JANCAE
Japan Association for Nonlinear CAE

UMMDp

Unified Material Model Driver for Plasticity

User's Guide Abaqus

Version 2.1 Adapted from original document.

Contents

1 Preface											
2	Related Sections of Abaqus User's Manual	4									
3	S Setup										
	3.1 Source Files	5									
	3.2 Abaqus Input File	5									
	3.3 Program Execution	6									
4	Input	8									
	4.1 Debug and Print	8									
	4.2 Elastic Properties	8									
	4.3 Yield Criteria										
	4.4 Isotropic Hardening Laws	17									
	4.5 Kinematic Hardening Laws										
	4.6 Uncoupled Rupture Criteria										
5	5 Example	24									

1 Preface

The Unified Material Model Driver for Plasticity (UMMDp) library is distributed as Fortran source codes. The Fortran compiler specified by the software vender in your analysis environment must be prepared. Please see the Abaqus manual for details of the environment required for compiling user subroutines.

In this guide, the sections of Abaqus' manual related to the use of the UMMDp are described below, as well as the details on how to use the UMMDp with Abaqus. In the following procedures, the prompts "%" and ">" represent the examples in UNIX/Linux and Windows, respectively. The common steps for using the UMMDp with Abaqus are:

- 1. Preparation of the UMMDp source files
 - Merge the UMMDp source files into one file.
- 2. Writing procedure to call tye UMMDp in the input data
 - To call the material user subroutine, specific keywords are required to be written in the input data. The keywords include the material constants, such as the coefficients of the yield criterion.
- 3. Execution of Abaqus with the UMMDp
 - When a command is typed to execute Abaqus, options are added to compile the UM-MDp and to link it to Abaqus.

2 Related Sections of Abaqus User's Manual

- 1. Command to execute with user-subroutine
 - Abaqus Analysis User's Guide
 - 3.2.2 Abaqus/Standard, Abaqus/Explicit, and Abaqus/CFD execution.
- 2. Option for execution without compile
 - Abaqus Analysis User's Guide
 - $\circ~3.2.18$ Making user-defined executables and subroutines.
- 3. Keywords for setup of the UMMDp
 - Abagus Keywords Reference Guide
 - *DEPVAR: define the number of solution-dependent state variables.
 - *ORIENTATION: define local material axis for anisotropy.
 - \circ *USER MATERIAL: define the material constants used in UMAT.
 - *USER OUTPUT VARIABLE: define the number of user output variables.
- 4. Specification of Abaqus user subroutines used in the UMMDp
 - Abaqus User Subroutines Reference Guide
 - 1.1.44 UMAT: user subroutine to define a material's mechanical behavior.
 - 1.1.58 UVARM: user subroutine to generate element output.
- 5. User defined mechanical properties with UMAT
 - Abaqus Analysis User's Guide
 - o 26.7.1 User-defined mechanical material behavior.

3 Setup

3.1 Source Files

Concatenate the UMMDp source files into one single file with the plug-in file first. Simply use the batch files (.sh/.bat) or run each command separately.

• Unix/Linux

```
% cd dir_ummdp
% cp plug_ummdp_abaqus.f jobname_ummdp.f
% cat ummdp*.f >> jobname_ummdp.f
```

• Windows

```
> cd dir_ummdp
> copy plug_ummdp_abaqus.f jobname_ummdp.f
> type ummdp*.f >> jobname_ummdp.f
```

3.2 Abaqus Input File

This section describes the keywords in the input data file for use in the UMMDp.

1. Definition of the principal axis for the material anisotropy (refer to the manual)

```
*ORIENTATION, NAME=ORI-1
1., O., O., O., 1., O.
3, O.
```

2. Definition of the material model (the details will be provided later)

```
*MATERIAL, NAME=UMMDp

*USER MATERIAL, CONSTANTS=27

O, 0, 1000.0, 0.3, 2, -0.069, 0.936, 0.079,

1.003, 0.524, 1.363, 0.954, 1.023, 1.069, 0.981, 0.476,

0.575, 0.866, 1.145, -0.079, 1.404, 1.051, 1.147, 8.0,

O, 1.0, 0
```

Note that a each line accedpts a maximum of 8 constants.

3. Define the number of internal state variables (SDV)

Set the number of state variables to 1+NTENS, where NTENS is the number of components of the tensor variables. NTENS=3 for plane stress or a shell element, and NTENS=6 for a solid element. The 1st "1" is reserved for the equivalent plastic strain, and NTENS is reserved for the plastic strain components. The following example corresponds to a solid element without kinematic hardening:

*DEPVAR

7,

In the case of kinematic hardening, the number of internal state variables corresponds to the equivalent plastic strain, plastic strain components and components of each partial back-stress tensor.

4. Define the user output variables (UVAR)

The UMMDp can output some user output variables. The request for user output variables is not mandatory, except when an uncoupled rupture criterion is used. If user output variables are requested, the following variables are output in the presented order:

- UVAR(1): equivalent stress computed through the yield criteria
- UVAR(2): flow stress computed through the isotropic hardening law
- UVAR(3:2+NTENS): total back-stress tensor components (when using a kinematic hard-ening law)
- UVAR(3+NTENS:end): rupture criterion parameter and variables (when using a kinematic hardening law)
- UVAR(3:2+NTENS): rupture criterion parameter and variables (when not using a kinematic hardening law)

*USER OUTPUT VARIABLES
8,

5. Define output variables for post processing

This keyword controls the output variables (e.g., equivalent plastic strain and equivalent stress) for post processing.

```
*OUTPUT, FIELD

*ELEMENT OUTPUT

LE, S, SDV, UVARM
```

3.3 Program Execution

To execute the program there are two options: (a) link the user subroutine in source code and (b) link the user subroutine previously compiled.

(a) To execute the program with the user subroutine in source code, execute the command:

```
%> abaqus job=jobname user=jobname_ummdp.f
```

(b)	To execute	the	program	with	the	user	subroutine	previously	compiled,	execute	the	com-
	mands:											

- > abaqus job=jobname user=jobname_ummdp.obj
- % abaqus job=jobname user=jobname_ummdp.o

The command that compiles the file jobname_ummdp.obj/o is:

%> abaqus make library=jobname_ummdp.f

4 Input

The input data in UMMDp is defined as follows:

- 1. Parameter for Debug and Print
- 2. Parameters for Elastic Properties
- 3. Parameters for Yield Criterion
- 4. Parameters for Isotropic Hardening Law
- 5. Parameters for Kinematic Hardening Law

The detail of data is shown as follows and in addition, an example of input data is described.

4.1 Debug and Print

The first input parameter corresponds to the definition of debug and print mode, defined by the variable nvbs0. The option selected here will have an effect on the .dat file from Abaqus execution. It is a mandatory parameter and the options are:

- 0 Error messages only
- 1 Summary of Multistage Return Mapping
- 2 Detail of Multistage Return Mapping and summary of Newton-Raphson
- 3 Detail of Newton-Raphson
- 4 Input/Output
- 5 All status for debug and print

4.2 Elastic Properties

- prela(1) ID for elastic properties
- prela(2~) Data depends on ID

Only isotropic Hooke elastic properties can be defined. There are 2 ways to set them:

- Young's Modulus and Poisson's Ratio ✓
 - ID: 0
 - Parameters: 2
 - \circ prela(1) = 0
 - o prela(2) = 200.0E+3 (Young's modulus E)
 - \circ prela(3) = 0.3 (Poisson's ratio ν)

- Bulk Modulus and Modulus of Rigidity ✓
 - ID: 1
 - Parameters: 2
 - o prela(1) = 1
 - o prela(2) = 166666.7 (Bulk modulus $K = E(1 2\nu)/3$))
 - prela(3) = 76923.08 (Modulus of rigidity $G = E(1 + \nu)/2$)

4.3 Yield Criteria

• pryld(1) - ID for yield function

(Negative values specify plane stress yield criteria)

• pryld(2~) - Data depends on ID

Identification number for yield criteria and required parameters are introduced. Please refer to the original papers for more detail on the formulation and meaning of parameters.

- von Mises ✓
 - □ von Mises, R., 1913. Mechanik der festen Korper im plastisch deformablen Zustand. Gottin Nachr Math Phys, 1:582–592.
 - ID: 0
 - \circ pryld(1) = 0
- Hill 1948 ✓
 - Hill, R., 1949. The theory of plane plastic strain for anisotropic metals. Proc Royal Soc Lond Ser Math Phys Sci 198, 428–437.
 - ID: 1
 - Parameters: 6
 - \circ pryld(1) = 1
 - o pryld(1+1) = F
 - \circ pryld(1+2) = G
 - o pryld(1+3) = H
 - \circ pryld(1+4) = L
 - o pryld(1+5) = M
 - o pryld(1+6) = N
 - \Box The parameters are the same as Hill's original paper. When F=G=H=1 and L=M=N=3, Hill's function is identical to von Mises.

■ Yld2004-18p ✓

- □ Barlat, F., Aretz, H., Yoon, J.-H., Karabin, M.E., Brem, J.C., Dick, R.E., 2005. Linear transformation-based anisotropic yield functions. Int J Plasticity 21, 1009–1039.
- ID: 2
- Parameters: 19
- o pryld(1) = 2
- \circ pryld(1+1) = c'_{12}
- \circ pryld(1+2) = c'_{13}
- \circ pryld(1+3) = c'_{21}
- \circ pryld(1+4) = c'_{23}
- \circ pryld(1+5) = c'_{31}
- \circ pryld(1+6) = c'_{32}
- \circ pryld(1+7) = c'_{44}
- \circ pryld(1+8) = c'_{55}
- \circ pryld(1+9) = c'_{66}
- \circ pryld(1+10) = c_{12}''
- \circ pryld(1+11) = c_{13}''
- \circ pryld(1+12) = c_{21}''
- o pryld(1+13) = c_{23}''
- \circ pryld(1+14) = c_{31}''
- \circ pryld(1+15) = c_{32}''
- \circ pryld(1+16) = $c_{44}^{"}$
- \circ pryld(1+17) = c_{55}''
- \circ pryld(1+18) = c'_{66}
- \circ pryld(1+19) = a (exponent)
- □ The order of parameters given as input is the same as in the original paper.

■ CPB 2006 ✓

- □ Cazacu, O., Plunkett, B., Barlat, F., 2006. Orthotropic yield criterion for hexagonal closed packed metals. Int J Plasticity 22, 1171–1194.
- ID: 3
- Parameters: 14

```
o pryld(1) = 3
```

$$\circ$$
 pryld(1+1) = C_{11}

$$\circ$$
 pryld(1+2) = C_{12}

$$\circ$$
 pryld(1+3) = C_{13}

$$\circ$$
 pryld(1+4) = C_{21}

$$\circ$$
 pryld(1+5) = C_{22}

$$\circ$$
 pryld(1+6) = C_{23}

$$\circ$$
 pryld(1+7) = C_{31}

$$\circ$$
 pryld(1+8) = C_{32}

$$\circ$$
 pryld(1+9) = C_{33}

$$\circ$$
 pryld(1+10) = C_{44}

$$\circ$$
 pryld(1+11) = C_{55}

$$\circ$$
 pryld(1+12) = C_{66}

$$\circ$$
 pryld(1+13) = a (exponent)

 \circ pryld(1+14) = k (tension-compression ratio)

■ Karafillis-Boyce 1993

- □ Karafillis, A.P., Boyce, M.C., 1993. A general anisotropic yield criterion using bounds and a transformation weighting tensor. J Mech Phys Solids 41, 1859–1886.
- ID: 4
- Parameters: 8

$$\circ$$
 pryld(1) = 4

$$\circ$$
 pryld(1+1) = C

$$\circ$$
 pryld(1+2) = α_1

$$\circ$$
 pryld(1+3) = α_2

$$\circ$$
 pryld(1+4) = γ_1

$$\circ$$
 pryld(1+5) = γ_2

$$\circ$$
 pryld(1+6) = γ_3

$$\circ$$
 pryld(1+7) = c

$$\circ$$
 pryld(1+8) = k (k of exponent $2k$)

■ Hu 2005

- $\hfill\Box$ Hu, W., 2005. An orthotropic yield criterion in a 3-D general stress state. Int J Plasticity 21, 1771–1796.
- ID: 5
- Parameters: 10
- o pryld(1) = 5
- \circ pryld(1+1) = X_1
- \circ pryld(1+2) = X_2
- \circ pryld(1+3) = X_3
- \circ pryld(1+4) = X_4
- \circ pryld(1+5) = X_5
- \circ pryld(1+6) = X_6
- \circ pryld(1+7) = X_7
- \circ pryld(1+8) = C_1
- \circ pryld(1+9) = C_2
- \circ pryld(1+10) = C_3

\blacksquare Yoshida 6th Polynomial

- □ Yoshida, F., Hamasaki, H., Uemori, T., 2013. A user-friendly 3D yield function to describe anisotropy of steel sheets. Int J Plasticity 45, 119–139.
- ID: 6
- Parameters: 16
- o pryld(1) = 6
- \circ pryld(1+1) = C_1
- \circ pryld(1+2) = C_2
- \circ pryld(1+3) = C_3
- \circ pryld(1+4) = C_4
- \circ pryld(1+5) = C_5
- \circ pryld(1+6) = C_6
- \circ pryld(1+7) = C_7
- \circ pryld(1+8) = C_8
- \circ pryld(1+9) = C_9
- \circ pryld(1+10) = C_{10}
- \circ pryld(1+11) = C_{11}
- \circ pryld(1+12) = C_{12}
- \circ pryld(1+13) = C_{13}
- \circ pryld(1+14) = C_{14}
- \circ pryld(1+15) = C_{15}
- \circ pryld(1+16) = C_{16}

■ Gotoh Biquadratic

- □ Gotoh, M., 1977. A theory of plastic anisotropy based on a yield function of fourth order (plane stress state)—I. Int J Mech Sci 19, 505–512.
- ID: -1
- Parameters: 9
- \circ pryld(1) = -1
- \circ pryld(1+1) = A_1
- \circ pryld(1+2) = A_2
- \circ pryld(1+3) = A_3
- \circ pryld(1+4) = A_4
- \circ pryld(1+5) = A_5
- \circ pryld(1+6) = A_6
- \circ pryld(1+7) = A_7
- \circ pryld(1+8) = A_8
- \circ pryld(1+9) = A_9

■ Yld2000-2d ✓

- □ Barlat, F., Brem, J.C., Yoon, J.-H., Chung, K., Dick, R.E., Lege, D.J., Pourboghrat, F., Choi, S.-H., Chu, E., 2003. Plane stress yield function for aluminum alloy sheets—part 1: theory. Int J Plasticity 19, 1297–1319.
- ID: -2
- Parameters: 9
- \circ pryld(1) = -2
- \circ pryld(1+1) = α_1
- \circ pryld(1+2) = α_2
- \circ pryld(1+3) = α_3
- \circ pryld(1+4) = α_4
- \circ pryld(1+5) = α_5
- \circ pryld(1+6) = α_6
- \circ pryld(1+7) = α_7
- \circ pryld(1+8) = α_8
- \circ pryld(1+9) = a (exponent)

■ Vegter

- □ Vegter, H., van den Boogaard, A.H., 2006. A plane stress yield function for anisotropic sheet material by interpolation of biaxial stress states. Int J Plasticity 22, 557–580.
- ID: -3
- Parameters: 3 + 4n

■ BBC 2005

- □ Banabic, D., Aretz, H., Comsa, D.S., Paraianu, L., 2005. An improved analytical description of orthotropy in metallic sheets. Int J Plasticity 21, 493–512.
- ID: −4
- Parameters: 9

```
\circ pryld(1) = -4
```

 \circ pryld(1+1) = k (k of exponent 2k)

 $\circ \text{ pryld}(1+3+(i-1)*4+4) = \text{omega}(i)$

- \circ pryld(1+2) = a
- \circ pryld(1+3) = b
- \circ pryld(1+4) = L
- \circ pryld(1+5) = M
- \circ pryld(1+6) = N
- \circ pryld(1+7) = P
- \circ pryld(1+8) = Q
- \circ pryld(1+9) = R

■ Yld89

- □ Barlat, F., Lian, K., 1989. Plastic behavior and stretchability of sheet metals. Part I: A yield function for orthotropic sheets under plane stress conditions. Int J Plasticity 5, 51–66.
- ID: -5
- Parameters: 4

```
\circ pryld(1) = -5
```

$$\circ$$
 pryld(1+1) = M (exponent)

- \circ pryld(1+2) = a
- \circ pryld(1+3) = h
- \circ pryld(1+4) = p

■ BBC 2008

- □ Comsa, D.-S., Banabic, D., 2008. Plane-stress yield criterion for highly-anisotropic sheet metals, in: NUMISHEET 2008, pp. 43–48.
- ID: -6
- Parameters: 2 + 8s

```
\circ pryld(1) = -6
```

$$\circ$$
 pryld(1+1) = $s \pmod{i}$

$$\circ$$
 pryld(1+2) = k (k of exponent $2k$)

$$\circ$$
 pryld(1+2+(i-1)*8+1) = l_1

$$\circ \text{ pryld}(1+2+(i-1)*8+2) = l_2$$

$$\circ$$
 pryld(1+2+(i-1)*8+3) = m_1

$$\circ \text{ pryld}(1+2+(i-1)*8+4) = m_2$$

$$\circ$$
 pryld(1+2+(i-1)*8+5) = m_3

$$\circ$$
 pryld(1+2+(i-1)*8+6) = n_1

$$\circ$$
 pryld(1+2+(i-1)*8+7) = n_2

$$\circ$$
 pryld(1+2+(i-1)*8+8) = n_3

■ Hill 1990

- $\hfill\Box$ Hill, R., 1990. Constitutive modelling of orthotropic plasticity in sheet metals. J Mech Phys Solids 38, 405–417.
- ID: -7
- Parameters: 5
- \circ pryld(1) = -7
- \circ pryld(1+1) = a
- \circ pryld(1+2) = b
- \circ pryld(1+3) = τ
- \circ pryld(1+4) = σ_b
- \circ pryld(1+5) = m

4.4 Isotropic Hardening Laws

- prihd(1) ID for isotropic hardening
- prihd(2~) Data depends on ID

The equation of flow curve is introduced for each law, where σ_y is the yield stress, σ_{y_0} is the initial yield stress and p the equivalent plastic strain.

- Perfectly Plastic ✓
 - ID: 0
 - Parameters: 1
 - \circ prihd(1) = 0
 - \circ prihd(1+1) = σ_y
- \blacksquare Linear Hardening: $\sigma_{\mathbf{y}} = \sigma_{\mathbf{y}_0} + Hp$
 - ID: 1
 - Parameters: 2
 - o prihd(1) = 1
 - \circ prihd(1+1) = σ_{y_0}
 - \circ prihd(1+2) = H

- Swift: $\sigma_{y} = K (\varepsilon_{0} + p)^{n}$
 - ID: 2
 - Parameters: 3
 - o prihd(1) = 2
 - \circ prihd(1+1) = K
 - \circ prihd(1+2) = ϵ_0
 - \circ prihd(1+3) = n
- \blacksquare Ludwick: $\sigma_{\mathbf{y}} = \sigma_{\mathbf{y}_0} + cp^n$ \checkmark
 - ID: 3
 - Parameters: 3
 - o prihd(1) = 3
 - \circ prihd(1+1) = σ_{y_0}
 - \circ prihd(1+2) = c
 - \circ prihd(1+3) = n
- Voce: $\sigma_{\mathbf{y}} = \sigma_{\mathbf{y}_0} + Q \left(1 \exp(-bp)\right)$ \checkmark
 - ID: 4
 - Parameters: 3
 - o prihd(1) = 4
 - \circ prihd(1+1) = σ_{y_0}
 - \circ prihd(1+2) = Q
 - \circ prihd(1+3) = b
- Voce + Linear: $\sigma_y = \sigma_{y_0} + Q(1 \exp(-bp)) + Hp$ ✓
 - ID: 5
 - Parameters: 4
 - \circ prihd(1) = 5
 - \circ prihd(1+1) = σ_{y_0}
 - \circ prihd(1+2) = Q
 - \circ prihd(1+3) = b
 - \circ prihd(1+4) = H

- Voce + Swift: $\sigma_y = a \left[\sigma_{y_0} + Q \left(1 \exp(-bp) \right) \right] + (1 a) \left[K(\varepsilon_0 + p)^n \right]$
 - ID: 6
 - Parameters: 7
 - \circ prihd(1) = 6
 - \circ prihd(1+1) = a
 - \circ prihd(1+2) = σ_{y_0}
 - \circ prihd(1+3) = Q
 - \circ prihd(1+4) = b
 - \circ prihd(1+5) = K
 - \circ prihd(1+6) = ε_0
 - \circ prihd(1+7) = n

4.5 Kinematic Hardening Laws

- prkin(1) ID for kinematic hardening
- prkin(2~) Data depends on ID

The equation of backstress is introduced for each law, where $\dot{\alpha}$ is the total increment of backstress tensor, $\dot{\alpha}_i$ is the a term of the total increment of backstress tensor, α is the backstress tensor, $\dot{\epsilon}^p$ is the increment of plastic strain tensor and \dot{p} is the increment of equivalent plastic strain. Depending on the law, a specific number of additional state variables (SDV) and user output variables (UVAR) are required. The variable k represents the number of tensor components (NTENS).

- No Kinematic Hardening ✓
 - ID: 0
 - \circ prkin(1) = 0
- Prager (1949): $\dot{\boldsymbol{\alpha}} = \frac{2}{3}c\dot{\boldsymbol{\varepsilon}}^{\mathrm{p}}$ ✓
 - ID: 1
 - Parameters: 1
 - State Variables: + k
 - \circ prkin(1) = 1
 - \circ prkin(1+1) = c

- Ziegler (1959): $\dot{\boldsymbol{\alpha}} = c \left(\boldsymbol{\sigma} \boldsymbol{\alpha} \right) \dot{p}$
 - ID: 2
 - Parameters: 1
 - State Variables: + k
 - \circ prkin(1) = 2
 - \circ prkin(1+1) = c
- - ID: 3
 - Parameters: 2
 - ullet State Variables: + k
 - \circ prkin(1) = 3
 - \circ prkin(1+1) = c
 - \circ prkin(1+2) = γ
- Chaboche (1979): $\dot{\boldsymbol{\alpha}} = \sum_{i=1}^{n} \dot{\boldsymbol{\alpha}}_i = \sum_{i=1}^{n} \left(\frac{2}{3}c_i\dot{\boldsymbol{\varepsilon}}^{\mathrm{p}} \gamma_i\boldsymbol{\alpha}_i\dot{p}\right)$ ✓
 - ID: 4
 - Parameters: 1 + 2n
 - State Variables: $+ n \times k$
 - User Output Variables: + k
 - o prkin(1) = 4
 - \circ prkin(1+1) = n
 - \circ prkin(1+1+(i*1)) = c_i
 - o prkin(1+1+(i*2)) = γ_i

- Chaboche (1979) Ziegler Type: $\dot{\boldsymbol{\alpha}} = \sum_{i=1}^{n} \dot{\boldsymbol{\alpha}}_{i} = \sum_{i=1}^{n} \left(\frac{c_{i}}{\overline{\eta}} \left(\boldsymbol{\sigma} \boldsymbol{\alpha} \right) \gamma_{i} \boldsymbol{\alpha}_{i} \right) \dot{p}$ ✓
 - ID: 5
 - Parameters: 1 + 2n
 - State Variables: $+ n \times k$
 - User Output Variables: + k
 - o prkin(1) = 5
 - \circ prkin(1+1) = n
 - \circ prkin(1+1+(i*1)) = c_i
 - \circ prkin(1+1+(i*2)) = γ_i
- Yoshida-Uemori
 - ID: 6
 - Parameters: 5
 - \circ prkin(1) = 6
 - \circ prkin(1+1) = C
 - \circ prkin(1+2) = Y
 - \circ prkin(1+3) = a
 - \circ prkin(1+4) = k
 - \circ prkin(1+5) = b

4.6 Uncoupled Rupture Criteria

- prrup(1) ID for uncoupled rupture criterion
- prrup($2\sim$) Data depends on ID

The equation of the uncoupled rupture criterion is introduced for each criterion, where W is the rupture parameter, σ_1 is the maximum principal stress, σ_h is the hydrostatic stress, $\bar{\sigma}$ is the equivalent stress, \dot{p} the equivalent plastic strain rate, and W_L the user-defined critical value. Depending on the criterion, a specific number of additional user output variables (UVAR) are required.

- \bullet No Uncoupled Rupture Criterion \checkmark
 - ID: 0
 - \circ prrup(1) = 0

- \blacksquare Equivalent Plastic Strain: $W = \int_0^{\varepsilon_{\mathrm{f}}} \dot{p} \, \mathrm{d}t \quad \checkmark$
 - ID: 1
 - Parameters: 1
 - User Output Variables: + 2
 - o prrup(1) = 1
 - \circ prrup(1+1) = $W_{\rm L}$
 - □ UVAR(_+1) = equivalent plastic strain
 - □ UVAR(_+2) = rupture parameter normalised by critical value
- Cockroft and Latham: $W = \int_0^{\varepsilon_{\rm f}} \frac{\sigma_1}{\bar{\sigma}} \, \mathrm{d}p$ ✓
 - ID: 2
 - Parameters: 1
 - User Output Variables: + 4
 - \circ prrup(1) = 2
 - \circ prrup(1+1) = $W_{\rm L}$
 - □ UVAR(_+1) = equivalent plastic strain
 - □ UVAR(_+2) = maximum principal stress
 - □ UVAR(_+3) = rupture parameter
 - □ UVAR(_+4) = rupture parameter normalised by critical value
- Rice and Tracey: $W = \int_0^{\varepsilon_{\rm f}} \exp\left(\frac{3}{2} \frac{\sigma_h}{\bar{\sigma}}\right) \, \mathrm{d}p$ ✓
 - ID: 3
 - Parameters: 1
 - User Output Variables: + 4
 - \circ prrup(1) = 3
 - \circ prrup(1+1) = $W_{\rm L}$
 - □ UVAR(_+1) = equivalent plastic strain
 - □ UVAR(_+2) = hydrostatic stress
 - □ UVAR(_+3) = rupture parameter
 - □ UVAR(_+4) = rupture parameter normalised by critical value

- Ayada: $W = \int_0^{\varepsilon_{\rm f}} \frac{\sigma_h}{\bar{\sigma}} \, \mathrm{d}p$ ✓
 - ID: 4
 - Parameters: 1
 - User Output Variables: + 4
 - \circ prrup(1) = 4
 - \circ prrup(1+1) = $W_{\rm L}$
 - □ UVAR(_+1) = equivalent plastic strain
 - □ UVAR(_+2) = hydrostatic stress
 - □ UVAR(_+3) = rupture parameter
 - $\ \square$ UVAR(_+4) = rupture parameter normalised by critical value
- Brozzo: $W = \int_0^{\varepsilon_{\rm f}} \frac{2\sigma_1}{3(\sigma_1 \sigma_h)} \, \mathrm{d}p$ ✓
 - ID: 5
 - Parameters: 1
 - \bullet User Output Variables: + 5
 - \circ prrup(1) = 5
 - \circ prrup(1+1) = $W_{\rm L}$
 - □ UVAR(_+1) = equivalent plastic strain
 - □ UVAR(_+2) = maximum principal stress
 - □ UVAR(_+3) = hydrostatic stress
 - □ UVAR(_+4) = rupture parameter
 - □ UVAR(_+5) = rupture parameter normalised by critical value

5 Example

• Debug and Print: Error messages only

• Elastic Properties: $E{=}200$ GPa, $\nu{=}0.3$

• Yield Criterion: Yld2004-18p (coefficients of AA6111-T4 given in the original paper)

• Isotropic Hardening Law: Swift

• Kinematic Hardening Law: Armstrong-Frederick (1966)

• Uncoupled Rupture Criterion: Ayada

The material parameters and IDs are given as input to the UMMDp in one dimensional array, named by default props in the program. In the beginning of the UMMDp, this array is copied to a new variable prop, and the variable to define debug and print mode is excluded from this new array.

o props(1)	= 0	Debug and Print ID
o props(2)	= 0	Elastic Property ID
o props(3)	= 200000	E
o props(4)	= 0.3	u
o props(5)	= 2	Yield Criterion ID
o props(6)	= 1.241024	c_{12}'
o props(7)	= 1.078271	c'_{13}
o props(8)	= 1.216463	c'_{21}
o props(9)	= 1.223867	c'_{23}
o props(10)	= 1.093105	c_{31}'
o props(11)	= 0.889161	c_{32}'
o props(12)	= 0.501909	c_{44}^{\prime}
o props(13)	= 0.557173	c_{55}^{\prime}
o props(14)	= 1.349094	c_{66}^{\prime}
o props(15)	= 0.775366	$c_{12}^{\prime\prime}$
o props(16)	= 0.922743	$c_{13}^{\prime\prime}$
o props(17)	= 0.765487	$c_{21}^{\prime\prime}$
o props(18)	= 0.793356	$c_{23}^{\prime\prime}$
o props(19)	= 0.918689	$c_{31}^{\prime\prime}$
o props(20)	= 1.027625	$c_{32}^{\prime\prime}$
o props(21)	= 1.115833	$c_{44}^{\prime\prime}$

```
o props(22) = 1.112273
                                           c_{55}''
                                           c_{66}''
\circ props(23) = 0.589787
\circ props(24) = 8
\circ props(25) = 2
                                           Isotropic Hardening Law ID
\circ props(26) = 541.0
                                           K
\circ props(27) = 0.0036
                                           \varepsilon_0
\circ props(28) = 0.249
                                           n
\circ props(29) = 3
                                           Kinematic Hardening Law ID
\circ props(30) = 1018.4245
                                           c
\circ props(31) = 22.85
                                           \gamma
\circ props(32) = 4
                                           Uncoupled Rupture Criterion ID
\circ props(33) = 0.5
                                           W_L
```

This prop(i) array is divided in the UMMDp as follow:

- prela(i) Elastic Properties
- pryld(i) Yield Criterion
- prihd(i) Isotropic Hardening Law
- prkin(i) Kinematic Hardening Law
- prrup(i) Uncoupled Rupture Criterion

The model ID is stored in the top of each of these arrays. Here, it is shown some parts of a three-dimensional example for the abaqus input file. The red letter indicates ID of each properties.

```
*MATERIAL, NAME=UMMDp

*USER MATERIAL, CONSTANTS=33

O, 0, 200000.0, 0.3, 2, 1.241024, 1.078271, 1.216463,
1.223867, 1.093105, 0.889161, 0.501909, 0.557173, 1.349094, 0.775366, 0.922743,
0.765487, 0.793356, 0.918689, 1.027625, 1.115833, 1.112273, 0.589787, 8.0,
2, 541.0, 0.0036, 0.249, 3, 1018.4245, 22.85, 4,
0.5

**
*DEPVAR
7,

**
*USER OUTPUT VARIABLES
12,
```