Note that the core of what we do in this class is proving an implication, using an implication, proving a "there exists", using a "there exists", proving a "for all", and using a "for all". So as you go through the questions below, please make sure you apply those ideas. One step at a time, show your work. Some additional comments/hints/expectations are in the footnotes.

- 1. Use the following hypotheses:
 - H1: For all $r \in M$, if r likes Disneyland, then r is an element in the set S.
 - H2: For all $c \in P$, if c walks to school, then c is a rock climber.
 - H3: Every element in the set M is an element in the set P.
 - H4: For all $b \in M$, if b does not like Disneyland, then b is not an element in the set P.
 - H5: For all $s \in S$, the person s walks to school.

to prove the proposition: For all $m \in M$, the person m is a rock climber.¹

Proof. From H3, we know that every element in the set M is an element in the set P. So, for all $m \in M$, $m \in P$. From H2, we know that for all $c \in P$, if c walks to school, then c is a rock climber. So, for all $m \in M$, if m walks to school, then m is a rock climber. From H5, we know that for all $s \in S$, the person s walks to school. So, for all $m \in M$, if m likes Disneyland, then m is an element in the set s. From H1, we know that for all s0 is an element in the set s1. From H4, we know that for all s1 in the set s2. From H4, we know that for all s2 is an element in the set s3. From H4, we know that for all s3 is an element in the set s4. From H4, we know that for all s5 is not an element in the set s6. From H4, if s6 does not like Disneyland, then s7 is not an element in the set s8. From H4, the person s9 is a rock climber.

¹As in the previous homework, take things one step at a time. To pick an example that is not from this HW (but apply what I am saying here to the this homework question), say we had a hypothesis For all $j \in T$, if j sings, then j plays baseball and we also knew $b \in T$. Then we'd get if b sings, then b plays baseball. Then, if we also later knew b sings, we can combine this with the implication to get b plays baseball.

2. Prove²: for all $a \in \mathbb{Z}$, for all $b \in \mathbb{Z}$, for all $c \in \mathbb{Z}$, if $a \mid b$, and $b \mid c$, then $a \mid c$.

This comment applies to question 1, but also to question 2, and to many of the questions below: do not ignore the "for all" at the beginning of the statement you prove.

3.	Prove:	for all	$x \in \mathbb{Z}$, i	$f x ext{ is even}$	n, then	x^2 is even	. After	processir	ng the "	for all",	provide	a direct	proof.	

4. Prove: for all $c \in \mathbb{Z}$, if c^2 is even, then c is even.	After processing the	"for all", provide an i	ndirect proof.

5.	Prove:	for all $c \in \mathbb{Z}$,	, if c^2 is even,	then c is even.	After processing	g the "for all",	provide a proof b	by contradiction.