

L#13 Arrays

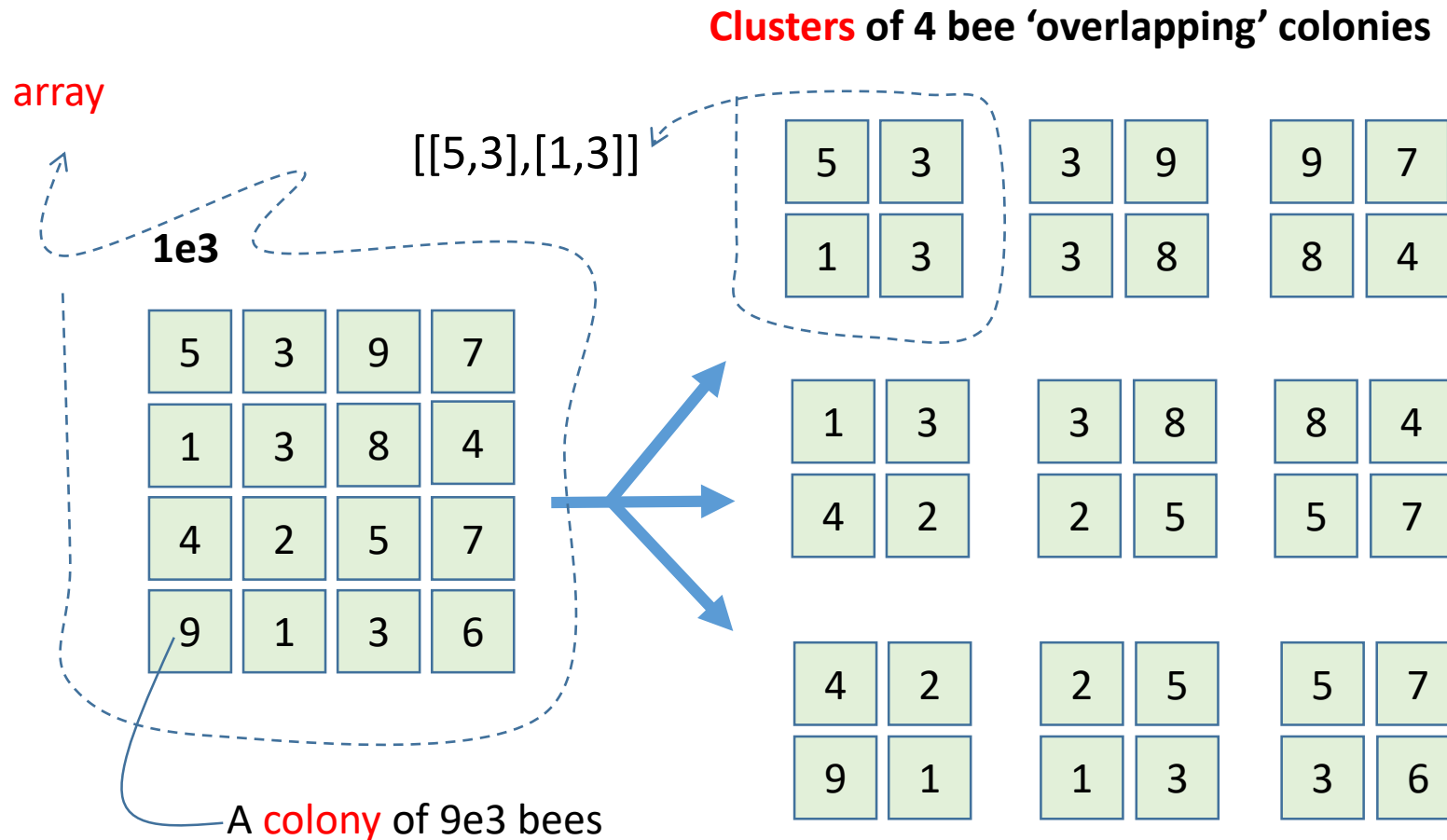
[Functions & Processing]

October 2019, April 2020 (---que año---)

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<https://docs.python.org/2.5/lib/typesseq.html>

“Clusters” in 2D Arrays

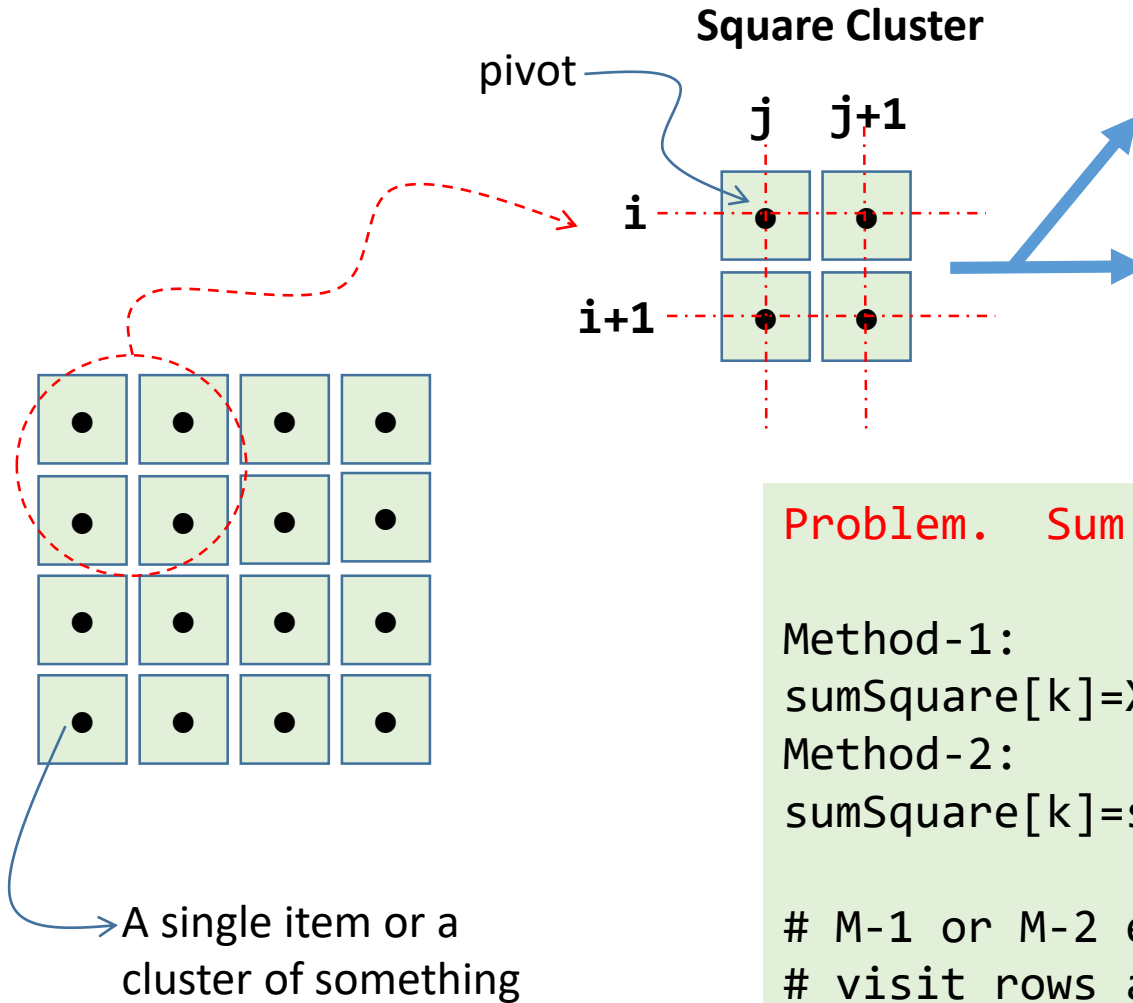


Example tasks:

- Sum
- Product
- Maximum (largest)
- Minimum (smallest)
- Average (mean)
- Even, odd, prime
- Count
- Sort (ascending, descending)
- Search
- Slicing
- Indexing (o position)
- Stacking (concatenate)
- Reshape
- Apply universal function: sum, sin, abs, log

Honey **bees** are social insects which live together in large, well-organized family groups. A colony typically consists of three kinds of adult **bees**: workers, drones, and a queen.

“Clusters” in 2D Arrays



Method-1 (formulate):

X[i,j]
X[i,j+1]
X[i+1,j]
X[i+1,j+1]

Method-2 (slicing):

X[i:i+2,j:j+2]

Problem. Sum elements in a cluster:

Method-1:

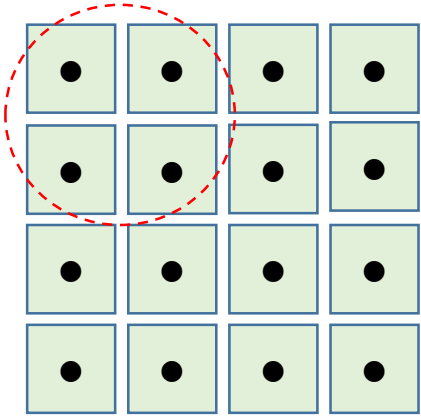
```
sumSquare[k]=X[i,j]+X[i,j+1]+X[i+1,j]+X[i+1,j+1]
```

Method-2:

```
sumSquare[k]=sum(X[i:i+2,j:j+2])
```

```
# M-1 or M-2 encapsulated into nested loops to
# visit rows and columns [i,j] of whole array
```

“Clusters” in 2D Arrays



Problem. Sum elements of each square clusters:

input array X, bla, bla, bla—customer style

```
n,m=shape(X)
```

```
N= # how many squares fit in row direction
```

```
M= # how many squares fit in col direction
```

```
k= # initialize k
```

```
for i in range(N)
```

```
    for j in range(M)
```

```
        sumSquare[k]=X[i,j]+X[i,j+1]+X[i+1,j]+X[i+1,j+1] # or
```

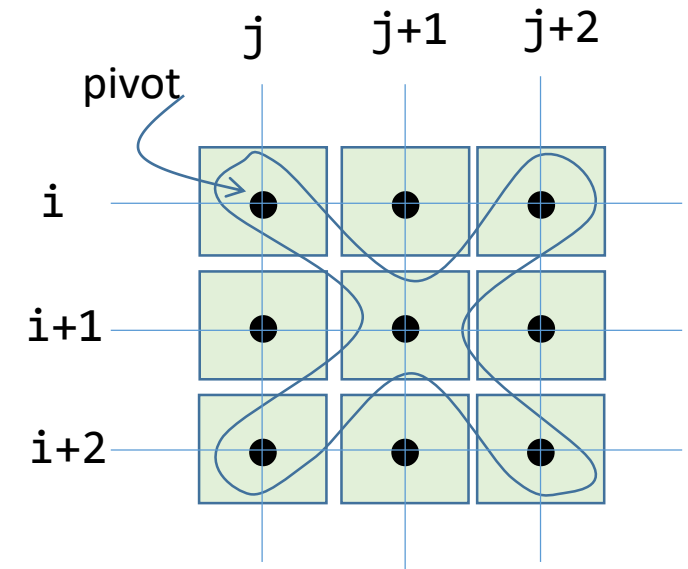
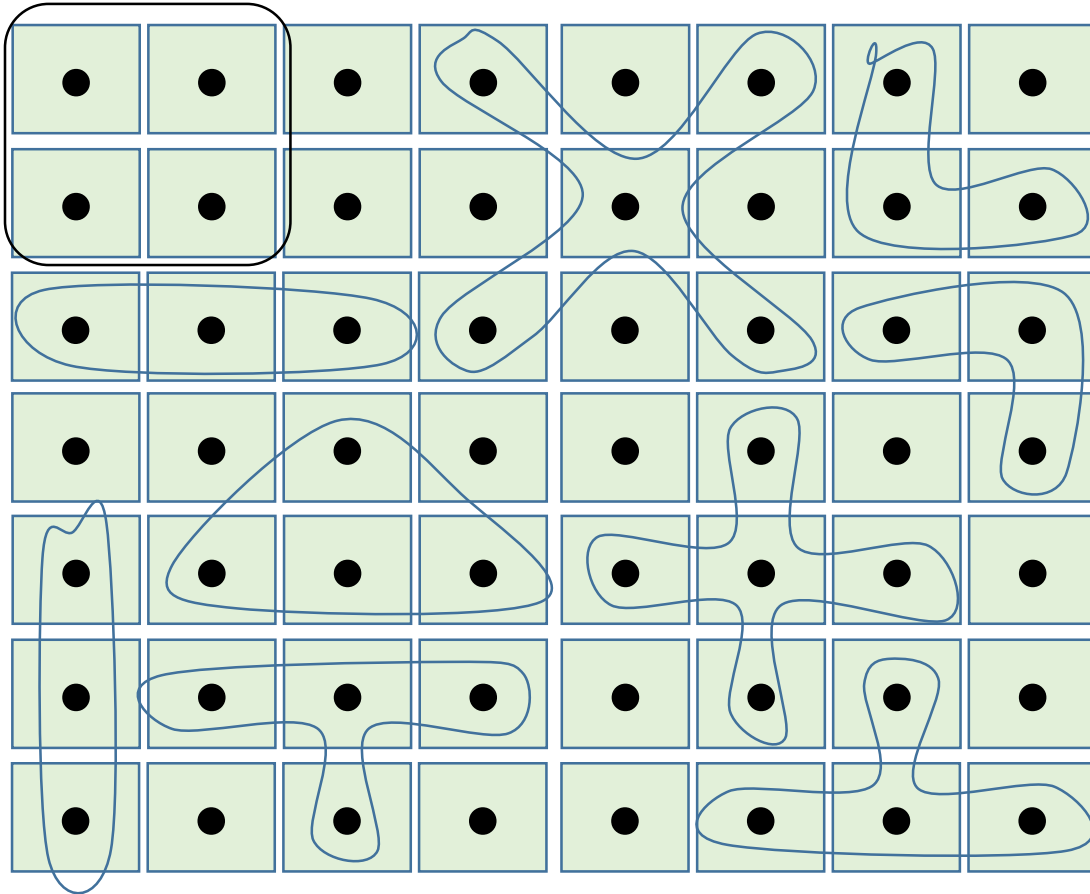
```
        sumSquare[k]=sum(X[i:i+2,j:j+2])
```

```
        k+=1
```

```
# Output--elaborate
```

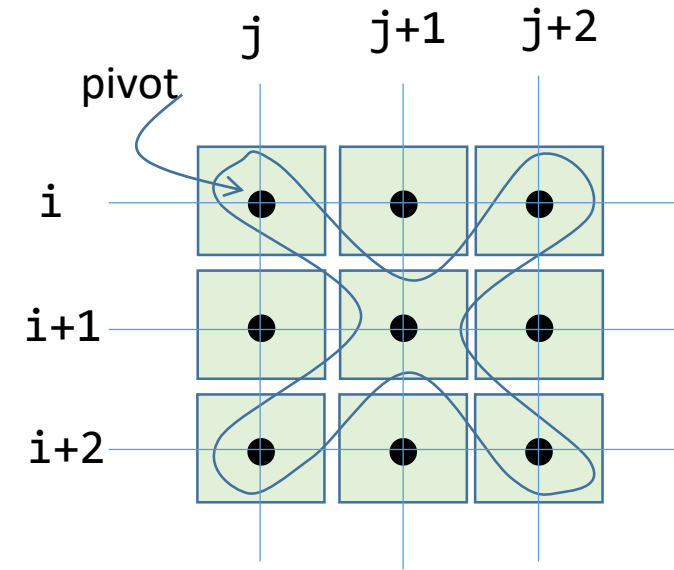
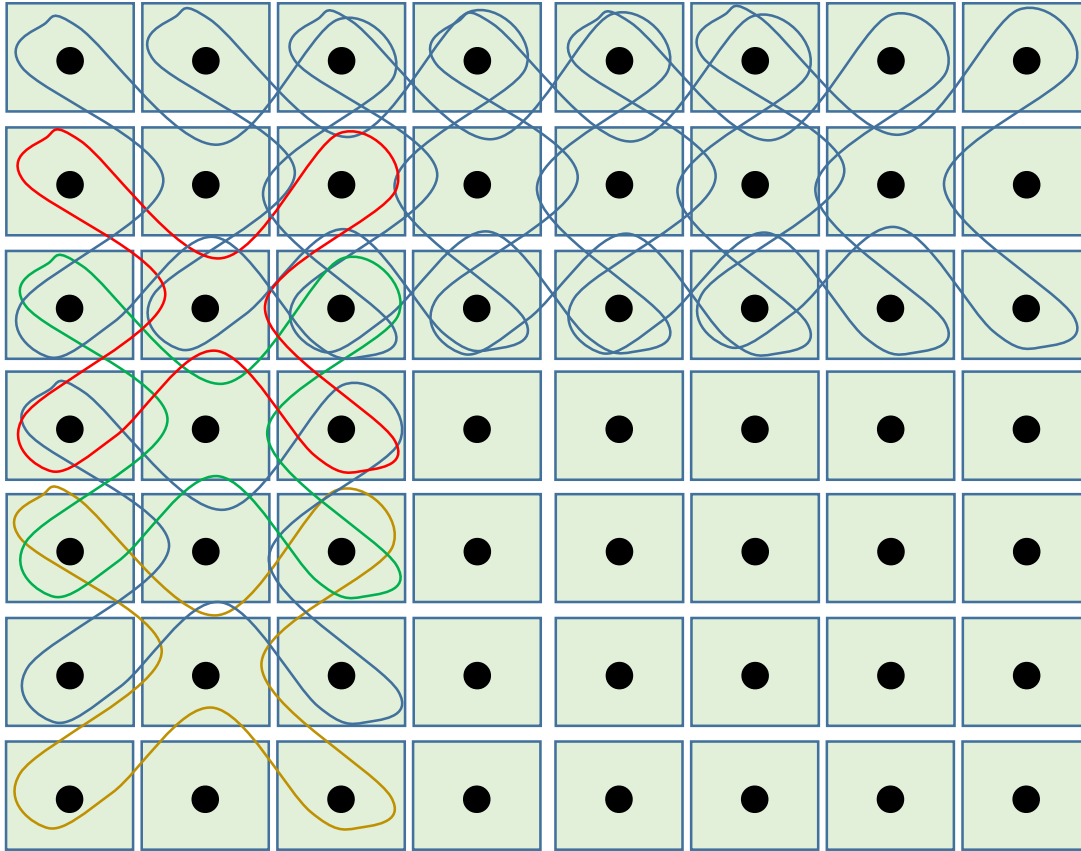
```
print(sumSquare)
```

“Clusters” in 2D Arrays



Choose a pivot element, all other elements are referenced based on pivot.

“Clusters” in 2D Arrays



- Choose a pivot element, all other elements are referenced based on pivot.
- Assume you want to add the elements in this shape.

$$CroixShape[k] = X[i, j] + X[i, j + 2] + X[i + 1, j + 1] + X[i + 2, j] + X[i + 2, j + 2]$$

Example: Array Element Overlap(1)

FILE: nestedLoops02.py



A

1	3	5	7	9
---	---	---	---	---

`A=np.array([1,3,5,7,9],int)`

B

2	4	9	7	5
---	---	---	---	---

`B=np.array([2,4,9,7,5],int)`

C

--	--	--

 "nada" `C=np.array([],int)` #initially empty

Nested Loops	List Comprehension
<pre>for a in A: for b in B: if a==b: C=np.append(C,a) print("C={}".format(C))</pre>	<pre>C=np.array([a for a in A for b in B if a==b]) print("C={}".format(C)) # This solution doesn't need of: # C=np.array([],int)</pre>

OUTPUT:
C=[5 7 9]

Example: Array Element Overlap(2)

FILE: nestedLoops02.py



A

1	3	5	7	9
---	---	---	---	---

```
A=np.array([1,3,5,7,9],int)
```

B

2	4	9	7	5
---	---	---	---	---

```
B=np.array([2,4,9,7,5],int)
```

C

--	--	--

 "nada"

```
C=np.array([],int)
```

in, not in (membership operators)	List Comprehension
<pre>for a in A: if a in B: if a not in C: C=np.append(C,a) print("C={}".format(C))</pre>	<pre>C=np.array([a for a in A if a in B if a not in C]) print("C={}".format(C))</pre>

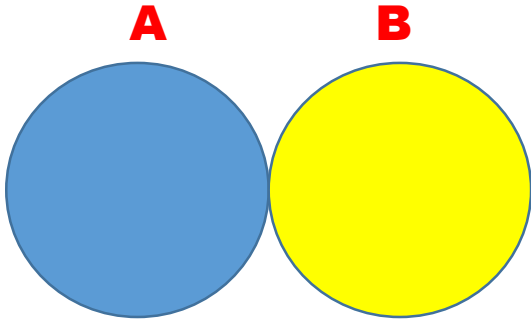
OUTPUT:
C=[5 7 9]



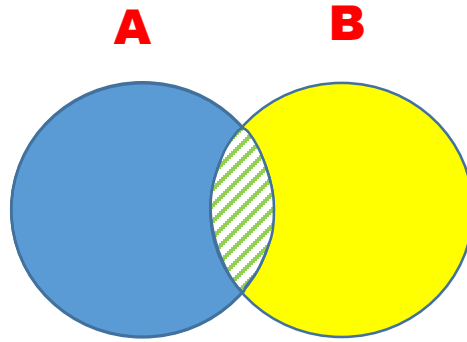
Venn diagram and overlapping



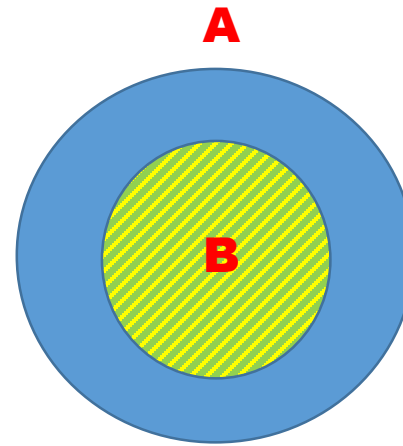
Possibilities are:



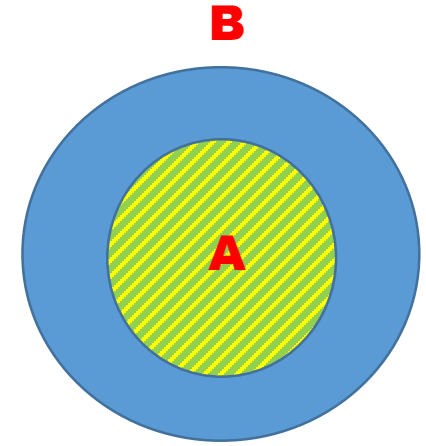
$$C = A \cap B = \phi$$



$$C = A \cap B$$



$$C = A \cap B = B$$



$$C = A \cap B = A$$

Elements that are in both sets: A and B

Creating 2D (or 3D) arrays: Reshape



arr

8	7	6	5	4	3	2	1
---	---	---	---	---	---	---	---

FILE: ArrayReshape.py

arr.reshape(2, 4)

8	7	6	5
4	3	2	1

arr.reshape(4, 2)

8	7
6	5
4	3
2	1

arr.reshape(2, 2, 2)

8	7
6	5

3D array

4	3
2	1

Reshape runs along the axis-0 of original array distributing elements in the new shape row by row (and page by page, if needed)

Reshape

```
import numpy as np
```

Output

```
arr = np.arange(8,0,-1)
print("Original array : \n", arr)
```

Original array :
[8 7 6 5 4 3 2 1]

```
# shape array with 2 rows and 4 columns
arr1 = arr.reshape(2, 4)
print("\nArray reshaped to 2 rows and 4 columns : \n", arr1)
```

Array reshaped to 2 rows and 4 columns :
[[8 7 6 5]
[4 3 2 1]]

```
# shape array with 2 rows and 4 columns
arr2 = arr.reshape(4,2)
print("\nArray reshaped to 2 rows and 4 columns : \n", arr2)
```

array reshaped to 2 rows and 4 columns :
[[8 7]
[6 5]
[4 3]
[2 1]]

```
# Constructs 3D array
arr3 = arr.reshape(2, 2, 2)
print("\nOriginal array reshaped to 3D : \n", arr3)
```

Original array reshaped to 3D :
[[[8 7]
[6 5]
[4 3]
[2 1]]]

FILE: ArrayReshape.py



Flatten Arrays

aplanar

Return a copy of the array collapsed into one dimension.

Original array: arr2

8	7	6	5
4	3	2	1

arr2=arr1.flatten(order='C')

arr2	8	7	6	5	4	3	2	1
------	---	---	---	---	---	---	---	---

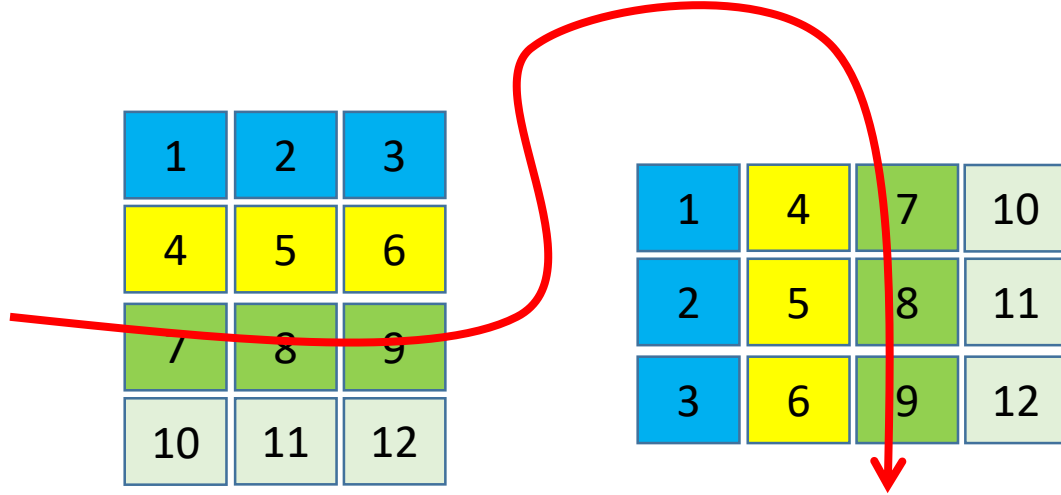
arr2=arr1.flatten(order='F')

arr2	8	4	7	3	6	2	5	1
------	---	---	---	---	---	---	---	---

Order options : {'C', 'F', 'A', 'K'}, order 'C' means to flatten in row-major (C-style) order 'F' means to flatten in column-major (Fortran-style) order.

FILE:flattenArray.py

Transpose: rows become columns



Mathematics:

$$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 10 & 11 & 12 \end{bmatrix}$$

$$A^T = \begin{bmatrix} 1 & 4 & 7 & 10 \\ 2 & 5 & 8 & 11 \\ 3 & 6 & 9 & 12 \end{bmatrix}$$

```
import numpy as np
```

```
A=np.array([[1,2,3],[4,5,6],[7,8,9],[10,11,12]])
```

```
print(A)
```

```
AT=A.transpose()
```

```
print(AT)
```

```
AT=A.T
```

```
print(AT)
```

OUTPUT

```
[[ 1  2  3]
 [ 4  5  6]
 [ 7  8  9]
 [10 11 12]]
[[ 1  4  7 10]
 [ 2  5  8 11]
 [ 3  6  9 12]]
```

FILE: transposeArray.py

2D array: Elementwise Operations

5.	3.	9.
3.	9.	5.
9.	5.	3.

 +

1.	1.	1.
1.	1.	1.
1.	1.	1.

 =

6.	4.	10.
4.	10.	6.
10.	6.	4.

```
import numpy as np
```

```
print(np.array([ [5,3,9],[3,9,5],[9,5,3]],float)+  
np.ones((3,3)))
```

5.	3.	9.
3.	9.	5.
9.	5.	3.

 -

1.	1.	1.
1.	1.	1.
1.	1.	1.

 =

4.	2.	8.
2.	8.	4.
8.	4.	2.

```
print(np.array([ [5,3,9],[3,9,5],[9,5,3]],float)-  
np.ones((3,3)))
```

5.	5.	5.
3.	3.	3.
9.	9.	9.

 *

1.	1.	1.
2.	2.	2.
.1	.1	.1

 =

5.	5.	5.
6.	6.	6.
.9	.9	.9

```
print(np.array([ [5,5,5],[3,3,3],[9,9,9]],float)*  
[[1,1,1],[2,2,2],[.1,.1,.1]])
```

Operator can be: +, -, *, /, %, //

Broadcasting (1)

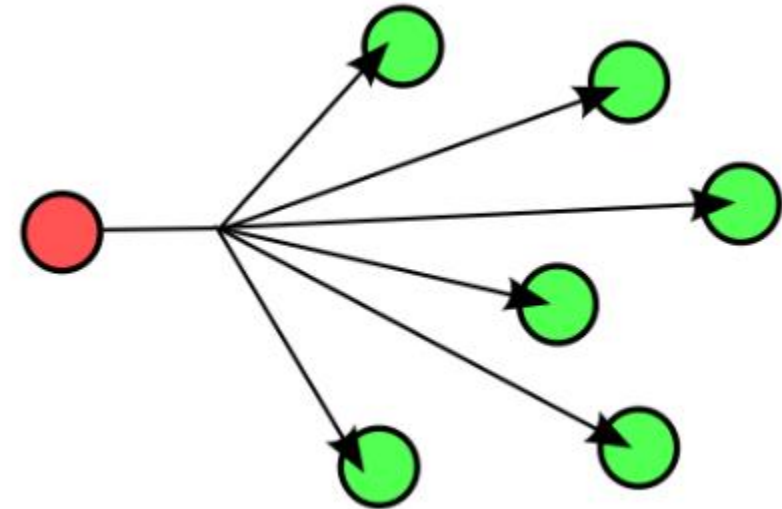
$$\begin{bmatrix} 5. & 3. & 9. \end{bmatrix} + \begin{bmatrix} 5. & 5. & 5. \end{bmatrix} = \begin{bmatrix} 10. & 8. & 14. \end{bmatrix}$$

$$\begin{bmatrix} 5. & 3. & 9. \\ 3. & 9. & 5. \\ 9. & 5. & 3. \end{bmatrix} + \begin{bmatrix} 1. & 1. & 1. \\ 1. & 1. & 1. \\ 1. & 1. & 1. \end{bmatrix} = \begin{bmatrix} 6. & 4. & 10. \\ 4. & 10. & 6. \\ 10. & 6. & 4. \end{bmatrix}$$

$$\begin{bmatrix} 5. & 3. & 9. \\ 3. & 9. & 5. \\ 9. & 5. & 3. \end{bmatrix} + \begin{bmatrix} 1. & 1. & 1. \\ 1. & 1. & 1. \\ 1. & 1. & 1. \end{bmatrix} = \begin{bmatrix} 6. & 4. & 10. \\ 4. & 10. & 6. \\ 10. & 6. & 4. \end{bmatrix}$$

$$\begin{bmatrix} 5. & 5. & 5. \\ 3. & 3. & 3. \\ 9. & 9. & 9. \end{bmatrix} + \begin{bmatrix} 1. & 1. & 1. \\ 1. & 1. & 1. \\ 1. & 1. & 1. \end{bmatrix} = \begin{bmatrix} 6. & 6. & 6. \\ 4. & 4. & 4. \\ 10. & 10. & 10. \end{bmatrix}$$

Allows to make operations with arrays of different shapes



Broadcasting(2): code & output

```
import numpy as np

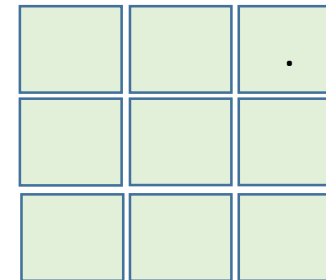
print(np.array([5,3,9],float)+5)
print(np.array([ [5,3,9],[3,9,5],[9,5,3]],float)+np.ones((3,)))

print(np.array([ [5,3,9],[3,9,5],[9,5,3]],float)+np.ones((3,)).reshape((3,1)))

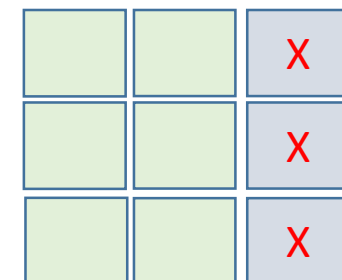
print(np.array([5,3,9],float).reshape((3,1))+np.ones((3,)))
```

```
[10.  8. 14.]
[[ 6.  4. 10.]
 [ 4. 10.  6.]
 [10.  6.  4.]]
[[ 6.  4. 10.]
 [ 4. 10.  6.]
 [10.  6.  4.]]
[[ 6.  6.  6.]
 [ 4.  4.  4.]
 [10. 10. 10.]]
```

Can't broadcast sorry



<operator>



Numpy Universal Functions [ufunc] : Element-Wise Operations

Numpy offers a large library of common mathematical functions called ufunc that compute element-wise on arrays, some examples are:

- `abs()`, `sqrt()`
- `log()`, `log10()`
- `exp()`, `sin()`
- `cos()`, `tanh()`
- `arcsin()`

`x=np.array([[1,2,3],[4,5,6]])`

1	2	3
4	5	6

`y=np.sin(x)`

0.8414	0.9093	0.1411
-0.7568	-0.9589	-0.2794

Sine is computed for each ONE of the arguments and stored into an array of same shape as argument

`[[0.84 0.91 0.14]
 [-0.76 -0.96 -0.28]]`

Visit the site, please

<https://docs.scipy.org/doc/numpy-1.13.0/reference/routines.math.html>

Mathematical functions

This a sample of all functions available, check the reference.

Trigonometric functions

<code>sin</code> (x, /[, out, where, casting, order, ...])	Trigonometric sine, element-wise.
<code>cos</code> (x, /[, out, where, casting, order, ...])	Cosine element-wise.
<code>tan</code> (x, /[, out, where, casting, order, ...])	Compute tangent element-wise.
<code>arcsin</code> (x, /[, out, where, casting, order, ...])	Inverse sine, element-wise.
<code>arccos</code> (x, /[, out, where, casting, order, ...])	Trigonometric inverse cosine, element-wise.
<code>arctan</code> (x, /[, out, where, casting, order, ...])	Trigonometric inverse tangent, element-wise.
<code>hypot</code> (x1, x2, /[, out, where, casting, ...])	Given the “legs” of a right triangle, return its hypotenuse.
<code>arctan2</code> (x1, x2, /[, out, where, casting, ...])	Element-wise arc tangent of <code>x1/x2</code> choosing the quadrant correctly.
<code>degrees</code> (x, /[, out, where, casting, order, ...])	Convert angles from radians to degrees.
<code>radians</code> (x, /[, out, where, casting, order, ...])	Convert angles from degrees to radians.
<code>unwrap</code> (p[, discount, axis])	Unwrap by changing deltas between values to 2π complement.
<code>deg2rad</code> (x, /[, out, where, casting, order, ...])	Convert angles from degrees to radians.
<code>rad2deg</code> (x, /[, out, where, casting, order, ...])	Convert angles from radians to degrees.

Sum function: many functions can perform operations in a specific axis

```
x=np.array([[1,2,3],[4,5,6]])
```

```
z=np.sum(x)
```

```
print(z)
```

```
m=np.sum(x,axis=0)
```

```
print(m)
```

```
n=np.sum(x,axis=1)
```

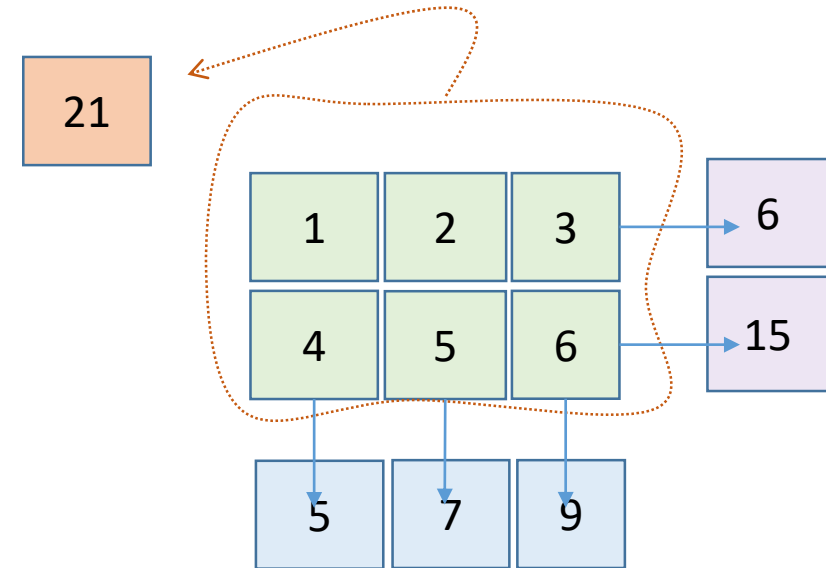
```
print(n)
```

OUTPUT

21

[5 7 9]

[6 15]



```
xx=np.array([ [[1,2,3], [4,5,6]] , [[7,8,9], [10,11,12]] ] )
```

```
p=np.sum(xx,axis=0)
```

```
print(p)
```

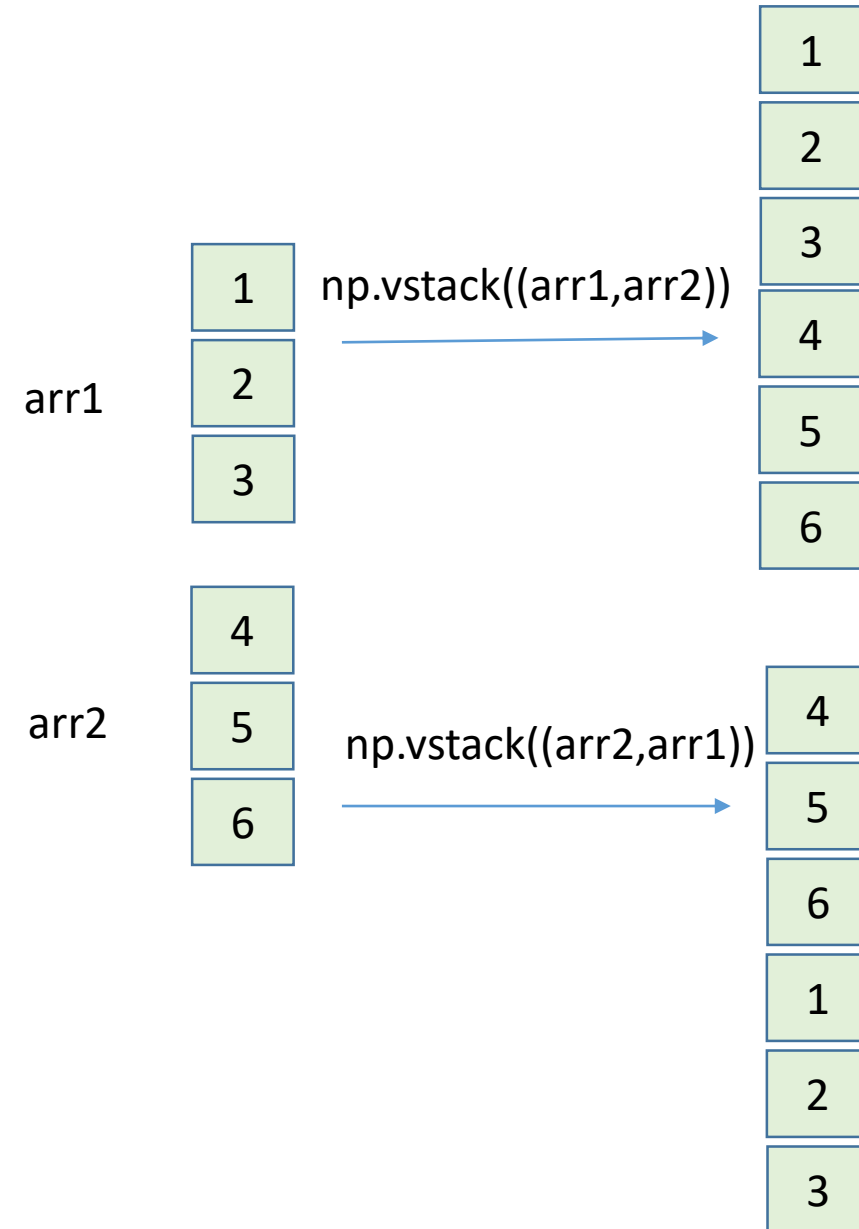
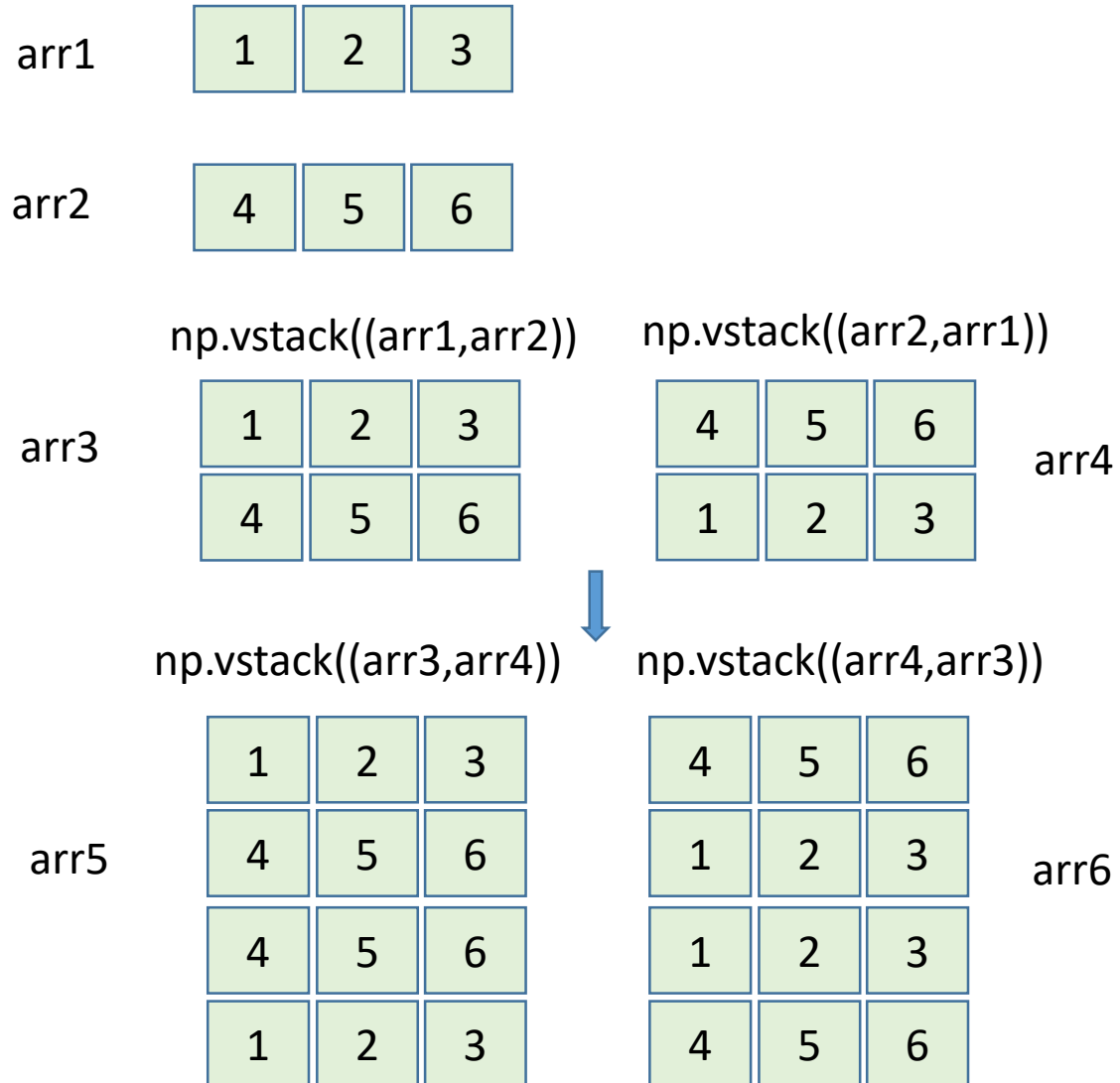
3D array

[[8 10 12]
[14 16 18]]

← Explain yourself, this one

vstack

The `vstack()` function is used to stack arrays in sequence vertically (row wise)



vstack sample code

Code	Output for row vectors	Output for column vectors
<pre>import numpy as np # Row vectors arr1 = np.array([1, 2, 3]) arr2 = np.array([4, 5, 6]) arr3=np.vstack((arr1,arr2)) print(arr3) arr4=np.vstack((arr2,arr1)) print(arr4) arr5=np.vstack((arr3,arr4)) print(arr5) # Column Vectors arr6=arr1.reshape((3,1)) print(arr6) arr7=arr2.reshape((3,1)) print(arr7) arr8=np.vstack((arr6,arr7)) print(arr8)</pre>	<pre>[[1 2 3] [4 5 6]] [[4 5 6] [1 2 3]] [[1 2 3] [4 5 6] [4 5 6] [1 2 3]]</pre>	<pre>[[1] [2] [3]] [[4] [5] [6]] [[1] [2] [3] [4] [5] [6]]</pre>

hstack

arr1

1	2	3
---	---	---

arr2

4	5	6
---	---	---

`np.hstack((arr1,arr2))`

arr3

1	2	3	4	5	6
---	---	---	---	---	---

arr1

1
2
3

arr2

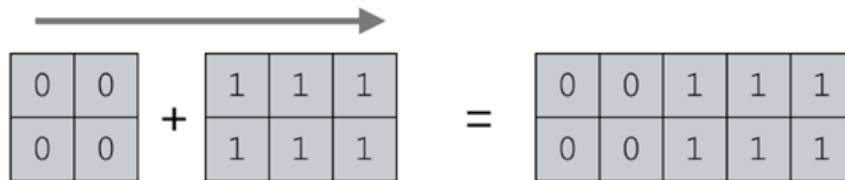
4
5
6

`np.hstack((arr1,arr2))`

arr3

1	4
2	5
3	6

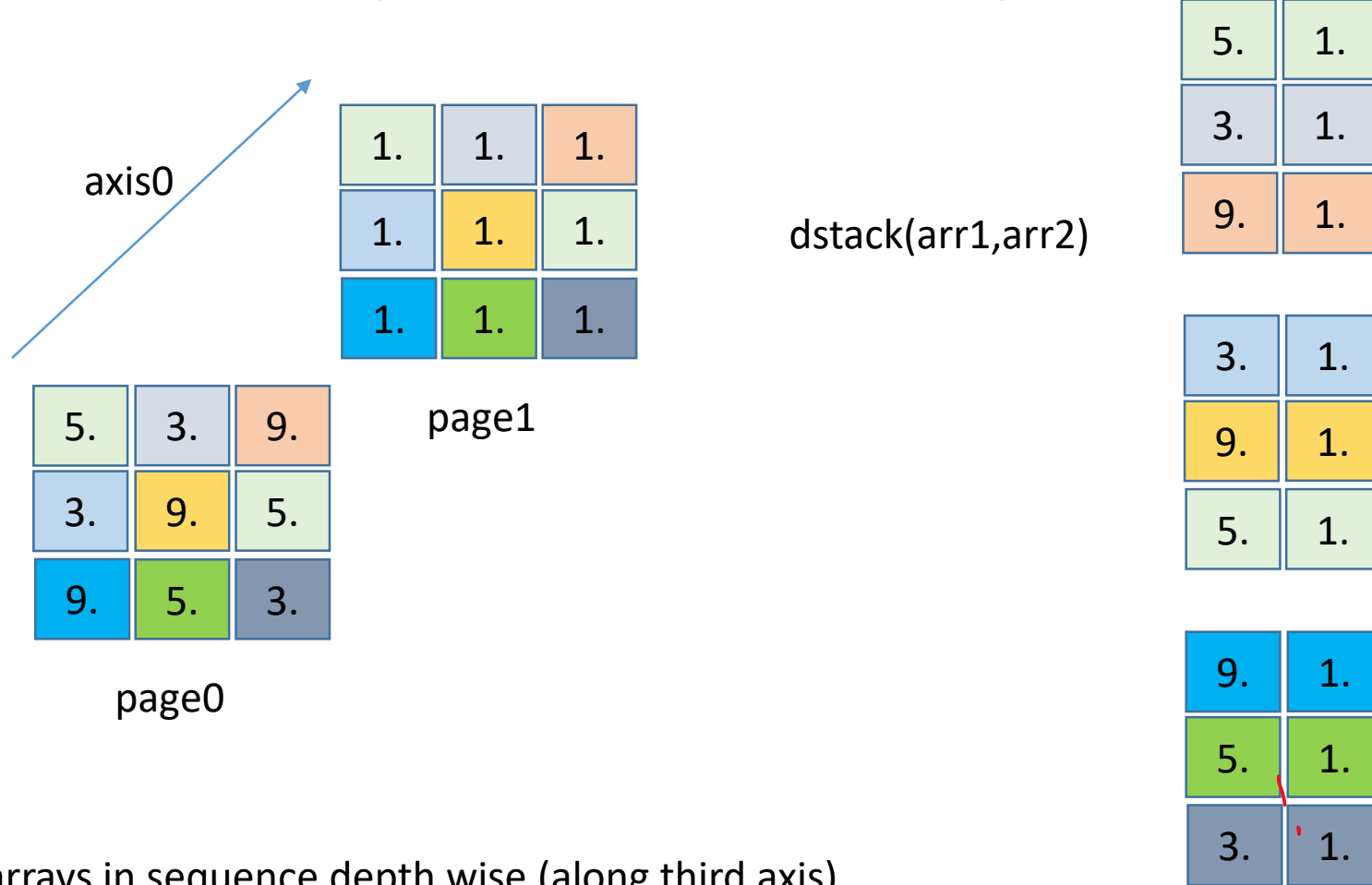
NUMPY HSTACK COMBINES NUMPY
ARRAYS HORIZONTALLY



hstack sample code

Code	Output
<pre>import numpy as np # Start with row vectors arr1 = np.array([1, 2, 3]) arr2 = np.array([4, 5, 6]) arr3=np.hstack((arr1,arr2)) print(arr3)</pre>	<pre>[1 2 3 4 5 6]</pre>
<pre># Start with column vectors arr1 = np.array([[1],[2],[3]]) arr2 = np.array([[4],[5],[6]]) arr3=np.hstack((arr1,arr2)) print(arr3)</pre>	<pre>[[1 4] [2 5] [3 6]]</pre>

`dstack('depth stack')(1) [optional]`



Stack arrays in sequence depth wise (along third axis).
This is equivalent to concatenation along the third axis after 2-D
arrays of shape (M,N) have been reshaped to $(M,N,1)$. Or if you
start with 1-D arrays of shape $(N,)$ have been reshaped to $(1,N,1)$.

dstack sample code(2) [optional]

Code	Output
<pre>import numpy as np arr0 = np.array([[5,3,9],[3,9,5],[9,5,3]]) arr1 = np.ones((3,3)) arr2= np.dstack((arr0,arr1)) print(arr2)</pre>	<pre>[[[5. 1.] [3. 1.] [9. 1.] [3. 1.] [9. 1.] [5. 1.] [9. 1.] [5. 1.] [3. 1.]]]</pre>

Array Formatted Output: `set_printoptions`

```
import numpy as np
x=np.array([1,2,3,4,5])
f1=x**3+x*np.exp(x)+1
f2=x**2+x*np.log(x)
f3=np.cos(np.sin(x))+np.exp(1/x)

M=np.vstack((x,f1,f2,f3))
# to set the number of decimals max
np.set_printoptions(precision=2)

print("M= \n",M)
MM=M[:, :3]*0.5
print("MM= \n",MM)
```

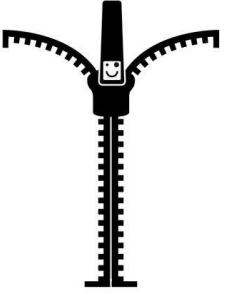
```
M=
[[ 1.    2.    3.    4.    5. ]
 [ 4.72 23.78 88.26 283.39 868.07]
 [ 1.    5.39 12.3  21.55 33.05]
 [ 3.38  2.26  2.39  2.01  1.8 ]]

MM=
[[ 0.5  1.  1.5 ]
 [ 2.36 11.89 44.13]
 [ 0.5  2.69 6.15]
 [ 1.69 1.13 1.19]]
```

Up to 2
decimals



zip & unzip



"Pepe"	"Cheo"	"Tito"	"Paco"	"Billo"
True	False	True	True	False
99	89	75	90	97
'A'	'B'	'C'	'A'	'A'

initializing lists

```
nameList = [ "Pepe", "Cheo", "Tito", "Paco", "Billo" ]
```

```
buenaGente=[True, False, True, True, False]
```

```
scoreList = [ 99, 89, 75, 90, 97 ]
```

```
gradeStr="ABCAA"
```

File: zip01.py

```
# using zip() to organize values
```

```
group = zip(nameList, buenaGente, scoreList, gradeStr)
```

```
# converting values to print as list of tuples
```

```
group = list(group)
```

```
# unzipping values
```

```
nameList, buenaGente, scoreList, gradeStr = zip(*group)
```

zip

unzip

('Pepe', True, 99, 'A')

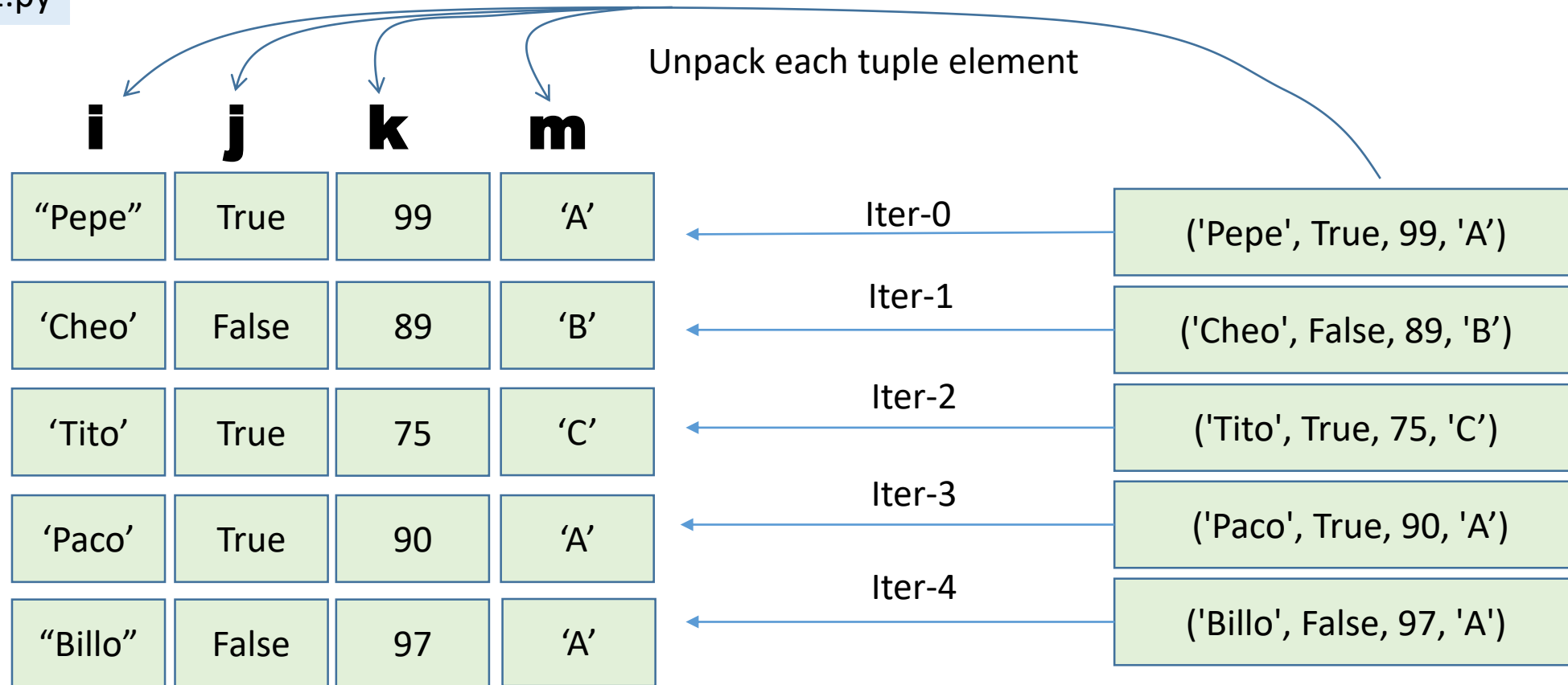
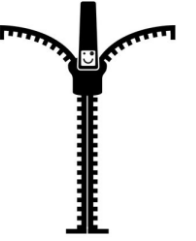
('Cheo', False, 89, 'B')

('Tito', True, 75, 'C')

('Paco', True, 90, 'A')

('Billo', False, 97, 'A')

```
[('Pepe', True, 99, 'A'),  
( 'Cheo', False, 89, 'B'),  
( 'Tito', True, 75, 'C'),  
( 'Paco', True, 90, 'A'),  
( 'Billo', False, 97, 'A')]
```



```
for i, j, k, m in zip(nameList, buenaGente, scoreList, gradeStr):
```

zip & unzip

For loop can iterate **simultaneously** over several items in sequences

Iterate over multiple sequences: zip & unzip

For loop can iterate **simultaneously** over several items in sequences

('Pepe', True, 99, 'A')

('Cheo', False, 89, 'B')

('Tito', True, 75, 'C')

('Paco', True, 90, 'A')

('Billo', False, 97, 'A')

name	buenaG?	score	grade
Pepe	True	99	A
Cheo	False	89	B
Tito	True	75	C
Paco	True	90	A
Billo	False	97	A

File: zip01.py

```
import numpy as np
```

```
# initializing lists
```

```
nameList = [ "Pepe", "Cheo", "Tito", "Paco", "Billo" ]
```

```
buenaGente=[True,False,True,True,False]
```

```
scoreList = [ 99, 89, 75, 90, 97 ]
```

```
gradeStr="ABCAA"
```

```
# iterating over multiple sequences with one for loop:
```

```
print('%7s %6s %7s %3s'%( 'name','buenaG?','score','grade'))
```

```
for i, j, k, m in zip(nameList, buenaGente, scoreList, gradeStr):
```

```
    print('%7s %6s %7.0f %3c' %(i, j, k, m))
```

```
# if sequences of different length, iterates until the shortest
```

Zip() function(1) (optional)

Organize elements from different sequences into tuples:

```
# initializing lists [File: zip01.py]
nameList = [ "Pepe", "Cheo", "Tito", "Paco","Billo" ]
rollList= [ 4, 2, 5, 3, 1 ]
scoreList = [ 99, 89, 75, 90, 97 ]
gradeStr="ABCAA" # or gradeList=['A','B','C','A','A']
```

```
# using zip() to organize values; group is a tuple
group = zip(rollList, nameList, scoreList, gradeStr)
```

each tuple element has 4 items

```
# converting values to print as list of tuples
group = list(group)
```

```
# printing resultant values
print("The zipped result is list of tuples :")
print(group)
```

The zipped result is a list of tuples :
[(4, 'Pepe', 99, 'A'), (2, 'Cheo', 89, 'B'),
(5, 'Tito', 75, 'C'), (3, 'Paco', 90, 'A'),
(1, 'Billo', 97, 'A')]

Unzipping (2) (optional)

Unpack elements of tuples:

```
# unzipping values
rollList, nameList, scoreList, gradeStr = zip(*group)
print ("\nThe unzipped result: \n",end=" ")

# printing initial lists
print ("The name list is : ",end=" ")
print (nameList)

print ("The roll list is : ",end=" ")
print (rollList)

print ("The score list is : ",end=" ")
print (scoreList)

print ("The grade string is : ",end=" ")
print (gradeStr)
```

The unzipped results:

The name list is : ('Pepe', 'Cheo', 'Tito', 'Paco', 'Billo')

The roll list is : (4, 2, 5, 3, 1)

The score list is : (99, 89, 75, 90, 97)

The grade string is : ('A', 'B', 'C', 'A', 'A')

adi's!

The word "adi's!" is written in a cursive, pink font. The letters 'a', 'd', and 'i' have small colored dots above them: a grey dot above 'a', a pink dot above 'd', and a green dot above 'i'. The 's' has an orange dot. The exclamation mark has a yellow and black striped top and a solid blue dot at the bottom. Below the word is a brown, wavy squiggle.