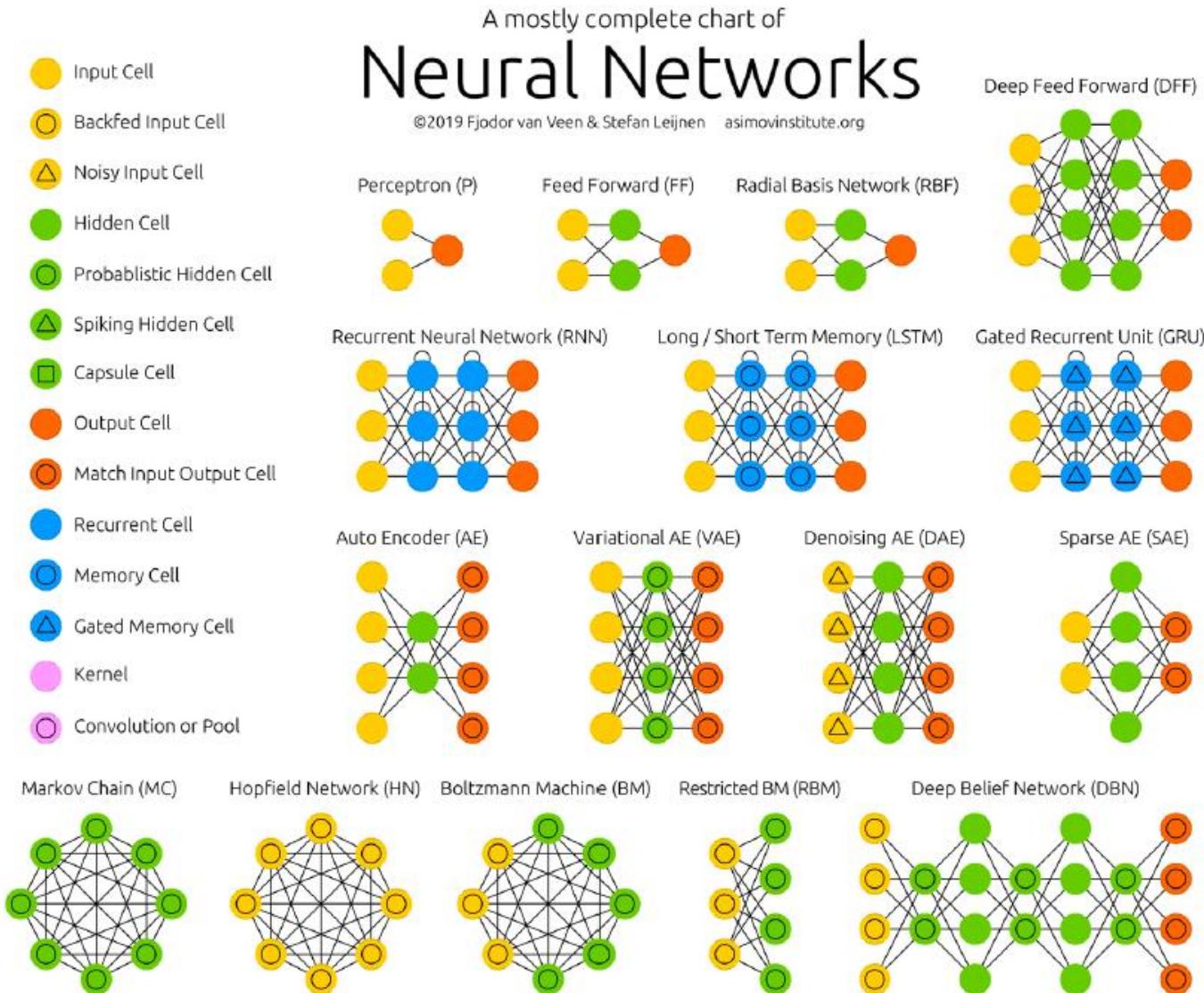
This function is a function of all the weights and biases in the NN (a priori a very large number), and the goal of training is to find its minimum.

- To start with, all weights are assigned randomly.
- After evaluating the NN on the training dataset, we can compute all the per-neuron differences with respect to the correct result.
- Computing the gradient of the loss, gives us a direction in which to tune the weights towards a local minimum

The process of correcting the weights is called backpropagation an error.



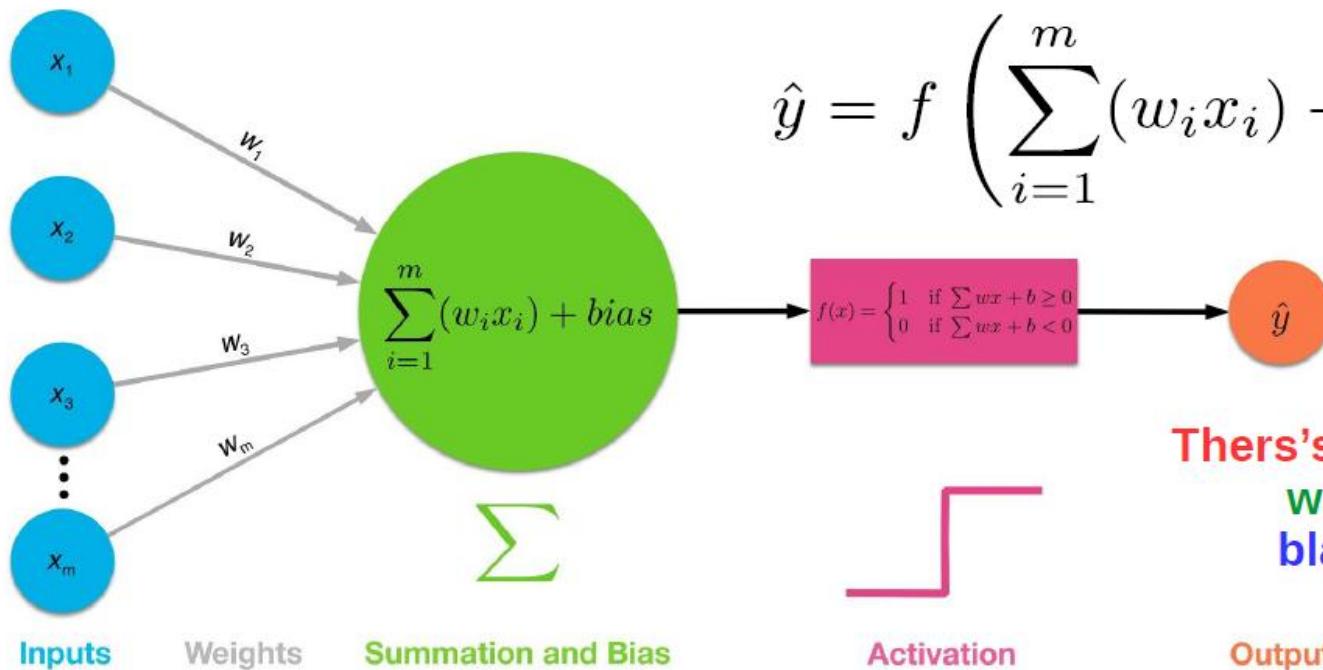
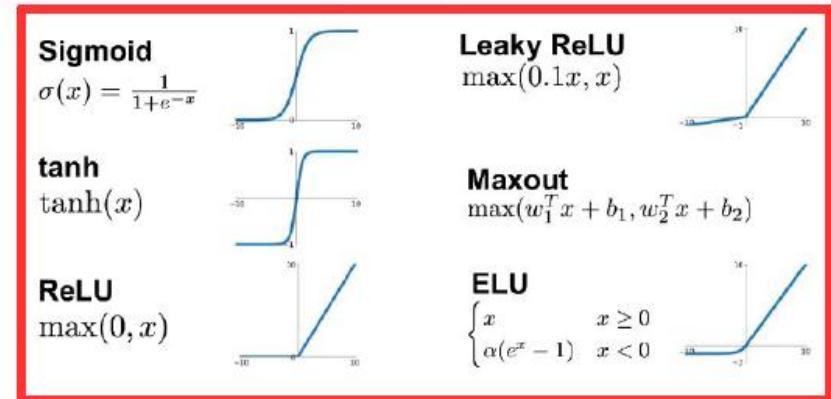
# How do NNs learn?



11/12/2024  
There are many more...

# How do NNs learn?

- Each input is multiplied by a weight.
- The weighted values are summed and a bias is added
- The result is passed to an activation function (non-linearity).**



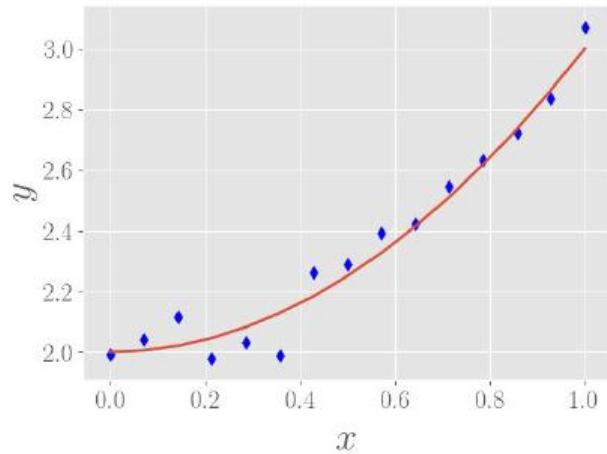
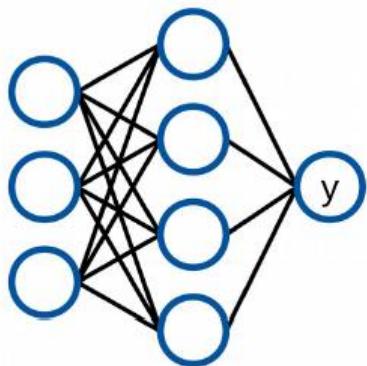
Activation

There's a colorful world inside black boxes!

# Typical Applications

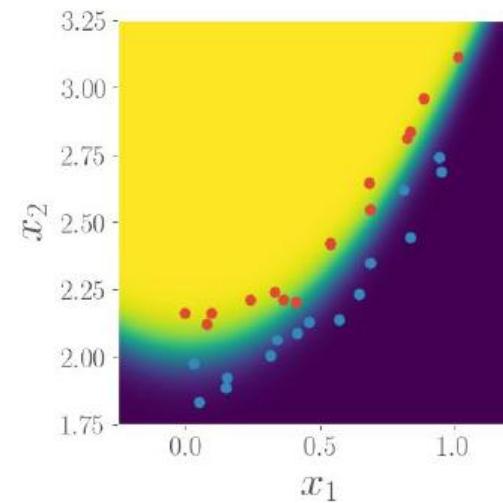
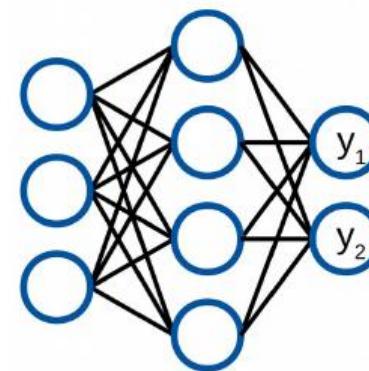
## Regression:

Predict a continuous label.



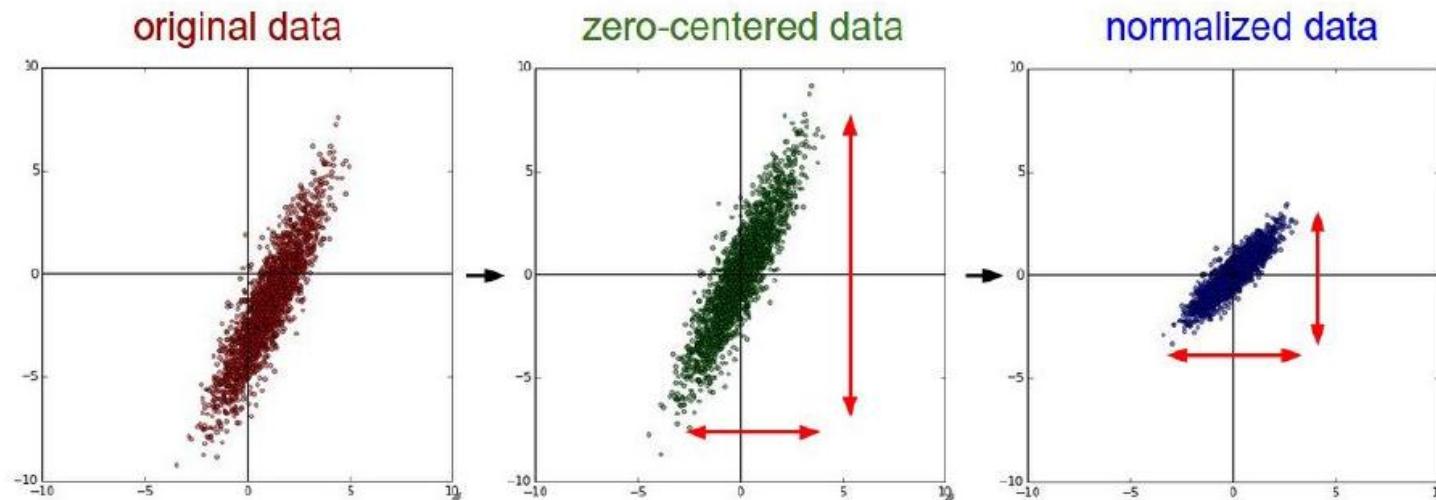
## Classification:

Separate events into multiple categories.



# Input Preprocessing

- ◆ Input features could have vastly different scales (e.g.  $p_T$  vs  $\eta$ ).
  - ◆ Difficult to find optimal values.
- ◆ Basic strategy: Normalize to mean=0 and variance=1.

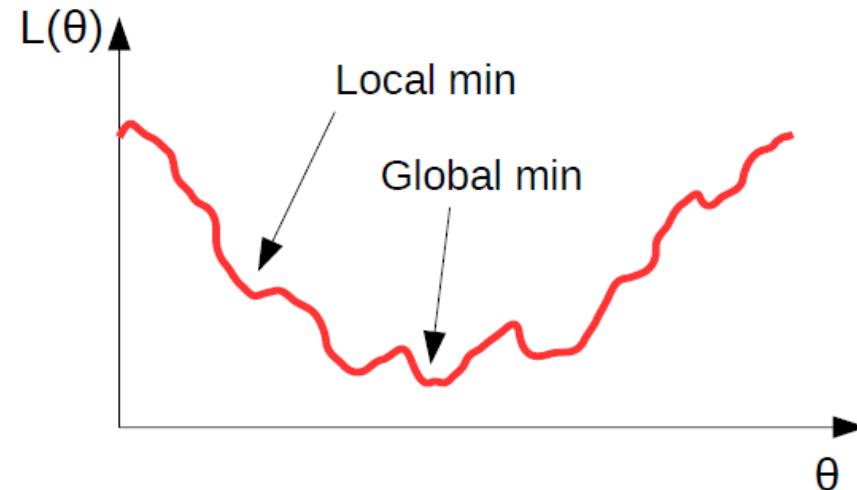


- ◆ Other options possible: decorrelation, non-linear transformation, ...

# Training

- ◆ Training starts specifying an input and a target dataset.
  - ◆ For each input set, the target is what the network should learn for that input.
- ◆ A loss function is required  $L(\theta)$ :
  - ◆ The loss function quantifies the mistakes the NN makes.  
E.g. *mean squared error* can be used for regression.

Training is the minimization of the loss function w.r.t. the NN parameters.



# Training: (Stochastic) Gradient Descent

- Given the increasing size of datasets and parameters, it is no more possible to directly minimize the loss function.

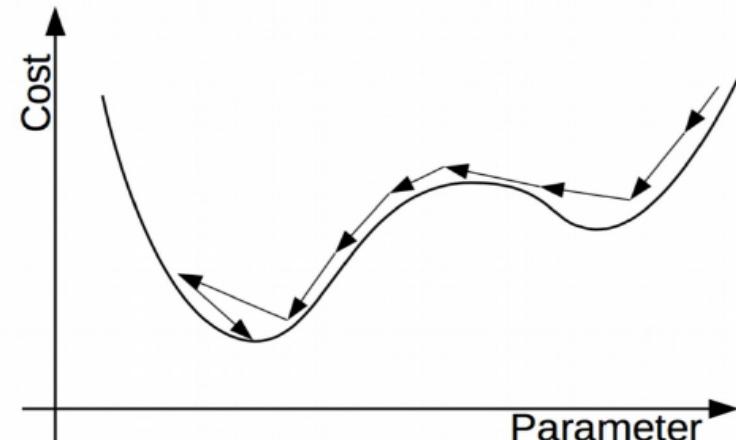
Iterative minimization by updating  $\theta$  in opposite direction of gradient.

$$\theta_i = \theta_{i-1} - \alpha \frac{\partial L}{\partial \theta}, \text{ where } \alpha \text{ is the so-called « learning rate ».}$$

- Evaluation and derivation of the loss function for the full dataset is costly:

## Stochastic gradient descent:

Calculate gradient for a small stochastic subset of the training sample (batch). → This also helps to avoid local minima!

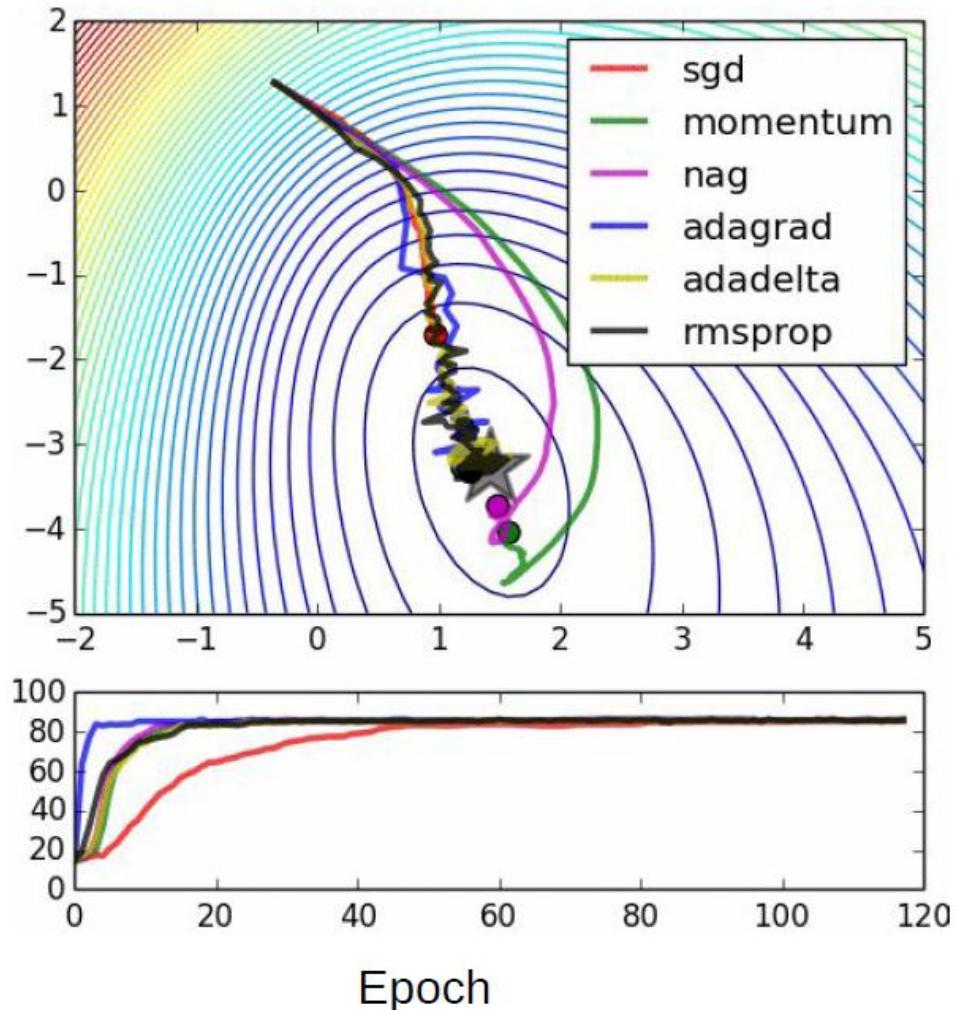


One iteration over the full training dataset is called *epoch*.

# Training: more optimisers

- More advanced options than fixed learning rate.

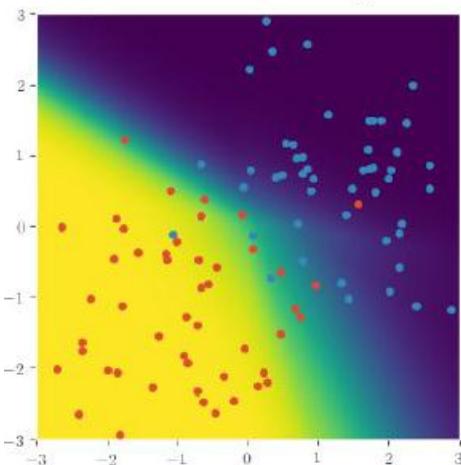
- Momentum:  
past gradients used as « velocity »
- Adaptive methods:  
different learning rates for each parameter and as a function of past gradients.



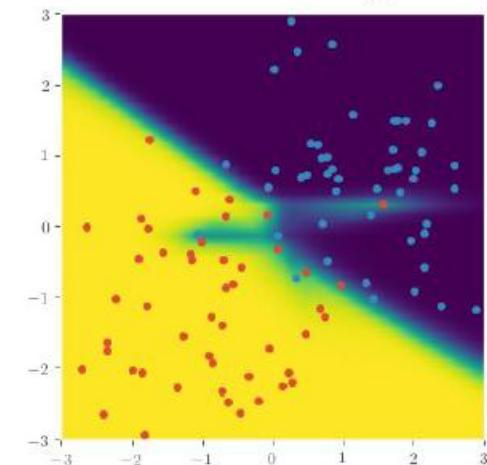
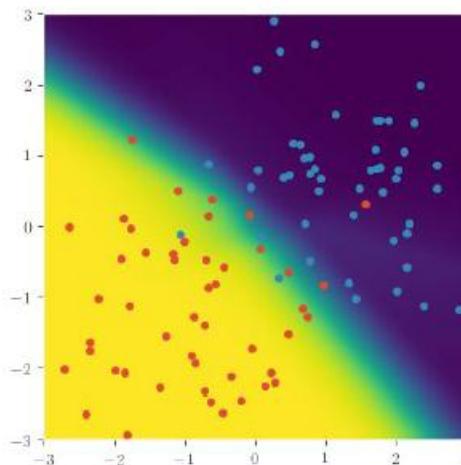
# Underfitting and overtraining

**Underfitting:** If model capacity is too low  
or if training is not enough  
→ bad performance.

**Underfitting**



**Overfitting**

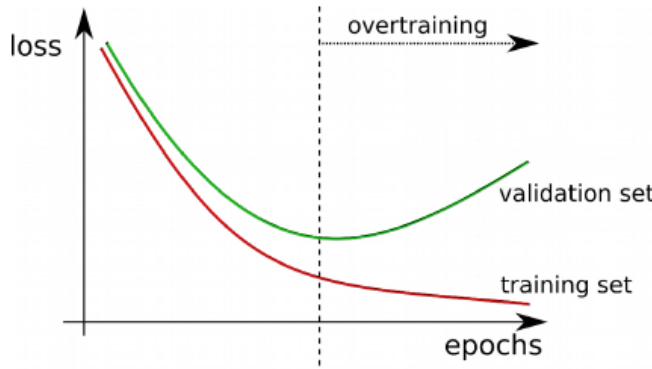


**Overfitting:** If model capacity is too high,  
network can « memorize » training samples  
→ bad generalization.

# Overtraining solutions

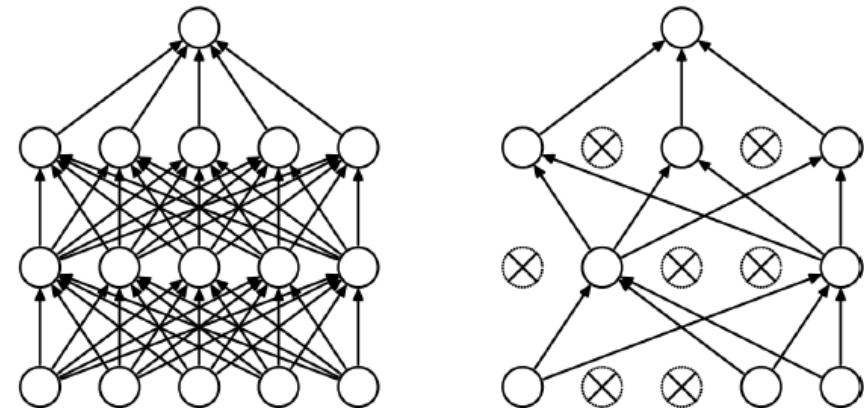
## Early stop:

Evaluate the performance of the network on a validation dataset.  
Stop when performance on validation set decreases



## Dropout:

Randomly drop a percentage of nodes at each training step.  
Learn redundant representations, hence giving a more robust model.



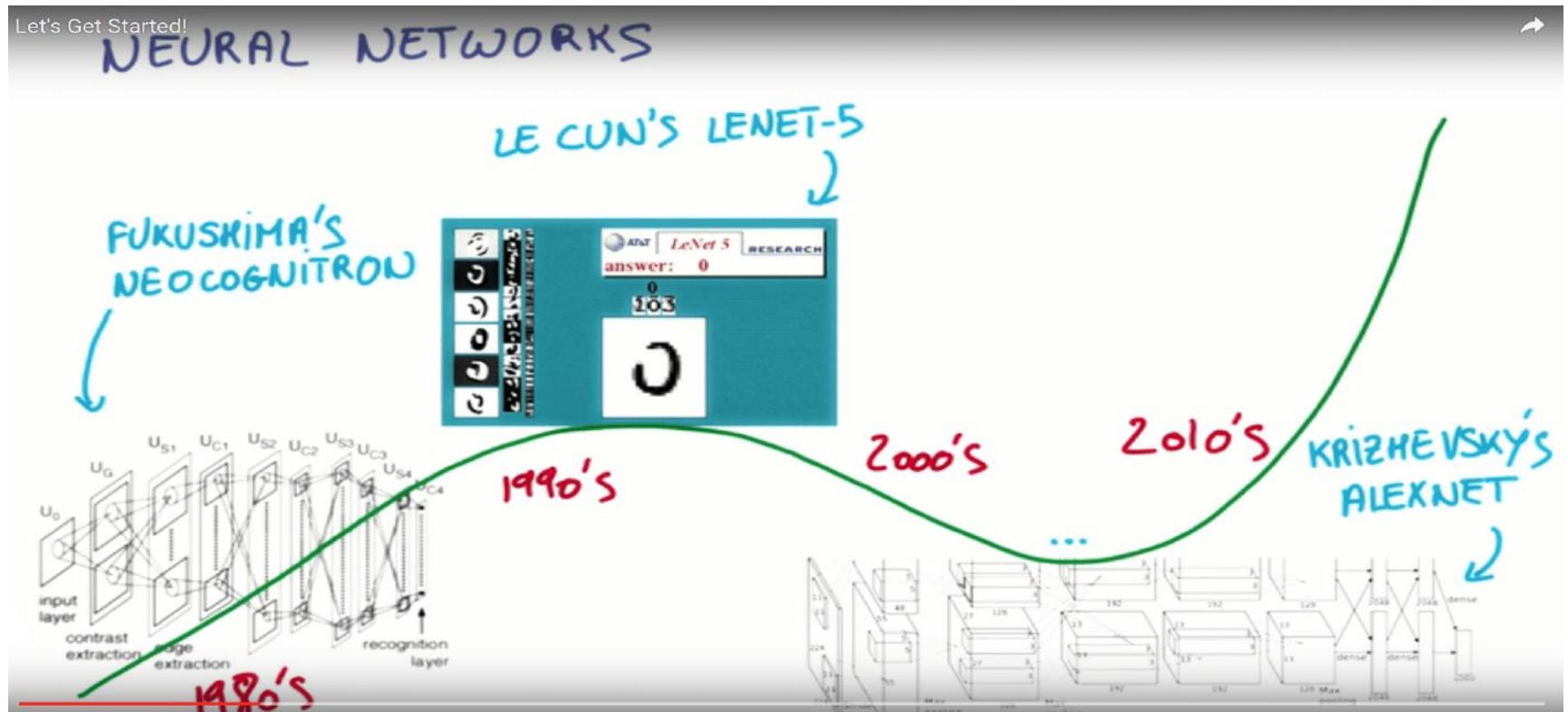
# **Deep-learning Neural Network**

**TensorFlow™**

**MNIST example**

# Neural network

**Since 2010 new era in Machine Learning:  
rapidly increasing areas of applications**



# Neural network

**Since 2010 new era: rapidly increasing areas of applications**

NEURAL NETWORKS → DEEP LEARNING

- 2009: SPEECH RECOGNITION
- 2012: COMPUTER VISION
- 2014: MACHINE TRANSLATION

① DATA!



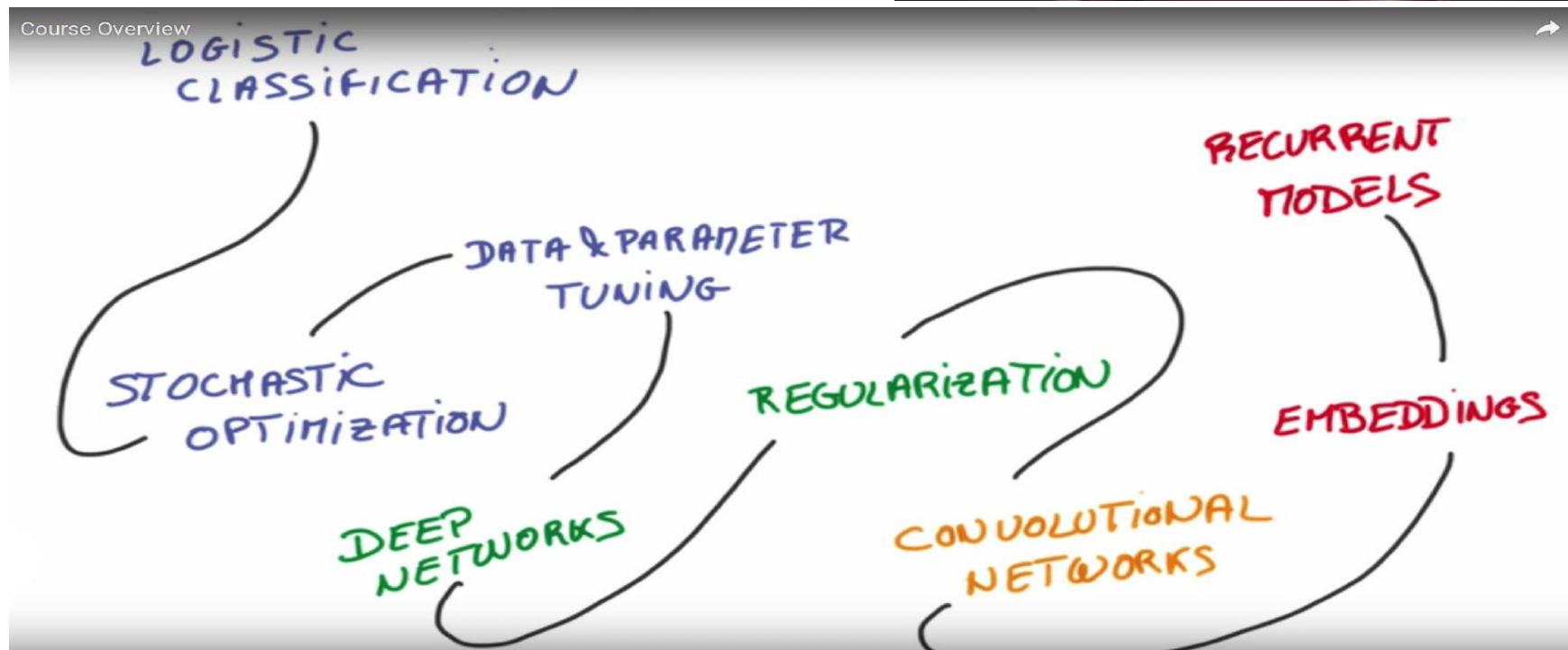
② GPUs!



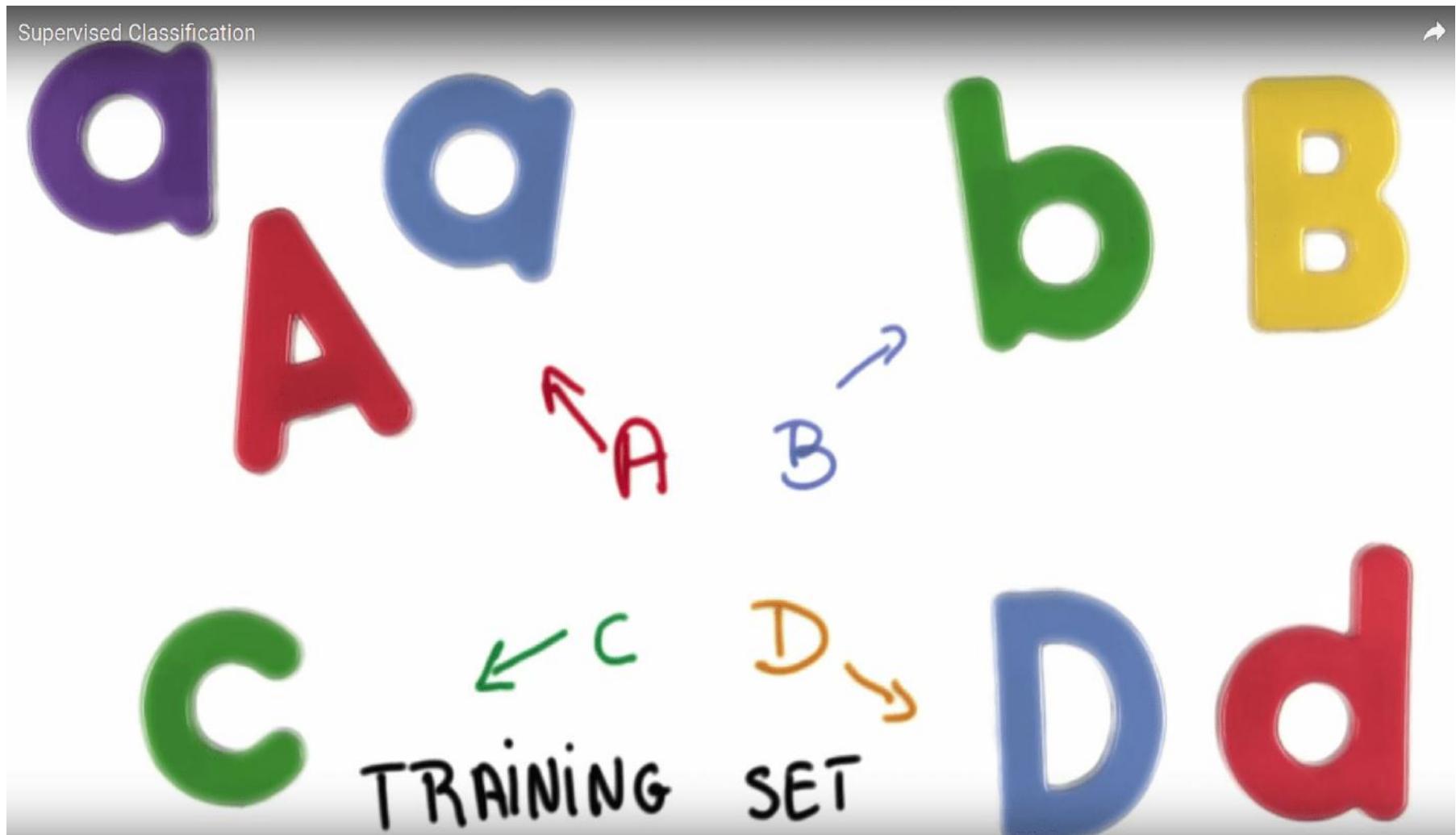
THANK YOU  
GAMERS!!!

# Deep-Learning tutorial @ udacity

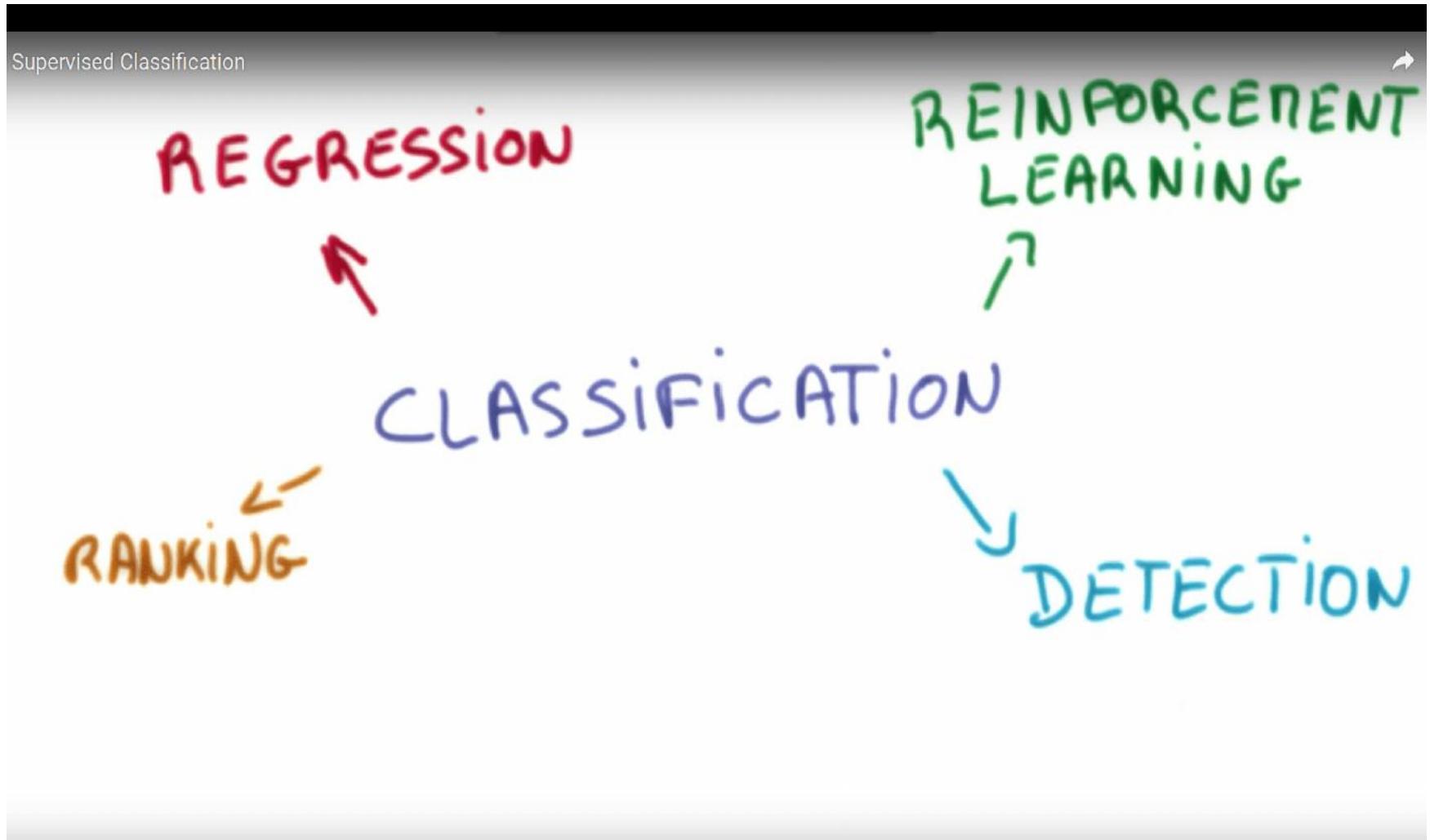
<https://www.udacity.com/course/deep-learning--ud730>



# Supervised Classifications



# Supervised Classifications



# Classifications for Detection

Classification For Detection Solution

DETECTION

PEDESTRIAN  
VS.  
NO PEDESTRIAN



Use a binary pedestrian / no pedestrian classifier. Slide it over all possible locations in the image.

# Classifications for Ranking

Classification For Ranking Solution

RANKING

Udacity deep learning

Web News Videos Images Shopping More ▾ Search tools

About 46,700 results (0.64 seconds)

Machine Learning: Supervised Learning - Udacity  
<https://www.udacity.com/wiki/ud675> ▾ Udacity ▾  
Oct 3, 2014 - Ethem Alpaydin, Introduction to Machine Learning. Second Edition. ...

CLASSIFIER

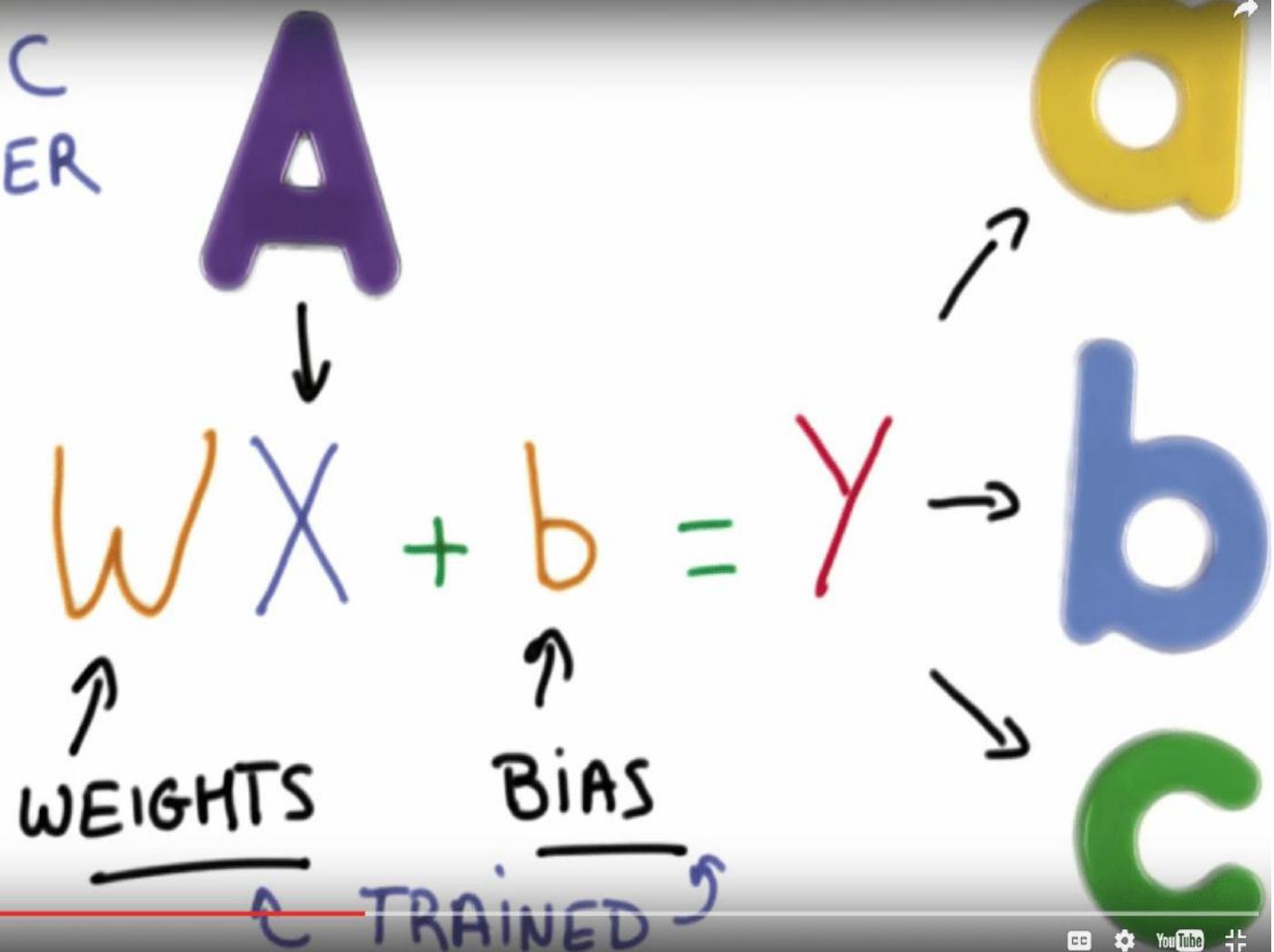
RELEVANT!

Use a classifier that takes the pair (query, web page) as an input, and classifies the pair as relevant / not relevant

# Logistic classifier: Linear model

Training Your Logistic Classifier

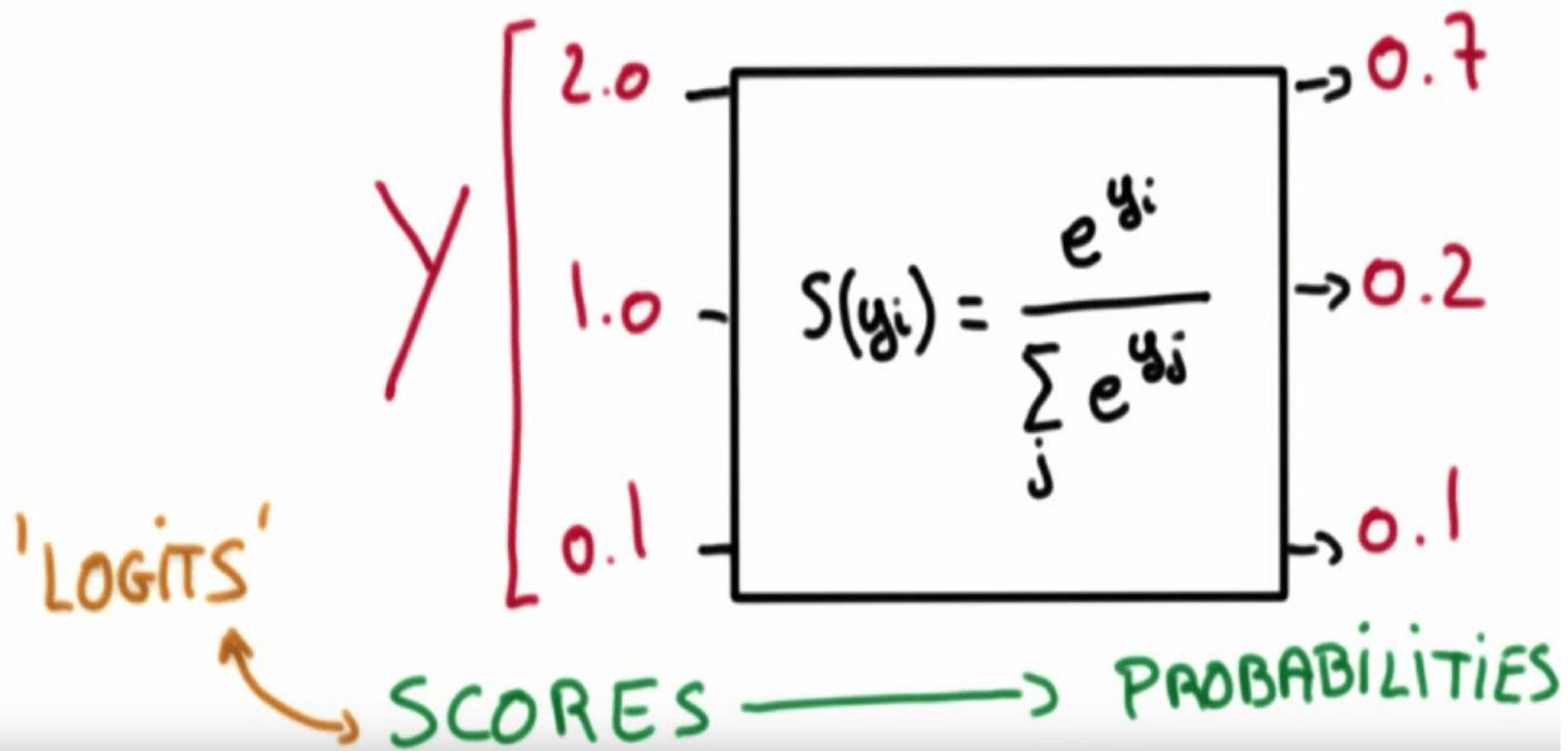
LOGISTIC  
CLASSIFIER



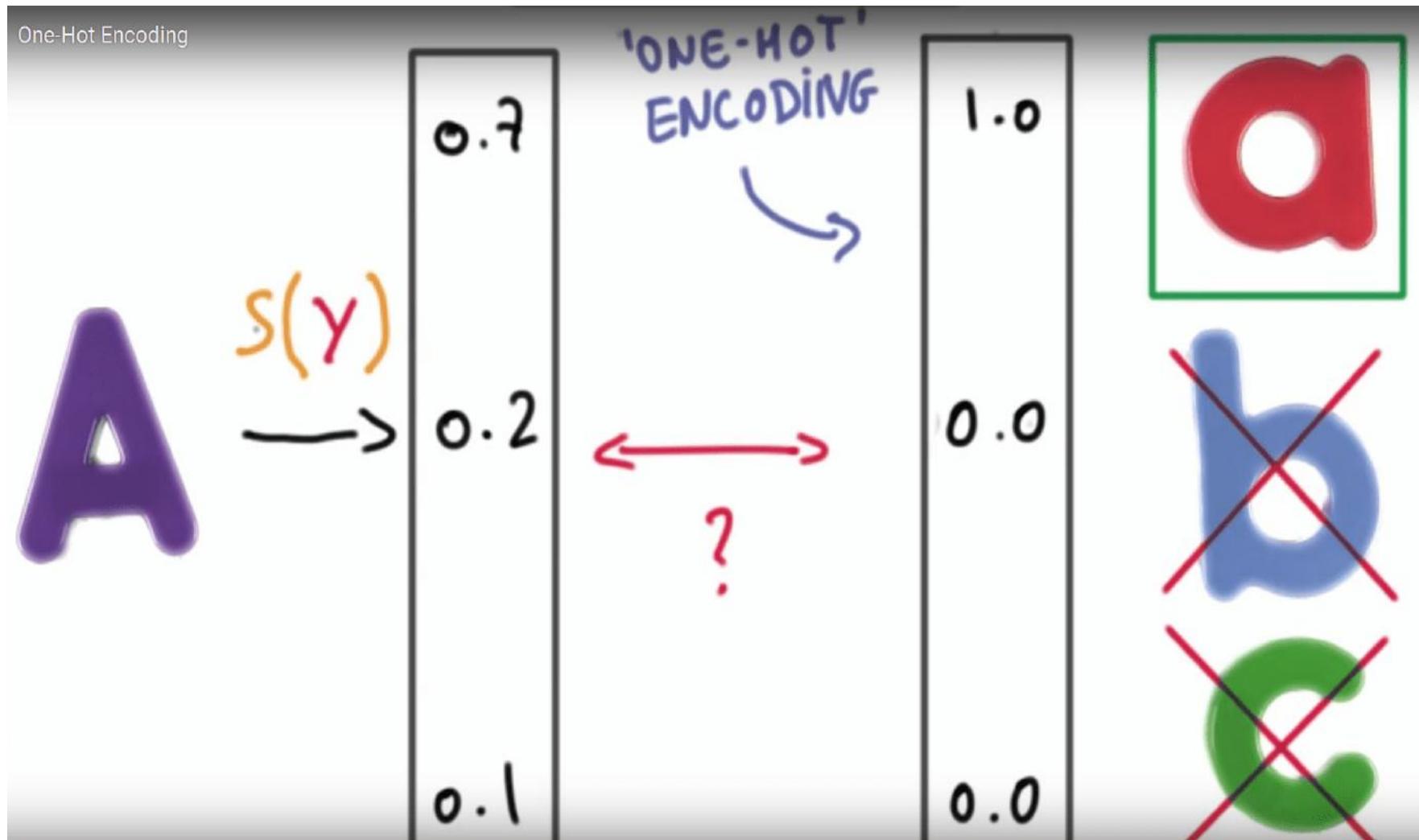
# Softmax

Training Your Logistic Classifier

SOFTMAX



# „One hot“ encoding



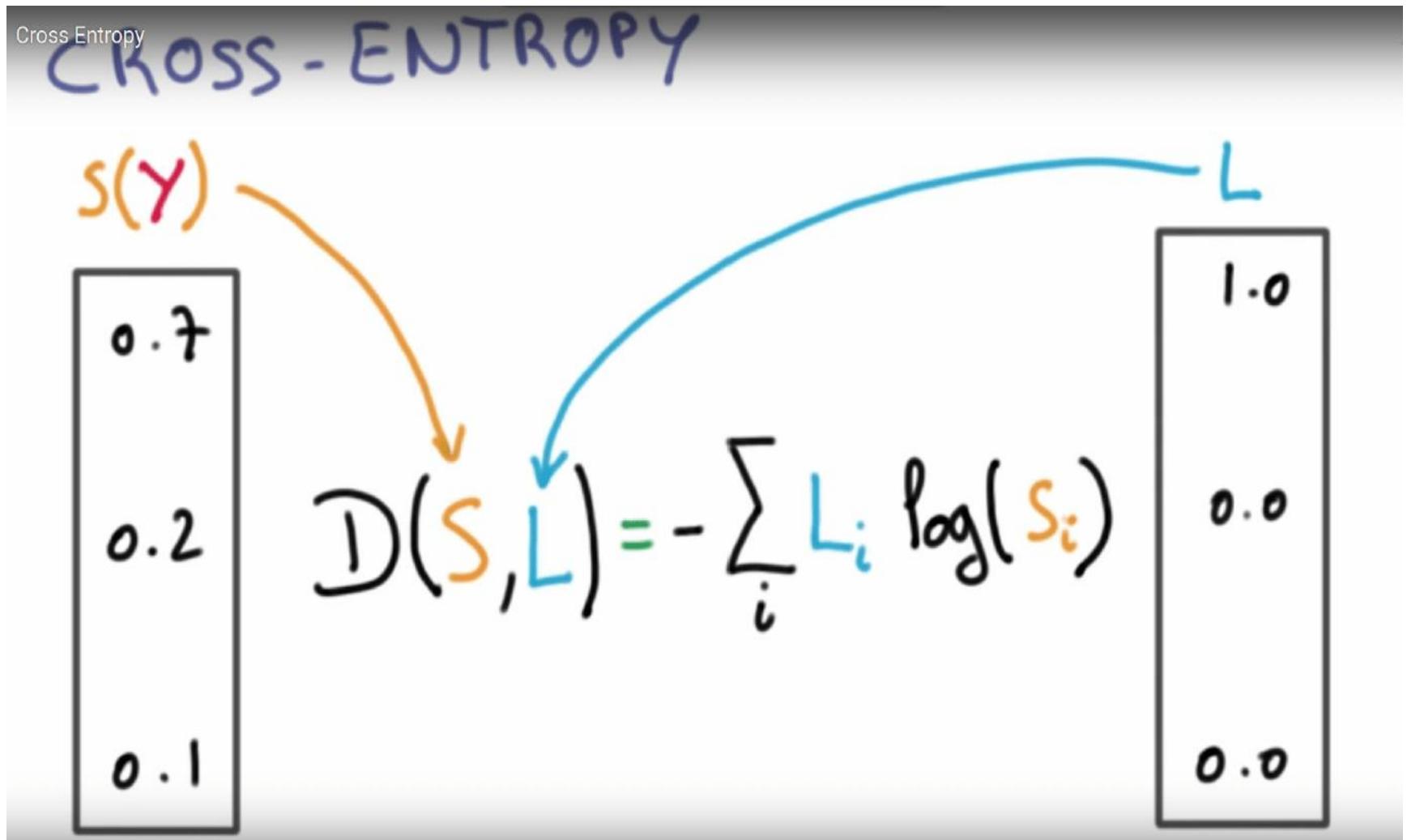
# „One hot“ encoding

Cross Entropy

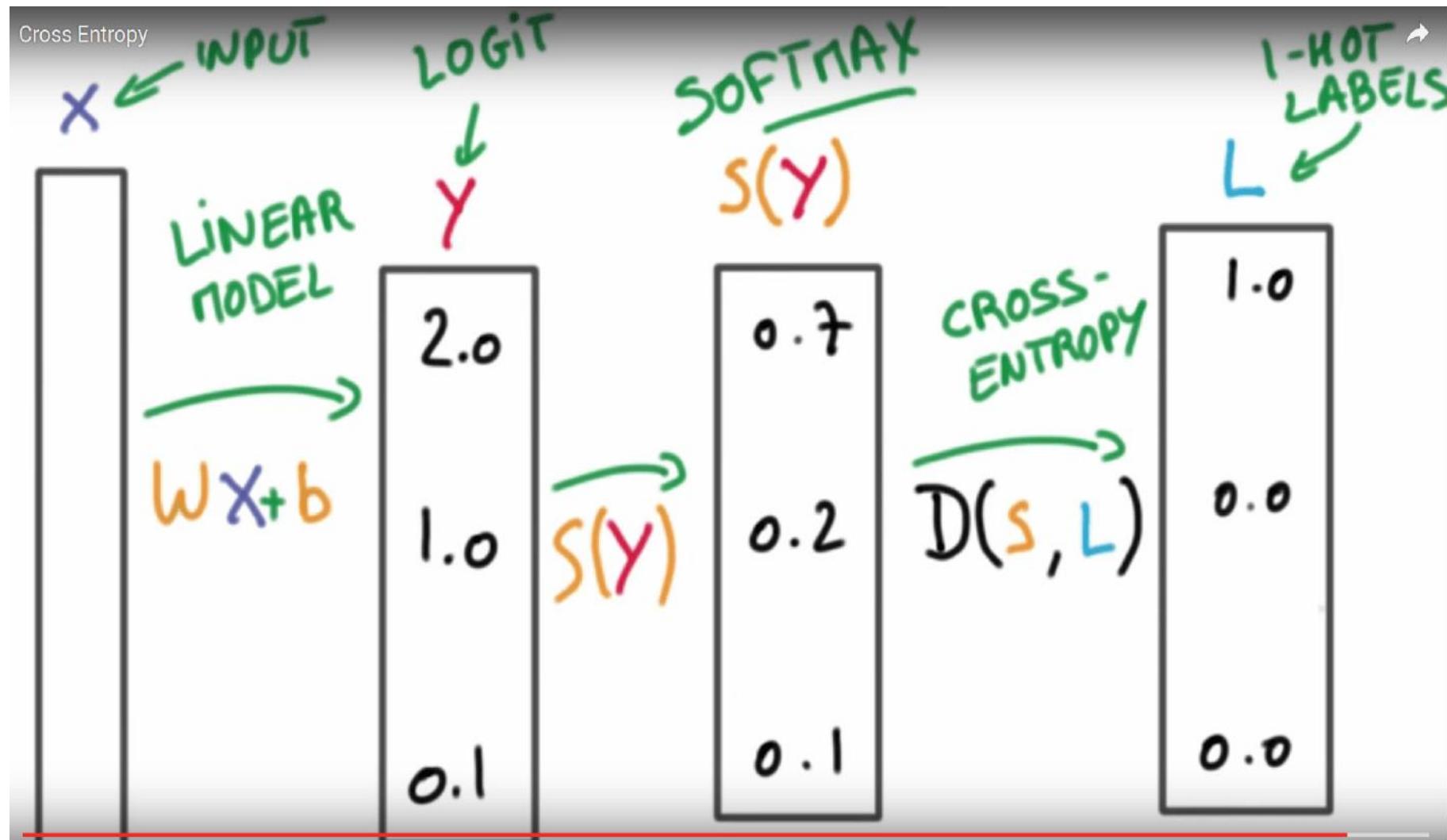
a →	0	0	0	0	0	0	0
b →	0	0	0	0	0	0	0
c →	0	0	0	0	0	0	0
d →	0	0	0	0	0	0	0
:	0	0	0	0	0	0	0
6	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

A diagram illustrating one-hot encoding. A vertical stack of 8 binary digits (bits) is shown for each character. The first bit (least significant) is labeled with a red '1' and circled in green, indicating it is the active or 'hot' bit for character 'd'. All other bits are '0'. The characters are listed vertically on the left: 'a', 'b', 'c', 'd', followed by three dots, then '6', and finally '0'. The top-left corner of the bit matrix contains the text 'Cross Entropy'.

# Optimisation: Cross-Entropy



# Multinomial logistic classification



# Optimisation of average loss

Minimizing Cross Entropy

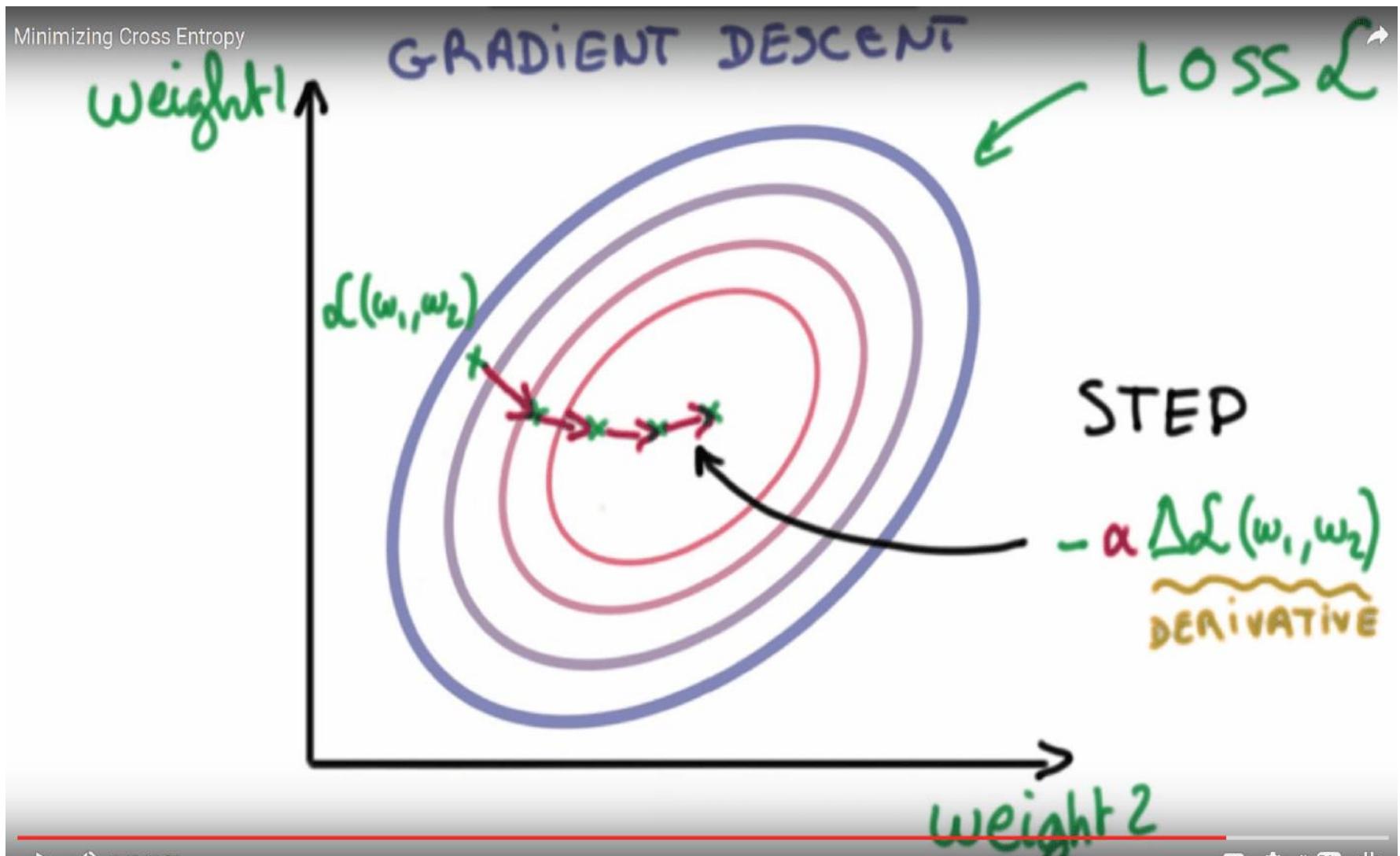
LOSS = AVERAGE CROSS-ENTROPY

$$\mathcal{L} = \frac{1}{N} \sum_i D(s(wx_i + b), L_i)$$

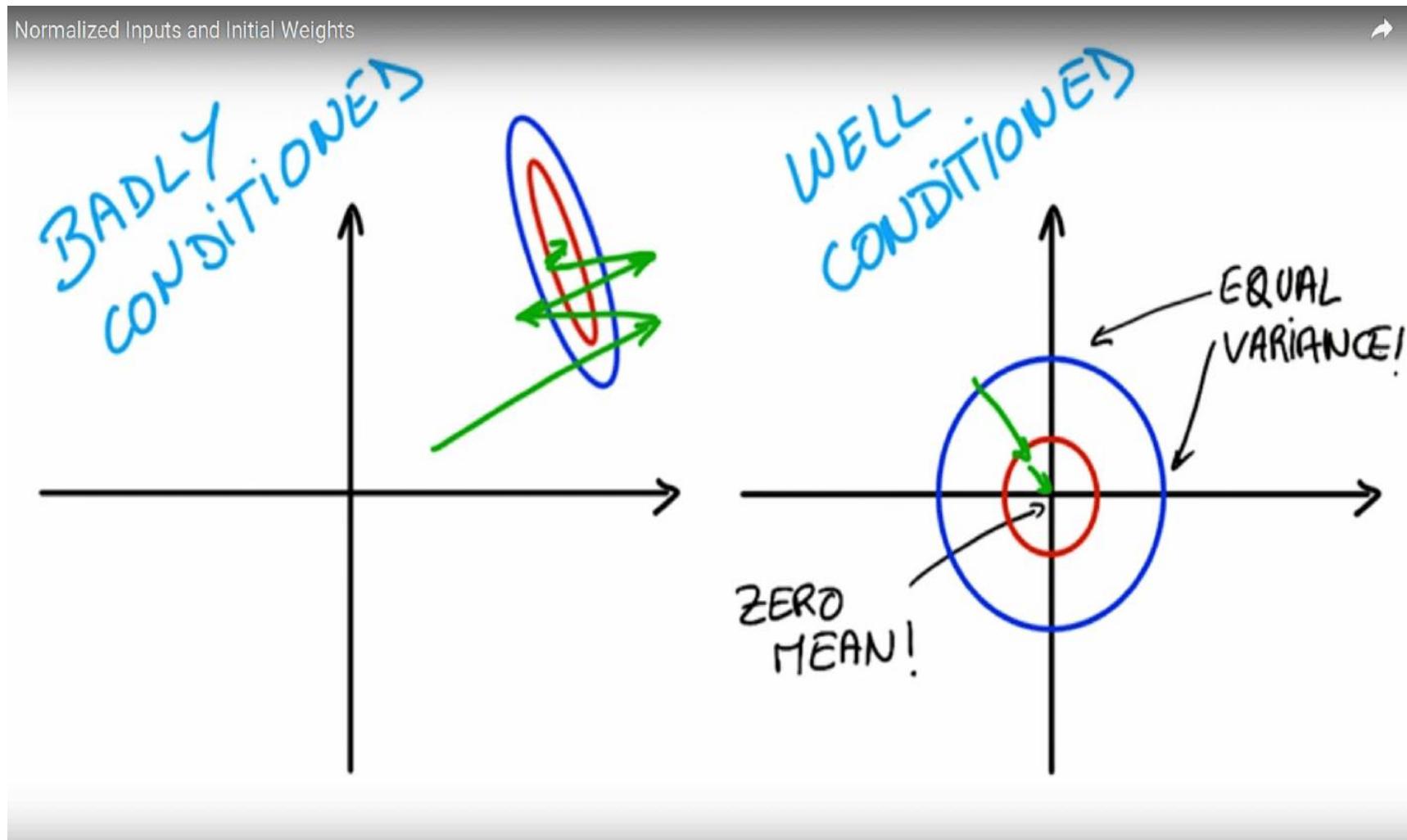
BIG MATRIX!!

BIG SUM!!

# Gradient decent



# Normalised input and output



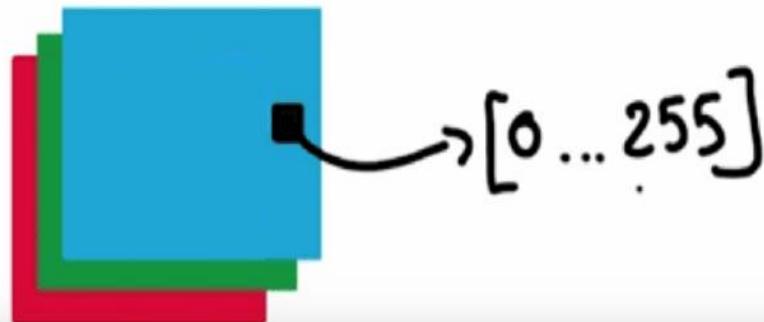
# Normalised input and output

IMAGES

$$\frac{R - 128}{128}$$

$$\frac{G - 128}{128}$$

$$\frac{B - 128}{128}$$



# Initialisation

Normalized Inputs and Initial Weights

INITIALISATION  
OF THE LOGISTIC  
CLASSIFIER

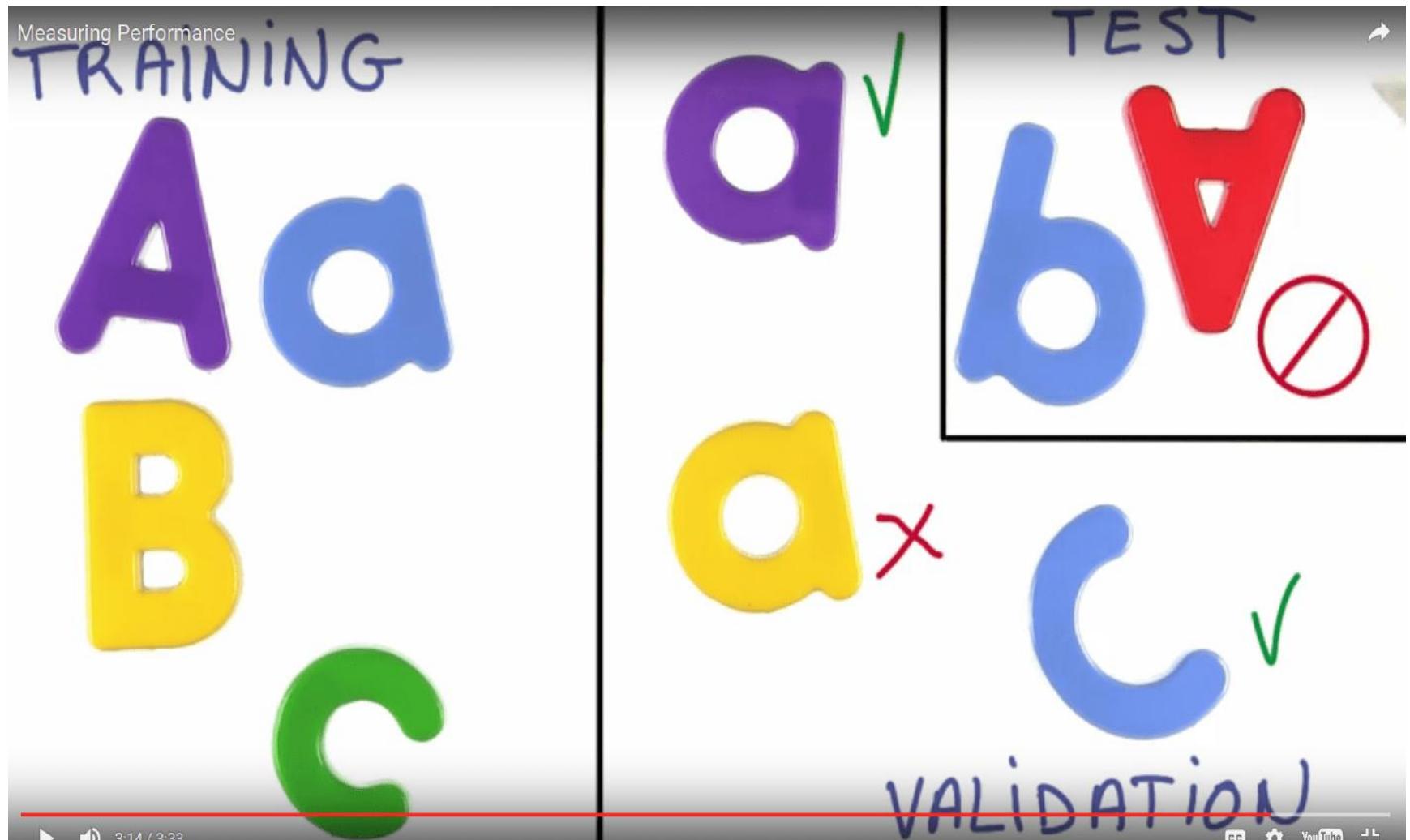
$$\frac{\text{pixels} - 128}{128}$$

$$\mathcal{L} = \frac{1}{N} \sum_i \mathcal{D}(S(\omega x_i + b), L_i)$$

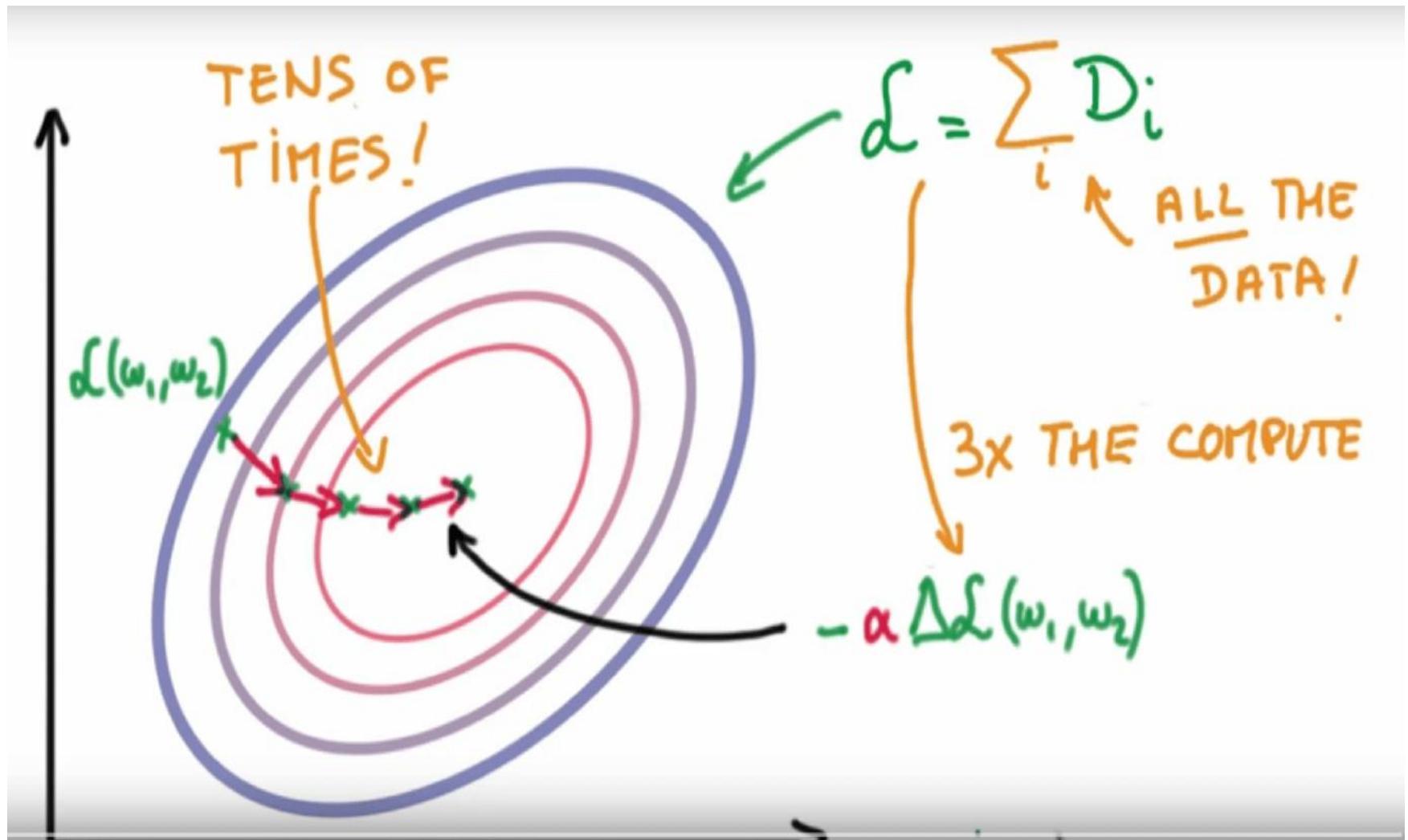
$$\phi$$



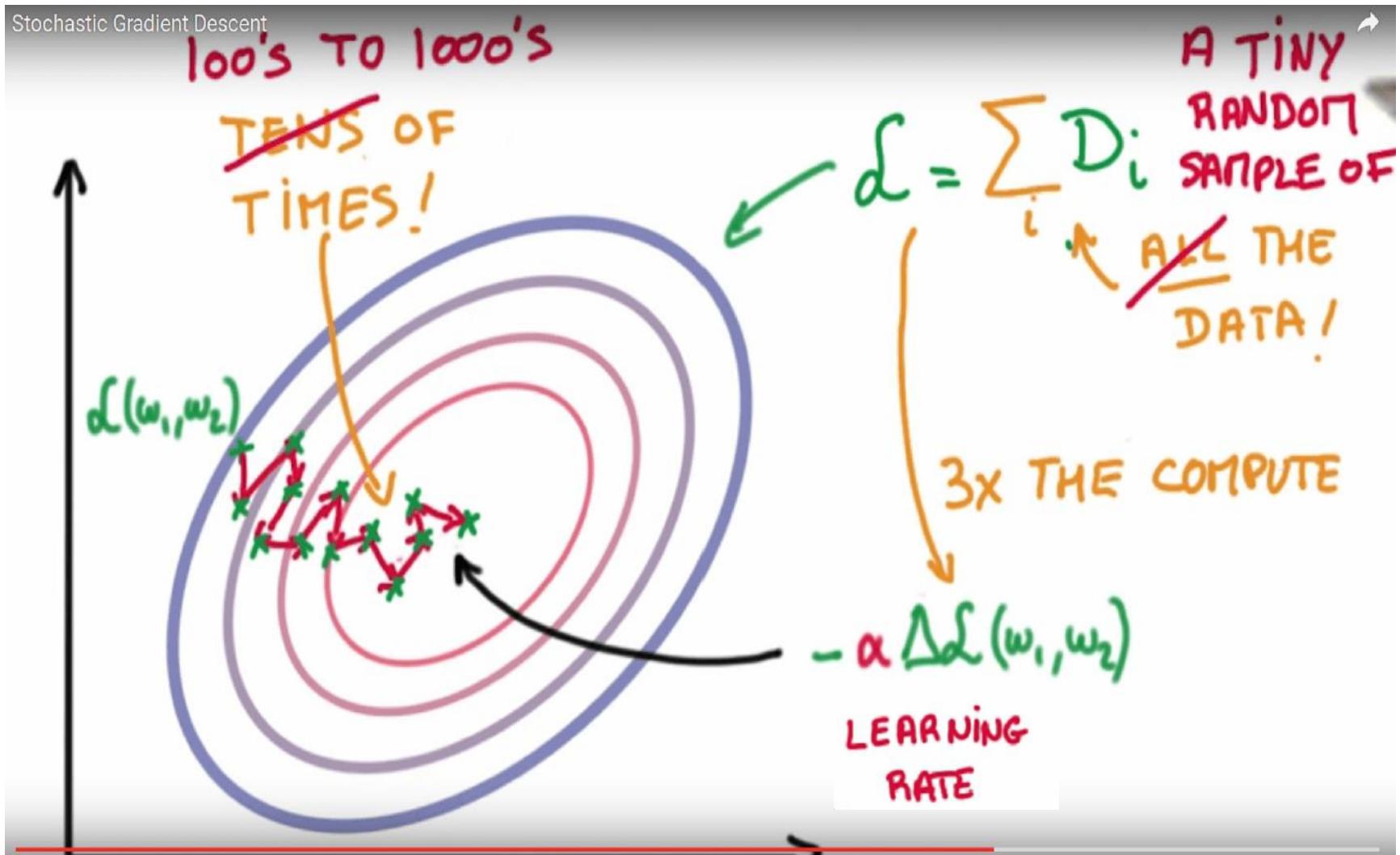
# Training, validation, testing



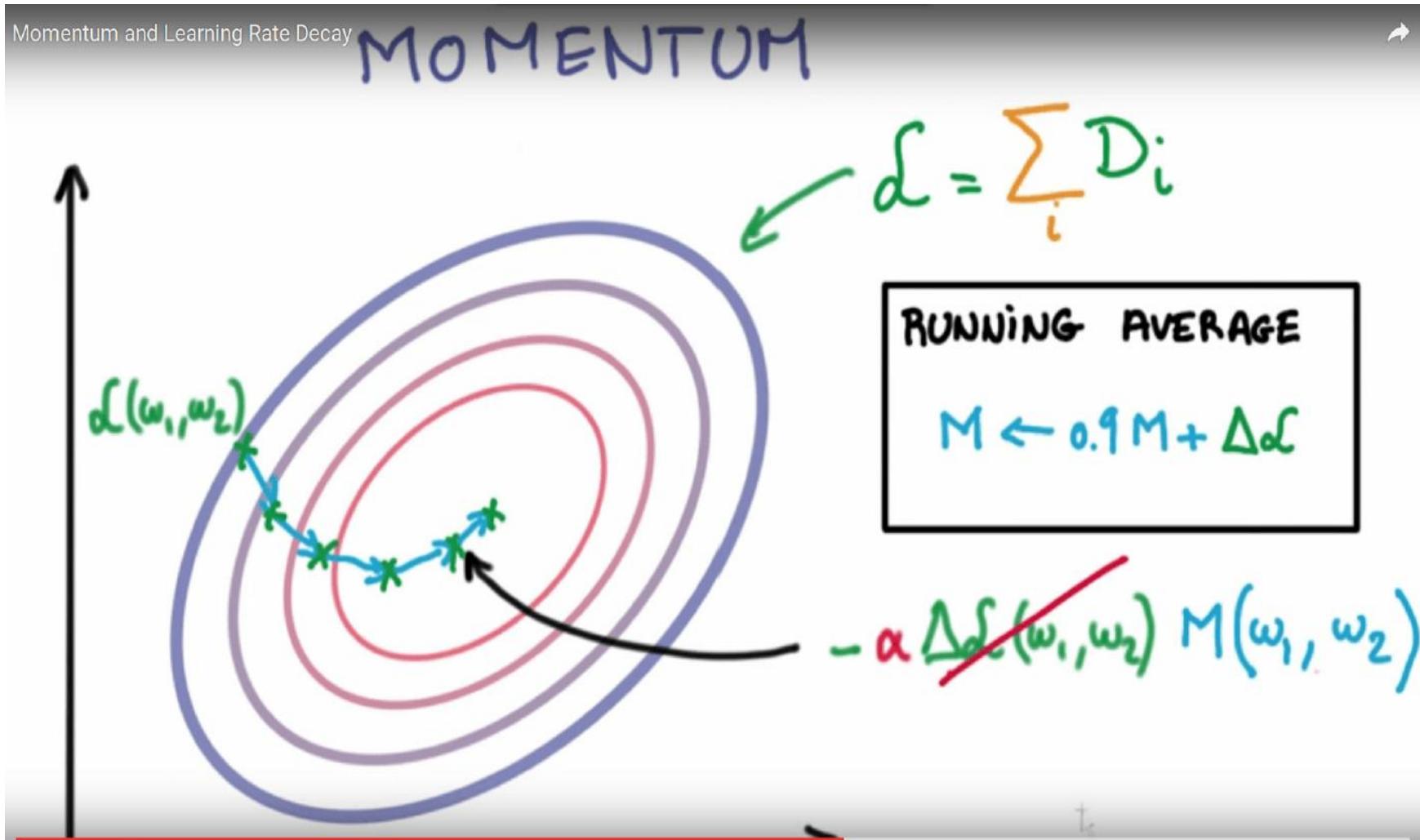
# Gradient Descent



# Stochastic Gradient Descent



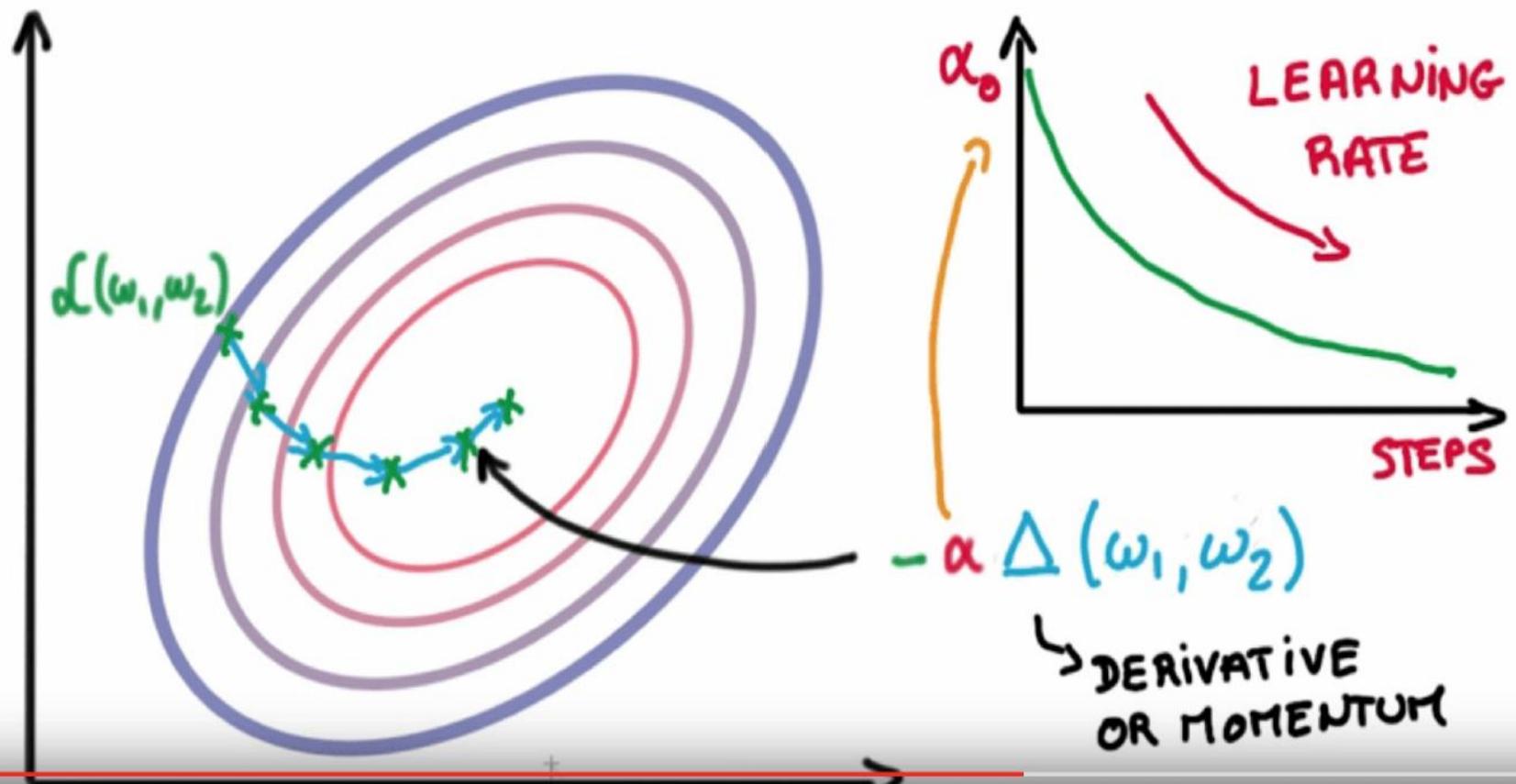
# SDG: optimising with momentum



# SDG: learning rate

Momentum and Learning Rate Decay

## LEARNING RATE DECAY

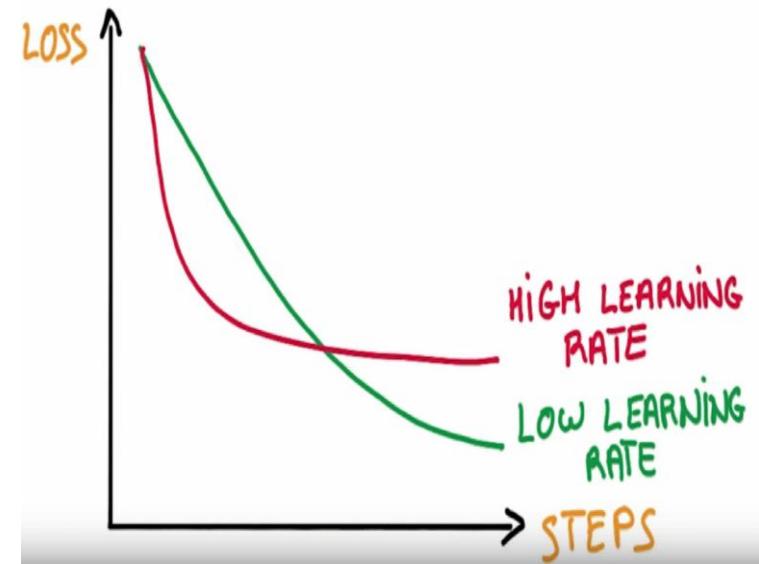


# SDG: „black magic”

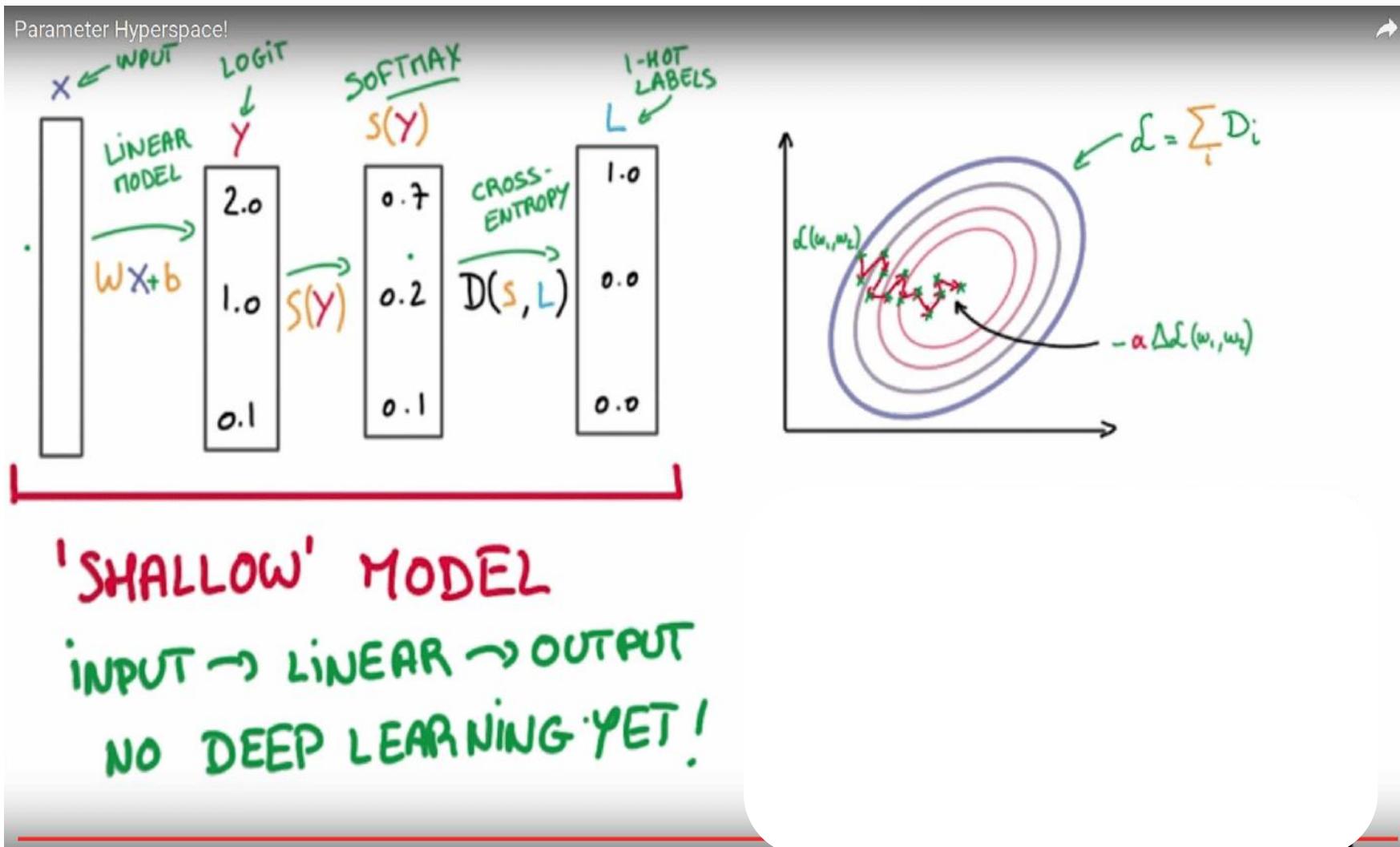
MANY HYPER-PARAMETERS

- INITIAL LEARNING RATE
- LEARNING RATE DECAY
- MOMENTUM
- BATCH SIZE
- WEIGHT INITIALIZATION

↑



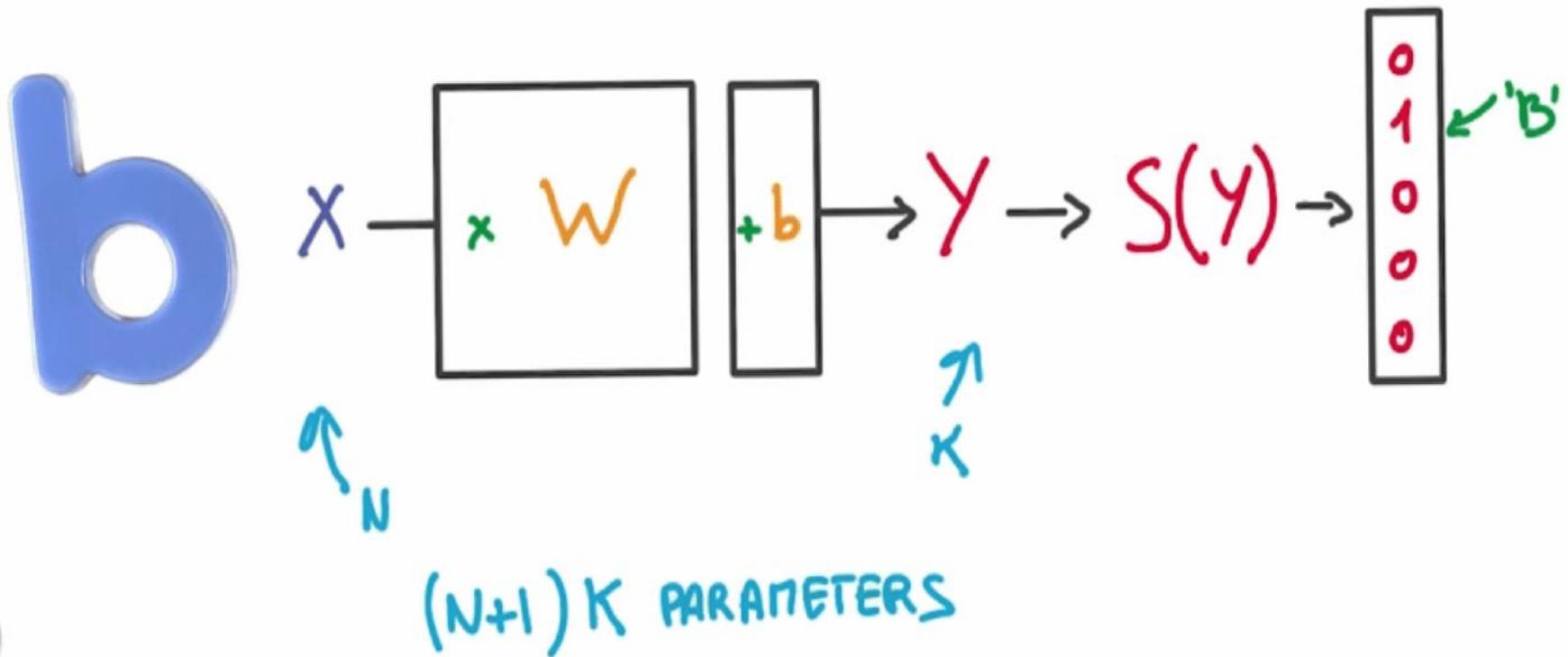
# Input – linear - output



# Linear models are linear

Linear Models are Limited

LINEAR MODEL COMPLEXITY



# Linear models are stable

$$Y = W X \rightarrow \Delta Y \sim |W| \Delta X$$

↑ SMALL      BOUNDED ↑      ↑ SMALL

$$Y = W X \rightarrow \frac{\Delta Y}{\Delta X} = W^T$$

↑ CONSTANTS

$$\frac{\Delta Y}{\Delta w} = X^T$$

↓

# Linear models are here to stay

- This is still linear

$$Y = \omega_1 \omega_2 \omega_3 X = w X$$

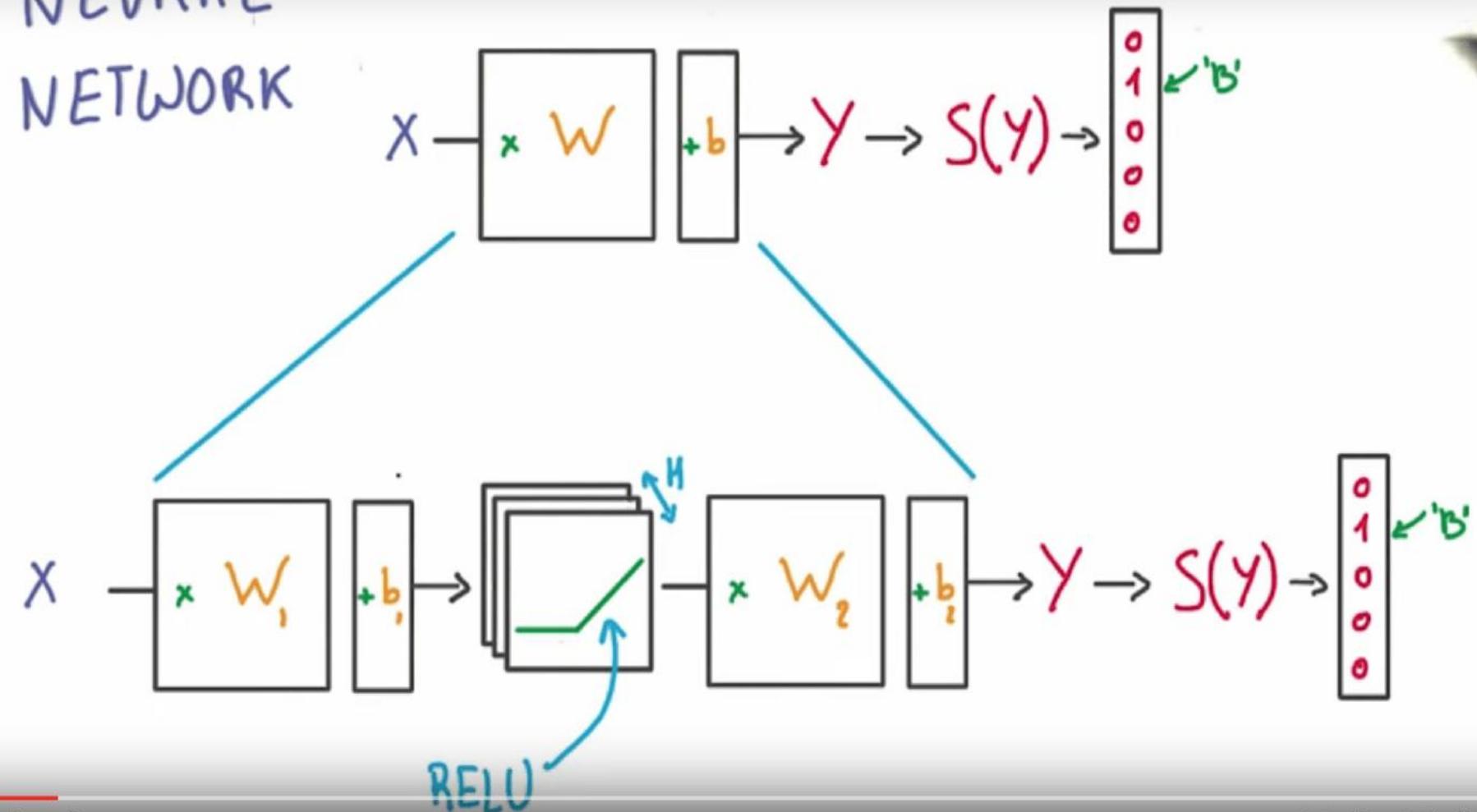
- Lets introduce non-linearity

$$Y = \omega_1 \omega_2 \omega_3 X = \textcolor{red}{B} \omega X$$

↑      ↑  
NON - LINEARITIES

# RELU: Rectified Linear Unit

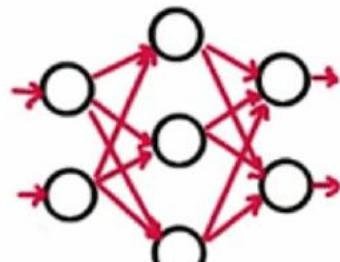
NEURAL  
NETWORK



# Networks of RELU

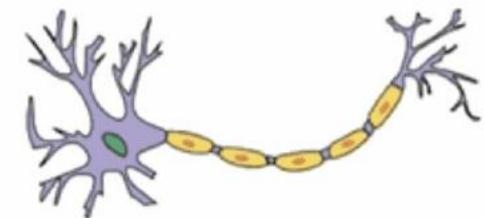
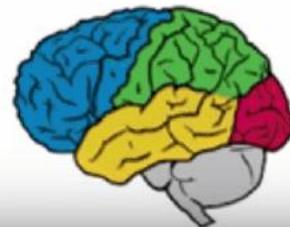
Network of ReLUs

NEURAL NETWORK



NEURONS?

HOW THE  
BRAIN WORKS?



NEUROMORPHIC  
ENGINEERING?

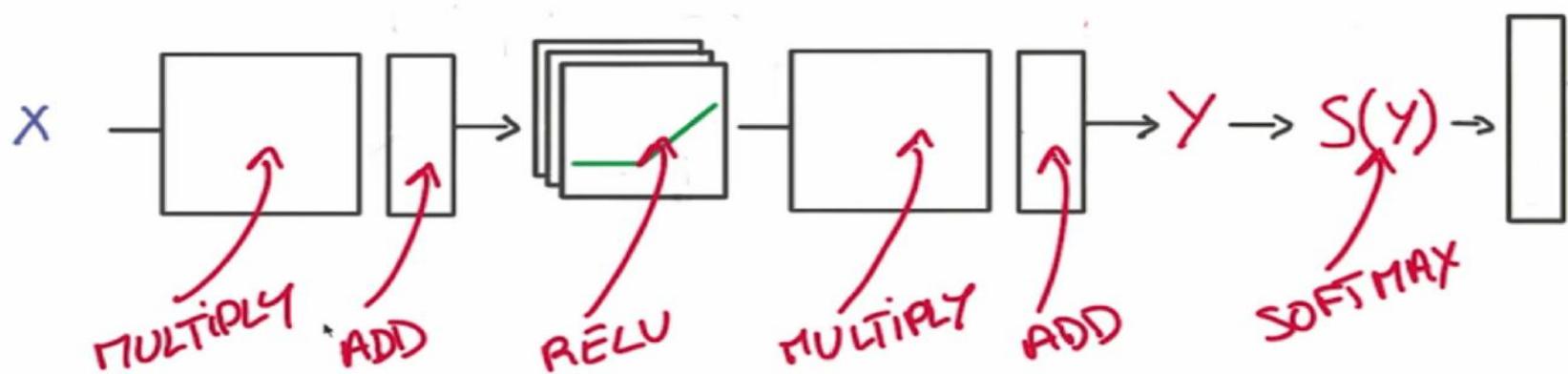
# The Chain Rule

$$[g(f(x))]' = g'(f(x)) \cdot f'(x)$$

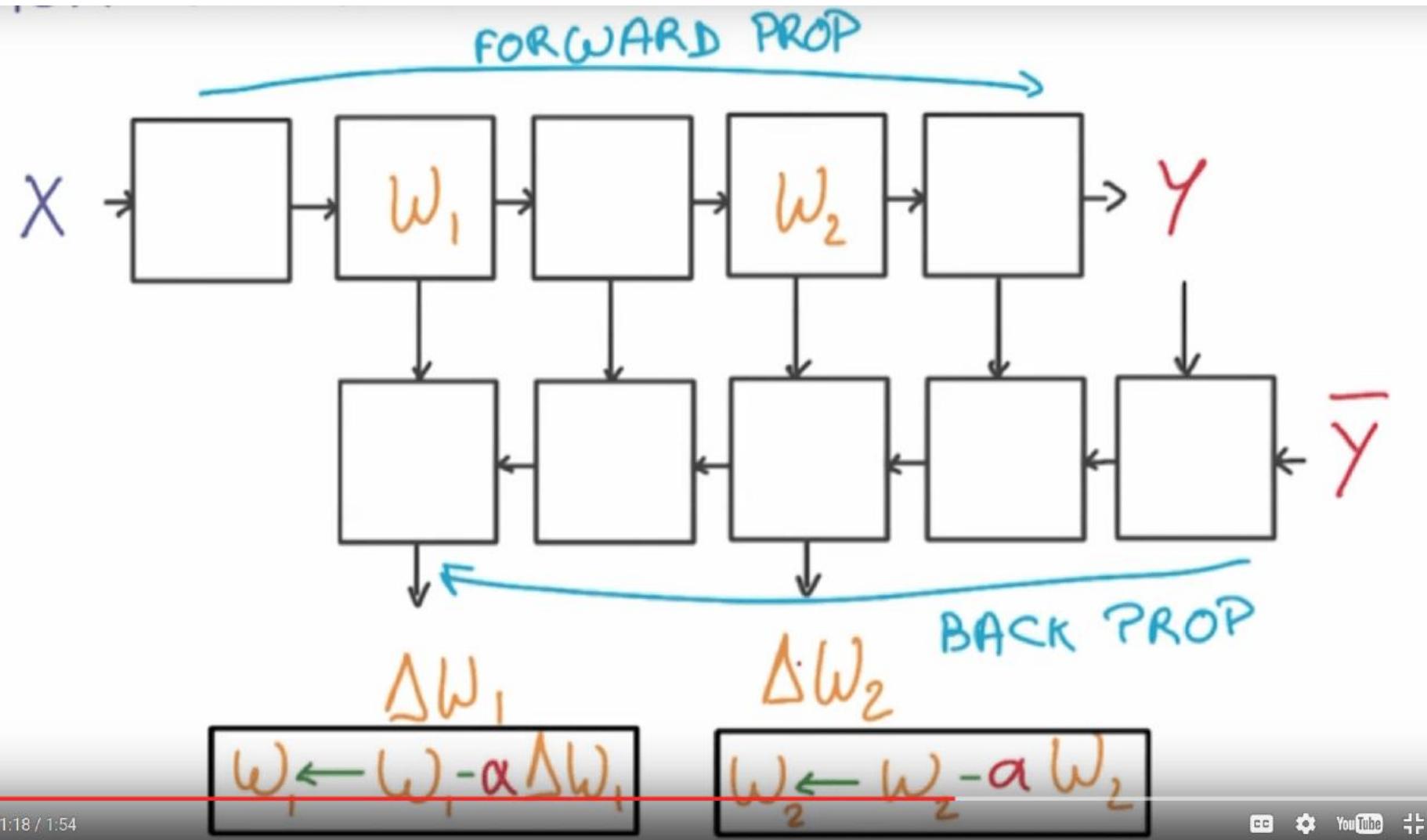
↗  
 DERIVATIVE

↗  
 PRODUCT

## STACKING UP SIMPLE OPERATIONS



# Back - propagation

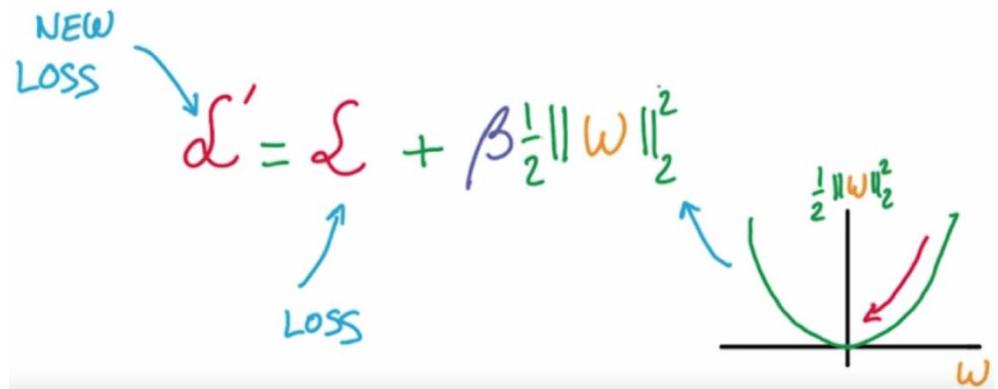


# Optimisation tricks

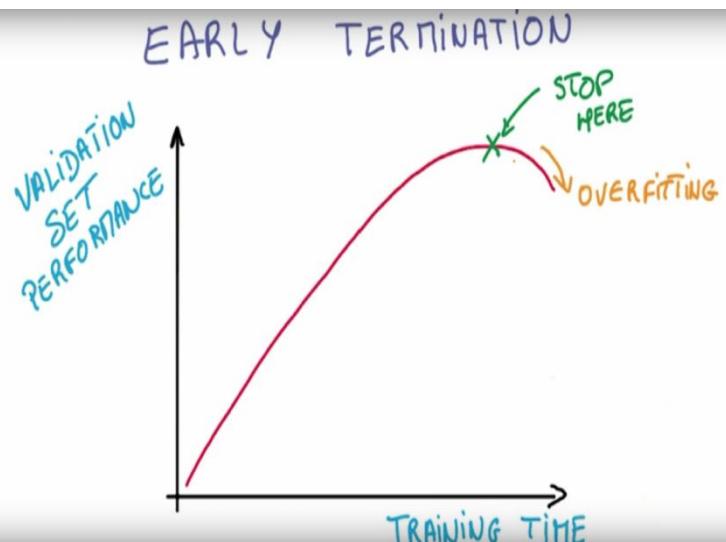
## REGULARIZATION



## L<sub>2</sub> REGULARIZATION

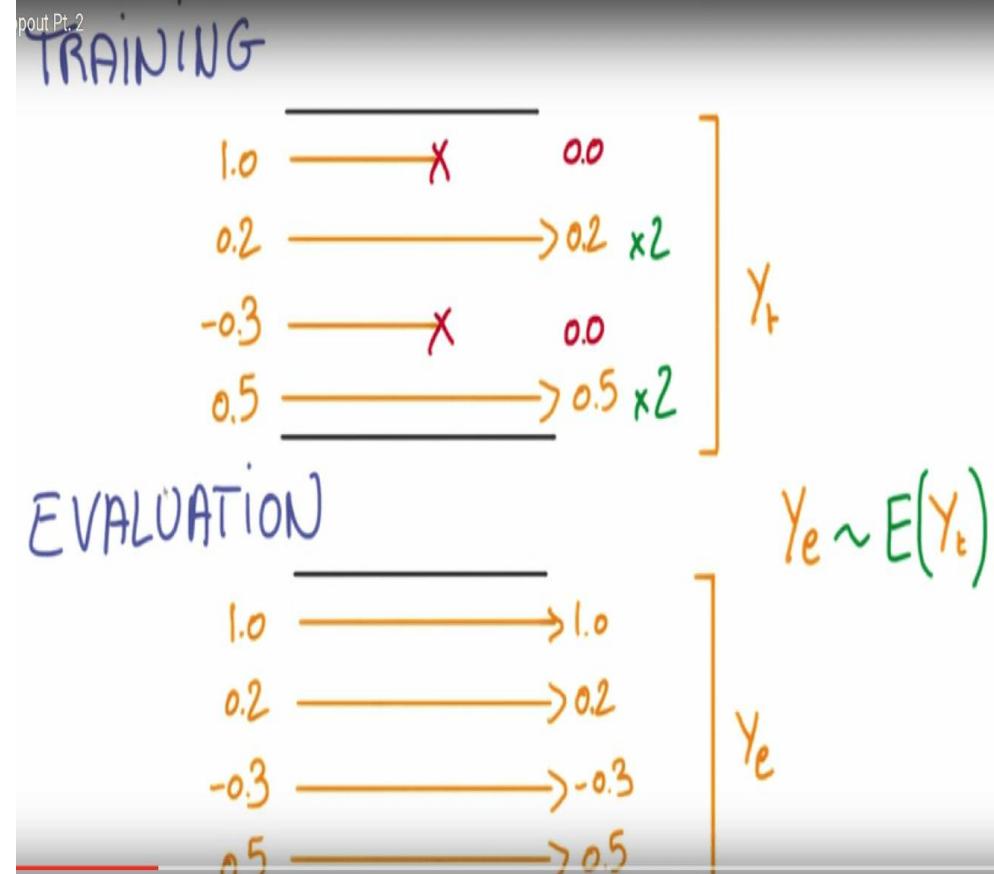
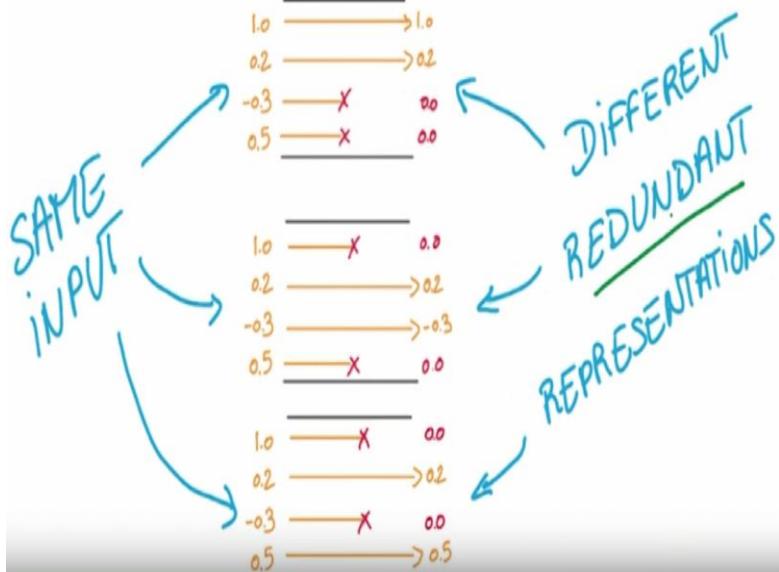


## EARLY TERMINATION

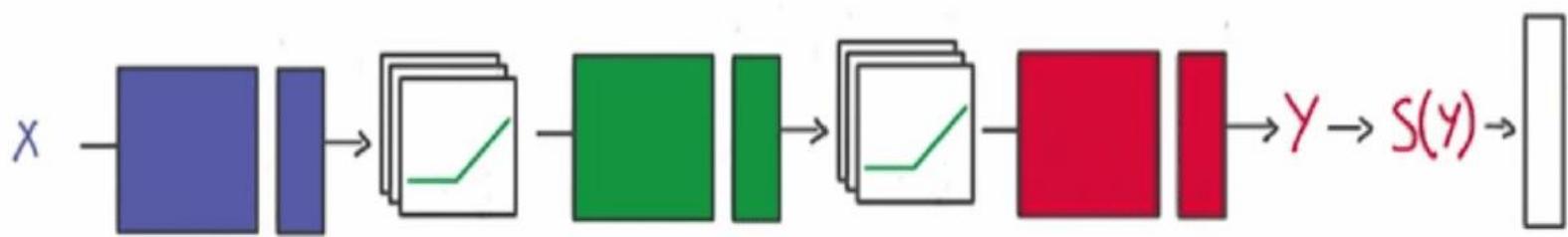
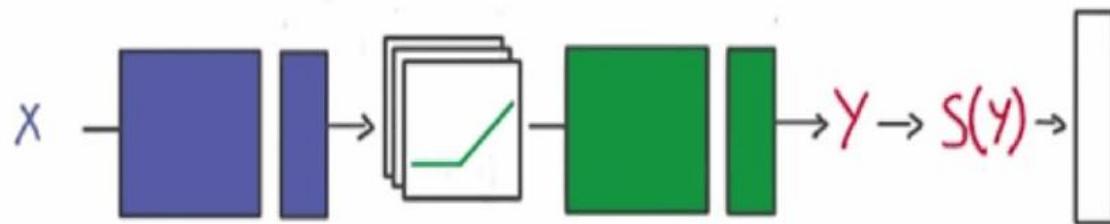


1.0	$x$	0.0
0.2		$> 0.2$
-0.3	$x$	0.0
0.5		$> 0.5$

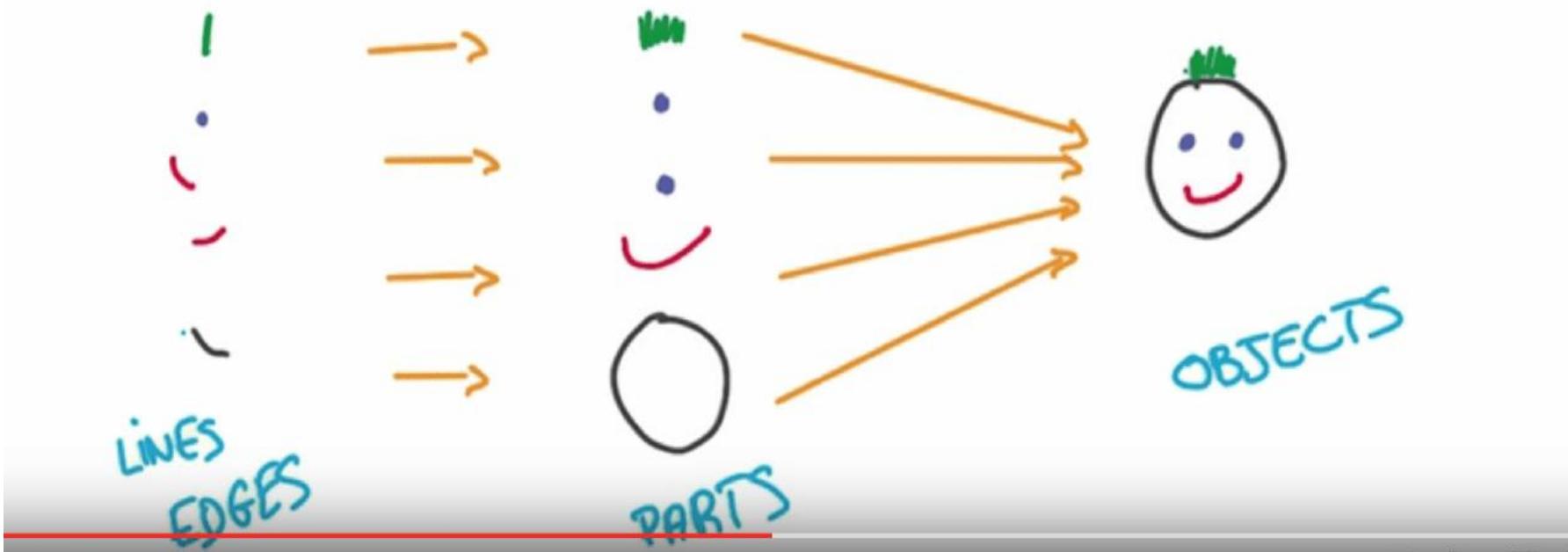
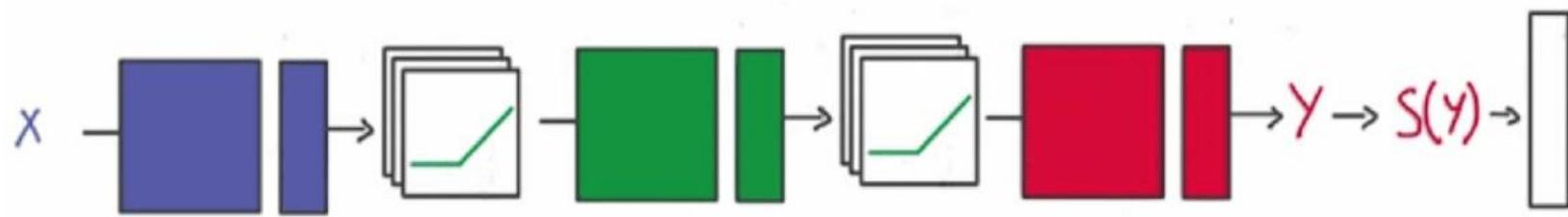
# Optimisation trick: dropout



# Deep networks



# Deep networks



# [tensorflow.org/paper/whitepaper2015.pdf](http://tensorflow.org/paper/whitepaper2015.pdf)

## **TensorFlow: Large-Scale Machine Learning on Heterogeneous Distributed Systems**

(Preliminary White Paper, November 9, 2015)

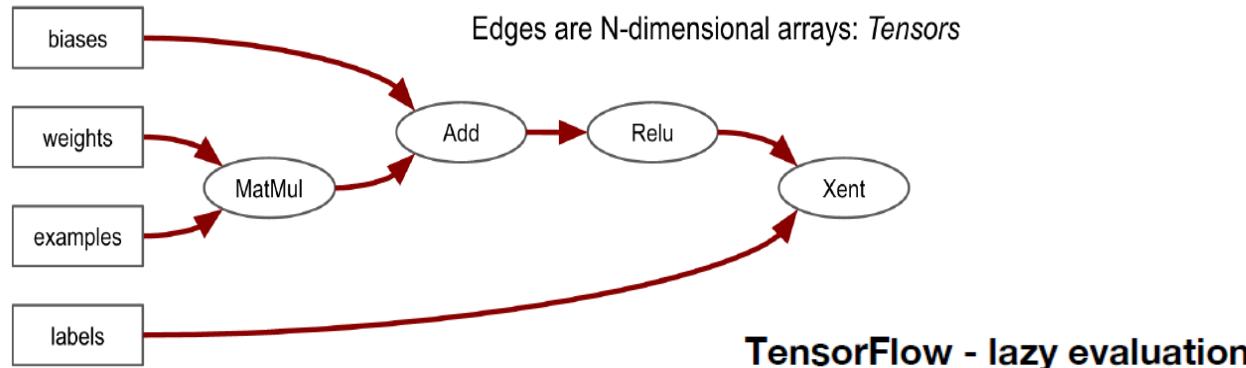
Martín Abadi, Ashish Agarwal, Paul Barham, Eugene Brevdo, Zhifeng Chen, Craig Citro, Greg S. Corrado, Andy Davis, Jeffrey Dean, Matthieu Devin, Sanjay Ghemawat, Ian Goodfellow, Andrew Harp, Geoffrey Irving, Michael Isard, Yangqing Jia, Rafal Jozefowicz, Lukasz Kaiser, Manjunath Kudlur, Josh Levenberg, Dan Mané, Rajat Monga, Sherry Moore, Derek Murray, Chris Olah, Mike Schuster, Jonathon Shlens, Benoit Steiner, Ilya Sutskever, Kunal Talwar, Paul Tucker, Vincent Vanhoucke, Vijay Vasudevan, Fernanda Viégas, Oriol Vinyals, Pete Warden, Martin Wattenberg, Martin Wicke, Yuan Yu, and Xiaoqiang Zhen<sup>\*</sup>  
Google Research\*

### **Abstract**

TensorFlow [1] is an interface for expressing machine learning algorithms, and an implementation for executing such algorithms. A computation expressed using TensorFlow can be executed with little or no change on a wide variety of heterogeneous systems, ranging from mobile devices such as phones and tablets up to large-scale distributed systems of hundreds of machines and thousands of computational devices such as GPU cards. The system is flexible and can be used to express a wide variety of algorithms, including training and inference algorithms for deep neural network models, and it has been used for conducting research and for deploying machine learning systems into production across more than a dozen areas of computer science and other fields, including speech recognition, computer vision, robotics, information retrieval, natural language processing, geographic information extraction, and computational drug discovery. This paper describes the TensorFlow interface and an implementation of that interface that we have built at Google. The TensorFlow API and a reference implementation were released as an open-source package under the Apache 2.0 license in November, 2015 and are available at [www.tensorflow.org](http://www.tensorflow.org).



TensorFlow is an open source software library for numerical computation using data flow graphs.



## What is a Data Flow Graph?

Data flow graphs describe mathematical computation with a directed graph of nodes & edges. Nodes typically implement mathematical operations, but can also represent endpoints to feed in data, push out results, or read/write persistent variables. Edges describe the input/output relationships between nodes. These data edges carry dynamically-sized multidimensional data arrays, or tensors. The flow of tensors through the graph is where TensorFlow gets its name. Nodes are assigned to computational devices and execute asynchronously and in parallel once all the tensors on their incoming edges becomes available.

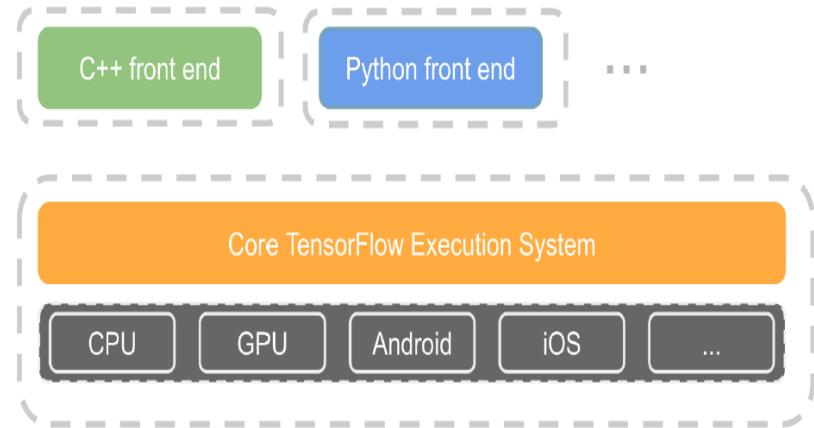
# Key Features

- Deep Flexibility
- True Portability
- Connect Research and Production
- Auto-Differentiation
- Language Options
- Maximize Performance



## Parallel Execution

- Launch graph in a Session
- Request output of some Ops with Run API
- TensorFlow computes set of Ops that must run to compute the requested outputs
- Ops execute, in parallel, as soon as their inputs are available



## There are hundreds of predefined Ops (and easy to add more)

- Basics: constant, random, placeholder, cast, shape
- Variables: assign, assign\_sub, assign\_add
- Queues: enqueue, enqueue\_batch, dequeue, blocking or not.
- Logical: equal, greater, less, where, min, max, argmin, argmax.
- Tensor computations: all math ops, matmul, determinant, inverse, cholesky.
- Images: encode, decode, crop, pad, resize, color spaces, random perturbations.
- Sparse tensors: represented as 3 tensors.
- ...

## And many neural net specific Ops

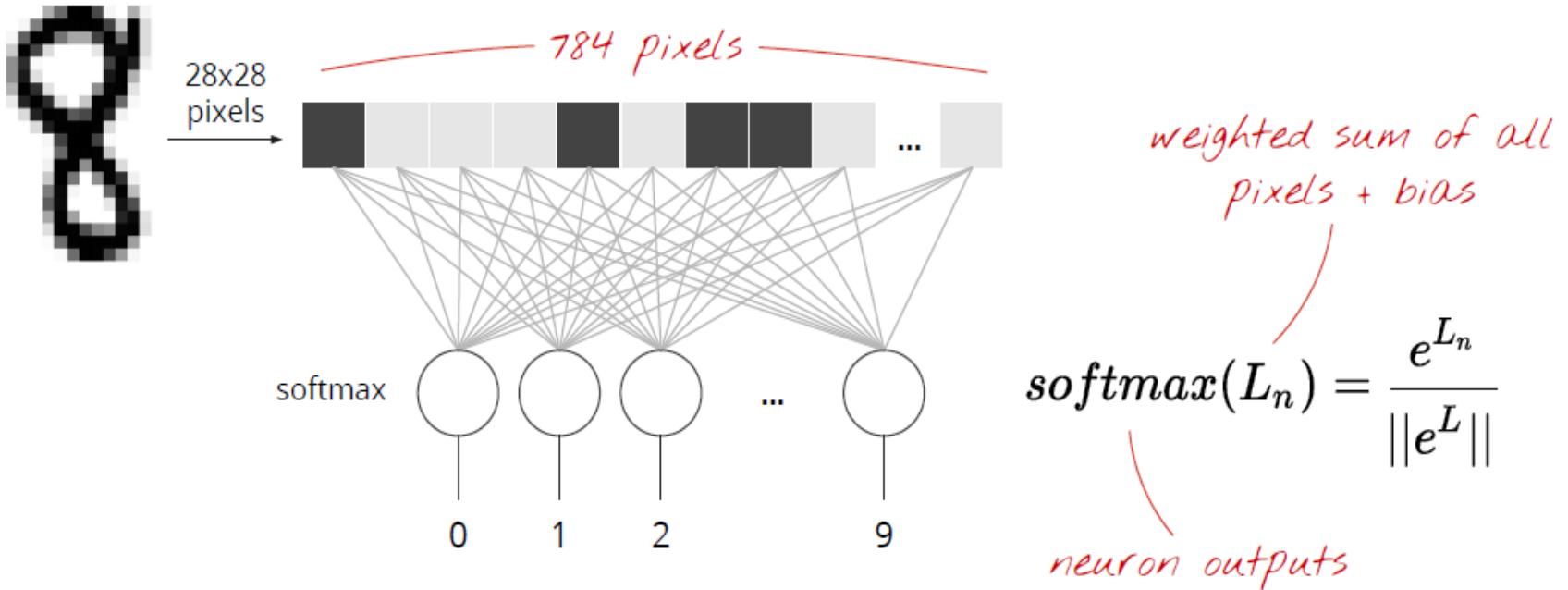
- Activations: sigmoid, tanh, relu, dropout, ...
- Pooling: avg, max.
- Convolutions: with many options.
- Normalization: local, batch, moving averages.
- Classification: softmax, softmax loss, cross entropy loss, topk.
- Embeddings: lookups/gather, scatter/updates.
- Sampling: candidate sampler (various options), sampling softmax.
- Updates: "fused ops" to speed-up optimizer updates (Adagrad, Momentum.)
- Summaries: Capture information for visualization.

# Hand-written digits: MNIST



MNIST = Mixed National Institute of Standards and Technology - Download the dataset at <http://yann.lecun.com/exdb/mnist/>

# Simple linear model



Slides from M. Gorner tutorial  
<http://www.youtube.com/watch?v=vq2nnJ4g6NO>

# TensorFlow full python code

```
import tensorflow as tf  
  
X = tf.placeholder(tf.float32, [None, 28, 28, 1])  
W = tf.Variable(tf.zeros([784, 10]))  
b = tf.Variable(tf.zeros([10]))  
init = tf.initialize_all_variables()  
  
# model  
Y = tf.nn.softmax(tf.matmul(tf.reshape(X, [-1, 784]), W) + b)  
  
# placeholder for correct answers  
Y_ = tf.placeholder(tf.float32, [None, 10])  
  
# Loss function  
cross_entropy = -tf.reduce_sum(Y_ * tf.log(Y))  
  
# % of correct answers found in batch  
is_correct = tf.equal(tf.argmax(Y, 1), tf.argmax(Y_, 1))  
accuracy = tf.reduce_mean(tf.cast(is_correct, tf.float32))
```

initialisation

model

SUCCESS metrics

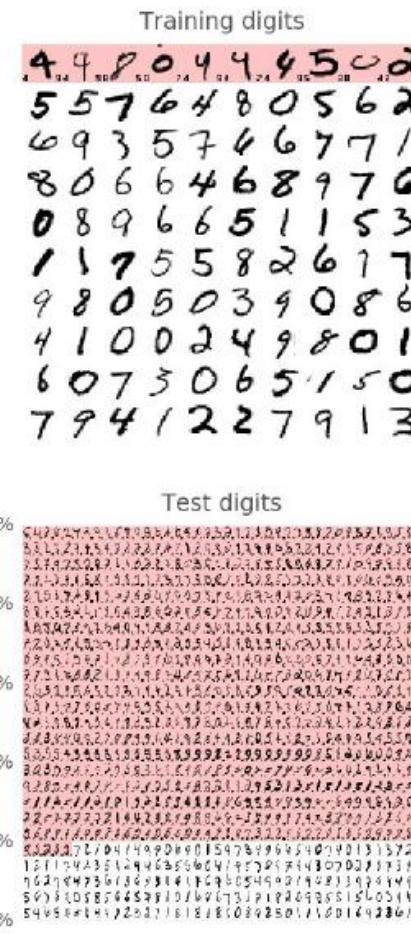
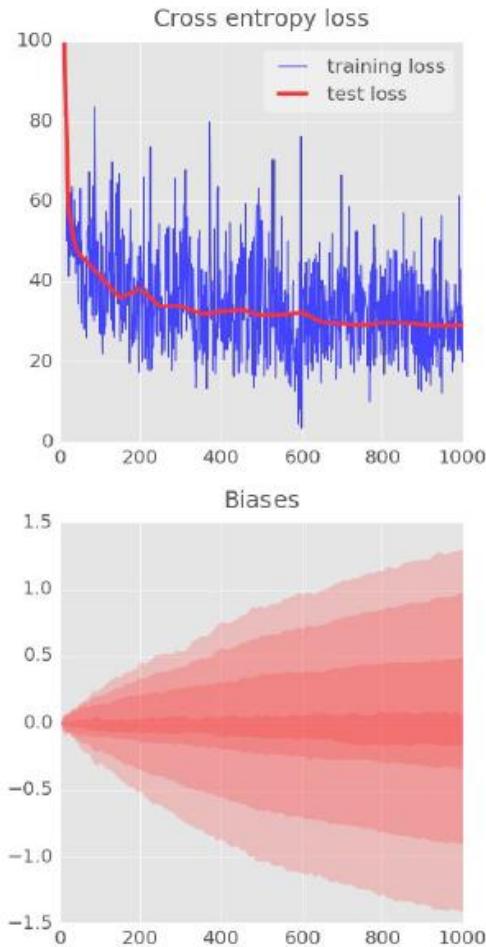
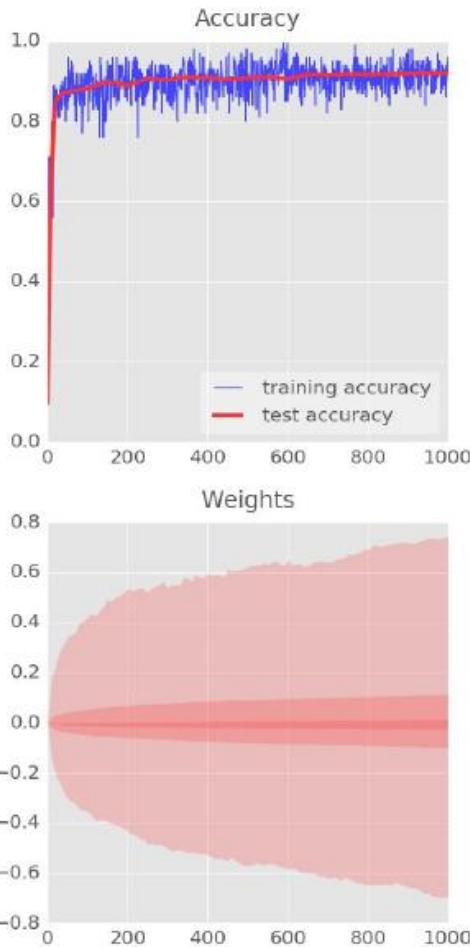
```
optimizer = tf.train.GradientDescentOptimizer(0.003)  
train_step = optimizer.minimize(cross_entropy)  
  
sess = tf.Session()  
sess.run(init)  
  
for i in range(10000):  
    # Load batch of images and correct answers  
    batch_X, batch_Y = mnist.train.next_batch(100)  
    train_data = {X: batch_X, Y_: batch_Y}  
  
    # train  
    sess.run(train_step, feed_dict=train_data)  
  
    # success ? add code to print it  
    a, c = sess.run([accuracy, cross_entropy], feed=train_data)  
  
    # success on test data ?  
    test_data = {X: mnist.test.images, Y_: mnist.test.labels}  
    a, c = sess.run([accuracy, cross_entropy], feed=test_data)
```

training step

Run

Slides from M. Gorner@youtube

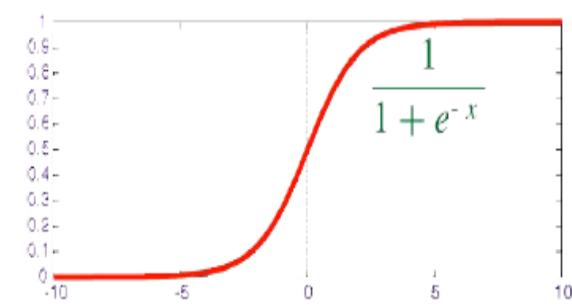
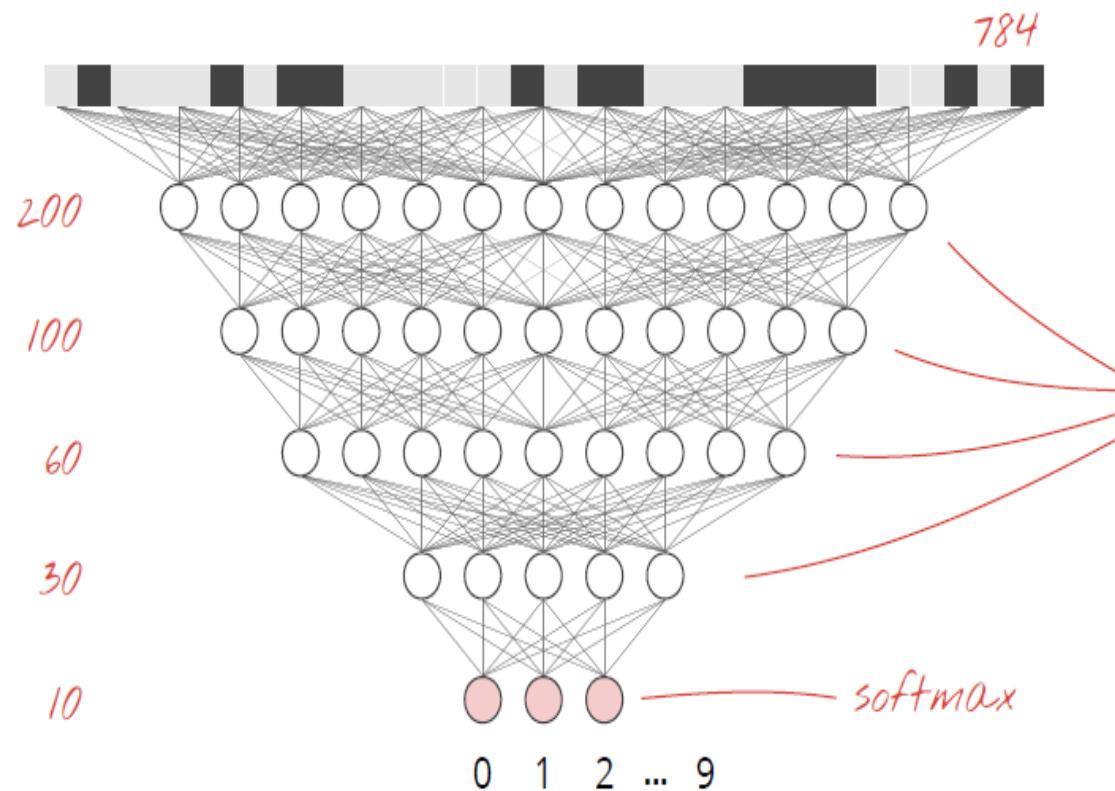
# Simple linear model



Slides from M. Gorner@youtube

# Multi-layer connected network

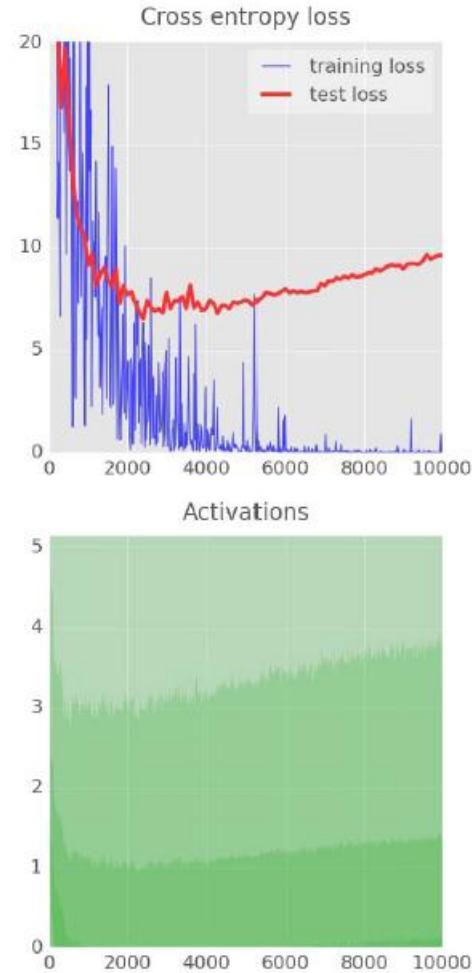
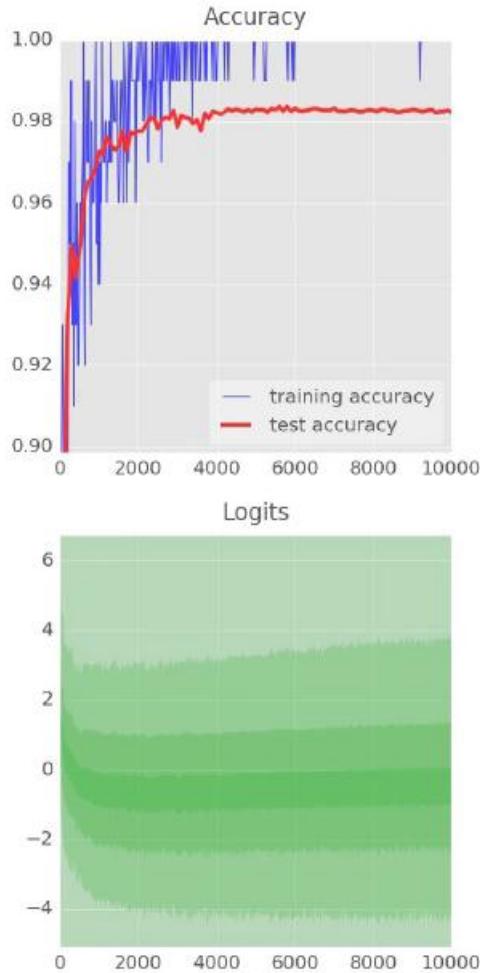
overKill



sigmoid function

Slides from M. Gorner@youtube

# Multi-layer connected network



Training digits

4 0 7 1 0 3 4 1 8 0  
5 0 0 8 3 6 0 1 8 3  
6 0 0 3 1 8 5 3 4 9  
1 9 2 5 8 0 2 0 1 0  
8 4 8 3 9 8 4 2 5 8  
0 6 1 4 5 3 8 5 5 1  
3 2 1 6 0 1 5 8 5 4  
8 6 6 2 0 9 1 0 4 5  
9 9 6 4 8 2 5 1 5 1  
0 5 8 1 1 2 7 9 9 0

Test digits

98%  
99%  
100%

98%  
99%  
100%

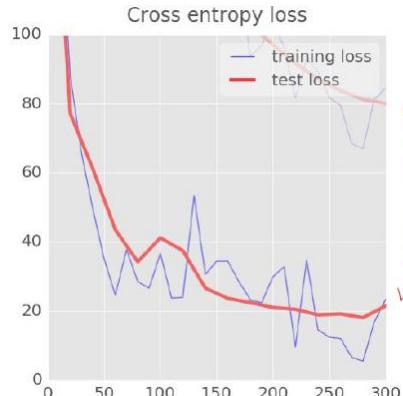
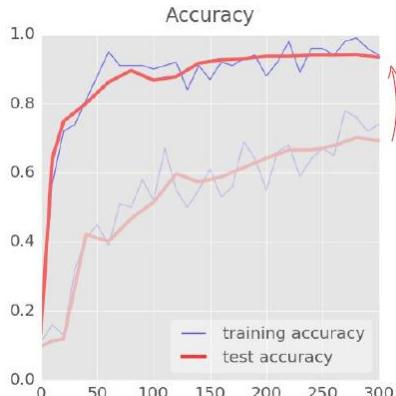
94%  
95%  
96%  
97%  
98%  
99%  
100%

90%  
91%  
92%  
93%  
94%  
95%  
96%  
97%  
98%  
99%  
100%

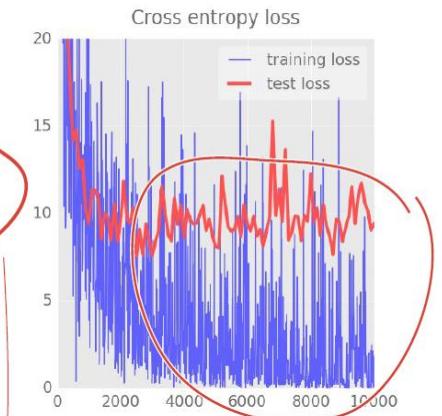
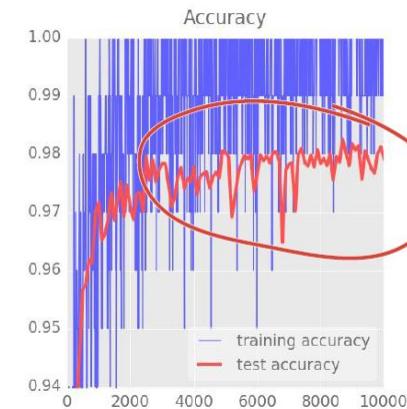
98!

# All tricks count

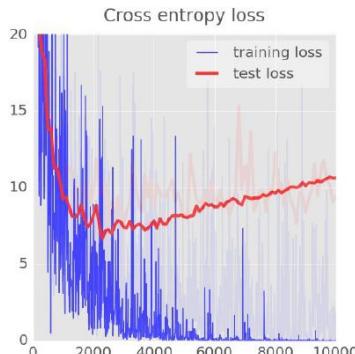
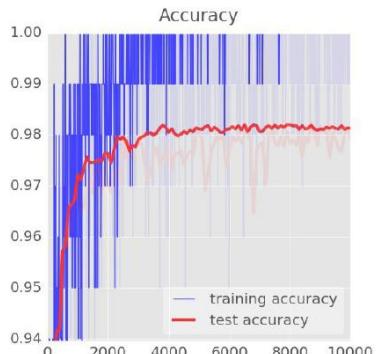
## Use RELU



## But noisy accuracy

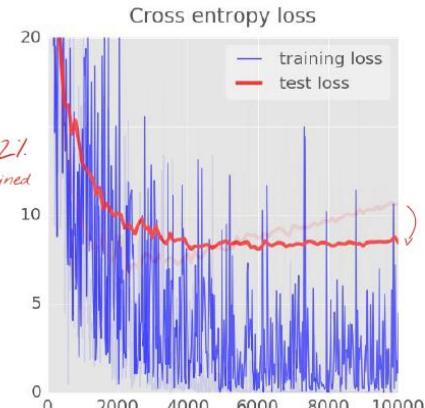
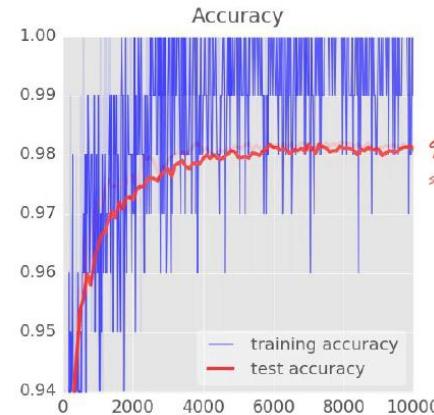


## Exponentially reduce learning rates



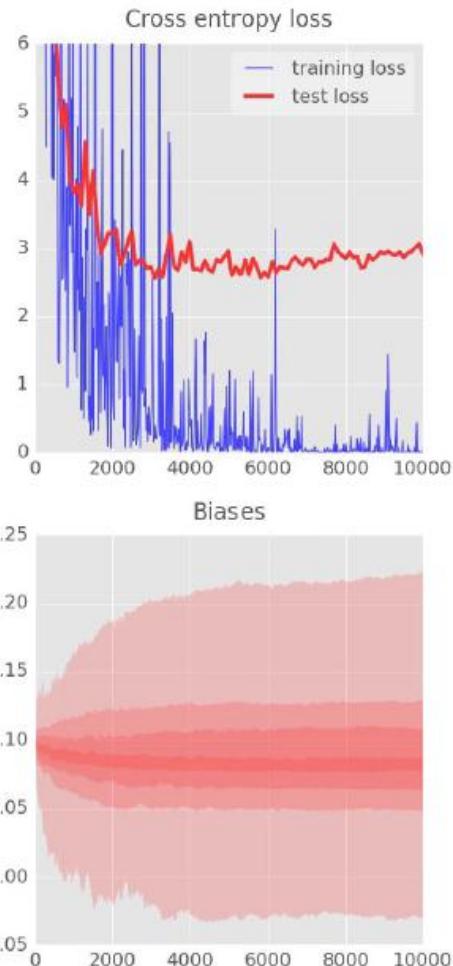
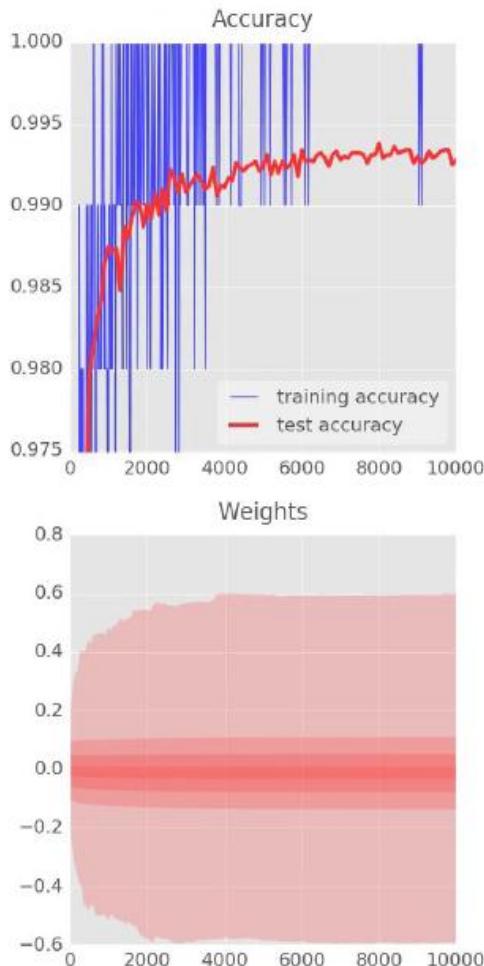
Learning rate 0.003 at start then dropping exponentially to 0.0001

## Add drop-out



RELU, decaying learning rate 0.003 → 0.0001 and dropout 0.75

# Can do better with conv network



# References

<http://www.deeplearning.book.org>

<http://download.tensorflow.org/paper/whitepaper2015.pdf>

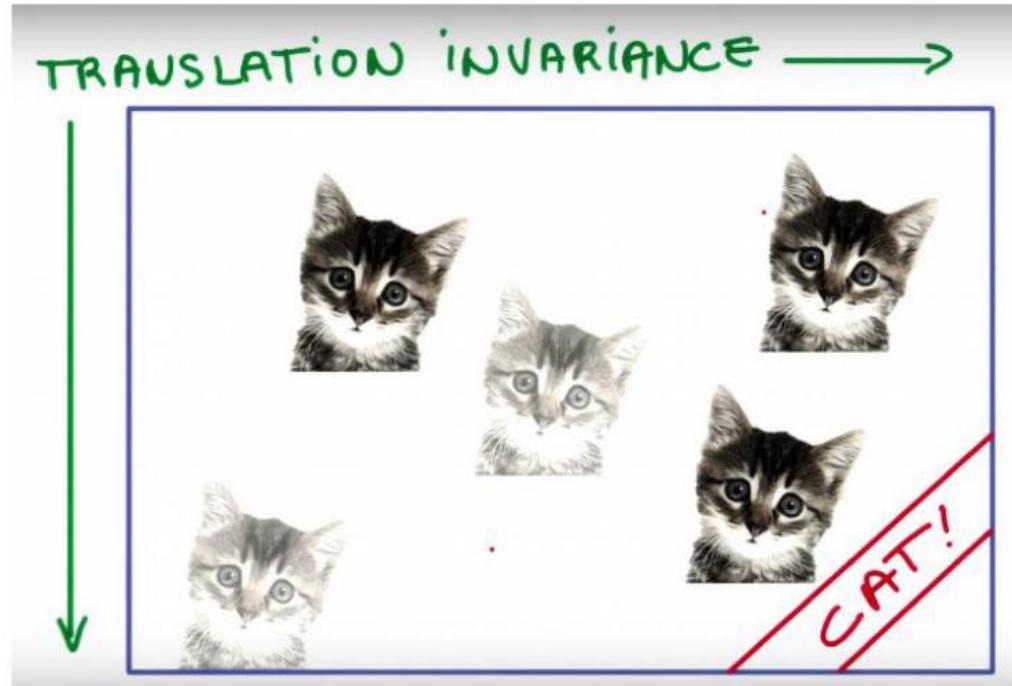
<https://www.tensorflow.org/>

<http://www.youtube.com/watch?v=vq2nnJ4g6NO>

<https://www.udacity.com/course/deep-learning--ud730>

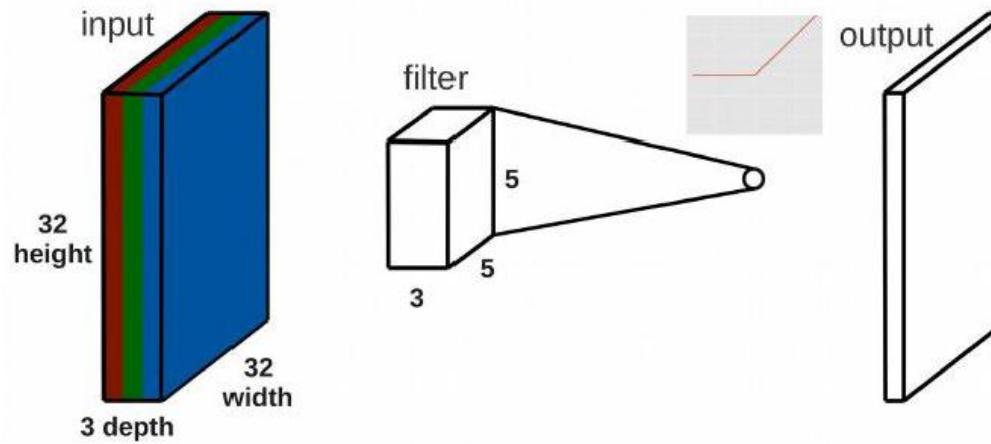
# Convolutional Neural Network

- ◆ Convolutional NNs are made to exploit local correlation and translation invariance.
- ◆ Typical application are image processing and computer vision.



# Convolutional Layer

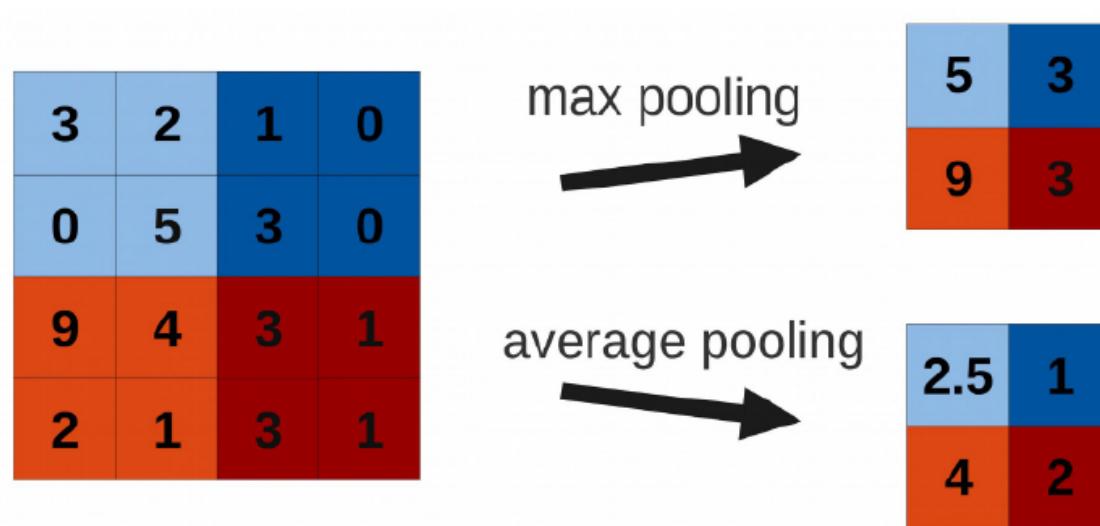
- ◆ A small filter (weight tensor) slides over the image to create a feature map.



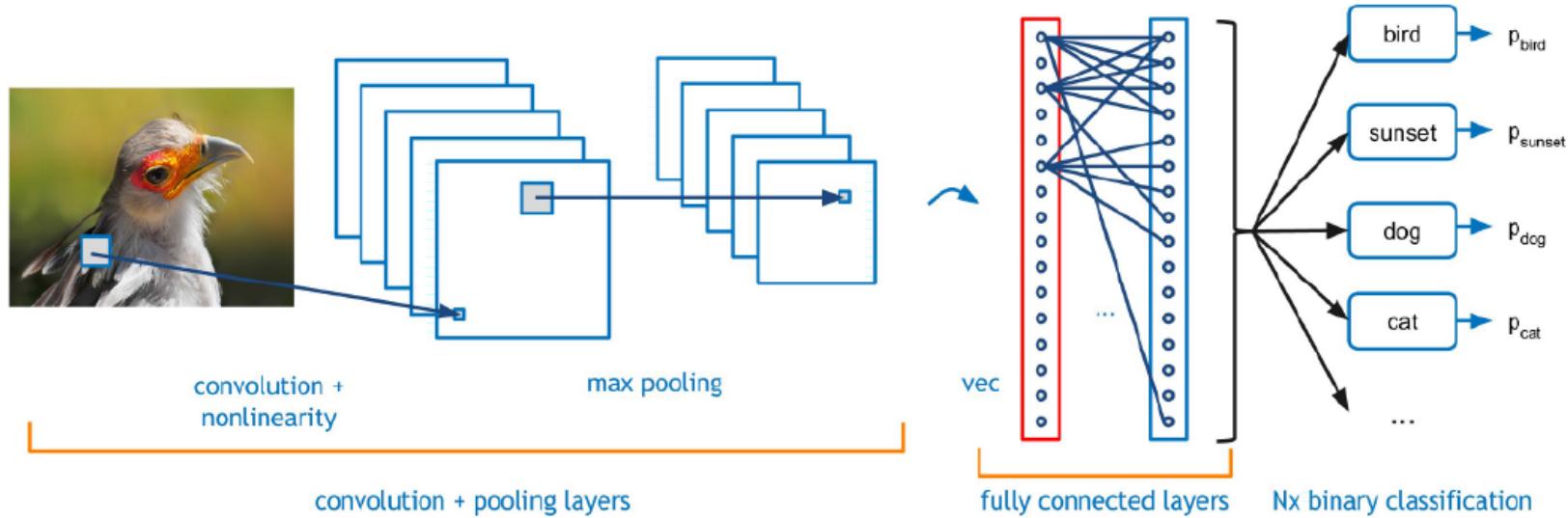
- ◆ Several filters could be stacked depth-wise.
- ◆ Several convolution can be applied one after the other to extract higher level features.

# Average and Max pooling layers

- ♦ When output size reduction is required:
  - ♦ Max pooling: takes the maximum of each patch.
  - ♦ Average pooling: takes the average of each patch.
- ♦ Eg: 2x2 filter with stride=2



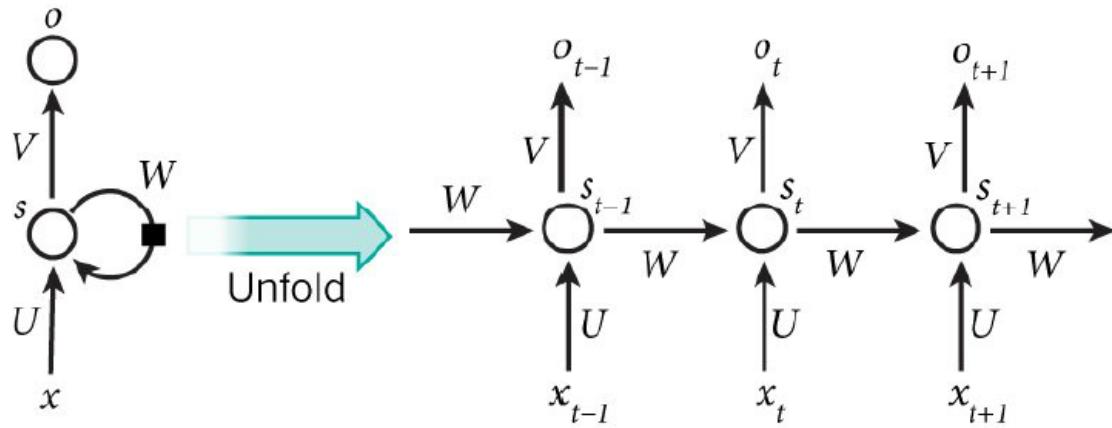
# Convolutional NN architecture



- ◆ Convolution and pooling layers to extract features.
- ◆ Fully connected layers used at the end to combine features.
- ◆ Applications in HEP: PID for neutrino experiments, jet tagging, reduction of seeds for tracking, etc..

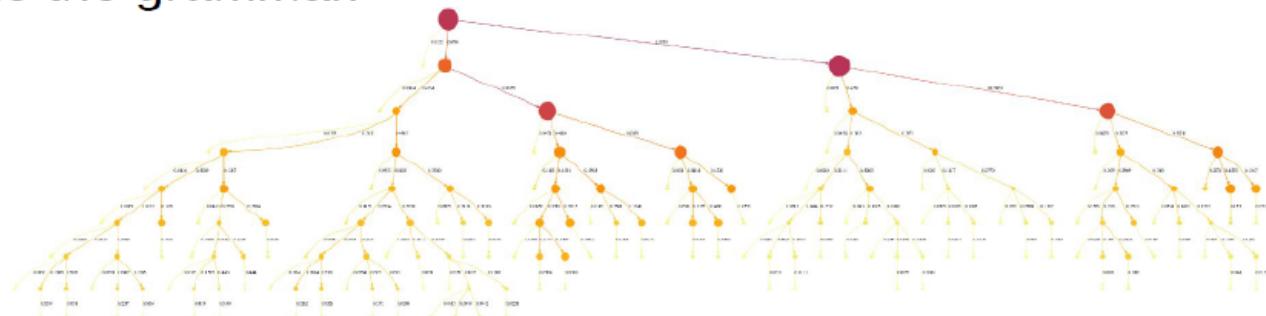
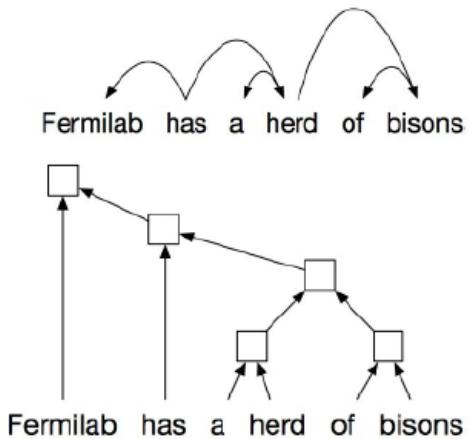
# Recursive NN

- Recursive NNs are deep NN created by applying the same set of weights recursively over a structured input of variable size.
- They are called recurrent because they perform the same task for every element of a sequence, with the output being depended on the previous computations.
- Typical applications in natural language processing: apply the recursive NN to each word in a sentence for text generation (predict the next word in the sequence), translation, etc..



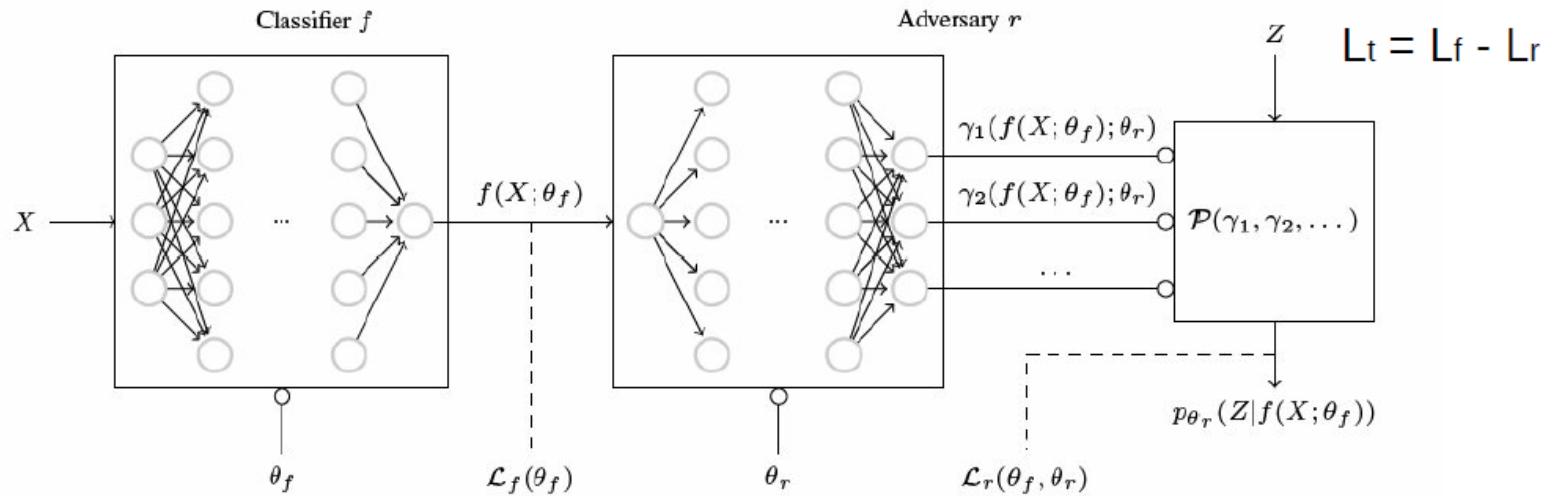
# Recursive NN: HEP application

- With particle-flow, collision raw data is converted in a list of particles.
- Complex objects (e.g. jets) are reconstructed by combining particles from this list.
- Image-processing approaches might not be the best in this case.
- Recursive NNs can be better suited.
  - Particles are like words in a sentence.
  - QCD is the grammar.



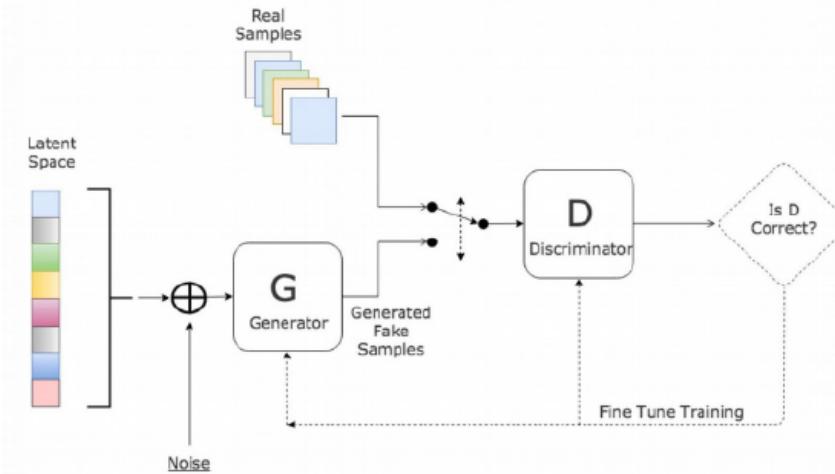
# Adversarial NN

- ◆ Two deep NNs in competition with each other.
- ◆ The first NN can be used to maximize the classification performance of signal against background events.
- ◆ The second NN can be trained to identify dependency on systematic uncertainty of the output of the first NN.
- ◆ The minimization of the global loss function guarantees optimal classification performance with reduced systematic dependence.



# Generative adversarial NN

- Adversarial NNs can also be used for image generation.
- A generator and a discriminator are trained in competition.
  - Generator: creates images starting from noise.
  - Discriminator: tries to distinguish between true and generated images.
- The global loss function is given by  $\text{Loss}(\text{gen}) - \text{Loss}(\text{discr})$ .
- The generator learns to make images that it has never seen simply by fooling the discriminator!**
- Application: gen of calo images, jets, and even high-level variables!



# Lorentz boost network: motivation

- ◆ Deep learning methods using high-level and low-level variables are outperforming shallow learning methods using high-level variables.
  - ◆ There is some information in low-level variables that high-level variables is not using.
- ◆ Deep learning methods using low-level variables only are not able to reproduce the same results as deep learning methods using also high-level variables.
  - ◆ Need of a new NN architecture to fully exploit low-level information and automatize the design of high-level variables.

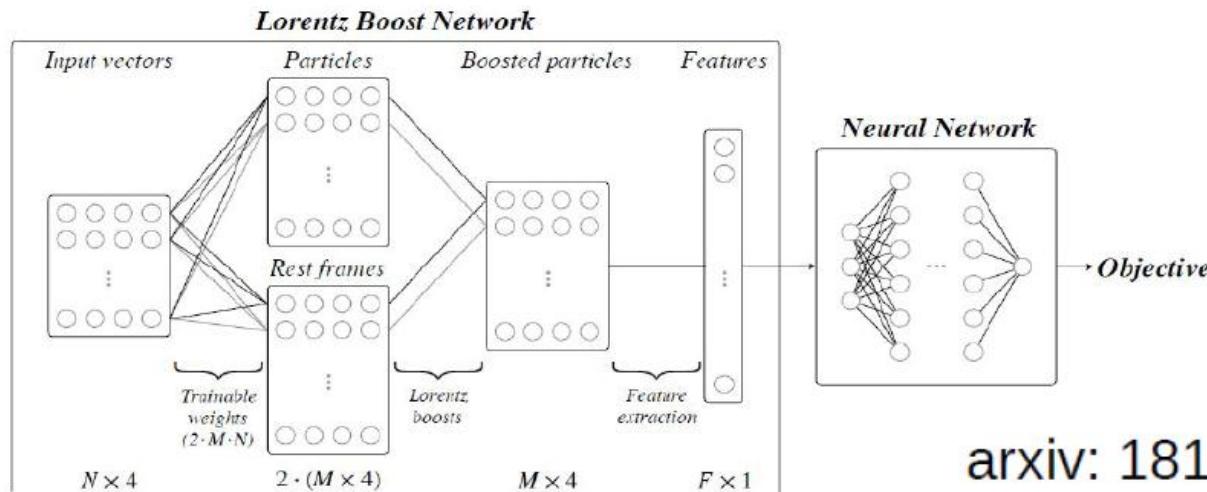
arxiv: 1812.09722

# LBN: network architecture

- ◆ Two stages approach:

combines them to form composite particles and rest frames.  
Composite particles are boosted in the rest frames where  
features are extracted.

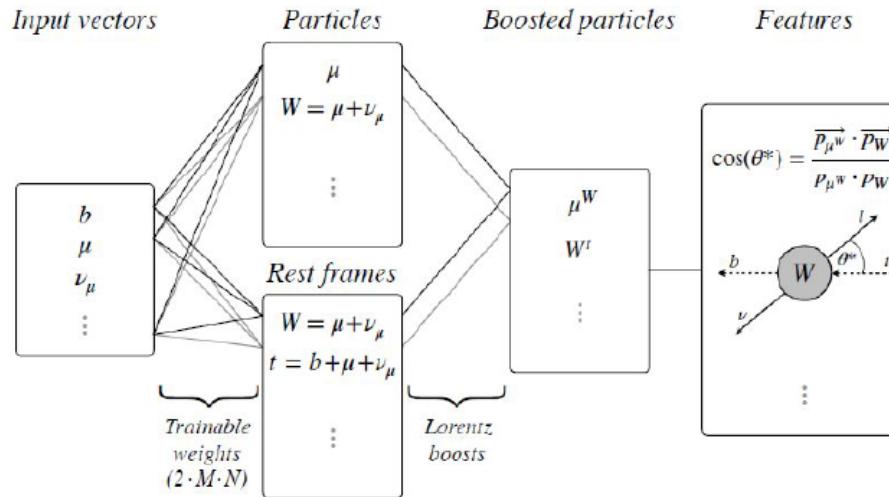
- ◆ An application specific NN uses LBN features as input.



arxiv: 1812.09722

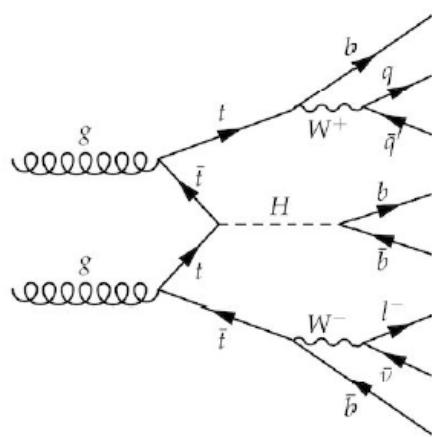
# LBN: features extraction

- Extract generic features from boosted particles.
  - Single particle features:  $E, m, pT, \eta, \phi$ .
  - Pairwise features: such as  $\cos(\theta)$  between all pairs.
- E.g.  $\cos(\theta^*)$  in the semi-leptonic decay of the top quark, defined as the angular difference between the direction of the charged lepton in the  $W$  rest frame and the direction of the  $W$  in the top rest frame.

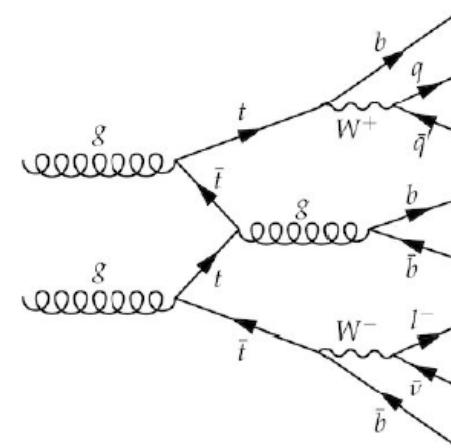


# LBN: application

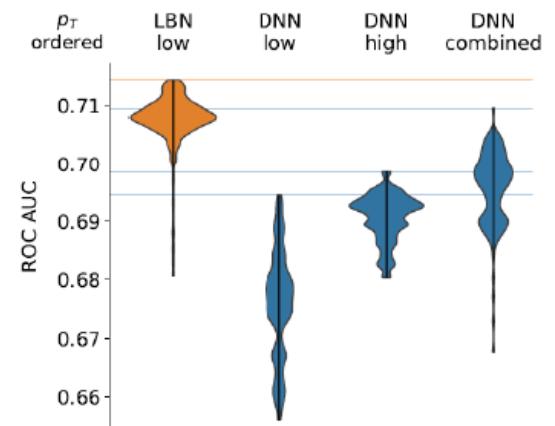
- LBN performance compared to standard DNN with low-, high- and combination of low- and high-level variables.



VS



- LBN shows improved performance in terms of ROC AUC.



# Conclusions

- ◆ Neural networks are widely used in HEP and will become more and more important.
- ◆ A quick overview of the basic structure of the most used NNs in HEP was given.
- ◆ New NNs layers, specifically engineered for HEP, were created.
  - ◆ In this case, high performance comes also with a good interpretability of the trained parameters.
  - ◆ NN is a quickly developing field. Exciting time to work on it and to find new applications for HEP.