

Graphs (cont'd.)

Exercise

Give the formal description of the directed graph below.



$$G_9 = (V_9, E_9)$$

$$V_9 = \{1, 2, 3, 4, 5, 6\}$$

$$E_9 = \{(1, 2), (1, 5), (2, 1), (2, 4), (5, 4), (5, 6), (6, 1), (6, 3)\}$$

Graph G_9

PATHS

Paths with length of 2: $V = \{1, 2, 4\}$

$\{1, 5, 4\}, \{1, 5, 6\}, \{2, 1, 5\}, \{6, 1, 2\}, \{5, 6, 3\}, \{5, 6, 1\}, \{6, 1, 2\}, \{1, 2, 1\}, \{2, 1, 2\}$

Paths with length of 3: $V = \{2, 1, 5, 4\},$

$\{6, 1, 2, 4\}, \{1, 5, 6, 3\}, \{2, 1, 5, 6\}, \{6, 1, 5, 4\}, \{5, 6, 1, 2\}, \{1, 5, 6, 1\}, \{5, 6, 1, 5\}, \{6, 1, 5, 6\}$

Paths with length of 4: $V = \{5, 6, 1, 2, 4\}, \{2, 1, 5, 6, 3\}, \{6, 1, 2, 4, 5\}$

SIMPLE PATHS

Simple paths with length of 2: $V = \{1, 2, 4\}, \{1, 5, 4\}, \{6, 1, 2\}, \{1, 5, 6\}, \{2, 1, 5\}, \{5, 6, 3\}, \{5, 6, 1\}, \{2, 1, 5\}$

Simple paths with length of 3: $V = \{2, 1, 5, 6\}, \{6, 1, 5, 4\}, \{6, 1, 2, 4\}, \{5, 6, 1, 2\}, \{1, 5, 6, 3\}, \{2, 1, 5, 4\}$

Simple paths with length of 4: $V = \{6, 1, 2, 4, 5\}, \{5, 6, 1, 2, 4\}, \{2, 1, 5, 6, 3\}$

SIMPLE CYCLE

Simple cycle with length of 2: $V = \{1, 2, 1\}, \{2, 1, 2\}$

Simple cycle with length of 3: $V = \{1, 5, 6, 1\}, \{5, 6, 1, 5\}, \{6, 1, 5, 6\}$

INDEGREE

Indegree of node 1: $V = \{ 2, 6 \}$

node 2: $V = \{ 1 \}$

node 3: $V = \{ 6 \}$

node 4: $V = \{ 2, 5 \}$

node 5: $V = \{ 1 \}$

node 6: $V = \{ 5 \}$

OUTDEGREE

Outdegree of node 1: $V = \{ 2, 5 \}$

node 2: $V = \{ 1, 4 \}$

node 3: $V = \{ \text{none} \}$

node 4: $V = \{ \text{none} \}$

node 5: $V = \{ 4, 6 \}$

node 6: $V = \{ 1, 3 \}$

ADJACENT TO

Adjacent to node 1: $V = \{ 2, 6 \}$

node 2: $V = \{ 1 \}$

node 3: $V = \{ 6 \}$

node 4: $V = \{ 2, 5 \}$

node 5: $V = \{ 1 \}$

node 6: $V = \{ 5 \}$

ADJACENT FROM

Adjacent from node 1: $V = \{ 2, 5 \}$

node 2: $V = \{ 1, 4 \}$

node 3: $V = \{ \text{none} \}$

node 4: $V = \{ \text{none} \}$

node 5: $V = \{ 4, 6 \}$

node 6: $V = \{ 1, 3 \}$

EDGES OF INCIDENT

Edges of incident to node 1: $E = \{1, 2\}, \{2, 1\}, \{1, 5\}, \{6, 1\}$

node 2: $E = \{1, 2\}, \{2, 1\}, \{2, 4\}$

node 3: $E = \{6, 3\}$

node 4: $E = \{2, 4\}, \{5, 4\}$

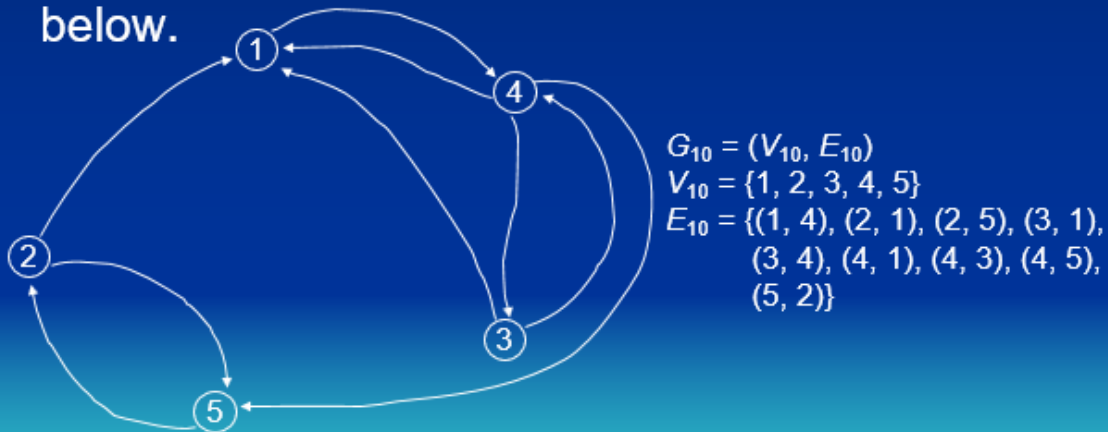
node 5: $E = \{1, 5\}, \{5, 6\}, \{5, 4\}$

node 6: $E = \{5, 6\}, \{6, 1\}, \{6, 3\}$

Graphs (cont'd.)

Exercise

Give the formal description of the directed graph below.



$$G_{10} = (V_{10}, E_{10})$$

$$V_{10} = \{1, 2, 3, 4, 5\}$$

$$E_{10} = \{(1, 4), (2, 1), (2, 5), (3, 1), (3, 4), (4, 1), (4, 3), (4, 5), (5, 2)\}$$

PATHS

Paths with length of 2: V

$= \{2, 1, 4\}, \{4, 5, 2\}, \{1, 4, 5\}, \{3, 4, 5\}, \{5, 2, 1\}, \{3, 1, 4\}, \{3, 4, 1\}, \{1, 4, 3\}, \{2, 5, 2\}, \{5, 2, 5\}, \{3, 4, 3\}, \{4, 3, 4\}$

Paths with length of 3: V

$= \{2, 1, 4, 3\}, \{5, 2, 1, 4\}, \{4, 5, 2, 1\}, \{2, 1, 4, 5\}, \{3, 1, 4, 5\}, \{3, 4, 5, 2\}, \{1, 4, 3, 1\}, \{4, 3, 1, 4\}, \{3, 1, 4, 3\}, \{1, 4, 5, 2\}$

Paths with length of 4: $V = \{3, 4, 5, 2, 1\}, \{5, 2, 1, 4, 5\}, \{5, 2, 1, 4, 3\}$

$, \{3, 1, 4, 5, 2\}, \{2, 1, 4, 5, 2\}, \{4, 5, 2, 1, 4\}, \{1, 4, 5, 2, 1\}$

SIMPLE PATHS

Simple paths with length of 2: V

$= \{3, 4, 5\}, \{2, 1, 4\}, \{4, 5, 2\}, \{3, 1, 4\}, \{3, 4, 1\}, \{4, 5, 2\}, \{4, 3, 1\}, \{1, 4, 5\}, \{5, 2, 1\}$

Simple paths with length of 3: $V =$

$\{3, 1, 4, 5\}, \{5, 2, 1, 4\}, \{1, 4, 5, 2\}, \{4, 5, 2, 1\}, \{3, 4, 5, 2\}, \{2, 1, 4, 5\}, \{2, 1, 4, 3\}$

Simple paths with length of 4: $V = \{3, 4, 5, 2, 1\}, \{3, 1, 4, 5, 2\}, \{5, 2, 1, 4, 3\}$

SIMPLE CYCLE

Simple cycle with length of 2: $V = \{2, 5, 2\}, \{5, 2, 5\}, \{4, 1, 4\}, \{1, 4, 1\}, \{3, 4, 3\}, \{4, 3, 4\}$

Simple cycle with length of 3: $V = \{3, 1, 4, 3\}, \{1, 4, 3, 1\}, \{4, 3, 1, 4\}$

Simple cycle with length of 4: $V = \{2, 1, 4, 5, 2\}, \{5, 2, 1, 4, 5\}, \{1, 4, 5, 2, 1\}, \{4, 5, 2, 1, 4\}$

INDEGREE

Indegree of node 1: $V = \{ 2,3,4 \}$

node 2: $V = \{ 5 \}$

node 3: $V = \{ 4 \}$

node 4: $V = \{ 1,3 \}$

node 5: $V = \{ 2,4 \}$

OUTDEGREE

Outdegree of node 1: $V = \{ 4 \}$

node 2: $V = \{ 1,5 \}$

node 3: $V = \{ 1,4 \}$

node 4: $V = \{ 1,3,5 \}$

node 5: $V = \{ 2 \}$

ADJACENT TO

Adjacent to node 1: $V = \{ 2,3,4 \}$

node 2: $V = \{ 5 \}$

node 3: $V = \{ 4 \}$

node 4: $V = \{ 1,3 \}$

node 5: $V = \{ 1,3 \}$

ADJACENT FROM

Adjacent from node 1: $V = \{ 4 \}$

node 2: $V = \{ 1,5 \}$

node 3: $V = \{ 1,4 \}$

node 4: $V = \{ 1,3,5 \}$

node 5: $V = \{ 2 \}$

EDGES OF INCIDENT

Edges of Incident to node 1: $V = \{1,4\},\{4,1\},\{3,1\},\{2,1\}$

node 2: $V = \{2,5\},\{5,2\},\{2,1\}$

node 3: $V = \{3,1\},\{4,3\},\{3,4\}$

node 4: $V = \{4,5\},\{4,3\},\{4,1\},\{1,4\},\{3,4\}$

node 5: $V = \{2,5\},\{4,5\},\{5,2\}$