

# Complexity Analysis

## 1. Linked List Choice

Chosen structure: **Doubly Linked List (DLL)**.

Reasoning:

- **Insertion/Deletion:**  $O(1)$  at head/tail or after a known node, because both `next` and `prev` are stored. Singly Linked List (SLL) needs  $O(n)$  to delete a middle node.
- **Bidirectional traversal:** DLL allows forward and backward iteration for debugging, dependency tracing, or cleanup.
- **Iteration:**  $O(n)$  sequential traversal is simple; overhead from extra pointer is negligible for small/medium lists.
- **Circular Linked List (CLL):** adds wrap-around complexity and complicates termination checks, not useful for task scheduling.
- **Vector:** good for random access but poor for frequent insert/delete ( $O(n)$  shifts).

**Conclusion:** DLL balances flexibility and simplicity for dynamic task management.

## 2. Time and Space Complexity Analysis

Component	Operation	Time	Space	Reason
LinkedList	<code>insertTask</code>	$O(1)$	$O(1)$	Insert at tail
	<code>deleteTask</code>	$O(n)$	$O(1)$	Linear search by ID
	<code>findTask</code>	$O(n)$	$O(1)$	Sequential traversal
Iterator (TaskIterator)	<code>hasNext</code>	$O(1)$	$O(1)$	Single pointer check
	<code>next</code>	$O(1)$	$O(1)$	Advance pointer
PriorityQueue (sorted DLL)	<code>enqueue</code>	$O(n)$	$O(1)$	Find correct position by priority
	<code>dequeue</code>	$O(1)$	$O(1)$	Remove head (highest priority)
Stack (ExpressionEvaluator)	<code>push</code> / <code>pop</code>	$O(1)$	$O(1)$	Linked-list node ops
	Infix→Postfix conversion	$O(n)$	$O(n)$	Each token processed once

Component	Operation	Time	Space	Reason
	<b>Postfix evaluation</b>	$O(n)$	$O(n)$	Each operator/operand handled once
<b>Recursive dependency check</b>	<code>hasCycleHelper</code>	$O(n)$	$O(n)$	DFS over task list using recursion stack

### 3. Trade-offs Discussion

- **DLL vs SLL:** DLL uses slightly more memory per node but enables backward traversal and constant-time deletion with known node pointers.
- **DLL vs CLL:** CLL avoids null checks but complicates iterator logic and cycle detection; DLL simpler and safer.
- **LinkedList vs Vector:** Vector provides random access ( $O(1)$ ) but expensive insertions ( $O(n)$ )—not ideal for dynamic scheduling.
- **Priority Queue design:**
  - **Sorted list:** `enqueue`  $O(n)$ , `dequeue`  $O(1)$ . Efficient when dequeuing is frequent (as in schedulers).
  - **Unsorted list:** `enqueue`  $O(1)$ , `dequeue`  $O(n)$ . Better if many inserts before few dequeues.
  - Chosen: **sorted list**, since scheduling repeatedly extracts the next high-priority task.

This structure mix minimizes complexity while keeping clarity and recursive operations manageable.