

It is easiest to download the instructions file, since you can see exactly how I got certain symbols. My suggestion is to rename the file right away, so that you don't actually turn in the instructions, but instead you turn in your work. If your name is Peter Parker, perhaps a good name for your LaTeX file is HW01-PeterParker.tex, and then this would end up created a PDF file called HW01-PeterParker.pdf. I am not requiring any specific naming, but renaming the instructions file right away is helpful.

Answer each question on a separate page. Use the newpage command (with a backslash in front of newpage) to separate pages. At the top of each page, you may choose to keep the question text and write your answer below, OR you can delete the question text and just have your answer. Either way is fine!

1. Find a piece-wise non-recursive formula for the sequence a_n whose first terms are: 2, 2, 5, 5, 8, 8, 11, 11, 14, 14, 17, 17 and so on.

Clarification: When $x = 1$ we have $y = 1$. When $x = 2$ then $y = 2$. When $x = 3$ then $y = 5$. However, I am just using x and y for convenience. Change the x s to n s, and the y s to a_n s when you turn in your homework.

- The formula for this question can be expressed as $a_n = \begin{cases} 2 + \frac{3(n-1)}{2} & \text{for all } n \text{ if } n \text{ is odd} \\ 2 + \frac{3(n-2)}{2} & \text{for all } n \text{ if } n \text{ is even} \end{cases}$.

2. For this homework question, let C be the set of all car brands.

- (a) With correct notation, state three elements of C .

- Let r be "Rolls-Royce", let f be "Ford", and let t be "Toyota". Then $r, f, t \in C$.

- (b) Write what $\boxed{r \in C}$ means in plain English.

- In plain english and applying my example for r , $r \in C$ means that Rolls-Royce is an element of the set of all car brands. More generally speaking, it just means that r is an element of the set C . Therefore, we can deduce that r is a car brand!

3. Let p be the proposition "Madison is the capital of Wisconsin", and let q be the proposition "Tables are a type of food", and let r be "Dogs are not animals". State each of the following in words:

- (a) $p \wedge q$

- Madison is the capital of Wisconsin and tables are a type of food.

- (b) $p \vee q$

- Madison is the capital of Wisconsin or tables are a type of food.

- (c) $(r \wedge p) \rightarrow q$

- If dogs are not animals and Madison is the capital of Wisconsin, then tables are a type of food.

- (d) $q \rightarrow \neg r$

- If tables are a type of food, then dogs are animals.

- (e) $r \wedge r$

- Dogs are not animals and dogs are not animals.

4. Let p be the proposition "Madison is the capital of Wisconsin", and let q be the proposition "Tables are a type of food", and let r be "Dogs are not animals". For each proposition below, state in symbols and ALSO determine if the proposition is true or false (and provide some explanation for why).

- (a) Madison is the capital of Wisconsin and dogs are not animals.

Symbolic representation: $p \wedge r$

Truth value: False

Explanation: We know conjunction of two propositions is true, in this case, only if both p and r are true. Since r ("Dogs are not animals") is clearly false, the entire statement is false.

p	q	r	$(p \rightarrow \neg q)$	$(q \vee r)$	$(p \rightarrow \neg q) \wedge (q \vee r)$
T	T	T			
T	T	F			
T	F	T			
T	F	F			
F	T	T			
F	T	F			
F	F	T			
F	F	F			

- (b) Madison is the capital of Wisconsin or dogs are animals.

Symbolic representation: $p \vee \neg r$

Truth value: True

Explanation: We also know the disjunction of two propositions is true if either p or $\neg r$ (the negation of r) is true. Since p ("Madison is the capital of Wisconsin") is true, the entire statement is true, regardless of the truth value of $\neg r$.

- (c) If dogs are animals, then tables are a type of food.

Symbolic representation: $\neg r \rightarrow q$

Explanation:

- (d) If Madison is not the capital of Wisconsin, then dogs are not animals.

Symbolic representation: $\neg p \rightarrow r$

Explanation:

- (e) Dogs are not animals or dogs are animals.

Symbolic representation: $r \vee \neg r$

Explanation:

5. Provide a complete truth table for $(p \rightarrow \neg q) \wedge (q \vee r)$.

Clarification: for a complete truth table, I am expecting you to "show your work" by giving relevant columns that lead up to the final column. For example, one of the columns you should display work for is $q \vee r$.