

# AVL Trees

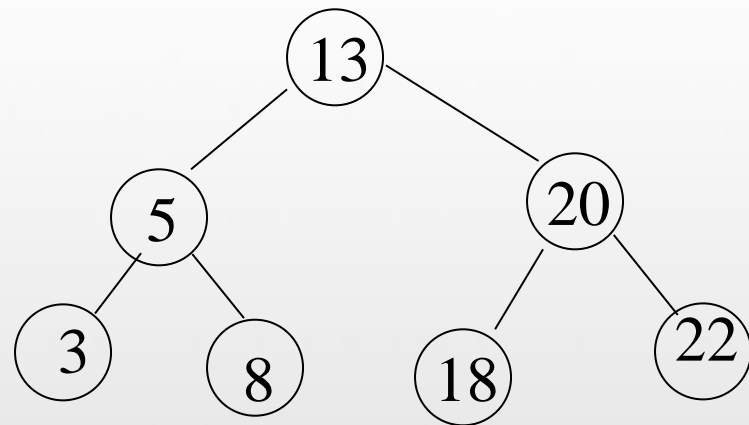
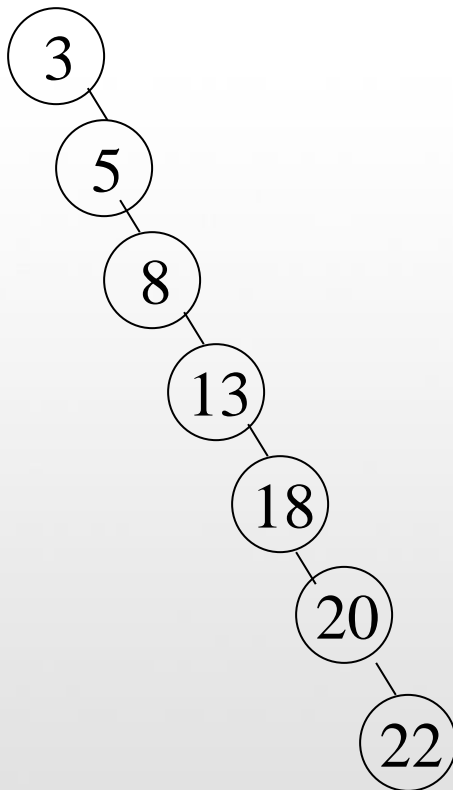
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COMP242

# Motivation

- ❑ When building a binary search tree, what type of trees would we like? Example: 3, 5, 8, 13, 18, 20, 22

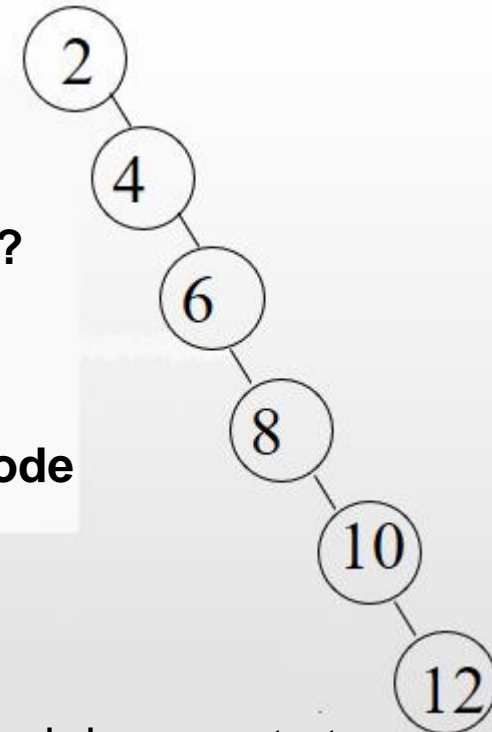


# Recall

- ❑ Best case running time of BST operations is  $O(\log N)$
- ❑ Worst case running time is  $O(N)$

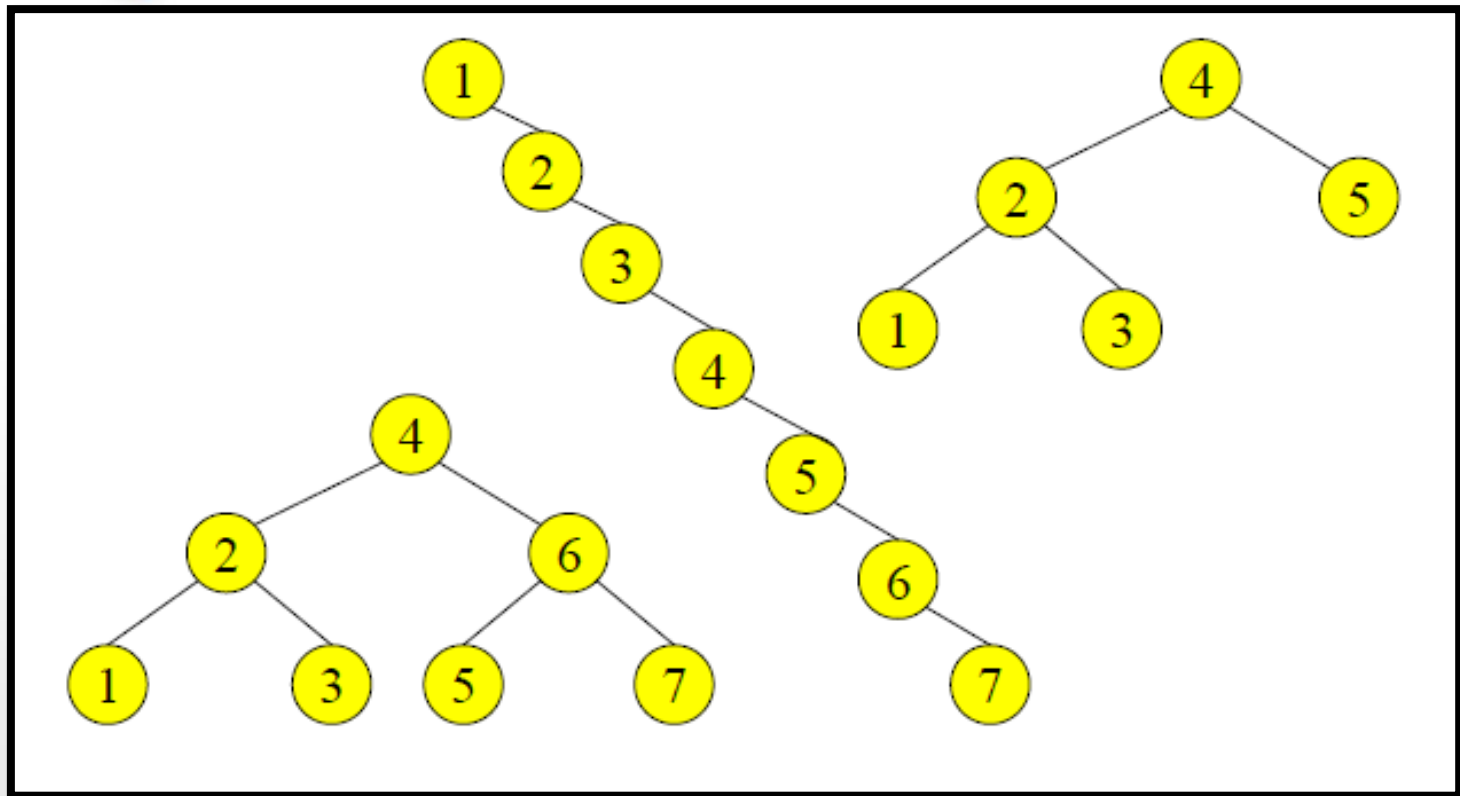
What happens when you Insert elements in ascending order?

- ❖ Insert: 2, 4, 6, 8, 10, 12 into an empty BST
- ❖ **Problem:** Lack of “balance”
- ❖ compare the height of left and right subtrees for each node



Unbalanced degenerate tree

# Balanced and unbalanced BST



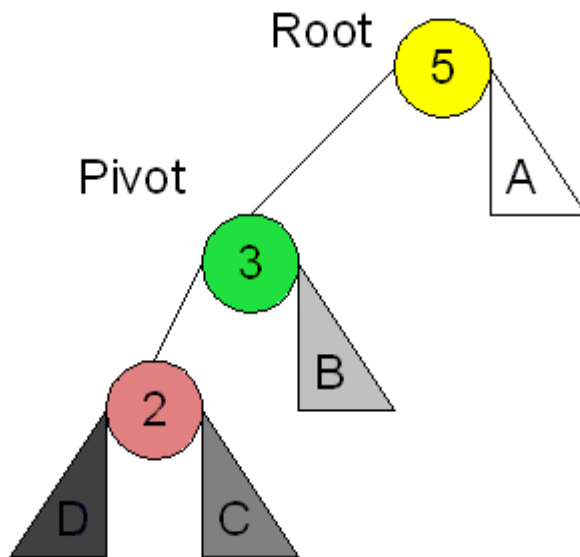
- ❖ If the BST is not balanced  
May end up with some nodes very deep

# AVL Trees

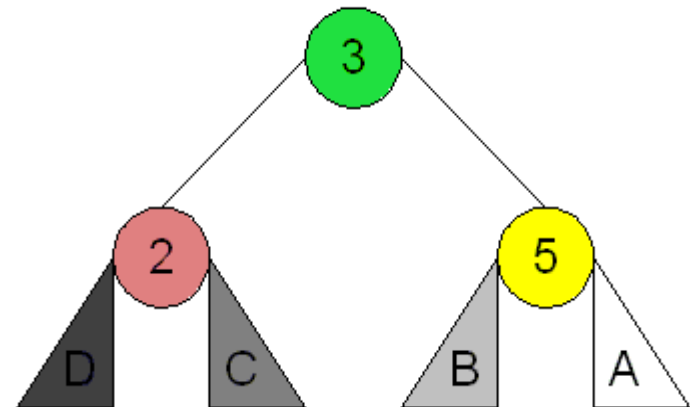
- ❑ Adelson-Velskii and Landis
- ❑ AVL trees are **height-balanced binary search trees**
- ❑ **Balance factor** of a node  
 $|\text{Height}(\text{left subtree}) - \text{Height}(\text{right subtree})|$
- ❑ An AVL tree has balance factor calculated **at every node**
- ❑ For every node, heights of left and right subtree can differ by **no more than 1**  
❖  $|\text{height}(\text{left}) - \text{height}(\text{right})| \leq 1$
- ❑ Store current heights in each node

# AVL Tree Rotation :Single Rotation

## Left Left Case

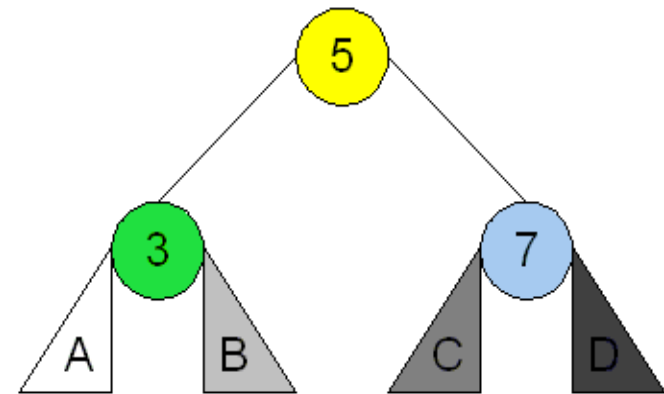
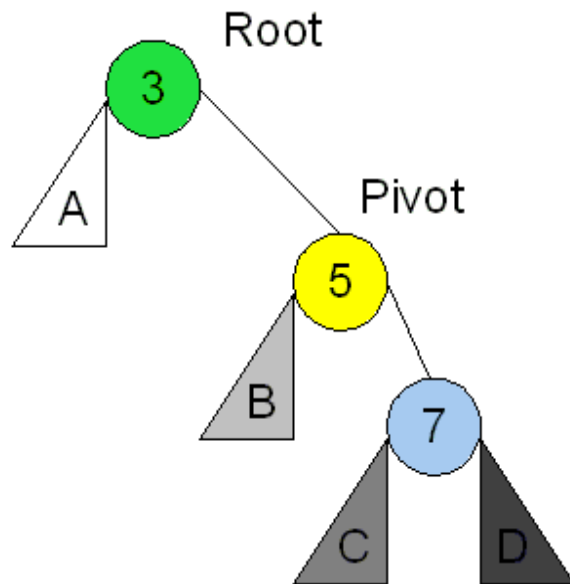


Right  
Rotation



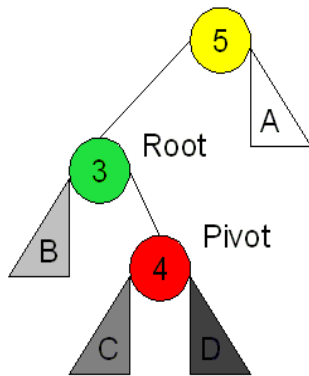
# AVL Tree Rotation :Single Rotation

## Right Right Case

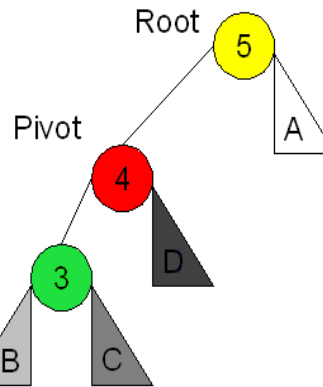


# AVL Tree Rotation : Double Rotation

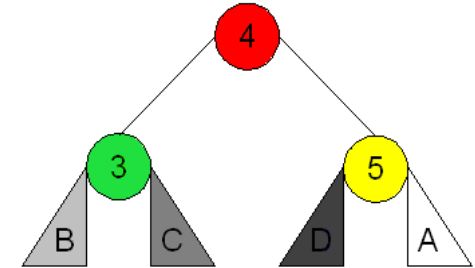
Left Right Case



Left  
Rotation



Right  
Rotation



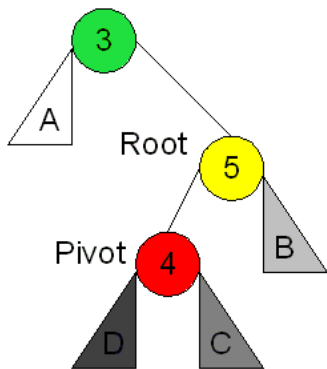
1

2

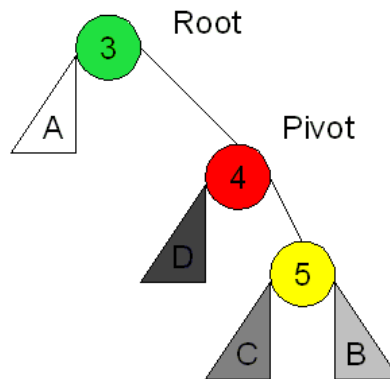


# AVL Tree Rotation : Double Rotation

## Right Left Case



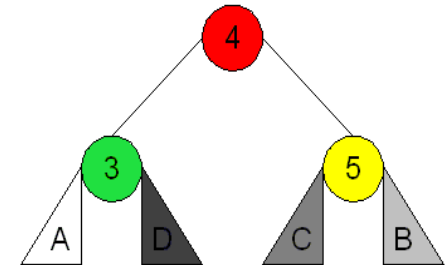
Right  
Rotation



Left  
Rotation

1

2



# AVL Tree Examples

- ❑ Insert 14, 17, 11, 7, 53, 4, 13 into an empty AVL tree
- ❑ Build an AVL tree with the following values  
15, 20, 24, 10, 13, 7, 30, 36, 25

Answers

# Implementation : AVL Tree

```
//Class Node for the AVL Tree
public class AVLTreeNode {
    int element;           //store data
    AVLTreeNode left;      // left child
    AVLTreeNode right;     //right child
    int height;            //Height

    public AVLTreeNode(int element) {           // Constructor
        this(element, null, null);
    }

    public AVLTreeNode(int element, AVLTreeNode left, AVLTreeNode right)
    {
        this.element=element;
        this.left=left;
        this.right=right;
        this.height=0;
    }
}
```

# Implementation : AVL Tree

```
// AVL Tree Class

public class AVL {

    private AVLTreeNode root;

    public AVL() {
        root=null;
    }

    /* Methods go here */

}
```

# AVL Tree : Height

```
// Return the height of a node e
private int height( AVLTreeNode e ){
    if( e == null )
        return -1;

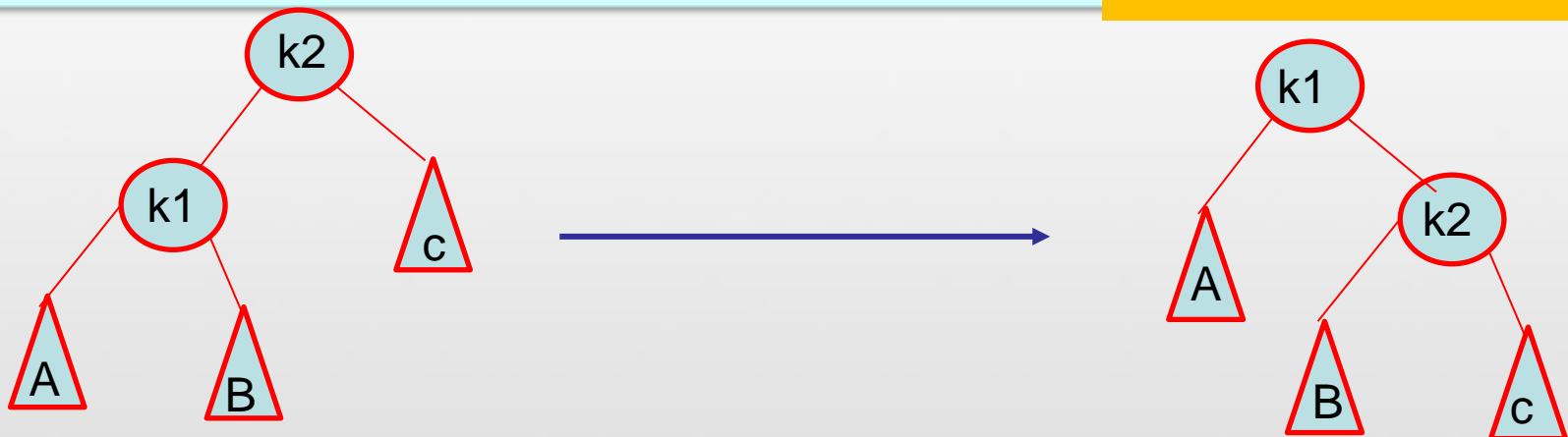
    return e.height;
}
```

# AVL Tree : RotateWithLeftChild

```
// Rotate binary tree node with left child(single rotate to right)
private AVLTreeNode rotateWithLeftChild(AVLTreeNode k2){
    AVLTreeNode k1 = k2.left;
    k2.left = k1.right;
    k1.right = k2;
    k2.height = Math.max(height(k2.left), height(k2.right)) + 1;
    k1.height = Math.max(height(k1.left), k2.height) + 1;
    return k1;
}
```

Why Add 1 ?

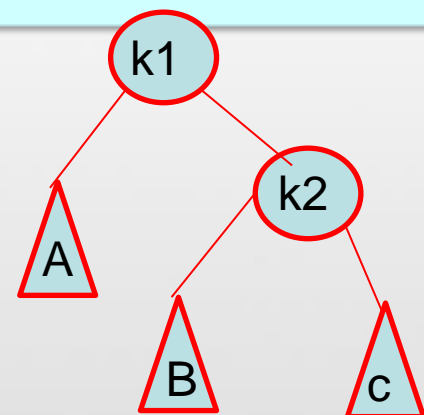
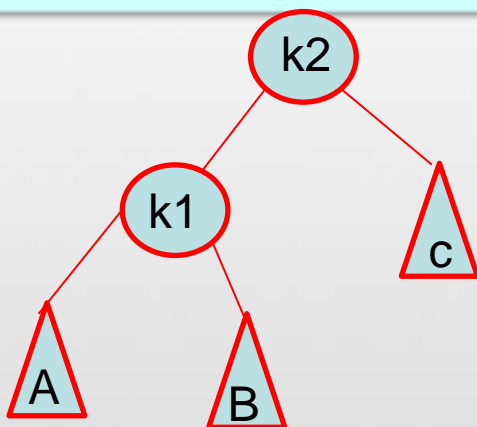
H.W ???



# AVL Tree : RotateWithRightChild

// Rotate binary tree node with right child (single rotate to left)

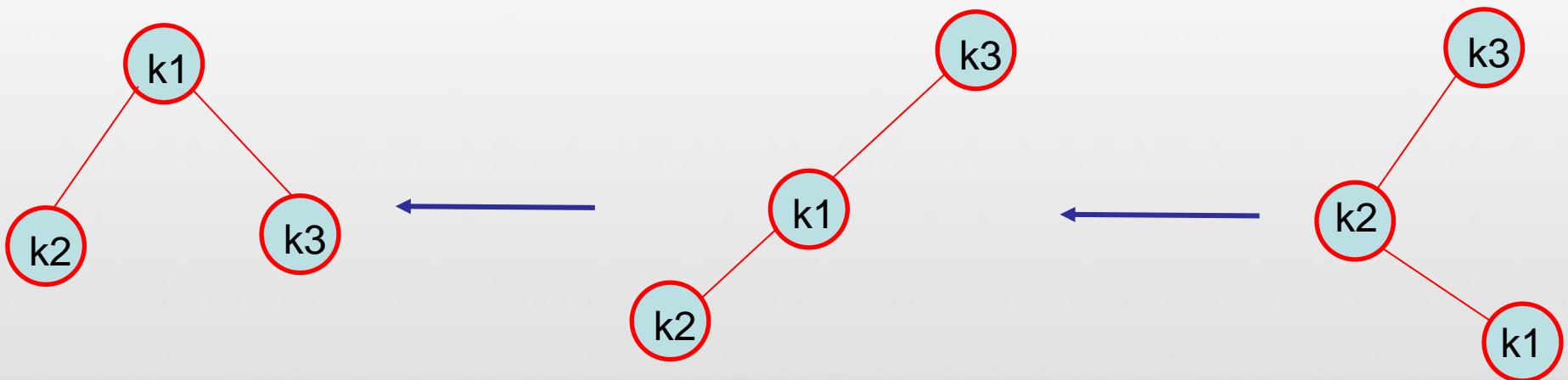
```
private AVLTreeNode rotateWithRightChild(AVLTreeNode k1) {  
    AVLTreeNode k2 = k1.right;  
    k1.right = k2.left;  
    k2.left = k1;  
    k1.height = Math.max(height(k1.left), height(k1.right)) + 1;  
    k2.height = Math.max(height(k2.right), k1.height) + 1;  
    return k2;  
}
```



# AVL Tree : DoubleWithLeftChild

```
/* Double rotate binary tree node: first left child with its  
right child; then node k3 with new left child */
```

```
private AVLTreeNode DoubleWithLeftChild(AVLTreeNode k3) {  
    k3.left = rotateWithRightChild( k3.left );  
    return rotateWithLeftChild( k3 );  
}
```

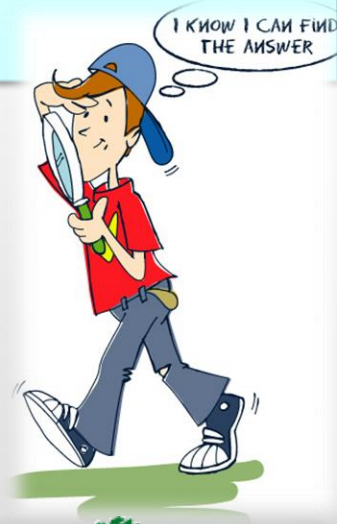
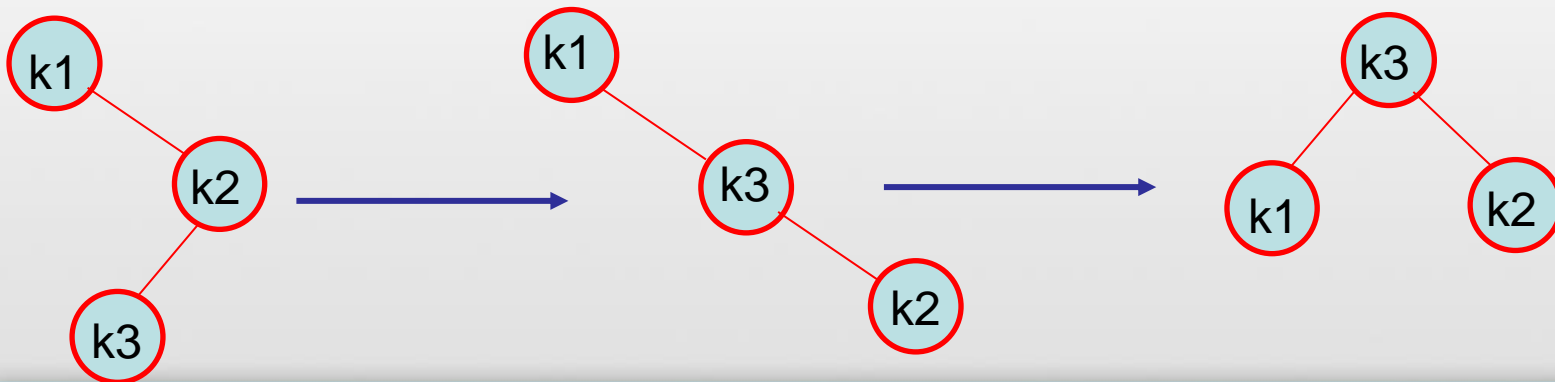




# AVL Tree : DoubleWithRightChild : H.W

```
/*Double rotate binary tree node: first right child  
with its left child; then node k1 with new right child */
```

```
private AVLTreeNode DoubleWithRightChild(AVLTreeNode k1){  
  
    k1.right = rotateWithLeftChild( k1.right );  
    return rotateWithRightChild( k1 );  
  
}
```



# *Extra Exercises*

## Question 1

### Lab 8: AVL Tree



# Question?



**“Success is the sum of small efforts, repeated day in and day out.”**  
Robert Collier