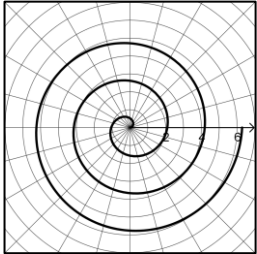
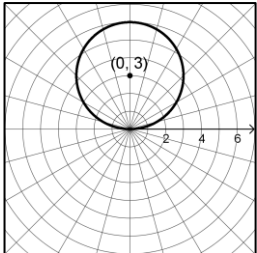
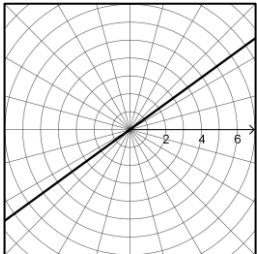
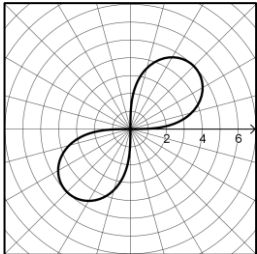
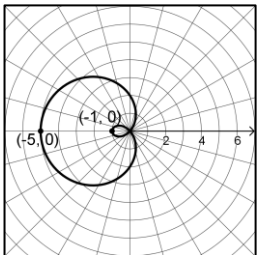
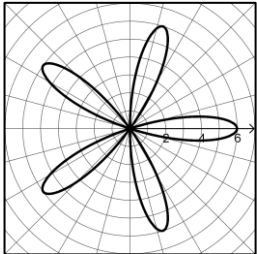


| Type of Graph | Equations | Properties | Example |
|---------------|---|---|---|
| Spiral | $r = a\theta$ | Begins at the origin spiraling outward in a counter-clockwise direction, crossing the polar axis at $(2\pi ak, 0)$ for $k = 0, 1, 2, 3, \dots$ | $r = \frac{1}{3}\theta$ with $0 \leq \theta \leq 6\pi$  |
| Circles | $r = a$ $r = 2a\sin\theta$ $r = 2a\cos\theta$ | If $r = a$, then a circle with radius $ a $ centered at $(0, 0)$ If $r = 2a\sin\theta$, then a circle with radius $ a $ centered at $(0, a)$ If $r = 2a\cos\theta$, then a circle with radius $ a $ centered at $(a, 0)$ | $r = 6\sin\theta$  |
| Lines | $\theta = \theta_0$ | A line passing through the origin with slope $m = \tan\theta_0$ | $\theta = \frac{\pi}{5}$  |

| Type of Graph | Equations | Properties | Example |
|---|--|--|---|
| Lemniscates | $r^2 = a^2 \sin \theta$ $r^2 = a^2 \cos \theta$ | <p>If $\sin \theta$, then two loops along the $y = x$ line each having a radius a</p> <p>If $\cos \theta$, then two loops along the $y = 0$ line each having a radius a</p> | $r^2 = 25 \sin(2\theta)$  |
| Limaçons Inner Loop ($a < b$) Cardioid ($a = b$) Dimple ($a > b$) | $r = a \pm b \sin \theta$ $r = a \pm b \cos \theta$ | <p>If $+b \sin \theta$ then extends upward, if $-b \sin \theta$ then extends downward; has y-intercepts at $(0, b \pm a)$; has x-intercepts at $(\pm a, 0)$; inner loop and cardioid also cross through origin</p> <p>If $+b \cos \theta$ then extends right, if $-b \cos \theta$ then extends left; has x-intercepts at $(b \pm a, 0)$; has y-intercepts at $(0, \pm a)$; inner loop and cardioid also cross through origin</p> | $r = 2 - 3 \cos \theta$  |
| Roses | $r = a \sin(n\theta)$ $r = a \cos(n\theta)$ | <p>If $\sin(n\theta)$, then no petals on either axis if n is even or 1 petal on y-axis if n is odd (alternates $+y$ or $-y$ for incrementally odd values)</p> <p>If $\cos(n\theta)$, then first petal on positive x-axis</p> <p># of petals: if n is odd then n petals, if n is even then $2n$ petals</p> | $r = 6 \cos(5\theta)$  |